ECE C147/247 HW4 Q2: Batch Normalization In this notebook, you will implement the batch normalization layers of a neural network to increase its performance. Please review the details of batch normalization from the lecture notes. utils has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc_net , nndl.layers , and nndl.layer_utils . ## Import and setups import time import numpy as np import matplotlib.pyplot as plt from nndl.fc net import * from nndl.layers import * from utils.data_utils import get_CIFAR10_data from utils.gradient check import eval numerical gradient, eval numerical gradient array from utils.solver import Solver %matplotlib inline plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots plt.rcParams['image.interpolation'] = 'nearest' plt.rcParams['image.cmap'] = 'gray' # for auto-reloading external modules # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython %load ext autoreload %autoreload 2 def rel error(x, y): """ returns relative error """ return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))# Load the (preprocessed) CIFAR10 data. data = get CIFAR10 data() for k in data.keys(): print('{}: {} '.format(k, data[k].shape)) X train: (49000, 3, 32, 32) y train: (49000,) X val: (1000, 3, 32, 32) y val: (1000,) X test: (1000, 3, 32, 32) y test: (1000,) Batchnorm forward pass Implement the training time batchnorm forward pass, batchnorm_forward , in nndl/layers.py . After that, test your implementation by running the following cell. # Check the training-time forward pass by checking means and variances # of features both before and after batch normalization # Simulate the forward pass for a two-layer network N, D1, D2, D3 = 200, 50, 60, 3X = np.random.randn(N, D1)W1 = np.random.randn(D1, D2)W2 = np.random.randn(D2, D3)a = np.maximum(0, X.dot(W1)).dot(W2)print('Before batch normalization:') print(' means: ', a.mean(axis=0)) print(' stds: ', a.std(axis=0)) # Means should be close to zero and stds close to one print('After batch normalization (gamma=1, beta=0)') a_norm, _ = batchnorm_forward(a, np.ones(D3), np.zeros(D3), {'mode': 'train'}) print(' mean: ', a_norm.mean(axis=0)) print(' std: ', a_norm.std(axis=0)) # Now means should be close to beta and stds close to gamma gamma = np.asarray([1.0, 2.0, 3.0])beta = np.asarray([11.0, 12.0, 13.0])a norm, = batchnorm forward(a, gamma, beta, {'mode': 'train'}) print('After batch normalization (nontrivial gamma, beta)') print(' means: ', a norm.mean(axis=0)) print(' stds: ', a norm.std(axis=0)) Before batch normalization: means: [-28.84907154 -25.88395893 -2.11862989] stds: [31.89265604 38.41952822 28.18587946] After batch normalization (gamma=1, beta=0) mean: [-2.22044605e-17 2.22044605e-17 -4.21884749e-17] std: [1. 1. 0.99999999] After batch normalization (nontrivial gamma, beta) means: [11. 12. 13.] 1.99999999 2.99999998] Implement the testing time batchnorm forward pass, batchnorm_forward, in nndl/layers.py. After that, test your implementation by running the following cell. In [4]: # Check the test-time forward pass by running the training-time # forward pass many times to warm up the running averages, and then # checking the means and variances of activations after a test-time # forward pass. N, D1, D2, D3 = 200, 50, 60, 3 W1 = np.random.randn(D1, D2)W2 = np.random.randn(D2, D3)bn_param = {'mode': 'train'} gamma = np.ones(D3)beta = np.zeros(D3)for t in np.arange(50): X = np.random.randn(N, D1)a = np.maximum(0, X.dot(W1)).dot(W2)batchnorm_forward(a, gamma, beta, bn_param) bn param['mode'] = 'test' X = np.random.randn(N, D1)a = np.maximum(0, X.dot(W1)).dot(W2)a_norm, _ = batchnorm_forward(a, gamma, beta, bn_param) # Means should be close to zero and stds close to one, but will be # noisier than training-time forward passes. print('After batch normalization (test-time):') print(' means: ', a_norm.mean(axis=0)) print(' stds: ', a_norm.std(axis=0)) After batch normalization (test-time): means: [5694.44183941 -11559.82501338 4320.14438343] stds: [9330.88699977 9424.10712598 9575.23599007] Batchnorm backward pass Implement the backward pass for the batchnorm layer, batchnorm_backward in nndl/layers.py . Check your implementation by running the following cell. # Gradient check batchnorm backward pass N, D = 4, 5x = 5 * np.random.randn(N, D) + 12gamma = np.random.randn(D) beta = np.random.randn(D) dout = np.random.randn(N, D) bn param = {'mode': 'train'} fx = lambda x: batchnorm_forward(x, gamma, beta, bn_param)[0] fg = lambda a: batchnorm_forward(x, gamma, beta, bn_param)[0] fb = lambda b: batchnorm_forward(x, gamma, beta, bn_param)[0] dx_num = eval_numerical_gradient_array(fx, x, dout) da_num = eval_numerical_gradient_array(fg, gamma, dout) db num = eval numerical gradient array(fb, beta, dout) _, cache = batchnorm_forward(x, gamma, beta, bn_param) dx, dgamma, dbeta = batchnorm_backward(dout, cache) print('dx error: ', rel_error(dx_num, dx)) print('dgamma error: ', rel_error(da_num, dgamma)) print('dbeta error: ', rel_error(db_num, dbeta)) dx error: 1.7703768271105096e-09 dgamma error: 3.707945705184271e-11 dbeta error: 3.275692151309245e-12 Implement a fully connected neural network with batchnorm layers Modify the FullyConnectedNet() class in nndl/fc_net.py to incorporate batchnorm layers. You will need to modify the class in the following areas: (1) The gammas and betas need to be initialized to 1's and 0's respectively in __init__. (2) The batchnorm_forward layer needs to be inserted between each affine and relu layer (except in the output layer) in a forward pass computation in loss . You may find it helpful to write an affine_batchnorm_relu() layer in nndl/layer_utils.py although this is not necessary. (3) The batchnorm_backward layer has to be appropriately inserted when calculating gradients. After you have done the appropriate modifications, check your implementation by running the following cell. Note, while the relative error for W3 should be small, as we backprop gradients more, you may find the relative error increases. Our relative error for W1 is on the order of 1e-4. N, D, H1, H2, C = 2, 15, 20, 30, 10X = np.random.randn(N, D)y = np.random.randint(C, size=(N,)) for reg in [0, 3.14]: print('Running check with reg = ', reg) model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C, reg=reg, weight_scale=5e-2, dtype=np.float64, use batchnorm=True) loss, grads = model.loss(X, y) print('Initial loss: ', loss) for name in sorted(grads): $f = lambda _: model.loss(X, y)[0]$ grad_num = eval_numerical_gradient(f, model.params[name], verbose=False, h=1e-5) print('{} relative error: {}'.format(name, rel_error(grad_num, grads[name]))) if reg == 0: print('\n') Running check with reg = 0Initial loss: 2.3428296959216444 W1 relative error: 0.0018034962629854376 W2 relative error: 3.962340404407421e-05 W3 relative error: 3.519007905294395e-10 b1 relative error: 0.002220443273692751 b2 relative error: 1.1102230246251565e-08 b3 relative error: 1.7625948184968003e-10 beta1 relative error: 3.2409224864496935e-08 beta2 relative error: 1.5593687895310636e-08 gammal relative error: 3.1089775687156094e-08 gamma2 relative error: 1.2000086744520607e-08 Running check with reg = 3.14Initial loss: 6.95488371352358 W1 relative error: 0.0001695121156961158 W2 relative error: 4.82658633053028e-06 W3 relative error: 7.172263548226862e-09 b1 relative error: 5.551115123125783e-09 b2 relative error: 4.440892098500626e-08 b3 relative error: 2.706977503819273e-10 beta1 relative error: 1.9583724009991693e-08 beta2 relative error: 1.6570164039795128e-08 gamma1 relative error: 4.618920964413653e-08 gamma2 relative error: 1.728582850964246e-08 Training a deep fully connected network with batch normalization. To see if batchnorm helps, let's train a deep neural network with and without batch normalization. # Try training a very deep net with batchnorm hidden dims = [100, 100, 100, 100, 100] $num_train = 1000$ small data = { 'X_train': data['X_train'][:num_train], 'y_train': data['y_train'][:num_train], 'X_val': data['X_val'], 'y_val': data['y_val'], weight scale = 2e-2bn_model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batchnorm=True) model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batchnorm=False) bn_solver = Solver(bn_model, small_data, num_epochs=10, batch_size=50, update_rule='adam', optim config={ 'learning_rate': 1e-3, verbose=True, print_every=200) bn solver.train() solver = Solver(model, small_data, num_epochs=10, batch_size=50, update_rule='adam', optim_config={ 'learning_rate': 1e-3, verbose=True, print_every=200) solver.train() (Iteration 1 / 200) loss: 2.300179 (Epoch 0 / 10) train acc: 0.119000; val acc: 0.104000 (Epoch 1 / 10) train acc: 0.322000; val_acc: 0.268000 (Epoch 2 / 10) train acc: 0.436000; val_acc: 0.311000 (Epoch 3 / 10) train acc: 0.535000; val_acc: 0.302000 (Epoch 4 / 10) train acc: 0.569000; val_acc: 0.337000 (Epoch 5 / 10) train acc: 0.607000; val_acc: 0.318000 (Epoch 6 / 10) train acc: 0.653000; val_acc: 0.306000 (Epoch 7 / 10) train acc: 0.739000; val acc: 0.345000 (Epoch 8 / 10) train acc: 0.725000; val acc: 0.299000 (Epoch 9 / 10) train acc: 0.769000; val_acc: 0.314000 (Epoch 10 / 10) train acc: 0.808000; val acc: 0.338000 (Iteration 1 / 200) loss: 2.303840 (Epoch 0 / 10) train acc: 0.146000; val acc: 0.143000 (Epoch 1 / 10) train acc: 0.243000; val_acc: 0.210000 (Epoch 2 / 10) train acc: 0.284000; val_acc: 0.254000 (Epoch 3 / 10) train acc: 0.316000; val acc: 0.246000 (Epoch 4 / 10) train acc: 0.374000; val acc: 0.274000 (Epoch 5 / 10) train acc: 0.407000; val_acc: 0.293000 (Epoch 6 / 10) train acc: 0.436000; val_acc: 0.283000 (Epoch 7 / 10) train acc: 0.502000; val_acc: 0.306000 (Epoch 8 / 10) train acc: 0.528000; val_acc: 0.308000 (Epoch 9 / 10) train acc: 0.575000; val acc: 0.304000 (Epoch 10 / 10) train acc: 0.598000; val acc: 0.326000 plt.subplot(3, 1, 1) plt.title('Training loss') plt.xlabel('Iteration') plt.subplot(3, 1, 2) plt.title('Training accuracy') plt.xlabel('Epoch') plt.subplot(3, 1, 3) plt.title('Validation accuracy') plt.xlabel('Epoch') plt.subplot(3, 1, 1) plt.plot(solver.loss_history, 'o', label='baseline') plt.plot(bn solver.loss history, 'o', label='batchnorm') plt.subplot(3, 1, 2) plt.plot(solver.train acc history, '-o', label='baseline') plt.plot(bn solver.train acc history, '-o', label='batchnorm') plt.subplot(3, 1, 3) plt.plot(solver.val acc history, '-o', label='baseline') plt.plot(bn solver.val acc history, '-o', label='batchnorm') for i in [1, 2, 3]: plt.subplot(3, 1, i) plt.legend(loc='upper center', ncol=4) plt.gcf().set size inches(15, 15) plt.show() <ipython-input-8-8e49aa315b6d>:13: MatplotlibDeprecationWarning: Adding an axes using the same arguments as a p revious axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance. plt.subplot(3, 1, 1) <ipython-input-8-8e49aa315b6d>:17: MatplotlibDeprecationWarning: Adding an axes using the same arguments as a p revious axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance. plt.subplot(3, 1, 2)<ipython-input-8-8e49aa315b6d>:21: MatplotlibDeprecationWarning: Adding an axes using the same arguments as a p revious axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance. plt.subplot(3, 1, 3)<ipython-input-8-8e49aa315b6d>:26: MatplotlibDeprecationWarning: Adding an axes using the same arguments as a p revious axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance. plt.subplot(3, 1, i) Training loss baseline batchnorm 2.25 2.00 1.75 1.50 1.25 1.00 0.75 0.50 25 50 75 125 150 175 100 200 Iteration Training accuracy 0.8 batchnorm 0.7 0.6 0.5 0.4 0.3 0.2 0.1 10 Epoch Validation accuracy 0.35 baseline batchnorm 0.30 0.25 0.20 0.15 0.10 2 Epoch Batchnorm and initialization The following cells run an experiment where for a deep network, the initialization is varied. We do training for when batchnorm layers are and are not included. # Try training a very deep net with batchnorm hidden dims = [50, 50, 50, 50, 50, 50, 50]num train = 1000small data = { 'X train': data['X train'][:num train], 'y train': data['y train'][:num train], 'X val': data['X val'], 'y_val': data['y val'], bn solvers = {} solvers = {} weight scales = np.logspace(-4, 0, num=20) for i, weight scale in enumerate(weight scales): print('Running weight scale {} / {}'.format(i + 1, len(weight scales))) bn model = FullyConnectedNet(hidden dims, weight scale=weight scale, use batchnorm=True) model = FullyConnectedNet(hidden dims, weight scale=weight scale, use batchnorm=False) bn solver = Solver(bn model, small data, num epochs=10, batch size=50, update rule='adam', optim config={ 'learning rate': 1e-3, verbose=False, print every=200) bn solver.train() bn solvers[weight_scale] = bn_solver solver = Solver(model, small data, num epochs=10, batch size=50, update rule='adam', optim config={ 'learning_rate': 1e-3, verbose=False, print every=200) solver.train() solvers[weight scale] = solver Running weight scale 1 / 20 Running weight scale 2 / 20 Running weight scale 3 / 20 Running weight scale 4 / 20 Running weight scale 5 / 20 Running weight scale 6 / 20 Running weight scale 7 / 20 Running weight scale 8 / 20 Running weight scale 9 / 20 Running weight scale 10 / 20 Running weight scale 11 / 20Running weight scale 12 / 20 Running weight scale 13 / 20 Running weight scale 14 / 20Running weight scale 15 / 20 Running weight scale 16 / 20 /Users/siddie/Desktop/Winter-2022/NN & DL/Neural Networks & Deep Learning/HW4/hw4-code/nndl/layers.py:444: Runt imeWarning: divide by zero encountered in log loss = -np.sum(np.log(probs[np.arange(N), y])) / N Running weight scale 17 / 20 Running weight scale 18 / 20 Running weight scale 19 / 20 Running weight scale 20 / 20 # Plot results of weight scale experiment best_train_accs, bn_best_train_accs = [], [] best_val_accs, bn_best_val_accs = [], [] final_train_loss, bn_final_train_loss = [], [] for ws in weight_scales: best_train_accs.append(max(solvers[ws].train_acc_history)) bn_best_train_accs.append(max(bn_solvers[ws].train_acc_history)) best_val_accs.append(max(solvers[ws].val_acc_history)) bn best val accs.append(max(bn solvers[ws].val acc history)) final_train_loss.append(np.mean(solvers[ws].loss_history[-100:])) bn_final_train_loss.append(np.mean(bn_solvers[ws].loss_history[-100:])) plt.subplot(3, 1, 1) plt.title('Best val accuracy vs weight initialization scale') plt.xlabel('Weight initialization scale') plt.ylabel('Best val accuracy') plt.semilogx(weight_scales, best_val_accs, '-o', label='baseline') plt.semilogx(weight_scales, bn_best_val_accs, '-o', label='batchnorm') plt.legend(ncol=2, loc='lower right') plt.subplot(3, 1, 2) plt.title('Best train accuracy vs weight initialization scale') plt.xlabel('Weight initialization scale') plt.ylabel('Best training accuracy') plt.semilogx(weight_scales, best_train_accs, '-o', label='baseline') plt.semilogx(weight_scales, bn_best_train_accs, '-o', label='batchnorm') plt.legend() plt.subplot(3, 1, 3) plt.title('Final training loss vs weight initialization scale') plt.xlabel('Weight initialization scale') plt.ylabel('Final training loss') plt.semilogx(weight_scales, final_train_loss, '-o', label='baseline') plt.semilogx(weight_scales, bn_final_train_loss, '-o', label='batchnorm') plt.legend() plt.gcf().set_size_inches(10, 15) plt.show() Best val accuracy vs weight initialization scale 0.35 0.30 0.25 Val 0.20 0.15 batchnorm baseline 10-3 10-4 10^{-2} 10^{-1} 10° Weight initialization scale Best train accuracy vs weight initialization scale 0.7 baseline batchnorm 0.6 Best training accuracy 0.3 0.2 0.1 10-3 10^{-4} 10^{-2} 10^{-1} 10° Weight initialization scale Final training loss vs weight initialization scale baseline 3.5 batchnorm 3.0 Final training loss 2.0 1.5 10^{-2} 10-1 10^{-4} 10^{-3} 10° Weight initialization scale Question: In the cell below, summarize the findings of this experiment, and WHY these results make sense. **Answer:** You fill this in. Batchnorm makes the model less sensitive to the initialization of the weights and bias parameters. As seen in the loss figure, the loss function of the model with batchnorm highlighted in orange is consistent with deviation no more than 0.3 units. But, in the case of baseline model, we can see the effect of random weight initialisation on the loss (Chaning from 2.3 to 1). With batchnorm, the training and validation accuracies are less sensitive to weight initializations in comparison with baseline model.