Convolutional neural networks In this notebook, we'll put together our convolutional layers to implement a 3-layer CNN. Then, we'll ask you to implement a CNN that can achieve > 65% validation error on CIFAR-10. If you have not completed the Spatial BatchNorm Notebook, please see the following description from that notebook: Please copy and paste your prior implemented code from HW #4 to start this assignment. If you did not correctly implement the layers in HW #4, you may collaborate with a classmate to use their layer implementations from HW #4. You may also visit TA or Prof OH to correct your implementation. You'll want to copy and paste from HW #4: layers.py for your FC network layers, as well as batchnorm and dropout. layer_utils.py for your combined FC network layers. optim.py for your optimizers. Be sure to place these in the nndl/ directory so they're imported correctly. Note, as announced in class, we will not be releasing our solutions. # As usual, a bit of setup import numpy as np import matplotlib.pyplot as plt from nndl.cnn import * from utils.data utils import get CIFAR10 data from utils.gradient check import eval numerical gradient array, eval numerical gradient from nndl.layers import * from nndl.conv layers import * from utils.fast layers import * from utils.solver import Solver %matplotlib inline plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots plt.rcParams['image.interpolation'] = 'nearest' plt.rcParams['image.cmap'] = 'gray' # for auto-reloading external modules # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython %load_ext autoreload %autoreload 2 def rel error(x, y): """ returns relative error """ return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))# Load the (preprocessed) CIFAR10 data. data = get CIFAR10 data() for k in data.keys(): print('{}: {} '.format(k, data[k].shape)) X train: (49000, 3, 32, 32) y train: (49000,) X val: (1000, 3, 32, 32) y_val: (1000,) X test: (1000, 3, 32, 32) y test: (1000,) Three layer CNN In this notebook, you will implement a three layer CNN. The ThreeLayerConvNet class is in nndl/cnn.py . You'll need to modify that code for this section, including the initialization, as well as the calculation of the loss and gradients. You should be able to use the building blocks you have either earlier coded or that we have provided. Be sure to use the fast layers. The architecture of this CNN will be: conv - relu - 2x2 max pool - affine - relu - affine - softmax We won't use batchnorm yet. You've also done enough of these to know how to debug; use the cells below. Note: As we are implementing several layers CNN networks. The gradient error can be expected for the eval_numerical_gradient() function. If your W1 max relative error and W2 max relative error are around or below 0.01, they should be acceptable. Other errors should be less than 1e-5. num inputs = 2input dim = (3, 16, 16)reg = 0.0num classes = 10 X = np.random.randn(num inputs, *input dim) y = np.random.randint(num classes, size=num inputs) model = ThreeLayerConvNet(num filters=3, filter size=3, input dim=input dim, hidden dim=7, dtype=np.float64) loss, grads = model.loss(X, y) for param name in sorted(grads): f = lambda : model.loss(X, y)[0]param grad num = eval numerical gradient(f, model.params[param name], verbose=False, h=1e-6) e = rel error(param grad num, grads[param name]) print('{} max relative error: {}'.format(param name, rel error(param grad num, grads[param name]))) W1 max relative error: 0.0039229543503380366 W2 max relative error: 0.0026798963346064695 W3 max relative error: 2.9185899895921736e-05 b1 max relative error: 1.0766309395490432e-05 b2 max relative error: 2.2296973510371742e-07 b3 max relative error: 6.236824694894559e-10 Overfit small dataset To check your CNN implementation, let's overfit a small dataset. num train = 100small data = { 'X train': data['X train'][:num train], 'y train': data['y train'][:num train], 'X val': data['X_val'], 'y val': data['y val'], model = ThreeLayerConvNet(weight scale=1e-2) solver = Solver(model, small data, num epochs=10, batch size=50, update rule='adam', optim config={ 'learning rate': 1e-3, verbose=True, print every=1) solver.train() (Iteration 1 / 20) loss: 2.325183 (Epoch 0 / 10) train acc: 0.210000; val acc: 0.128000 (Iteration 2 / 20) loss: 2.859539 (Epoch 1 / 10) train acc: 0.210000; val acc: 0.106000 (Iteration 3 / 20) loss: 2.675631 (Iteration 4 / 20) loss: 2.547447 (Epoch 2 / 10) train acc: 0.280000; val acc: 0.134000 (Iteration 5 / 20) loss: 2.490574 (Iteration 6 / 20) loss: 1.855074 (Epoch 3 / 10) train acc: 0.330000; val acc: 0.207000 (Iteration 7 / 20) loss: 1.787314 (Iteration 8 / 20) loss: 1.835055 (Epoch 4 / 10) train acc: 0.580000; val acc: 0.188000 (Iteration 9 / 20) loss: 1.258561 (Iteration 10 / 20) loss: 1.211132 (Epoch 5 / 10) train acc: 0.590000; val acc: 0.160000 (Iteration 11 / 20) loss: 1.245911 (Iteration 12 / 20) loss: 1.075001 (Epoch 6 / 10) train acc: 0.620000; val acc: 0.216000 (Iteration 13 / 20) loss: 1.038730 (Iteration 14 / 20) loss: 1.117598 (Epoch 7 / 10) train acc: 0.820000; val acc: 0.233000 (Iteration 15 / 20) loss: 0.750677 (Iteration 16 / 20) loss: 0.685618 (Epoch 8 / 10) train acc: 0.860000; val acc: 0.228000 (Iteration 17 / 20) loss: 0.566079 (Iteration 18 / 20) loss: 0.350751 (Epoch 9 / 10) train acc: 0.890000; val acc: 0.212000 (Iteration 19 / 20) loss: 0.537815 (Iteration 20 / 20) loss: 0.680158 (Epoch 10 / 10) train acc: 0.900000; val acc: 0.200000 plt.subplot(2, 1, 1) plt.plot(solver.loss history, 'o') plt.xlabel('iteration') plt.ylabel('loss') plt.subplot(2, 1, 2) plt.plot(solver.train acc history, '-o') plt.plot(solver.val acc history, '-o') plt.legend(['train', 'val'], loc='upper left') plt.xlabel('epoch') plt.ylabel('accuracy') plt.show() 2.5 2.0 088 1.5 1.0 0.5 2.5 0.0 5.0 7.5 10.0 12.5 15.0 17.5 iteration val 0.8 0.7 0.6 accuracy 0.5 0.4 0.3 0.2 0.1 6 epoch Train the network Now we train the 3 layer CNN on CIFAR-10 and assess its accuracy. In [9]: model = ThreeLayerConvNet(weight scale=0.001, hidden dim=500, reg=0.001) solver = Solver(model, data, num_epochs=1, batch_size=50, update rule='adam', optim config={ 'learning rate': 1e-3, verbose=True, print every=20) solver.train() (Iteration 1 / 980) loss: 2.304519 (Epoch 0 / 1) train acc: 0.106000; val acc: 0.112000 (Iteration 21 / 980) loss: 2.182474 (Iteration 41 / 980) loss: 2.055637 (Iteration 61 / 980) loss: 2.015527 (Iteration 81 / 980) loss: 1.747509 (Iteration 101 / 980) loss: 1.673627 (Iteration 121 / 980) loss: 1.732240 (Iteration 141 / 980) loss: 1.475226 (Iteration 161 / 980) loss: 2.027153 (Iteration 181 / 980) loss: 1.699494 (Iteration 201 / 980) loss: 1.612863 (Iteration 221 / 980) loss: 1.778262 (Iteration 241 / 980) loss: 1.614608 (Iteration 261 / 980) loss: 1.940361 (Iteration 281 / 980) loss: 1.713780 (Iteration 301 / 980) loss: 1.626900 (Iteration 321 / 980) loss: 1.719155 (Iteration 341 / 980) loss: 1.748550 (Iteration 361 / 980) loss: 1.797033 (Iteration 381 / 980) loss: 1.465187 (Iteration 401 / 980) loss: 1.706747 (Iteration 421 / 980) loss: 1.710475 (Iteration 441 / 980) loss: 1.930407 (Iteration 461 / 980) loss: 1.862908 (Iteration 481 / 980) loss: 1.555936 (Iteration 501 / 980) loss: 1.362443 (Iteration 521 / 980) loss: 1.781068 (Iteration 541 / 980) loss: 1.379948 (Iteration 561 / 980) loss: 1.765419 (Iteration 581 / 980) loss: 1.440890 (Iteration 601 / 980) loss: 1.304435 (Iteration 621 / 980) loss: 1.564034 (Iteration 641 / 980) loss: 1.584206 (Iteration 661 / 980) loss: 1.427583 (Iteration 681 / 980) loss: 1.564917 (Iteration 701 / 980) loss: 1.631626 (Iteration 721 / 980) loss: 1.434416 (Iteration 741 / 980) loss: 1.559580 (Iteration 761 / 980) loss: 1.206771 (Iteration 781 / 980) loss: 1.836259 (Iteration 801 / 980) loss: 1.917589 (Iteration 821 / 980) loss: 1.501216 (Iteration 841 / 980) loss: 1.640303 (Iteration 861 / 980) loss: 1.363111 (Iteration 881 / 980) loss: 1.430887 (Iteration 901 / 980) loss: 1.516662 (Iteration 921 / 980) loss: 1.494434 (Iteration 941 / 980) loss: 1.473915 (Iteration 961 / 980) loss: 1.385337 (Epoch 1 / 1) train acc: 0.459000; val acc: 0.472000 Get > 65% validation accuracy on CIFAR-10. In the last part of the assignment, we'll now ask you to train a CNN to get better than 65% validation accuracy on CIFAR-10. Things you should try: • Filter size: Above we used 7x7; but VGGNet and onwards showed stacks of 3x3 filters are good. Number of filters: Above we used 32 filters. Do more or fewer do better? • Batch normalization: Try adding spatial batch normalization after convolution layers and vanilla batch normalization aafter affine layers. Do your networks train faster? • Network architecture: Can a deeper CNN do better? Consider these architectures: [conv-relu-pool]xN - conv - relu - [affine]xM - [softmax or SVM] [conv-relu-pool]XN - [affine]XM - [softmax or SVM] [conv-relu-conv-relu-pool]xN - [affine]xM - [softmax or SVM] Tips for training For each network architecture that you try, you should tune the learning rate and regularization strength. When doing this there are a couple important things to keep in mind: If the parameters are working well, you should see improvement within a few hundred iterations • Remember the coarse-to-fine approach for hyperparameter tuning: start by testing a large range of hyperparameters for just a few training iterations to find the combinations of parameters that are working at all. • Once you have found some sets of parameters that seem to work, search more finely around these parameters. You may need to train for more epochs. # Implement a CNN to achieve greater than 65% validation accuracy model = ThreeLayerConvNet(weight scale = 0.001, hidden dim = 500, reg = 0.001,num filters = 64, filter size = 3) solver = Solver(model, data, num epochs=10, batch size=500, update rule='adam', optim config={ 'learning_rate': 1e-3, 1r decay=0.9, verbose=True, print every=15) solver.train() # print out the validation and test accuracy y val max = np.argmax(model.loss(data['X val']), axis=1) y test max = np.argmax(model.loss(data['X test']), axis=1) print('Validation set accuracy: {}'.format(np.mean(y val max == data['y val']))) print('Test set accuracy: {}'.format(np.mean(y_test_max == data['y_test']))) # END YOUR CODE HERE (Iteration 1 / 980) loss: 2.306750 (Epoch 0 / 10) train acc: 0.104000; val acc: 0.112000 (Iteration 16 / 980) loss: 1.875861 (Iteration 31 / 980) loss: 1.727335 (Iteration 46 / 980) loss: 1.612002 (Iteration 61 / 980) loss: 1.544193 (Iteration 76 / 980) loss: 1.309349 (Iteration 91 / 980) loss: 1.281215 (Epoch 1 / 10) train acc: 0.581000; val acc: 0.560000 (Iteration 106 / 980) loss: 1.282992 (Iteration 121 / 980) loss: 1.291973 (Iteration 136 / 980) loss: 1.204956 (Iteration 151 / 980) loss: 1.190480 (Iteration 166 / 980) loss: 1.251083 (Iteration 181 / 980) loss: 1.172586 (Iteration 196 / 980) loss: 1.131847 (Epoch 2 / 10) train acc: 0.620000; val acc: 0.603000 (Iteration 211 / 980) loss: 1.066770 (Iteration 226 / 980) loss: 1.084402 (Iteration 241 / 980) loss: 1.083245 (Iteration 256 / 980) loss: 1.114625 (Iteration 271 / 980) loss: 1.018875 (Iteration 286 / 980) loss: 1.014123 (Epoch 3 / 10) train acc: 0.661000; val acc: 0.631000 (Iteration 301 / 980) loss: 1.093395 (Iteration 316 / 980) loss: 0.965458 (Iteration 331 / 980) loss: 0.992495 (Iteration 346 / 980) loss: 0.982317 (Iteration 361 / 980) loss: 0.904174 (Iteration 376 / 980) loss: 0.926157 (Iteration 391 / 980) loss: 0.906463 (Epoch 4 / 10) train acc: 0.726000; val acc: 0.634000 (Iteration 406 / 980) loss: 0.950047 (Iteration 421 / 980) loss: 0.885359 (Iteration 436 / 980) loss: 0.863559 (Iteration 451 / 980) loss: 0.946079 (Iteration 466 / 980) loss: 0.789447 (Iteration 481 / 980) loss: 0.820740 (Epoch 5 / 10) train acc: 0.769000; val acc: 0.640000 (Iteration 496 / 980) loss: 0.825014 (Iteration 511 / 980) loss: 0.730814 (Iteration 526 / 980) loss: 0.865063 (Iteration 541 / 980) loss: 0.873117 (Iteration 556 / 980) loss: 0.704718 (Iteration 571 / 980) loss: 0.757800 (Iteration 586 / 980) loss: 0.783915 (Epoch 6 / 10) train acc: 0.761000; val acc: 0.653000 (Iteration 601 / 980) loss: 0.718778 (Iteration 616 / 980) loss: 0.746557 (Iteration 631 / 980) loss: 0.739426 (Iteration 646 / 980) loss: 0.729680 (Iteration 661 / 980) loss: 0.708834 (Iteration 676 / 980) loss: 0.851334 (Epoch 7 / 10) train acc: 0.817000; val acc: 0.678000 (Iteration 691 / 980) loss: 0.657606 (Iteration 706 / 980) loss: 0.691037 (Iteration 721 / 980) loss: 0.640211 (Iteration 736 / 980) loss: 0.663333 (Iteration 751 / 980) loss: 0.630992 (Iteration 766 / 980) loss: 0.613800 (Iteration 781 / 980) loss: 0.610026 (Epoch 8 / 10) train acc: 0.850000; val acc: 0.672000 (Iteration 796 / 980) loss: 0.684875 (Iteration 811 / 980) loss: 0.645196 (Iteration 826 / 980) loss: 0.505507 (Iteration 841 / 980) loss: 0.593875 (Iteration 856 / 980) loss: 0.594060 (Iteration 871 / 980) loss: 0.525813 (Epoch 9 / 10) train acc: 0.831000; val acc: 0.666000 (Iteration 886 / 980) loss: 0.531386 (Iteration 901 / 980) loss: 0.499404 (Iteration 916 / 980) loss: 0.545275 (Iteration 931 / 980) loss: 0.495120 (Iteration 946 / 980) loss: 0.449716 (Iteration 961 / 980) loss: 0.481002 (Iteration 976 / 980) loss: 0.520237 (Epoch 10 / 10) train acc: 0.883000; val acc: 0.676000 Validation set accuracy: 0.678 Test set accuracy: 0.661 CNN.py import numpy as np from nndl.layers import * from nndl.conv layers import * from utils.fast layers import * from nndl.layer utils import * from nndl.conv layer utils import * import pdb class ThreeLayerConvNet(object): A three-layer convolutional network with the following architecture: conv - relu - 2x2 max pool - affine - relu - affine - softmax The network operates on minibatches of data that have shape (N, C, H, W) consisting of N images, each with height H and width W and with C input channels. def __init__(self, input_dim=(3, 32, 32), num filters=32, filter size=7, hidden dim=100, num classes=10, weight scale=1e-3, reg=0.0, dtype=np.float32, use batchnorm=False): - input dim: Tuple (C, H, W) giving size of input data - num filters: Number of filters to use in the convolutional layer - filter size: Size of filters to use in the convolutional layer - hidden dim: Number of units to use in the fully-connected hidden layer - num classes: Number of scores to produce from the final affine layer. - weight scale: Scalar giving standard deviation for random initialization of weights. - reg: Scalar giving L2 regularization strength - dtype: numpy datatype to use for computation. self.use batchnorm = use_batchnorm self.params = {} self.reg = reg self.dtype = dtype # ----- # # YOUR CODE HERE: Initialize the weights and biases of a three layer CNN. To initialize: - the biases should be initialized to zeros. - the weights should be initialized to a matrix with entries drawn from a Gaussian distribution with zero mean and standard deviation given by weight scale. # ----- # C, H, W = input dim size W1 = (num filters, C, filter size, filter size) size b1 = num filters Con_output = (num_filters, C, H, W) $size_W2 = (hidden_dim, (H//2) * (W//2) * num_filters)$ size b2 = hidden dimsize_W3 = (num_classes, hidden_dim) size b3 = num classes self.params['W1'] = np.random.normal(loc=0.0, scale=weight_scale, size = size_W1) self.params['b1'] = np.zeros(size_b1) self.params['W2'] = np.random.normal(loc=0.0,scale=weight_scale,size = size_W2).T self.params['b2'] = np.zeros(size_b2) self.params['W3'] = np.random.normal(loc=0.0,scale=weight_scale,size = size_W3).T self.params['b3'] = np.zeros(size b3) # ----- # # END YOUR CODE HERE for k, v in self.params.items(): self.params[k] = v.astype(dtype) def loss(self, X, y=None): Evaluate loss and gradient for the three-layer convolutional network. Input / output: Same API as TwoLayerNet in fc net.py. W1, b1 = self.params['W1'], self.params['b1'] W2, b2 = self.params['W2'], self.params['b2'] W3, b3 = self.params['W3'], self.params['b3'] # pass conv param to the forward pass for the convolutional layer filter size = W1.shape[2] conv param = {'stride': 1, 'pad': (filter size - 1) / 2} # pass pool param to the forward pass for the max-pooling layer pool param = {'pool height': 2, 'pool width': 2, 'stride': 2} # ------ # # YOUR CODE HERE: Implement the forward pass of the three layer CNN. Store the output scores as the variable "scores". layer1 out, combined cache = conv relu pool forward(X, W1, b1, conv param, pool param) fc1 out, fc1 cache = affine relu forward(layer1 out, W2, b2) scores, fc2 cache = affine forward(fc1 out, W3, b3) # END YOUR CODE HERE if y is None: return scores loss, grads = 0, {} # YOUR CODE HERE: Implement the backward pass of the three layer CNN. Store the grads in the grads dictionary, exactly as before (i.e., the gradient of self.params[k] will be grads[k]). Store the loss as "loss", and # don't forget to add regularization on ALL weight matrices. # ----- # loss, dscores = softmax loss(scores, y) loss += self.reg * 0.5 * (np.sum(np.square(W1)) + np.sum(np.square(W2)) + np.sum(np.square(W3))) dx3, dw3, db3 = affine backward(dscores, fc2 cache) dx2, dw2, db2 = affine relu backward(dx3, fc1 cache) dx1, dw1, db1 = conv relu pool backward(<math>dx2, combined cache) grads['W3'], grads['b3'] = dw3 + self.reg * W3, db3grads['W2'], grads['b2'] = dw2 + self.reg * W2, db2grads['W1'], grads['b1'] = dw1 + self.reg * W1, db1 # END YOUR CODE HERE return loss, grads pass Conv_layers.py import numpy as np from nndl.layers import * import pdb def conv_forward_naive(x, w, b, conv_param): A naive implementation of the forward pass for a convolutional layer. The input consists of N data points, each with C channels, height H and width W. We convolve each input with F different filters, where each filter spans all C channels and has height HH and width HH. Input: - x: Input data of shape (N, C, H, W) - w: Filter weights of shape (F, C, HH, WW) - b: Biases, of shape (F,) - conv_param: A dictionary with the following keys: 'stride': The number of pixels between adjacent receptive fields in the horizontal and vertical directions. - 'pad': The number of pixels that will be used to zero-pad the input. Returns a tuple of: - out: Output data, of shape (N, F, H', W') where H' and W' are given by H' = 1 + (H + 2 * pad - HH) / strideW' = 1 + (W + 2 * pad - WW) / stride- cache: (x, w, b, conv param) out = None pad = conv param['pad'] stride = conv param['stride'] # YOUR CODE HERE: Implement the forward pass of a convolutional neural network. Store the output as 'out'. Hint: to pad the array, you can use the function np.pad. # ----- # N, C, H, W = x.shapeF, C, HH, WW = w.shapepadded x = (np.pad(x, ((0, 0), (0, 0), (pad, pad), (pad, pad)), 'constant')) $out_height = np.int(((H + 2 * pad - HH) / stride) + 1)$ out width = np.int(((W + 2 * pad - WW) / stride) + 1)out = np.zeros([N, F, out height, out width]) for img in range(N): for kernal in range(F): for row in range(out height): for col in range(out width): out[img, kernal, row, col] = np.sum(w[kernal, ...] * \ padded x[imq, :, row*stride:row*stride+HH, col*stride:col*stride # END YOUR CODE HERE cache = (x, w, b, conv param)return out, cache def conv backward naive(dout, cache): A naive implementation of the backward pass for a convolutional layer. Inputs: - dout: Upstream derivatives. - cache: A tuple of (x, w, b, conv param) as in conv forward naive Returns a tuple of: - dx: Gradient with respect to x - dw: Gradient with respect to w - db: Gradient with respect to b dx, dw, db = None, None, NoneN, F, out height, out width = dout.shape x, w, b, conv param = cache stride, pad = [conv param['stride'], conv param['pad']] xpad = np.pad(x, ((0,0), (0,0), (pad,pad), (pad,pad)), mode='constant')num_filts, _, f_height, f_width = w.shape # YOUR CODE HERE: Implement the backward pass of a convolutional neural network. # Calculate the gradients: dx, dw, and db. _, _, H, W = x.shape # [N, 3, 32, 32]dx_temp = np.zeros_like(xpad) # initial to all zeros dw = np.zeros like(w)db = np.zeros like(b)# Calculate dB. for kernal in range(F): db[kernal] += np.sum(dout[:, kernal, :, :]) # sum all N img's kernal -> [32, 32], then sum all 32x32 eleme # Calculate dw. for img in range(N): # for each image for kernal in range(F): # for each kernal for row in range(out height): # from top to bottom for col in range(out width): # from left to right dw[kernal, ...] += dout[img, kernal, row, col] * xpad[img, :, row*stride:row*stride+f height, col*str # Calculate dx. for img in range(N): # for each image for kernal in range(F): # for each kernal for row in range(out height): # from top to bottom for col in range(out width): # from left to right dx temp[img, :, row*stride:row*stride+f height, col*stride:col*stride+f width] += dout[img, kernal, r dx = dx temp[:, :, pad:H+pad, pad:W+pad]# END YOUR CODE HERE return dx, dw, db def max pool forward naive(x, pool param): A naive implementation of the forward pass for a max pooling layer. Inputs: - x: Input data, of shape (N, C, H, W) - pool param: dictionary with the following keys: 'pool height': The height of each pooling region - 'pool width': The width of each pooling region - 'stride': The distance between adjacent pooling regions Returns a tuple of: - out: Output data - cache: (x, pool param) out = None # YOUR CODE HERE: # Implement the max pooling forward pass. pool height = pool param.get('pool height') pool width = pool param.get('pool width') stride = pool param.get('stride') N, C, H, W = x.shapeout_height = np.int(((H - pool_height) / stride) + 1) $out_width = np.int(((W - pool_width) / stride) + 1)$ out = np.zeros([N, C, out height, out width]) for img in range(N): for channel in range(C): for row in range(out height): for col in range (out width): out[img, channel, row, col] = np.max(x[img, channel, row*stride:row*stride+pool height, col*stride:co # END YOUR CODE HERE cache = (x, pool param)return out, cache def max pool backward naive(dout, cache): A naive implementation of the backward pass for a max pooling layer. Inputs: - dout: Upstream derivatives - cache: A tuple of (x, pool param) as in the forward pass. - dx: Gradient with respect to x dx = None x, pool param = cache pool height, pool width, stride = pool param['pool height'], pool param['pool width'], pool param['stride'] # ----- # # YOUR CODE HERE: # Implement the max pooling backward pass. N, C, H, W = x.shape _, _, dout_height, dout_width = dout.shape dx = np.zeros like(x)for img in range(N): for channel in range(C): for row in range(dout height): for col in range(dout width): max idx = np.argmax(x[img, channel, row*stride:row*stride+pool height, col*stride:col*stride+pool wid max position = np.unravel index(max idx, [pool height, pool width]) dx[img, channel, row*stride:row*stride+pool height, col*stride:col*stride+pool width][max position] = # END YOUR CODE HERE return dx def spatial batchnorm forward(x, gamma, beta, bn param): Computes the forward pass for spatial batch normalization. Inputs: - x: Input data of shape (N, C, H, W) - gamma: Scale parameter, of shape (C,) - beta: Shift parameter, of shape (C,) - bn param: Dictionary with the following keys: - mode: 'train' or 'test'; required - eps: Constant for numeric stability - momentum: Constant for running mean / variance. momentum=0 means that old information is discarded completely at every time step, while momentum=1 means that new information is never incorporated. The default of momentum=0.9 should work well in most situations. - running mean: Array of shape (D,) giving running mean of features - running var Array of shape (D,) giving running variance of features Returns a tuple of: - out: Output data, of shape (N, C, H, W) - cache: Values needed for the backward pass out, cache = None, None # YOUR CODE HERE: Implement the spatial batchnorm forward pass. # You may find it useful to use the batchnorm forward pass you # implemented in HW #4. # ============ # N, C, H, W = x.shape # [N, 3, 32, 32]x transpose = x.transpose(0, 2, 3, 1) $x_reshape = np.reshape(x_transpose, (N*H*W, C)) # reshape to 2D to do batchnorm$ out 2d, cache = batchnorm forward(x reshape, gamma, beta, bn param) out = out 2d.reshape((N, H, W, C)).transpose(0, 3, 1, 2) # reshape back # ----- # # END YOUR CODE HERE return out, cache def spatial batchnorm backward(dout, cache): Computes the backward pass for spatial batch normalization. Inputs: - dout: Upstream derivatives, of shape (N, C, H, W) - cache: Values from the forward pass Returns a tuple of: - dx: Gradient with respect to inputs, of shape (N, C, H, W) - dgamma: Gradient with respect to scale parameter, of shape (C,) - dbeta: Gradient with respect to shift parameter, of shape (C,) dx, dgamma, dbeta = None, None, None # YOUR CODE HERE: Implement the spatial batchnorm backward pass. # You may find it useful to use the batchnorm forward pass you # implemented in HW #4. # ----- # dx = np.zeros like(dout)N, C, H, W = dout.shapedout transpose = dout.transpose((0, 2, 3, 1)) dout reshape = np.reshape(dout transpose, (N*H*W, C)) # reshape to 2D to do batchnorm dx 2d, dgamma, dbeta = batchnorm backward(dout reshape, cache) $dx = dx_2d.reshape((N, H, W, C)).transpose(0, 3, 1, 2) # reshape back$ # END YOUR CODE HERE return dx, dgamma, dbeta Layers.py

The content of the	dx dw db # # #	<pre>w, b = cache , dw, db = None, None, None ===================================</pre>
### 1995	م م	<pre>= np.reshape(dx_reshape, x.shape) # N * D = x_reshape.T.dot(dout) # D * M = dout.T.dot(np.ones(x.shape[0])) # M * 1 ==================================</pre>
# March 19 10 10 10 10 10 10 10 10 10 10 10 10 10	In - Re	mputes the forward pass for a layer of rectified linear units (ReLUs). put: x: Inputs, of any shape turns a tuple of: out: Output, of the same shape as x cache: x
### 1995	# # # ou #	# YOUR CODE HERE: Implement the ReLU forward pass. ===================================
The content of the	ca re ef ""	<pre>che = x turn out, cache relu_backward(dout, cache): " mputes the backward pass for a layer of rectified linear units (ReLUs).</pre>
The content of the co	- Re - """ x	<pre>cache: Input x, of same shape as dout turns: dx: Gradient with respect to x " = cache =</pre>
	# dx # #	= (x > 0) * (dout) ===================================
The control of the co	Fo Du co Du an	rward pass for batch normalization. ring training the sample mean and (uncorrected) sample variance are mputed from minibatch statistics and used to normalize the incoming data. ring training we also keep an exponentially decaying running mean of the mean d variance of each feature, and these averages are used to normalize data
When make a register and regist	ru ru No be	exponential decay based on the momentum parameter: nning_mean = momentum * running_mean + (1 - momentum) * sample_mean nning_var = momentum * running_var + (1 - momentum) * sample_var te that the batch normalization paper suggests a different test-time havior: they compute sample mean and variance for each feature using a rge number of training images rather than using a running average. For
Section of the control of the contro	th of In	ey do not require an additional estimation step; the torch7 implementation batch normalization also uses running averages. put: x: Data of shape (N, D) gamma: Scale parameter of shape (D,) beta: Shift paremeter of shape (D,) bn_param: Dictionary with the following keys: - mode: 'train' or 'test'; required
Security of the polar polar polar content of the	Re-	<pre>- momentum: Constant for running mean / variance running_mean: Array of shape (D,) giving running mean of features - running_var Array of shape (D,) giving running variance of features turns a tuple of: out: of shape (N, D) cache: A tuple of values needed in the backward pass " de = bn_param['mode']</pre>
A CONTRACTOR OF THE CONTRACTOR	N, ru ru ou if	<pre>mentum = bn_param.get('momentum', 0.9) D = x.shape nning_mean = bn_param.get('running_mean', np.zeros(D, dtype=x.dtype)) nning_var = bn_param.get('running_var', np.zeros(D, dtype=x.dtype)) t, cache = None, None mode == 'train':</pre>
And the control of th		# A few steps here: # (1) Calculate the running mean and variance of the minibatch. # (2) Normalize the activations with the running mean and variance. # (3) Scale and shift the normalized activations. Store this # as the variable 'out' # (4) Store any variables you may need for the backward pass in # the 'cache' variable. # ====================================
The control of the co		<pre>minibatch_var = np.var(x, axis=0) x_normalize = (x - minibatch_mean) / np.sqrt(minibatch_var + eps) out = gamma * x_normalize + beta running_mean = momentum * running_mean + (1 - momentum) * minibatch_mean running_var = momentum * running_var + (1 - momentum) * minibatch_var bn_param['running_mean'] = running_mean bn_param['running_var'] = running_var</pre>
### Common Commo		<pre>'minibatch_var': minibatch_var, 'x_centralize': (x - minibatch_mean), 'x_normalize': x_normalize, 'gamma': gamma, 'eps': eps } # ===================================</pre>
A CONTRACTOR CONTRACTO		<pre>if mode == 'test': # ===================================</pre>
and process of the control of the co	el	# ========== # # END YOUR CODE HERE # ========== # se: raise ValueError('Invalid forward batchnorm mode "%s"' % mode)
Section of the control of the contro	bn bn re ef "" Ba	<pre>_param['running_mean'] = running_mean _param['running_var'] = running_var turn out, cache batchnorm_backward(dout, cache): " ckward pass for batch normalization. r this implementation, you should write out a computation graph for</pre>
The control of the co	ba in In - - Re	tch normalization on paper and propagate gradients backward through termediate nodes. puts: dout: Upstream derivatives, of shape (N, D) cache: Variable of intermediates from batchnorm_forward. turns a tuple of: dx: Gradient with respect to inputs x, of shape (N, D) dgamma: Gradient with respect to scale parameter gamma, of shape (D,)
The process of the process of the control of the process of the pr	- dx # # # #	dbeta: Gradient with respect to shift parameter beta, of shape (D,) " , dgamma, dbeta = None, None, None
Suggi and any experience of a posterior set, section (1) and a sec	mi x_x_ga ep # dx dx sq	<pre>nibatch_var = cache.get('minibatch_var') centralize = cache.get('x_centralize') normalize = cache.get('x_normalize') mma = cache.get('gamma') s = cache.get('eps') calculate dx hat = dout * gamma mul = dxhat / np.sqrt(minibatch_var + eps) rt_var = np.sqrt(minibatch_var + eps)</pre>
Power manufactures come: **Contract Contract (Indiana)** **Indiana Contract (Indiana)** **Contract Contract (Indiana)** **Contract Contract (Indiana)** **Contract Contract (Indiana)** **Contract Contract (Indiana)** **The contract (Indiana)** **Contract Co	ds dv dx dx dx dx dx dx	<pre>qrt_var = -np.sum(dxhat * x_centralize, axis=0) / (sqrt_var**2) ar = dsqrt_var * 0.5 / sqrt_var mu2 = 2 * x_centralize * dvar * np.ones_like(dout) / N 1 = dxmu1 + dxmu2 2 = -np.sum(dx1, axis=0) * np.ones_like(dout) / N = dx1 + dx2 calculate dbeta and dgamma eta = np.sum(dout, axis=0)</pre>
Compared position of any analyse	# # re	turn dx, dgamma, dbeta dropout_forward(x, dropout_param):
- Since the rest independent and the content of the rest took, must be too decreed and that was been to multiply the injury of the rest took, must be budget by most and second partial by the injury of the rest took, must be budget by most and second partial by the injury of the rest took, must be budget by most and second partial by the rest took of the rest to	_	 x: Input data, of any shape dropout_param: A dictionary with the following keys: - p: Dropout parameter. We drop each neuron output with probability p. - mode: 'test' or 'train'. If the mode is train, then perform dropout; if the mode is test, then just return the input. - seed: Seed for the random number generator. Passing seed makes this function deterministic, which is needed for gradient checking but not in
if mode = 'trach': 2 Your cook state: 2 Annual mode to the enterpress analyses contact pace decays tracking time. 3 Annual mode in the enterpress and a cook a catherina in out, and those the enterpress mode. 3 Annual = 'trach': 2 Your cape state: 4 Your cape state: 5 Your cape state: 5 Your cape state: 5 Your cape state: 6 Your cape state: 7 Your cape state: 7 Your cape state: 8 Your cape state: 9 Your cape state: 9 Your cape state: 1 Your cape state: 1 Your cape state: 1 Your cape state: 2 Your cape state: 2 Your cape state: 2 Your cape state: 2 Your cape state: 3 Your cape state: 4 Your cape state: 5 Your cape state: 5 Your cape state: 6 Your cape state: 7 Your cape state: 8 Your cape state: 9 Your cape state: 1 Your cape state: 2 Your cape state: 2 Your cape state: 2 Your cape state: 2 Your cape state: 3 Your cape state: 4 Your cape state: 5 Your cape state: 6 Your cape state: 7 Your cape state: 8 Your cape state: 9 Your cape state: 1 Your cape state: 2 Your cape state: 1 Your cape state: 2 Your cape state: 2 Your cape state: 3 Your cape state: 4 Your cape state: 5 Your cape state: 5 Your cape state: 6 Your cape state: 7 Your cape state: 8 Your cape state: 9 Your cape state: 1 Your cape state: 2 Your cape state: 2 Your cape state: 2 Your cape state: 2 Your cape state: 3 Your cape state: 4 Your cape state: 5 Your cape state: 6 Your cape state: 7 Your cape state: 9 Your cape state: 1 Your cape s	- "" p, if	out: Array of the same shape as x. cache: A tuple (dropout_param, mask). In training mode, mask is the dropout mask that was used to multiply the input; in test mode, mask is None. " mode = dropout_param['p'], dropout_param['mode'] 'seed' in dropout_param: np.random.seed(dropout_param['seed'])
Substitute of the control of the con	ou if	<pre>mode == 'train': # ====================================</pre>
couls = X = 2009 POOR COOR MERE 2 = 2009 POOR COOR MERE 2 = 2009 POOR COOR MERE 3 = 2009 POOR COOR MERE 4 = 2009 POOR COOR MERE 5 = 2009 POOR COOR MERE 5 = 2009 POOR COOR MERE 5 = 2009 POOR COOR MERE 6 = 2009 POOR COOR MERE 6 = 2009 POOR MERE 7 = 2009 POOR POOR POOR POOR POOR POOR POOR POO	el	out = x * mask # # # END YOUR CODE HERE # # # if mode == 'test': # #
return out, cache ff discount backward(dout, cache): "Pusions the backward(dout, cache): "pusion of the backward(dout, cache): "pus	ca	# ======== # out = x # ========= # # END YOUR CODE HERE # ========= # che = (dropout_param, mask)
corport param, mosk = cache mode = desport param, mosk = cache mode = desport param, mode = cache mode = desport param, mode) the = Mone if mode == 'train': \$ * YOUR COCS MERG: \$ * Liminomer the inverted despont backward pass during training time. \$ * MONE COCS MERG: \$ * END YOUR COCS MERG: \$ * YOUR COCS MERG: \$ * YOUR COCS MERG: \$ * SAD YOUR COCS MERG: \$ * S	ef "" Pe In	dropout_backward(dout, cache): " rform the backward pass for (inverted) dropout. puts:
### Spice of the inversed dropout backward pass during training time.	- dr mo	<pre>dout: Upstream derivatives, of any shape cache: (dropout_param, mask) from dropout_forward. " opout_param, mask = cache de = dropout_param['mode'] = None mode == 'train':</pre>
<pre>f Your Cook MERE: f Toplement the inverted dropout backward pass during test time. f EAU YOUR COOK HERE f END YOUR COOK HERE f = FEWN YOUR COOK H</pre>		# YOUR CODE HERE: # Implement the inverted dropout backward pass during training time. # ====================================
return dx of sym_loss(x, y): "new Computes the loss and gradient using for multiclass SVM classification. Inputs: -x: Input data, of shape (N, C) where x[i, j] is the score for the jth class for the ith input. -y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and 0 <= y[i] < C Returns a tuple of: -loss: Scalar giving the loss -dx: Gradient of the loss with respect to x """ N = x.shape[0] correct_class_scores = x[np.arange(N), y] margins = np.maximum(0, x - correct_class_scores[:, np.newaxis] + 1.0) margins = np.sum(margins) / N num_pos = np.sum(margins) / N vector of labels, of shape (N, c) where x[i, j] is the score for the jth class for the ith input. -y: Vector of labels, of shape (N, where y[i] is the label for x[i] and 0 <- y[i] < C Returns a tuple of: -loss: Scalar giving the loss -dx: Gradient of the loss with respect to x """ probs = np.exp(x - np.max(x, axis=1, keepdims=True)) probs np.exp(x - np.max(x, axis=1, keepdims=True)) probs np.sum(probs, axis=1, keepdims=True)) probs np.sum(probs, axis=1, keepdims=True)) probs np.sum(probs, axis=1, keepdims=True)) N = x.shape[0] loss = -np.sum(nplog(probs[np.arange(N), y])) / N dx probs.copy() dx(np.arange(N), y] = 1		# ========= # # YOUR CODE HERE: # Implement the inverted dropout backward pass during test time. # ======= # dx = dout # ========= # # END YOUR CODE HERE
<pre>D <= y[i] < C Returns a tuple of: loss: Scalar giving the loss dx: Gradient of the loss with respect to x """ N = x.shape[0] correct_class_scores = x[np.arange(N), y] margins = np.maxinum(0, x - correct_class_scores[:, np.newaxis] + 1.0) margins[np.arange(N), y] = 0 loss = np.sum(margins) / N num_pos = np.sum(margins) > 0, axis=1) dx = np.zeros_like(x) dx[mp.arange(N), y] -= num_pos dx /= N return loss, dx ef softmax_loss(x, y): """ Computes the loss and gradient for softmax classification. Inputs: -x: Input data, of shape (N, C) where x[i, j] is the score for the jth class for the ith input. -y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and 0 <= y[i] < C Returns a tuple of: -loss: Scalar giving the loss -dx: Gradient of the loss with respect to x """ probs = np.exp(x - np.max(x, axis=1, keepdims=True)) probs /= np.sum(np.log(probs[np.arange(N), y])) / N dx = probs.copy() dx(np.arange(N), y] -= 1 dx /= N</pre>	ef "" Co In	<pre>turn dx svm_loss(x, y): " mputes the loss and gradient using for multiclass SVM classification. puts: x: Input data, of shape (N, C) where x[i, j] is the score for the jth class</pre>
<pre>margins[np.arange(N), y] = 0 loss = np.sum(margins) / N num_pos = np.sum(margins) > 0, axis=1) dx = np.zeros_like(x) dx[margins > 0] = 1 dx[np.arange(N), y] -= num_pos dx /= N return loss, dx ef softmax_loss(x, y): """ Computes the loss and gradient for softmax classification. Inputs: - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class for the ith input y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and 0 <= y[i] < C Returns a tuple of: - loss: Scalar giving the loss - dx: Gradient of the loss with respect to x """ probs = np.exp(x - np.max(x, axis=1, keepdims=True)) probs /= np.sum(probs, axis=1, keepdims=True) N = x.shape[0] loss = -np.sum(np.log(probs[np.arange(N), y])) / N dx = probs.copy() dx[np.arange(N), y] -= 1 dx/e /= N</pre>	Re - N CO	<pre>y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and 0 <= y[i] < C turns a tuple of: loss: Scalar giving the loss dx: Gradient of the loss with respect to x " = x.shape[0] rrect_class_scores = x[np.arange(N), y]</pre>
<pre>Computes the loss and gradient for softmax classification. Inputs: - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class for the ith input y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and 0 <= y[i] < C Returns a tuple of: - loss: Scalar giving the loss - dx: Gradient of the loss with respect to x """ probs = np.exp(x - np.max(x, axis=1, keepdims=True)) probs /= np.sum(probs, axis=1, keepdims=True) N = x.shape[0] loss = -np.sum(np.log(probs[np.arange(N), y])) / N dx = probs.copy() dx[np.arange(N), y] -= 1 dx /= N</pre>	ma lo nu dx dx dx dx	<pre>rgins[np.arange(N), y] = 0 ss = np.sum(margins) / N m_pos = np.sum(margins > 0, axis=1) = np.zeros_like(x) [margins > 0] = 1 [np.arange(N), y] -= num_pos /= N</pre>
<pre>- loss: Scalar giving the loss - dx: Gradient of the loss with respect to x """ probs = np.exp(x - np.max(x, axis=1, keepdims=True)) probs /= np.sum(probs, axis=1, keepdims=True) N = x.shape[0] loss = -np.sum(np.log(probs[np.arange(N), y])) / N dx = probs.copy() dx[np.arange(N), y] -= 1 dx /= N</pre>	Co In	mputes the loss and gradient for softmax classification. puts: x: Input data, of shape (N, C) where x[i, j] is the score for the jth class for the ith input. y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
dx[np.arange(N), y] = 1 dx /= N	pr pr N	<pre>loss: Scalar giving the loss dx: Gradient of the loss with respect to x " obs = np.exp(x - np.max(x, axis=1, keepdims=True)) obs /= np.sum(probs, axis=1, keepdims=True) = x.shape[0] ss = -np.sum(np.log(probs[np.arange(N), y])) / N</pre>
	dx dx dx	<pre>= probs.copy() [np.arange(N), y] -= 1 /= N</pre>

import numpy as np
import pdb

Inputs:

Returns a tuple of:

YOUR CODE HERE:

END YOUR CODE HERE

cache = (x, w, b)
return out, cache

- out: output, of shape (N, M)
- cache: (x, w, b)

def affine_forward(x, w, b):

Computes the forward pass for an affine (fully-connected) layer.

The input x has shape (N, d_1 , ..., d_k) and contains a minibatch of N

examples, where each example x[i] has shape (d_1, \ldots, d_k) . We will reshape each input into a vector of dimension $D = d_1 * \ldots * d_k$, and then transform it to an output vector of dimension M.

x: A numpy array containing input data, of shape (N, d_1, ..., d_k)
w: A numpy array of weights, of shape (D, M)
b: A numpy array of biases, of shape (M,)

Calculate the output of the forward pass. Notice the dimensions # of w are D x M, which is the transpose of what we did in earlier # assignments.
