ECE C147/247 HW4 Q3: Dropout

In this notebook, you will implement dropout. Then we will ask you to train a network with batchnorm and dropout, and acheive over 55% accuracy on CIFAR-10.

`utils` has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes `nndl.fc_net`, `nndl.layers`, and `nndl.layer_utils`.

In [1]:
```
## Import and setups

import time
import numpy as np
import matplotlib.pyplot as plt
from nndl.fc_net import *
from nndl.layers import *
from utils.data_utils import get_CIFAR10_data
from utils.gradient_check import eval_numerical_gradient, eval_numerical_gradient_array
from utils.solver import Solver

%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
%load_ext autoreload
%autoreload 2

def rel_error(x, y):
  """ returns relative error """
  return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

In [2]:
```
# Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
for k in data.keys():
  print('{}: {} '.format(k, data[k].shape))
```

```
X_train: (49000, 3, 32, 32)
y_train: (49000,)
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

Dropout forward pass

Implement the training and test time dropout forward pass, `dropout_forward`, in `nndl/layers.py`. After that, test your implementation by running the following cell.

In [3]:
```
x = np.random.randn(500, 500) + 10

for p in [0.3, 0.6, 0.75]:
  out, _ = dropout_forward(x, {'mode': 'train', 'p': p})
  out_test, _ = dropout_forward(x, {'mode': 'test', 'p': p})

  print('Running tests with p = ', p)
  print('Mean of input: ', x.mean())
  print('Mean of train-time output: ', out.mean())
  print('Mean of test-time output: ', out_test.mean())
  print('Fraction of train-time output set to zero: ', (out == 0).mean())
  print('Fraction of test-time output set to zero: ', (out_test == 0).mean())
```

```
Running tests with p =  0.3
Mean of input:  9.99685010214567
Mean of train-time output:  9.973354144793436
Mean of test-time output:  9.99685010214567
Fraction of train-time output set to zero:  0.301636
Fraction of test-time output set to zero:  0.0
Running tests with p =  0.6
Mean of input:  9.99685010214567
Mean of train-time output:  9.995998684721517
Mean of test-time output:  9.99685010214567
Fraction of train-time output set to zero:  0.599936
Fraction of test-time output set to zero:  0.0
Running tests with p =  0.75
Mean of input:  9.99685010214567
Mean of train-time output:  10.00209523824298
Mean of test-time output:  9.99685010214567
Fraction of train-time output set to zero:  0.749776
Fraction of test-time output set to zero:  0.0
```

Dropout backward pass

Implement the backward pass, `dropout_backward`, in `nndl/layers.py`. After that, test your gradients by running the following cell:

In [4]:
```
x = np.random.randn(10, 10) + 10
dout = np.random.randn(*x.shape)

dropout_param = {'mode': 'train', 'p': 0.8, 'seed': 123}
out, cache = dropout_forward(x, dropout_param)
dx = dropout_backward(dout, cache)
dx_num = eval_numerical_gradient_array(lambda xx: dropout_forward(xx, dropout_param)[0], x, dout)

print('dx relative error: ', rel_error(dx, dx_num))
```

```
dx relative error:  1.892906988930252e-11
```

Implement a fully connected neural network with dropout layers

Modify the `FullyConnectedNet()` class in `nndl/fc_net.py` to incorporate dropout. A dropout layer should be incorporated after every ReLU layer. Concretely, there shouldn't be a dropout at the output layer since there is no ReLU at the output layer. You will need to modify the class in the following areas:

(1) In the forward pass, you will need to incorporate a dropout layer after every relu layer.

(2) In the backward pass, you will need to incorporate a dropout backward pass layer.

Check your implementation by running the following code. Our W1 gradient relative error is on the order of 1e-6 (the largest of all the relative errors).

In [5]:
```
N, D, H1, H2, C = 2, 15, 20, 30, 10
X = np.random.randn(N, D)
y = np.random.randint(C, size=(N,))

for dropout in [0, 0.25, 0.5]:
  print('Running check with dropout = ', dropout)
  model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C,
                            weight_scale=5e-2, dtype=np.float64,
                            dropout=dropout, seed=123)

  loss, grads = model.loss(X, y)
  print('Initial loss: ', loss)

  for name in sorted(grads):
    f = lambda _: model.loss(X, y)[0]
    grad_num = eval_numerical_gradient(f, model.params[name], verbose=False, h=1e-5)
    print('{} relative error: {}'.format(name, rel_error(grad_num, grads[name])))
  print('\n')
```

```
Running check with dropout =  0
Initial loss:  2.3051948273987857
W1 relative error: 2.5272575382129597e-07
W2 relative error: 1.5034484922161239e-05
W3 relative error: 2.7534468139587135e-07
b1 relative error: 2.936957506391204e-06
b2 relative error: 5.0513393785120424e-08
b3 relative error: 1.1740467838205477e-10


Running check with dropout =  0.25
Initial loss:  2.3052077546540826
W1 relative error: 2.6138469533439284e-07
W2 relative error: 5.022056554497157e-07
W3 relative error: 4.4563160427353564e-08
b1 relative error: 7.397117495005868e-08
b2 relative error: 7.151679404650099e-10
b3 relative error: 1.003974732116764e-10


Running check with dropout =  0.5
Initial loss:  2.3035667586595423
W1 relative error: 1.1401257489261862e-06
W2 relative error: 1.847669394519882e-07
W3 relative error: 6.5966195253431734e-09
b1 relative error: 7.716395914021063e-08
b2 relative error: 1.1975910493629166e-09
b3 relative error: 1.4558471033827801e-10
```

Dropout as a regularizer

In class, we claimed that dropout acts as a regularizer by effectively bagging. To check this, we will train two small networks, one with dropout and one without dropout.

In [6]:
```
# Train two identical nets, one with dropout and one without

num_train = 500
small_data = {
  'X_train': data['X_train'][:num_train],
  'y_train': data['y_train'][:num_train],
  'X_val': data['X_val'],
  'y_val': data['y_val'],
}

solvers = {}
dropout_choices = [0, 0.6]
for dropout in dropout_choices:
  model = FullyConnectedNet([100, 100, 100], dropout=dropout)

  solver = Solver(model, small_data,
                  num_epochs=25, batch_size=100,
                  update_rule='adam',
                  optim_config={
                    'learning_rate': 5e-4,
                  },
                  verbose=True, print_every=100)
  solver.train()
  solvers[dropout] = solver
```

```
(Iteration 1 / 125) loss: 2.300804
(Epoch 0 / 25) train acc: 0.220000; val_acc: 0.168000
(Epoch 1 / 25) train acc: 0.188000; val_acc: 0.147000
(Epoch 2 / 25) train acc: 0.266000; val_acc: 0.200000
(Epoch 3 / 25) train acc: 0.338000; val_acc: 0.262000
(Epoch 4 / 25) train acc: 0.378000; val_acc: 0.278000
(Epoch 5 / 25) train acc: 0.428000; val_acc: 0.297000
(Epoch 6 / 25) train acc: 0.468000; val_acc: 0.323000
(Epoch 7 / 25) train acc: 0.494000; val_acc: 0.287000
(Epoch 8 / 25) train acc: 0.566000; val_acc: 0.328000
(Epoch 9 / 25) train acc: 0.572000; val_acc: 0.322000
(Epoch 10 / 25) train acc: 0.622000; val_acc: 0.324000
(Epoch 11 / 25) train acc: 0.670000; val_acc: 0.279000
(Epoch 12 / 25) train acc: 0.710000; val_acc: 0.338000
(Epoch 13 / 25) train acc: 0.746000; val_acc: 0.319000
(Epoch 14 / 25) train acc: 0.792000; val_acc: 0.307000
(Epoch 15 / 25) train acc: 0.834000; val_acc: 0.297000
(Epoch 16 / 25) train acc: 0.876000; val_acc: 0.327000
(Epoch 17 / 25) train acc: 0.886000; val_acc: 0.320000
(Epoch 18 / 25) train acc: 0.918000; val_acc: 0.314000
(Epoch 19 / 25) train acc: 0.922000; val_acc: 0.290000
(Epoch 20 / 25) train acc: 0.944000; val_acc: 0.306000
(Iteration 101 / 125) loss: 0.156105
(Epoch 21 / 25) train acc: 0.968000; val_acc: 0.302000
(Epoch 22 / 25) train acc: 0.978000; val_acc: 0.302000
(Epoch 23 / 25) train acc: 0.976000; val_acc: 0.289000
(Epoch 24 / 25) train acc: 0.986000; val_acc: 0.285000
(Epoch 25 / 25) train acc: 0.978000; val_acc: 0.311000
(Iteration 1 / 125) loss: 2.298716
(Epoch 0 / 25) train acc: 0.132000; val_acc: 0.146000
(Epoch 1 / 25) train acc: 0.118000; val_acc: 0.131000
(Epoch 2 / 25) train acc: 0.220000; val_acc: 0.214000
(Epoch 3 / 25) train acc: 0.206000; val_acc: 0.180000
(Epoch 4 / 25) train acc: 0.220000; val_acc: 0.193000
(Epoch 5 / 25) train acc: 0.264000; val_acc: 0.229000
(Epoch 6 / 25) train acc: 0.268000; val_acc: 0.203000
(Epoch 7 / 25) train acc: 0.266000; val_acc: 0.212000
(Epoch 8 / 25) train acc: 0.282000; val_acc: 0.236000
(Epoch 9 / 25) train acc: 0.310000; val_acc: 0.255000
(Epoch 10 / 25) train acc: 0.320000; val_acc: 0.267000
(Epoch 11 / 25) train acc: 0.338000; val_acc: 0.273000
(Epoch 12 / 25) train acc: 0.346000; val_acc: 0.278000
(Epoch 13 / 25) train acc: 0.332000; val_acc: 0.279000
(Epoch 14 / 25) train acc: 0.328000; val_acc: 0.284000
(Epoch 15 / 25) train acc: 0.354000; val_acc: 0.271000
(Epoch 16 / 25) train acc: 0.386000; val_acc: 0.277000
(Epoch 17 / 25) train acc: 0.388000; val_acc: 0.297000
(Epoch 18 / 25) train acc: 0.402000; val_acc: 0.280000
(Epoch 19 / 25) train acc: 0.388000; val_acc: 0.274000
(Epoch 20 / 25) train acc: 0.386000; val_acc: 0.274000
(Iteration 101 / 125) loss: 1.919649
(Epoch 21 / 25) train acc: 0.402000; val_acc: 0.272000
(Epoch 22 / 25) train acc: 0.440000; val_acc: 0.286000
(Epoch 23 / 25) train acc: 0.458000; val_acc: 0.295000
(Epoch 24 / 25) train acc: 0.462000; val_acc: 0.311000
(Epoch 25 / 25) train acc: 0.466000; val_acc: 0.297000
```

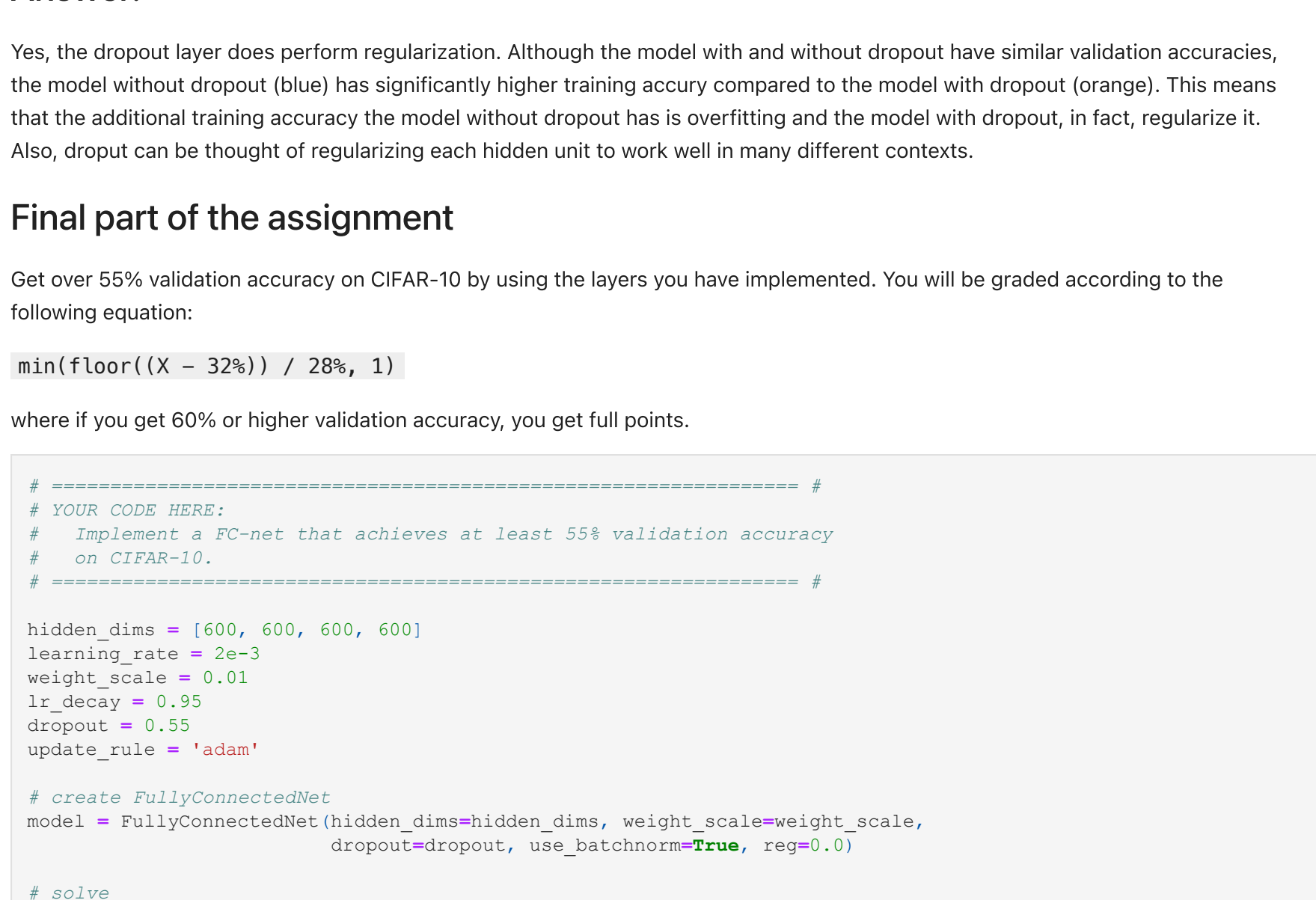
In [7]:
```
# Plot train and validation accuracies of the two models

train_accs = []
val_accs = []
for dropout in dropout_choices:
  solver = solvers[dropout]
  train_accs.append(solver.train_acc_history[-1])
  val_accs.append(solver.val_acc_history[-1])

plt.subplot(3, 1, 1)
for dropout in dropout_choices:
  plt.plot(solvers[dropout].train_acc_history, 'o', label='%.2f dropout' % dropout)
plt.title('Train accuracy')
plt.xlabel('Epoch')
plt.ylabel('Accuracy')
plt.legend(ncol=2, loc='lower right')

plt.subplot(3, 1, 2)
for dropout in dropout_choices:
  plt.plot(solvers[dropout].val_acc_history, 'o', label='%.2f dropout' % dropout)
plt.title('Val accuracy')
plt.xlabel('Epoch')
plt.ylabel('Accuracy')
plt.legend(ncol=2, loc='lower right')

plt.gcf().set_size_inches(15, 15)
plt.show()
```



Question

Based off the results of this experiment, is dropout performing regularization? Explain your answer.

Answer:

Yes, the dropout layer does perform regularization. Although the model with and without dropout have similar validation accuracies, the model without dropout (blue) has significantly higher training accury compared to the model with dropout (orange). This means that the additional training accuracy the model without dropout has is overfitting and the model with dropout, in fact, regularize it. Also, droput can be thought of regularizing each hidden unit to work well in many different contexts.

Final part of the assignment

Get over 55% validation accuracy on CIFAR-10 by using the layers you have implemented. You will be graded according to the following equation:

`min(floor((X - 32%)) / 28%, 1)`

where if you get 60% or higher validation accuracy, you get full points.

In [9]:
```
# ================================================================ #
# YOUR CODE HERE:
#   Implement a FC-net that achieves at least 55% validation accuracy
#   on CIFAR-10.
# ================================================================ #

hidden_dims = [600, 600, 600, 600]
learning_rate = 2e-3
weight_scale = 0.01
lr_decay = 0.95
dropout = 0.55
update_rule = 'adam'

# create FullyConnectedNet
model = FullyConnectedNet(hidden_dims=hidden_dims, weight_scale=weight_scale,
                          dropout=dropout, use_batchnorm=True, reg=0.0)

# solve
solver = Solver(model, data,
              num_epochs=100, batch_size=100,
              update_rule=update_rule,
              optim_config={
                'learning_rate': learning_rate,
              },
              lr_decay=lr_decay,
              verbose=True, print_every=100)
solver.train()

# print out the validation accuracy
y_test_pred = np.argmax(model.loss(data['X_test']), axis=1)
y_val_pred = np.argmax(model.loss(data['X_val']), axis=1)
print('Validation set accuracy: {}'.format(np.mean(y_val_pred == data['y_val'])))
print('Test set accuracy: {}'.format(np.mean(y_test_pred == data['y_test'])))


# ================================================================ #
# END YOUR CODE HERE
# ================================================================ #
```

```
(Iteration 1 / 49000) loss: 2.368804
(Epoch 0 / 100) train acc: 0.185000; val_acc: 0.167000
(Iteration 101 / 49000) loss: 1.862784
(Iteration 201 / 49000) loss: 1.807049
(Iteration 301 / 49000) loss: 1.745462
(Iteration 401 / 49000) loss: 1.755246
(Epoch 1 / 100) train acc: 0.418000; val_acc: 0.438000
(Iteration 501 / 49000) loss: 1.707795
(Iteration 601 / 49000) loss: 1.741667
(Iteration 701 / 49000) loss: 1.721698
(Iteration 801 / 49000) loss: 1.446650
(Iteration 901 / 49000) loss: 1.553775
(Epoch 2 / 100) train acc: 0.490000; val_acc: 0.458000
(Iteration 1001 / 49000) loss: 1.891812
(Iteration 1101 / 49000) loss: 1.525608
(Iteration 1201 / 49000) loss: 1.562973
(Iteration 1301 / 49000) loss: 1.481514
(Iteration 1401 / 49000) loss: 1.561436
(Epoch 3 / 100) train acc: 0.507000; val_acc: 0.488000
(Iteration 1501 / 49000) loss: 1.469753
(Iteration 1601 / 49000) loss: 1.493207
(Iteration 1701 / 49000) loss: 1.414905
(Iteration 1801 / 49000) loss: 1.325406
(Iteration 1901 / 49000) loss: 1.476521
(Epoch 4 / 100) train acc: 0.511000; val_acc: 0.497000
(Iteration 2001 / 49000) loss: 1.366378
(Iteration 2101 / 49000) loss: 1.435045
(Iteration 2201 / 49000) loss: 1.594414
(Iteration 2301 / 49000) loss: 1.445463
(Iteration 2401 / 49000) loss: 1.424264
(Epoch 5 / 100) train acc: 0.529000; val_acc: 0.514000
(Iteration 2501 / 49000) loss: 1.543489
(Iteration 2601 / 49000) loss: 1.365315
(Iteration 2701 / 49000) loss: 1.511149
(Iteration 2801 / 49000) loss: 1.629832
(Iteration 2901 / 49000) loss: 1.535492
(Epoch 6 / 100) train acc: 0.523000; val_acc: 0.524000
(Iteration 3001 / 49000) loss: 1.651523
(Iteration 3101 / 49000) loss: 1.404341
(Iteration 3201 / 49000) loss: 1.321157
(Iteration 3301 / 49000) loss: 1.326001
(Iteration 3401 / 49000) loss: 1.494231
(Epoch 7 / 100) train acc: 0.566000; val_acc: 0.524000
(Iteration 3501 / 49000) loss: 1.351739
(Iteration 3601 / 49000) loss: 1.660494
(Iteration 3701 / 49000) loss: 1.394698
(Iteration 3801 / 49000) loss: 1.499673
(Iteration 3901 / 49000) loss: 1.292914
(Epoch 8 / 100) train acc: 0.553000; val_acc: 0.539000
(Iteration 4001 / 49000) loss: 1.580306
(Iteration 4101 / 49000) loss: 1.417105
(Iteration 4201 / 49000) loss: 1.438272
(Iteration 4301 / 49000) loss: 1.368299
(Iteration 4401 / 49000) loss: 1.386760
(Epoch 9 / 100) train acc: 0.560000; val_acc: 0.537000
(Iteration 4501 / 49000) loss: 1.303273
(Iteration 4601 / 49000) loss: 1.329969
(Iteration 4701 / 49000) loss: 1.316058
(Iteration 4801 / 49000) loss: 1.219810
(Epoch 10 / 100) train acc: 0.575000; val_acc: 0.543000
(Iteration 4901 / 49000) loss: 1.399363
(Iteration 5001 / 49000) loss: 1.321516
(Iteration 5101 / 49000) loss: 1.323961
(Iteration 5201 / 49000) loss: 1.320811
(Iteration 5301 / 49000) loss: 1.231963
(Epoch 11 / 100) train acc: 0.614000; val_acc: 0.549000
(Iteration 5401 / 49000) loss: 1.380101
(Iteration 5501 / 49000) loss: 1.201157
(Iteration 5601 / 49000) loss: 1.203552
(Iteration 5701 / 49000) loss: 1.353704
(Iteration 5801 / 49000) loss: 1.240033
(Epoch 12 / 100) train acc: 0.590000; val_acc: 0.539000
(Iteration 5901 / 49000) loss: 1.211575
(Iteration 6001 / 49000) loss: 1.337146
(Iteration 6101 / 49000) loss: 1.416619
(Iteration 6201 / 49000) loss: 1.247955
(Iteration 6301 / 49000) loss: 1.151628
(Epoch 13 / 100) train acc: 0.607000; val_acc: 0.542000
(Iteration 6401 / 49000) loss: 1.381991
(Iteration 6501 / 49000) loss: 1.306083
(Iteration 6601 / 49000) loss: 1.263972
(Iteration 6701 / 49000) loss: 1.008625
(Iteration 6801 / 49000) loss: 1.301901
(Epoch 14 / 100) train acc: 0.598000; val_acc: 0.560000
(Iteration 6901 / 49000) loss: 1.199095
(Iteration 7001 / 49000) loss: 1.080947
(Iteration 7101 / 49000) loss: 1.390401
(Iteration 7201 / 49000) loss: 1.284882
(Iteration 7301 / 49000) loss: 1.147238
(Epoch 15 / 100) train acc: 0.627000; val_acc: 0.557000
(Iteration 7401 / 49000) loss: 1.127628
(Iteration 7501 / 49000) loss: 1.229679
(Iteration 7601 / 49000) loss: 1.302084
(Iteration 7701 / 49000) loss: 1.223759
(Iteration 7801 / 49000) loss: 1.164815
(Epoch 16 / 100) train acc: 0.626000; val_acc: 0.552000
(Iteration 7901 / 49000) loss: 1.247635
(Iteration 8001 / 49000) loss: 1.171963
(Iteration 8101 / 49000) loss: 0.995238
(Iteration 8201 / 49000) loss: 1.239742
(Iteration 8301 / 49000) loss: 1.239255
(Epoch 17 / 100) train acc: 0.641000; val_acc: 0.571000
(Iteration 8401 / 49000) loss: 1.429346
(Iteration 8501 / 49000) loss: 1.204427
(Iteration 8601 / 49000) loss: 1.075615
(Iteration 8701 / 49000) loss: 1.016951
(Iteration 8801 / 49000) loss: 1.217487
(Epoch 18 / 100) train acc: 0.674000; val_acc: 0.564000
(Iteration 8901 / 49000) loss: 1.307140
(Iteration 9001 / 49000) loss: 1.055895
(Iteration 9101 / 49000) loss: 1.105365
(Iteration 9201 / 49000) loss: 1.181401
(Iteration 9301 / 49000) loss: 1.010250
(Epoch 19 / 100) train acc: 0.655000; val_acc: 0.570000
(Iteration 9401 / 49000) loss: 1.164261
(Iteration 9501 / 49000) loss: 1.243444
(Iteration 9601 / 49000) loss: 1.288294
(Iteration 9701 / 49000) loss: 0.994167
(Epoch 20 / 100) train acc: 0.665000; val_acc: 0.571000
(Iteration 9801 / 49000) loss: 1.118267
(Iteration 9901 / 49000) loss: 1.331903
(Iteration 10001 / 49000) loss: 1.065374
(Iteration 10101 / 49000) loss: 1.172186
(Iteration 10201 / 49000) loss: 1.291121
(Epoch 21 / 100) train acc: 0.646000; val_acc: 0.563000
(Iteration 10301 / 49000) loss: 1.069844
(Iteration 10401 / 49000) loss: 1.136097
(Iteration 10501 / 49000) loss: 0.939506
(Iteration 10601 / 49000) loss: 1.282977
(Iteration 10701 / 49000) loss: 1.209112
(Epoch 22 / 100) train acc: 0.673000; val_acc: 0.575000
(Iteration 10801 / 49000) loss: 1.071739
(Iteration 10901 / 49000) loss: 1.163670
(Iteration 11001 / 49000) loss: 1.026890
(Iteration 11101 / 49000) loss: 1.250122
(Iteration 11201 / 49000) loss: 1.240166
(Epoch 23 / 100) train acc: 0.673000; val_acc: 0.576000
(Iteration 11301 / 49000) loss: 0.958271
(Iteration 11401 / 49000) loss: 1.024924
(Iteration 11501 / 49000) loss: 0.957055
(Iteration 11601 / 49000) loss: 1.035051
(Iteration 11701 / 49000) loss: 1.153221
(Epoch 24 / 100) train acc: 0.665000; val_acc: 0.572000
(Iteration 11801 / 49000) loss: 1.157622
(Iteration 11901 / 49000) loss: 1.166782
(Iteration 12001 / 49000) loss: 1.240300
(Iteration 12101 / 49000) loss: 0.965574
(Iteration 12201 / 49000) loss: 1.010264
(Epoch 25 / 100) train acc: 0.653000; val_acc: 0.572000
(Iteration 12301 / 49000) loss: 1.030296
(Iteration 12401 / 49000) loss: 1.113278
(Iteration 12501 / 49000) loss: 1.169410
(Iteration 12601 / 49000) loss: 1.136060
(Iteration 12701 / 49000) loss: 1.283430
(Epoch 26 / 100) train acc: 0.697000; val_acc: 0.561000
(Iteration 12801 / 49000) loss: 0.989076
(Iteration 12901 / 49000) loss: 1.106504
(Iteration 13001 / 49000) loss: 0.971786
(Iteration 13101 / 49000) loss: 1.165516
(Iteration 13201 / 49000) loss: 1.105684
(Epoch 27 / 100) train acc: 0.690000; val_acc: 0.569000
(Iteration 13301 / 49000) loss: 1.022431
(Iteration 13401 / 49000) loss: 1.059711
(Iteration 13501 / 49000) loss: 1.174263
(Iteration 13601 / 49000) loss: 1.094403
(Iteration 13701 / 49000) loss: 1.054292
(Epoch 28 / 100) train acc: 0.710000; val_acc: 0.572000
(Iteration 13801 / 49000) loss: 1.114179
(Iteration 13901 / 49000) loss: 1.257944
(Iteration 14001 / 49000) loss: 1.069323
(Iteration 14101 / 49000) loss: 1.113557
(Iteration 14201 / 49000) loss: 0.946266
(Epoch 29 / 100) train acc: 0.691000; val_acc: 0.561000
(Iteration 14301 / 49000) loss: 1.047627
(Iteration 14401 / 49000) loss: 1.037860
(Iteration 14501 / 49000) loss: 0.938981
(Iteration 14601 / 49000) loss: 1.200740
(Epoch 30 / 100) train acc: 0.684000; val_acc: 0.573000
(Iteration 14701 / 49000) loss: 1.037305
(Iteration 14801 / 49000) loss: 1.272926
(Iteration 14901 / 49000) loss: 0.900214
(Iteration 15001 / 49000) loss: 1.175724
(Iteration 15101 / 49000) loss: 1.055826
(Epoch 31 / 100) train acc: 0.690000; val_acc: 0.570000
(Iteration 15201 / 49000) loss: 0.997450
(Iteration 15301 / 49000) loss: 1.073754
(Iteration 15401 / 49000) loss: 1.151598
(Iteration 15501 / 49000) loss: 1.018678
(Iteration 15601 / 49000) loss: 0.954948
(Epoch 32 / 100) train acc: 0.734000; val_acc: 0.569000
(Iteration 15701 / 49000) loss: 1.150949
(Iteration 15801 / 49000) loss: 1.041394
(Iteration 15901 / 49000) loss: 1.104018
(Iteration 16001 / 49000) loss: 0.926311
(Iteration 16101 / 49000) loss: 1.168481
(Epoch 33 / 100) train acc: 0.712000; val_acc: 0.575000
(Iteration 16201 / 49000) loss: 0.964470
(Iteration 16301 / 49000) loss: 1.182668
(Iteration 16401 / 49000) loss: 0.995676
(Iteration 16501 / 49000) loss: 1.102167
(Iteration 16601 / 49000) loss: 1.113402
(Epoch 34 / 100) train acc: 0.733000; val_acc: 0.574000
(Iteration 16701 / 49000) loss: 0.987856
(Iteration 16801 / 49000) loss: 1.012500
(Iteration 16901 / 49000) loss: 1.235728
(Iteration 17001 / 49000) loss: 1.072272
(Iteration 17101 / 49000) loss: 0.979338
(Epoch 35 / 100) train acc: 0.715000; val_acc: 0.578000
(Iteration 17201 / 49000) loss: 0.875236
(Iteration 17301 / 49000) loss: 1.016472
(Iteration 17401 / 49000) loss: 1.102627
(Iteration 17501 / 49000) loss: 1.117850
(Iteration 17601 / 49000) loss: 1.139715
(Epoch 36 / 100) train acc: 0.702000; val_acc: 0.569000
(Iteration 17701 / 49000) loss: 1.004151
(Iteration 17801 / 49000) loss: 1.030979
(Iteration 17901 / 49000) loss: 1.035874
(Iteration 18001 / 49000) loss: 0.965332
(Iteration 18101 / 49000) loss: 0.959946
(Epoch 37 / 100) train acc: 0.719000; val_acc: 0.568000
(Iteration 18201 / 49000) loss: 1.095089
(Iteration 18301 / 49000) loss: 0.887651
(Iteration 18401 / 49000) loss: 1.112029
(Iteration 18501 / 49000) loss: 1.078794
(Iteration 18601 / 49000) loss: 0.935568
(Epoch 38 / 100) train acc: 0.725000; val_acc: 0.584000
(Iteration 18701 / 49000) loss: 1.130590
(Iteration 18801 / 49000) loss: 1.035197
(Iteration 18901 / 49000) loss: 0.910668
(Iteration 19001 / 49000) loss: 1.075651
(Iteration 19101 / 49000) loss: 0.963635
(Epoch 39 / 100) train acc: 0.729000; val_acc: 0.577000
(Iteration 19201 / 49000) loss: 1.287657
(Iteration 19301 / 49000) loss: 1.003213
(Iteration 19401 / 49000) loss: 0.977760
(Iteration 19501 / 49000) loss: 0.940475
(Epoch 40 / 100) train acc: 0.738000; val_acc: 0.580000
(Iteration 19601 / 49000) loss: 0.864108
(Iteration 19701 / 49000) loss: 0.979389
(Iteration 19801 / 49000) loss: 0.988361
(Iteration 19901 / 49000) loss: 0.873222
(Iteration 20001 / 49000) loss: 0.992816
(Epoch 41 / 100) train acc: 0.757000; val_acc: 0.575000
(Iteration 20101 / 49000) loss: 0.940622
(Iteration 20201 / 49000) loss: 0.966386
(Iteration 20301 / 49000) loss: 1.298711
(Iteration 20401 / 49000) loss: 0.981520
(Iteration 20501 / 49000) loss: 0.973895
(Epoch 42 / 100) train acc: 0.723000; val_acc: 0.586000
(Iteration 20601 / 49000) loss: 0.783726
(Iteration 20701 / 49000) loss: 1.042928
(Iteration 20801 / 49000) loss: 1.031922
(Iteration 20901 / 49000) loss: 1.095034
(Iteration 21001 / 49000) loss: 0.802713
(Epoch 43 / 100) train acc: 0.741000; val_acc: 0.591000
(Iteration 21101 / 49000) loss: 0.778208
(Iteration 21201 / 49000) loss: 1.091723
(Iteration 21301 / 49000) loss: 1.115276
(Iteration 21401 / 49000) loss: 0.996474
(Iteration 21501 / 49000) loss: 0.980960
(Epoch 44 / 100) train acc: 0.750000; val_acc: 0.588000
(Iteration 21601 / 49000) loss: 1.004290
(Iteration 21701 / 49000) loss: 1.088332
(Iteration 21801 / 49000) loss: 0.977486
(Iteration 21901 / 49000) loss: 1.054688
(Iteration 22001 / 49000) loss: 1.007092
(Epoch 45 / 100) train acc: 0.772000; val_acc: 0.588000
(Iteration 22101 / 49000) loss: 1.040364
(Iteration 22201 / 49000) loss: 0.963634
(Iteration 22301 / 49000) loss: 0.955362
(Iteration 22401 / 49000) loss: 0.945201
(Iteration 22501 / 49000) loss: 0.962926
(Epoch 46 / 100) train acc: 0.744000; val_acc: 0.592000
(Iteration 22601 / 49000) loss: 0.795306
(Iteration 22701 / 49000) loss: 1.030281
(Iteration 22801 / 49000) loss: 1.033841
(Iteration 22901 / 49000) loss: 0.961851
(Iteration 23001 / 49000) loss: 0.997412
(Epoch 47 / 100) train acc: 0.752000; val_acc: 0.581000
(Iteration 23101 / 49000) loss: 1.040023
(Iteration 23201 / 49000) loss: 0.904962
(Iteration 23301 / 49000) loss: 1.039762
(Iteration 23401 / 49000) loss: 0.943500
(Iteration 23501 / 49000) loss: 1.061302
(Epoch 48 / 100) train acc: 0.730000; val_acc: 0.581000
(Iteration 23601 / 49000) loss: 0.980078
(Iteration 23701 / 49000) loss: 0.951201
(Iteration 23801 / 49000) loss: 1.124112
(Iteration 23901 / 49000) loss: 0.798422
(Iteration 24001 / 49000) loss: 0.970480
(Epoch 49 / 100) train acc: 0.773000; val_acc: 0.585000
(Iteration 24101 / 49000) loss: 0.999506
(Iteration 24201 / 49000) loss: 0.855080
(Iteration 24301 / 49000) loss: 0.861211
(Iteration 24401 / 49000) loss: 1.006833
(Epoch 50 / 100) train acc: 0.743000; val_acc: 0.578000
(Iteration 24501 / 49000) loss: 1.003164
(Iteration 24601 / 49000) loss: 0.951641
(Iteration 24701 / 49000) loss: 1.090954
(Iteration 24801 / 49000) loss: 0.918728
(Iteration 24901 / 49000) loss: 0.930378
(Epoch 51 / 100) train acc: 0.758000; val_acc: 0.588000
(Iteration 25001 / 49000) loss: 1.181985
(Iteration 25101 / 49000) loss: 0.812790
(Iteration 25201 / 49000) loss: 1.038813
(Iteration 25301 / 49000) loss: 1.071370
(Iteration 25401 / 49000) loss: 0.796176
(Epoch 52 / 100) train acc: 0.752000; val_acc: 0.585000
(Iteration 25501 / 49000) loss: 1.144954
(Iteration 25601 / 49000) loss: 0.944377
(Iteration 25701 / 49000) loss: 1.138453
(Iteration 25801 / 49000) loss: 0.990313
(Iteration 25901 / 49000) loss: 0.915563
(Epoch 53 / 100) train acc: 0.777000; val_acc: 0.577000
(Iteration 26001 / 49000) loss: 1.039719
(Iteration 26101 / 49000) loss: 1.076385
(Iteration 26201 / 49000) loss: 0.906678
(Iteration 26301 / 49000) loss: 0.930168
(Iteration 26401 / 49000) loss: 1.050276
(Epoch 54 / 100) train acc: 0.772000; val_acc: 0.581000
(Iteration 26501 / 49000) loss: 1.025582
(Iteration 26601 / 49000) loss: 1.120754
(Iteration 26701 / 49000) loss: 0.921766
(Iteration 26801 / 49000) loss: 0.977084
(Iteration 26901 / 49000) loss: 0.817611
(Epoch 55 / 100) train acc: 0.746000; val_acc: 0.583000
(Iteration 27001 / 49000) loss: 1.024761
(Iteration 27101 / 49000) loss: 0.910321
(Iteration 27201 / 49000) loss: 0.772592
(Iteration 27301 / 49000) loss: 0.977188
(Iteration 27401 / 49000) loss: 0.923547
(Epoch 56 / 100) train acc: 0.746000; val_acc: 0.576000
(Iteration 27501 / 49000) loss: 0.784866
(Iteration 27601 / 49000) loss: 0.927114
(Iteration 27701 / 49000) loss: 0.980834
(Iteration 27801 / 49000) loss: 1.156081
(Iteration 27901 / 49000) loss: 0.960951
(Epoch 57 / 100) train acc: 0.773000; val_acc: 0.581000
(Iteration 28001 / 49000) loss: 0.937897
(Iteration 28101 / 49000) loss: 0.909295
(Iteration 28201 / 49000) loss: 0.860213
(Iteration 28301 / 49000) loss: 0.853147
(Iteration 28401 / 49000) loss: 0.888216
(Epoch 58 / 100) train acc: 0.745000; val_acc: 0.579000
(Iteration 28501 / 49000) loss: 0.966800
(Iteration 28601 / 49000) loss: 0.873873
(Iteration 28701 / 49000) loss: 1.003696
(Iteration 28801 / 49000) loss: 0.898831
(Iteration 28901 / 49000) loss: 0.946593
(Epoch 59 / 100) train acc: 0.777000; val_acc: 0.584000
(Iteration 29001 / 49000) loss: 0.818414
(Iteration 29101 / 49000) loss: 0.965242
(Iteration 29201 / 49000) loss: 1.001254
(Iteration 29301 / 49000) loss: 0.932301
(Epoch 60 / 100) train acc: 0.773000; val_acc: 0.586000
(Iteration 29401 / 49000) loss: 0.877197
(Iteration 29501 / 49000) loss: 0.867969
(Iteration 29601 / 49000) loss: 1.001996
(Iteration 29701 / 49000) loss: 1.058211
(Iteration 29801 / 49000) loss: 0.889824
(Epoch 61 / 100) train acc: 0.769000; val_acc: 0.586000
(Iteration 29901 / 49000) loss: 0.817788
(Iteration 30001 / 49000) loss: 1.029092
(Iteration 30101 / 49000) loss: 0.826729
(Iteration 30201 / 49000) loss: 0.877080
(Iteration 30301 / 49000) loss: 0.888737
(Epoch 62 / 100) train acc: 0.761000; val_acc: 0.589000
(Iteration 30401 / 49000) loss: 1.044946
(Iteration 30501 / 49000) loss: 1.008125
(Iteration 30601 / 49000) loss: 1.079937
(Iteration 30701 / 49000) loss: 0.938385
(Iteration 30801 / 49000) loss: 1.110585
(Epoch 63 / 100) train acc: 0.756000; val_acc: 0.583000
(Iteration 30901 / 49000) loss: 1.069518
(Iteration 31001 / 49000) loss: 0.778256
(Iteration 31101 / 49000) loss: 0.907207
(Iteration 31201 / 49000) loss: 1.061106
(Iteration 31301 / 49000) loss: 0.853104
(Epoch 64 / 100) train acc: 0.759000; val_acc: 0.587000
(Iteration 31401 / 49000) loss: 0.984279
(Iteration 31501 / 49000) loss: 0.977298
(Iteration 31601 / 49000) loss: 0.886769
(Iteration 31701 / 49000) loss: 0.706246
(Iteration 31801 / 49000) loss: 0.938222
(Epoch 65 / 100) train acc: 0.777000; val_acc: 0.591000
(Iteration 31901 / 49000) loss: 0.966905
(Iteration 32001 / 49000) loss: 0.698999
(Iteration 32101 / 49000) loss: 1.005880
(Iteration 32201 / 49000) loss: 1.076777
(Iteration 32301 / 49000) loss: 1.008022
(Epoch 66 / 100) train acc: 0.753000; val_acc: 0.587000
(Iteration 32401 / 49000) loss: 0.936593
(Iteration 32501 / 49000) loss: 1.028871
(Iteration 32601 / 49000) loss: 1.259206
(Iteration 32701 / 49000) loss: 0.924877
(Iteration 32801 / 49000) loss: 0.997265
(Epoch 67 / 100) train acc: 0.773000; val_acc: 0.589000
(Iteration 32901 / 49000) loss: 0.916587
(Iteration 33001 / 49000) loss: 0.820689
(Iteration 33101 / 49000) loss: 0.916362
(Iteration 33201 / 49000) loss: 1.008112
(Iteration 33301 / 49000) loss: 0.876682
(Epoch 68 / 100) train acc: 0.771000; val_acc: 0.585000
(Iteration 33401 / 49000) loss: 1.410132
(Iteration 33501 / 49000) loss: 0.840992
(Iteration 33601 / 49000) loss: 0.777145
(Iteration 33701 / 49000) loss: 0.793184
(Iteration 33801 / 49000) loss: 0.689751
(Epoch 69 / 100) train acc: 0.765000; val_acc: 0.585000
(Iteration 33901 / 49000) loss: 0.962608
(Iteration 34001 / 49000) loss: 0.615425
(Iteration 34101 / 49000) loss: 0.969550
(Iteration 34201 / 49000) loss: 0.932119
(Epoch 70 / 100) train acc: 0.778000; val_acc: 0.579000
(Iteration 34301 / 49000) loss: 0.877220
(Iteration 34401 / 49000) loss: 1.062375
(Iteration 34501 / 49000) loss: 0.905724
(Iteration 34601 / 49000) loss: 0.969037
(Iteration 34701 / 49000) loss: 1.021737
(Epoch 71 / 100) train acc: 0.799000; val_acc: 0.588000
(Iteration 34801 / 49000) loss: 1.008637
(Iteration 34901 / 49000) loss: 0.971686
(Iteration 35001 / 49000) loss: 0.985582
(Iteration 35101 / 49000) loss: 0.890205
(Iteration 35201 / 49000) loss: 1.110361
(Epoch 72 / 100) train acc: 0.790000; val_acc: 0.589000
(Iteration 35301 / 49000) loss: 1.108602
(Iteration 35401 / 49000) loss: 0.878091
(Iteration 35501 / 49000) loss: 0.774451
(Iteration 35601 / 49000) loss: 1.024424
(Iteration 35701 / 49000) loss: 1.018490
(Epoch 73 / 100) train acc: 0.755000; val_acc: 0.586000
(Iteration 35801 / 49000) loss: 0.956727
(Iteration 35901 / 49000) loss: 0.936243
(Iteration 36001 / 49000) loss: 0.814536
(Iteration 36101 / 49000) loss: 1.026445
(Iteration 36201 / 49000) loss: 0.990114
(Epoch 74 / 100) train acc: 0.783000; val_acc: 0.584000
(Iteration 36301 / 49000) loss: 0.932943
(Iteration 36401 / 49000) loss: 0.982317
(Iteration 36501 / 49000) loss: 0.816908
(Iteration 36601 / 49000) loss: 1.080194
(Iteration 36701 / 49000) loss: 0.983827
(Epoch 75 / 100) train acc: 0.796000; val_acc: 0.587000
(Iteration 36801 / 49000) loss: 0.911780
(Iteration 36901 / 49000) loss: 0.919162
(Iteration 37001 / 49000) loss: 0.895114
(Iteration 37101 / 49000) loss: 0.744821
(Iteration 37201 / 49000) loss: 0.795689
(Epoch 76 / 100) train acc: 0.792000; val_acc: 0.584000
(Iteration 37301 / 49000) loss: 1.068627
(Iteration 37401 / 49000) loss: 0.960497
(Iteration 37501 / 49000) loss: 0.906046
(Iteration 37601 / 49000) loss: 0.961386
(Iteration 37701 / 49000) loss: 0.910121
(Epoch 77 / 100) train acc: 0.784000; val_acc: 0.577000
(Iteration 37801 / 49000) loss: 0.941305
(Iteration 37901 / 49000) loss: 0.988594
(Iteration 38001 / 49000) loss: 0.741209
(Iteration 38101 / 49000) loss: 1.129410
(Iteration 38201 / 49000) loss: 0.990653
(Epoch 78 / 100) train acc: 0.801000; val_acc: 0.581000
(Iteration 38301 / 49000) loss: 0.892736
(Iteration 38401 / 49000) loss: 0.790982
(Iteration 38501 / 49000) loss: 0.893479
(Iteration 38601 / 49000) loss: 0.935859
(Iteration 38701 / 49000) loss: 1.085245
(Epoch 79 / 100) train acc: 0.774000; val_acc: 0.584000
(Iteration 38801 / 49000) loss: 1.001974
(Iteration 38901 / 49000) loss: 0.924982
(Iteration 39001 / 49000) loss: 0.940076
(Iteration 39101 / 49000) loss: 0.781813
(Epoch 80 / 100) train acc: 0.801000; val_acc: 0.589000
(Iteration 39201 / 49000) loss: 0.981694
(Iteration 39301 / 49000) loss: 0.823310
(Iteration 39401 / 49000) loss: 0.942871
(Iteration 39501 / 49000) loss: 0.978009
(Iteration 39601 / 49000) loss: 0.833432
(Epoch 81 / 100) train acc: 0.781000; val_acc: 0.585000
(Iteration 39701 / 49000) loss: 0.920631
(Iteration 39801 / 49000) loss: 0.944635
(Iteration 39901 / 49000) loss: 0.873000
(Iteration 40001 / 49000) loss: 1.097199
(Iteration 40101 / 49000) loss: 0.949917
(Epoch 82 / 100) train acc: 0.784000; val_acc: 0.590000
(Iteration 40201 / 49000) loss: 0.999634
(Iteration 40301 / 49000) loss: 0.933291
(Iteration 40401 / 49000) loss: 0.747902
(Iteration 40501 / 49000) loss: 1.044417
(Iteration 40601 / 49000) loss: 1.034874
(Epoch 83 / 100) train acc: 0.774000; val_acc: 0.581000
(Iteration 40701 / 49000) loss: 0.853248
(Iteration 40801 / 49000) loss: 0.903673
(Iteration 40901 / 49000) loss: 0.774443
(Iteration 41001 / 49000) loss: 0.813548
(Iteration 41101 / 49000) loss: 1.124046
(Epoch 84 / 100) train acc: 0.781000; val_acc: 0.582000
(Iteration 41201 / 49000) loss: 0.916701
(Iteration 41301 / 49000) loss: 0.872769
(Iteration 41401 / 49000) loss: 0.730722
(Iteration 41501 / 49000) loss: 0.868039
(Iteration 41601 / 49000) loss: 0.805727
(Epoch 85 / 100) train acc: 0.782000; val_acc: 0.586000
(Iteration 41701 / 49000) loss: 0.795492
(Iteration 41801 / 49000) loss: 0.727824
(Iteration 41901 / 49000) loss: 0.809199
(Iteration 42001 / 49000) loss: 1.038341
(Iteration 42101 / 49000) loss: 0.659731
(Epoch 86 / 100) train acc: 0.800000; val_acc: 0.585000
(Iteration 42201 / 49000) loss: 0.809126
(Iteration 42301 / 49000) loss: 0.952355
(Iteration 42401 / 49000) loss: 0.717736
(Iteration 42501 / 49000) loss: 1.023665
(Iteration 42601 / 49000) loss: 0.787582
(Epoch 87 / 100) train acc: 0.787000; val_acc: 0.590000
(Iteration 42701 / 49000) loss: 0.742728
(Iteration 42801 / 49000) loss: 0.924297
(Iteration 42901 / 49000) loss: 1.093492
(Iteration 43001 / 49000) loss: 0.925003
(Iteration 43101 / 49000) loss: 1.149552
(Epoch 88 / 100) train acc: 0.782000; val_acc: 0.589000
(Iteration 43201 / 49000) loss: 0.891990
(Iteration 43301 / 49000) loss: 0.690976
(Iteration 43401 / 49000) loss: 0.874908
(Iteration 43501 / 49000) loss: 0.856239
(Iteration 43601 / 49000) loss: 1.097977
(Epoch 89 / 100) train acc: 0.775000; val_acc: 0.593000
(Iteration 43701 / 49000) loss: 0.763565
(Iteration 43801 / 49000) loss: 0.876280
(Iteration 43901 / 49000) loss: 0.967333
(Iteration 44001 / 49000) loss: 0.744472
(Epoch 90 / 100) train acc: 0.796000; val_acc: 0.585000
(Iteration 44101 / 49000) loss: 0.815871
(Iteration 44201 / 49000) loss: 0.766808
(Iteration 44301 / 49000) loss: 0.902052
(Iteration 44401 / 49000) loss: 0.844943
(Iteration 44501 / 49000) loss: 0.844524
(Epoch 91 / 100) train acc: 0.792000; val_acc: 0.583000
(Iteration 44601 / 49000) loss: 0.905785
(Iteration 44701 / 49000) loss: 0.823092
(Iteration 44801 / 49000) loss: 1.209675
(Iteration 44901 / 49000) loss: 0.968879
(Iteration 45001 / 49000) loss: 0.903965
(Epoch 92 / 100) train acc: 0.795000; val_acc: 0.586000
(Iteration 45101 / 49000) loss: 0.885516
(Iteration 45201 / 49000) loss: 0.874946
(Iteration 45301 / 49000) loss: 0.925858
(Iteration 45401 / 49000) loss: 0.862400
(Iteration 45501 / 49000) loss: 0.937819
(Epoch 93 / 100) train acc: 0.785000; val_acc: 0.590000
(Iteration 45601 / 49000) loss: 0.920478
(Iteration 45701 / 49000) loss: 0.794251
(Iteration 45801 / 49000) loss: 0.719172
(Iteration 45901 / 49000) loss: 0.824656
(Iteration 46001 / 49000) loss: 0.776993
(Epoch 94 / 100) train acc: 0.776000; val_acc: 0.589000
(Iteration 46101 / 49000) loss: 0.968397
(Iteration 46201 / 49000) loss: 0.922017
(Iteration 46301 / 49000) loss: 0.753013
(Iteration 46401 / 49000) loss: 0.842782
(Iteration 46501 / 49000) loss: 1.056771
(Epoch 95 / 100) train acc: 0.786000; val_acc: 0.585000
(Iteration 46601 / 49000) loss: 0.937924
(Iteration 46701 / 49000) loss: 1.126898
(Iteration 46801 / 49000) loss: 0.727208
(Iteration 46901 / 49000) loss: 1.149421
(Iteration 47001 / 49000) loss: 0.888218
(Epoch 96 / 100) train acc: 0.794000; val_acc: 0.585000
(Iteration 47101 / 49000) loss: 0.825604
(Iteration 47201 / 49000) loss: 0.994337
(Iteration 47301 / 49000) loss: 0.874650
(Iteration 47401 / 49000) loss: 1.115838
(Iteration 47501 / 49000) loss: 1.052833
(Epoch 97 / 100) train acc: 0.789000; val_acc: 0.585000
(Iteration 47601 / 49000) loss: 0.975527
(Iteration 47701 / 49000) loss: 0.793176
(Iteration 47801 / 49000) loss: 0.825106
(Iteration 47901 / 49000) loss: 0.962648
(Iteration 48001 / 49000) loss: 0.912906
(Epoch 98 / 100) train acc: 0.774000; val_acc: 0.584000
(Iteration 48101 / 49000) loss: 0.832927
(Iteration 48201 / 49000) loss: 0.967818
(Iteration 48301 / 49000) loss: 0.812962
(Iteration 48401 / 49000) loss: 0.723271
(Iteration 48501 / 49000) loss: 0.881264
(Epoch 99 / 100) train acc: 0.779000; val_acc: 0.586000
(Iteration 48601 / 49000) loss: 0.889207
(Iteration 48701 / 49000) loss: 0.922376
(Iteration 48801 / 49000) loss: 0.958328
(Iteration 48901 / 49000) loss: 0.827294
(Epoch 100 / 100) train acc: 0.781000; val_acc: 0.584000
Validation set accuracy: 0.591
Test set accuracy: 0.584
```

In [ ]:

```python
import numpy as np


def affine_forward(x, w, b):
  """
  Computes the forward pass for an affine (fully-connected) layer.

  The input x has shape (N, d_1, ..., d_k) and contains a minibatch of N
  examples, where each example x[i] has shape (d_1, ..., d_k). We will
  reshape each input into a vector of dimension D = d_1 * ... * d_k, and
  then transform it to an output vector of dimension M.

  Inputs:
  - x: A numpy array containing input data, of shape (N, d_1, ..., d_k)
  - w: A numpy array of weights, of shape (D, M)
  - b: A numpy array of biases, of shape (M,)

  Returns a tuple of:
  - out: output, of shape (N, M)
  - cache: (x, w, b)
  """

  # ================================================================ #
  # YOUR CODE HERE:
  #   Calculate the output of the forward pass.  Notice the dimensions
  #   of w are D x M, which is the transpose of what we did in earlier
  #   assignments.
  # ================================================================ #



  x_res = x.reshape((x.shape[0], w.shape[0])) # Shape of N * D
  out = x_res.dot(w) + b.reshape((1, b.shape[0])) # Shape of N * M


  # ================================================================ #
  # END YOUR CODE HERE
  # ================================================================ #

  cache = (x, w, b)
  return out, cache


def affine_backward(dout, cache):
  """
  Computes the backward pass for an affine layer.

  Inputs:
  - dout: Upstream derivative, of shape (N, M)
  - cache: Tuple of:
    - x: A numpy array containing input data, of shape (N, d_1, ..., d_k)
    - w: A numpy array of weights, of shape (D, M)
    - b: A numpy array of biases, of shape (M,)

  Returns a tuple of:
  - dx: Gradient with respect to x, of shape (N, d1, ..., d_k)
  - dw: Gradient with respect to w, of shape (D, M)
  - db: Gradient with respect to b, of shape (M,)
  """
  x, w, b = cache
  dx, dw, db = None, None, None

  # ================================================================ #
  # YOUR CODE HERE:
  #   Calculate the gradients for the backward pass.
  # Notice:
  #   dout is N x M
  #   dx should be N x d1 x ... x dk; it relates to dout through multiplication with w, which is D x M
  #   dw should be D x M; it relates to dout through multiplication with x, which is N x D after reshaping
  #   db should be M; it is just the sum over dout examples
  # ================================================================ #


  x_res = np.reshape(x, (x.shape[0], w.shape[0]))
  dx_res = dout.dot(w.T)
  dx = np.reshape(dx_res, x.shape) # Shape of N * D
  dw = x_res.T.dot(dout) # Shape of D * M
  db = dout.T.dot(np.ones(x.shape[0]))  # Shape of M * 1


  # ================================================================ #
  # END YOUR CODE HERE
  # ================================================================ #

  return dx, dw, db

def relu_forward(x):
  """
  Computes the forward pass for a layer of rectified linear units (ReLUs).

  Input:
  - x: Inputs, of any shape

  Returns a tuple of:
  - out: Output, of the same shape as x
  - cache: x
  """
  # ================================================================ #
  # YOUR CODE HERE:
  #   Implement the ReLU forward pass.
  # ================================================================ #

  out = np.maximum(0, x)

  # ================================================================ #
  # END YOUR CODE HERE
  # ================================================================ #

  cache = x
  return out, cache


def relu_backward(dout, cache):
  """
  Computes the backward pass for a layer of rectified linear units (ReLUs).

  Input:
  - dout: Upstream derivatives, of any shape
  - cache: Input x, of same shape as dout

  Returns:
  - dx: Gradient with respect to x
  """
  x = cache

  # ================================================================ #
  # YOUR CODE HERE:
  #   Implement the ReLU backward pass
  # ================================================================ #

  dx = (x > 0) * (dout)


  # ================================================================ #
  # END YOUR CODE HERE
  # ================================================================ #

  return dx

def batchnorm_forward(x, gamma, beta, bn_param):
  """
  Forward pass for batch normalization.

  During training the sample mean and (uncorrected) sample variance are
  computed from minibatch statistics and used to normalize the incoming data.
  During training we also keep an exponentially decaying running mean of the mean
  and variance of each feature, and these averages are used to normalize data
  at test-time.

  At each timestep we update the running averages for mean and variance using
  an exponential decay based on the momentum parameter:

  running_mean = momentum * running_mean + (1 - momentum) * sample_mean
  running_var = momentum * running_var + (1 - momentum) * sample_var

  Note that the batch normalization paper suggests a different test-time
  behavior: they compute sample mean and variance for each feature using a
  large number of training images rather than using a running average. For
  this implementation we have chosen to use running averages instead since
  they do not require an additional estimation step; the torch7 implementation
  of batch normalization also uses running averages.

  Input:
  - x: Data of shape (N, D)
  - gamma: Scale parameter of shape (D,)
  - beta: Shift paremeter of shape (D,)
  - bn_param: Dictionary with the following keys:
    - mode: 'train' or 'test'; required
    - eps: Constant for numeric stability
    - momentum: Constant for running mean / variance.
    - running_mean: Array of shape (D,) giving running mean of features
    - running_var Array of shape (D,) giving running variance of features

  Returns a tuple of:
  - out: of shape (N, D)
  - cache: A tuple of values needed in the backward pass
  """
  mode = bn_param['mode']
  eps = bn_param.get('eps', 1e-5)
  momentum = bn_param.get('momentum', 0.9)

  N, D = x.shape
  running_mean = bn_param.get('running_mean', np.zeros(D, dtype=x.dtype))
  running_var = bn_param.get('running_var', np.zeros(D, dtype=x.dtype))

  out, cache = None, None
  if mode == 'train':

    # ================================================================ #
    # YOUR CODE HERE:
    #   A few steps here:
    #     (1) Calculate the running mean and variance of the minibatch.
    #     (2) Normalize the activations with the running mean and variance.
    #     (3) Scale and shift the normalized activations.  Store this
    #         as the variable 'out'
    #     (4) Store any variables you may need for the backward pass in
    #         the 'cache' variable.
    # ================================================================ #

   mean_minibatch = np.mean(x, axis=0)
   var_minibatch  = np.var(x, axis=0)
   x_normalize = (x - mean_minibatch) / np.sqrt(var_minibatch + eps)
   out = gamma * x_normalize + beta

   mean_running = running_mean
   var_running  = running_var

   mean_running = momentum * mean_running + (1 - momentum) * mean_minibatch
   var_running  = momentum * var_running + (1 - momentum) * var_minibatch
   bn_param['running_mean'] = mean_running
   bn_param['running_var'] = var_running

   cache = {
      'minibatch_var': var_minibatch,
      'x_centralize': (x - mean_minibatch),
      'x_normalize': x_normalize,
      'gamma': gamma,
      'eps': eps
   }


    # ================================================================ #
    # END YOUR CODE HERE
    # ================================================================ #

  elif mode == 'test':



    # ================================================================ #
    # YOUR CODE HERE:
    #   Calculate the testing time normalized activation.  Normalize using
    #   the running mean and variance, and then scale and shift appropriately.
    #   Store the output as 'out'.
    # ================================================================ #
    out = gamma * (x - running_mean) / np.sqrt(running_var + eps) + beta


    # ================================================================ #
    # END YOUR CODE HERE
    # ================================================================ #

  else:
    raise ValueError('Invalid forward batchnorm mode "%s"' % mode)

  # Store the updated running means back into bn_param
  bn_param['running_mean'] = running_mean
  bn_param['running_var'] = running_var

  return out, cache

def batchnorm_backward(dout, cache):
  """
  Backward pass for batch normalization.

  For this implementation, you should write out a computation graph for
  batch normalization on paper and propagate gradients backward through
  intermediate nodes.

  Inputs:
  - dout: Upstream derivatives, of shape (N, D)
  - cache: Variable of intermediates from batchnorm_forward.

  Returns a tuple of:
  - dx: Gradient with respect to inputs x, of shape (N, D)
  - dgamma: Gradient with respect to scale parameter gamma, of shape (D,)
  - dbeta: Gradient with respect to shift parameter beta, of shape (D,)
  """
  dx, dgamma, dbeta = None, None, None

  # ================================================================ #
  # YOUR CODE HERE:
  #   Implement the batchnorm backward pass, calculating dx, dgamma, and dbeta.
  # ================================================================ #

  N = dout.shape[0]
  minibatch_var = cache.get('minibatch_var')
  x_centralize = cache.get('x_centralize')
  x_normalize = cache.get('x_normalize')
  gamma = cache.get('gamma')
  eps = cache.get('eps')

  # calculate dx
  dxhat = dout * gamma
  dxmu1 = dxhat / np.sqrt(minibatch_var + eps)
  sqrt_var = np.sqrt(minibatch_var + eps)
  dsqrt_var = -np.sum(dxhat * x_centralize, axis=0) / (sqrt_var**2)
  dvar = dsqrt_var * 0.5 / sqrt_var
  dxmu2 = 2 * x_centralize * dvar * np.ones_like(dout) / N
  dx1 = dxmu1 + dxmu2
  dx2 = -np.sum(dx1, axis=0) * np.ones_like(dout) / N
  dx = dx1 + dx2

  # calculate dbeta and dgamma
  dbeta = np.sum(dout, axis=0)
  dgamma = np.sum(dout * x_normalize, axis=0)
  # ================================================================ #
  # END YOUR CODE HERE
  # ================================================================ #

  return dx, dgamma, dbeta

def dropout_forward(x, dropout_param):
  """
  Performs the forward pass for (inverted) dropout.

  Inputs:
  - x: Input data, of any shape
  - dropout_param: A dictionary with the following keys:
    - p: Dropout parameter. We drop each neuron output with probability p.
    - mode: 'test' or 'train'. If the mode is train, then perform dropout;
      if the mode is test, then just return the input.
    - seed: Seed for the random number generator. Passing seed makes this
      function deterministic, which is needed for gradient checking but not in
      real networks.

  Outputs:
  - out: Array of the same shape as x.
  - cache: A tuple (dropout_param, mask). In training mode, mask is the dropout
    mask that was used to multiply the input; in test mode, mask is None.
  """
  p, mode = dropout_param['p'], dropout_param['mode']
  if 'seed' in dropout_param:
    np.random.seed(dropout_param['seed'])

  mask = None
  out = None

  if mode == 'train':
    # ================================================================ #
    # YOUR CODE HERE:
    #   Implement the inverted dropout forward pass during training time.
    #   Store the masked and scaled activations in out, and store the
    #   dropout mask as the variable mask.
    # ================================================================ #

    mask = (np.random.random_sample(x.shape) >= p) / (1 - p)
    out = x * mask

    # ================================================================ #
    # END YOUR CODE HERE
    # ================================================================ #

  elif mode == 'test':

    # ================================================================ #
    # YOUR CODE HERE:
    #   Implement the inverted dropout forward pass during test time.
    # ================================================================ #

    out = x

    # ================================================================ #
    # END YOUR CODE HERE
    # ================================================================ #

  cache = (dropout_param, mask)
  out = out.astype(x.dtype, copy=False)

  return out, cache

def dropout_backward(dout, cache):
  """
  Perform the backward pass for (inverted) dropout.

  Inputs:
  - dout: Upstream derivatives, of any shape
  - cache: (dropout_param, mask) from dropout_forward.
  """
  dropout_param, mask = cache
  mode = dropout_param['mode']

  dx = None
  if mode == 'train':
    # ================================================================ #
    # YOUR CODE HERE:
    #   Implement the inverted dropout backward pass during training time.
    # ================================================================ #

    dx = dout * mask

    # ================================================================ #
    # END YOUR CODE HERE
    # ================================================================ #
  elif mode == 'test':
    # ================================================================ #
    # YOUR CODE HERE:
    #   Implement the inverted dropout backward pass during test time.
    # ================================================================ #

    dx = dout

    # ================================================================ #
    # END YOUR CODE HERE
    # ================================================================ #
  return dx

def svm_loss(x, y):
  """
  Computes the loss and gradient using for multiclass SVM classification.

  Inputs:
  - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
    for the ith input.
  - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
    0 <= y[i] < C

  Returns a tuple of:
  - loss: Scalar giving the loss
  - dx: Gradient of the loss with respect to x
  """
  N = x.shape[0]
  correct_class_scores = x[np.arange(N), y]
  margins = np.maximum(0, x - correct_class_scores[:, np.newaxis] + 1.0)
  margins[np.arange(N), y] = 0
  loss = np.sum(margins) / N
  num_pos = np.sum(margins > 0, axis=1)
  dx = np.zeros_like(x)
  dx[margins > 0] = 1
  dx[np.arange(N), y] -= num_pos
  dx /= N
  return loss, dx


def softmax_loss(x, y):
  """
  Computes the loss and gradient for softmax classification.

  Inputs:
  - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
    for the ith input.
  - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
    0 <= y[i] < C

  Returns a tuple of:
  - loss: Scalar giving the loss
  - dx: Gradient of the loss with respect to x
  """

  probs = np.exp(x - np.max(x, axis=1, keepdims=True))
  probs /= np.sum(probs, axis=1, keepdims=True)
  N = x.shape[0]
  loss = -np.sum(np.log(probs[np.arange(N), y])) / N
  dx = probs.copy()
  dx[np.arange(N), y] -= 1
  dx /= N
  return loss, dx
```

In [ ]:

```python
import numpy as np
from .layers import *
from .layer_utils import *


class TwoLayerNet(object):
  """
  A two-layer fully-connected neural network with ReLU nonlinearity and
  softmax loss that uses a modular layer design. We assume an input dimension
  of D, a hidden dimension of H, and perform classification over C classes.

  The architecure should be affine - relu - affine - softmax.

  Note that this class does not implement gradient descent; instead, it
  will interact with a separate Solver object that is responsible for running
  optimization.

  The learnable parameters of the model are stored in the dictionary
  self.params that maps parameter names to numpy arrays.
  """

  def __init__(self, input_dim=3*32*32, hidden_dims=100, num_classes=10,
               dropout=0, weight_scale=1e-3, reg=0.0):
    """
    Initialize a new network.

    Inputs:
    - input_dim: An integer giving the size of the input
    - hidden_dims: An integer giving the size of the hidden layer
    - num_classes: An integer giving the number of classes to classify
    - dropout: Scalar between 0 and 1 giving dropout strength.
    - weight_scale: Scalar giving the standard deviation for random
      initialization of the weights.
    - reg: Scalar giving L2 regularization strength.
    """
    self.params = {}
    self.reg = reg

    # ================================================================ #
    # YOUR CODE HERE:
    #   Initialize W1, W2, b1, and b2.  Store these as self.params['W1'],
    #   self.params['W2'], self.params['b1'] and self.params['b2']. The
    #   biases are initialized to zero and the weights are initialized
    #   so that each parameter has mean 0 and standard deviation weight_scale.
    #   The dimensions of W1 should be (input_dim, hidden_dim) and the
    #   dimensions of W2 should be (hidden_dims, num_classes)
    # ================================================================ #

    W1_size = (input_dim, hidden_dims)
    W2_size = (hidden_dims,num_classes)

    self.params['W1'] = np.random.normal(loc=0.0,scale=weight_scale,size = W1_size)
    self.params['b1'] = np.zeros(hidden_dims)
    self.params['W2'] = np.random.normal(loc=0.0,scale=weight_scale,size = W2_size)
    self.params['b2'] = np.zeros(num_classes)

    # ================================================================ #
    # END YOUR CODE HERE
    # ================================================================ #

  def loss(self, X, y=None):
    """
    Compute loss and gradient for a minibatch of data.

    Inputs:
    - X: Array of input data of shape (N, d_1, ..., d_k)
    - y: Array of labels, of shape (N,). y[i] gives the label for X[i].

    Returns:
    If y is None, then run a test-time forward pass of the model and return:
    - scores: Array of shape (N, C) giving classification scores, where
      scores[i, c] is the classification score for X[i] and class c.

    If y is not None, then run a training-time forward and backward pass and
    return a tuple of:
    - loss: Scalar value giving the loss
    - grads: Dictionary with the same keys as self.params, mapping parameter
      names to gradients of the loss with respect to those parameters.
    """
    scores = None

    # ================================================================ #
    # YOUR CODE HERE:
    #   Implement the forward pass of the two-layer neural network. Store
    #   the class scores as the variable 'scores'.  Be sure to use the layers
    #   you prior implemented.
    # ================================================================ #

    W1 = self.params['W1']
    b1 = self.params['b1']
    W2 = self.params['W2']
    b2 = self.params['b2']

    H, cache_h = affine_relu_forward(X, W1, b1)
    Z, cache_z = affine_forward(H, W2, b2)

    scores = Z

    # ================================================================ #
    # END YOUR CODE HERE
    # ================================================================ #

    # If y is None then we are in test mode so just return scores
    if y is None:
      return scores

    loss, grads = 0, {}
    # ================================================================ #
    # YOUR CODE HERE:
    #   Implement the backward pass of the two-layer neural net.  Store
    #   the loss as the variable 'loss' and store the gradients in the
    #   'grads' dictionary.  For the grads dictionary, grads['W1'] holds
    #   the gradient for W1, grads['b1'] holds the gradient for b1, etc.
    #   i.e., grads[k] holds the gradient for self.params[k].
    #
    #   Add L2 regularization, where there is an added cost 0.5*self.reg*W^2
    #   for each W.  Be sure to include the 0.5 multiplying factor to
    #   match our implementation.
    #
    #   And be sure to use the layers you prior implemented.
    # ================================================================ #

    loss, dz = softmax_loss(scores, y)
    loss += 0.5*self.reg*(np.sum(W1*W1) + np.sum(W2*W2))

    dh, dw2, db2 = affine_backward(dz, cache_z)
    dx, dw1, db1 = affine_relu_backward(dh, cache_h)

    grads['W1'] = dw1 + self.reg * W1
    grads['b1'] = db1
    grads['W2'] = dw2 + self.reg * W2
    grads['b2'] = db2

    # ================================================================ #
    # END YOUR CODE HERE
    # ================================================================ #

    return loss, grads


class FullyConnectedNet(object):
  """
  A fully-connected neural network with an arbitrary number of hidden layers,
  ReLU nonlinearities, and a softmax loss function. This will also implement
  dropout and batch normalization as options. For a network with L layers,
  the architecture will be

  {affine - [batch norm] - relu - [dropout]} x (L - 1) - affine - softmax

  where batch normalization and dropout are optional, and the {...} block is
  repeated L - 1 times.

  Similar to the TwoLayerNet above, learnable parameters are stored in the
  self.params dictionary and will be learned using the Solver class.
  """

  def __init__(self, hidden_dims, input_dim=3*32*32, num_classes=10,
               dropout=0, use_batchnorm=False, reg=0.0,
               weight_scale=1e-2, dtype=np.float32, seed=None):
    """
    Initialize a new FullyConnectedNet.

    Inputs:
    - hidden_dims: A list of integers giving the size of each hidden layer.
    - input_dim: An integer giving the size of the input.
    - num_classes: An integer giving the number of classes to classify.
    - dropout: Scalar between 0 and 1 giving dropout strength. If dropout=0 then
      the network should not use dropout at all.
    - use_batchnorm: Whether or not the network should use batch normalization.
    - reg: Scalar giving L2 regularization strength.
    - weight_scale: Scalar giving the standard deviation for random
      initialization of the weights.
    - dtype: A numpy datatype object; all computations will be performed using
      this datatype. float32 is faster but less accurate, so you should use
      float64 for numeric gradient checking.
    - seed: If not None, then pass this random seed to the dropout layers. This
      will make the dropout layers deteriminstic so we can gradient check the
      model.
    """
    self.use_batchnorm = use_batchnorm
    self.use_dropout = dropout > 0
    self.reg = reg
    self.num_layers = 1 + len(hidden_dims)
    self.dtype = dtype
    self.params = {}

    # ================================================================ #
    # YOUR CODE HERE:
    #   Initialize all parameters of the network in the self.params dictionary.
    #   The weights and biases of layer 1 are W1 and b1; and in general the
    #   weights and biases of layer i are Wi and bi. The
    #   biases are initialized to zero and the weights are initialized
    #   so that each parameter has mean 0 and standard deviation weight_scale.
    #
    #   BATCHNORM: Initialize the gammas of each layer to 1 and the beta
    #   parameters to zero.  The gamma and beta parameters for layer 1 should
    #   be self.params['gamma1'] and self.params['beta1'].  For layer 2, they
    #   should be gamma2 and beta2, etc. Only use batchnorm if self.use_batchnorm
    #   is true and DO NOT do batch normalize the output scores.
    # ================================================================ #

    cur_dim = input_dim
    for idx, hidden_dim in enumerate(hidden_dims):
      self.params['W' + str(idx + 1)] = np.random.randn(cur_dim, hidden_dim) * weight_scale
      self.params['b' + str(idx + 1)] = np.zeros(hidden_dim)

      if self.use_batchnorm:
        self.params['gamma' + str(idx + 1)] = np.ones(hidden_dim)
        self.params['beta' + str(idx + 1)] = np.zeros(hidden_dim)

      cur_dim = hidden_dim

    self.params['W' + str(self.num_layers)] = np.random.randn(cur_dim, num_classes) * weight_scale
    self.params['b' + str(self.num_layers)] = np.zeros(num_classes)

    # ================================================================ #
    # END YOUR CODE HERE
    # ================================================================ #

    # When using dropout we need to pass a dropout_param dictionary to each
    # dropout layer so that the layer knows the dropout probability and the mode
    # (train / test). You can pass the same dropout_param to each dropout layer.
    self.dropout_param = {}
    if self.use_dropout:
      self.dropout_param = {'mode': 'train', 'p': dropout}
      if seed is not None:
        self.dropout_param['seed'] = seed

    # With batch normalization we need to keep track of running means and
    # variances, so we need to pass a special bn_param object to each batch
    # normalization layer. You should pass self.bn_params[0] to the forward pass
    # of the first batch normalization layer, self.bn_params[1] to the forward
    # pass of the second batch normalization layer, etc.
    self.bn_params = []
    if self.use_batchnorm:
      self.bn_params = [{'mode': 'train'} for i in np.arange(self.num_layers - 1)]

    # Cast all parameters to the correct datatype
    for k, v in self.params.items():
      self.params[k] = v.astype(dtype)


  def loss(self, X, y=None):
    """
    Compute loss and gradient for the fully-connected net.

    Input / output: Same as TwoLayerNet above.
    """
    X = X.astype(self.dtype)
    mode = 'test' if y is None else 'train'

    # Set train/test mode for batchnorm params and dropout param since they
    # behave differently during training and testing.
    if self.dropout_param is not None:
      self.dropout_param['mode'] = mode
    if self.use_batchnorm:
      for bn_param in self.bn_params:
        bn_param[mode] = mode

    scores = None

    # ================================================================ #
    # YOUR CODE HERE:
    #   Implement the forward pass of the FC net and store the output
    #   scores as the variable "scores".
    #
    #   BATCHNORM: If self.use_batchnorm is true, insert a bathnorm layer
    #   between the affine_forward and relu_forward layers.  You may
    #   also write an affine_batchnorm_relu() function in layer_utils.py.
    #
    #   DROPOUT: If dropout is non-zero, insert a dropout layer after
    #   every ReLU layer.
    # ================================================================ #

    fc_cache = {}
    relu_cache = {}
    batchnorm_cache = {}
    dropout_cache = {}

    # flatten image
    X = np.reshape(X, [X.shape[0], -1])

    # go through all layers
    for i in range(self.num_layers - 1):
      # fc layer
      fc_out, fc_cache[str(i + 1)] = affine_forward(X, self.params['W' + str(i + 1)], self.params['b' + str(i +

      # batchnorm layer
      relu_input = fc_out
      if self.use_batchnorm:
        batchnorm_out, batchnorm_cache[str(i + 1)] = batchnorm_forward(fc_out, self.params['gamma' + str(i + 1)
        relu_input = batchnorm_out
      relu_out, relu_cache[str(i + 1)] = relu_forward(relu_input)

      # dropout layer
      if self.use_dropout:
        relu_out, dropout_cache[str(i + 1)] = dropout_forward(relu_out, self.dropout_param)

      # update X
      X = relu_out.copy()

    # output FC layer with no relu
    scores, final_cache = affine_forward(X, self.params['W' + str(self.num_layers)], self.params['b' + str(self


    # ================================================================ #
    # END YOUR CODE HERE
    # ================================================================ #

    # If test mode return early
    if mode == 'test':
      return scores

    loss, grads = 0.0, {}
    # ================================================================ #
    # YOUR CODE HERE:
    #   Implement the backwards pass of the FC net and store the gradients
    #   in the grads dict, so that grads[k] is the gradient of self.params[k]
    #   Be sure your L2 regularization includes a 0.5 factor.
    #
    #   BATCHNORM: Incorporate the backward pass of the batchnorm.
    #
    #   DROPOUT: Incorporate the backward pass of dropout.
    # ================================================================ #

    loss, dx = softmax_loss(scores, y)
    loss += 0.5 * self.reg * (np.sum(np.square(self.params['W' + str(self.num_layers)])))
    dx_back, dw_back, db_back = affine_backward(dx, final_cache)
    grads['W' + str(self.num_layers)] = dw_back + self.reg * self.params['W' + str(self.num_layers)]
    grads['b' + str(self.num_layers)] = db_back

    # go backward all layers and update weights, bias, gammas and betas
    for i in range(self.num_layers - 1, 0, -1):
      # dropout layer
      if self.use_dropout:
        dx_back = dropout_backward(dx_back, dropout_cache[str(i)])
      dx_relu = relu_backward(dx_back, relu_cache[str(i)])

      # batchnorm layer
      affine_backward_input = dx_relu
      if self.use_batchnorm:
        dx_bn, dgamma, dbeta = batchnorm_backward(dx_relu, batchnorm_cache[str(i)])
        grads['gamma' + str(i)] = dgamma
        grads['beta' + str(i)] = dbeta
        affine_backward_input = dx_bn
      dx_back, dw_back, db_back = affine_backward(affine_backward_input, fc_cache[str(i)])

      grads['W' + str(i)] = dw_back + self.reg * self.params['W' + str(i)]
      grads['b' + str(i)] = db_back
      loss += 0.5 * self.reg * (np.sum(np.square(self.params['W' + str(i)])))


    # ================================================================ #
    # END YOUR CODE HERE
    # ================================================================ #

    return loss, grads
```

In [ ]:

```python
import numpy as np


"""
This file implements various first-order update rules that are commonly used for
training neural networks. Each update rule accepts current weights and the
gradient of the loss with respect to those weights and produces the next set of
weights. Each update rule has the same interface:

def update(w, dw, config=None):

Inputs:
  - w: A numpy array giving the current weights.
  - dw: A numpy array of the same shape as w giving the gradient of the
    loss with respect to w.
  - config: A dictionary containing hyperparameter values such as learning rate,
    momentum, etc. If the update rule requires caching values over many
    iterations, then config will also hold these cached values.

Returns:
  - next_w: The next point after the update.
  - config: The config dictionary to be passed to the next iteration of the
    update rule.

NOTE: For most update rules, the default learning rate will probably not perform
well; however the default values of the other hyperparameters should work well
for a variety of different problems.

For efficiency, update rules may perform in-place updates, mutating w and
setting next_w equal to w.
"""


def sgd(w, dw, config=None):
  """
  Performs vanilla stochastic gradient descent.

  config format:
  - learning_rate: Scalar learning rate.
  """
  if config is None: config = {}
  config.setdefault('learning_rate', 1e-2)

  w -= config['learning_rate'] * dw
  return w, config


def sgd_momentum(w, dw, config=None):
  """
  Performs stochastic gradient descent with momentum.

  config format:
  - learning_rate: Scalar learning rate.
  - momentum: Scalar between 0 and 1 giving the momentum value.
    Setting momentum = 0 reduces to sgd.
  - velocity: A numpy array of the same shape as w and dw used to store a moving
    average of the gradients.
  """
  if config is None: config = {}
  config.setdefault('learning_rate', 1e-2)
  config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
  v = config.get('velocity', np.zeros_like(w))   # gets velocity, else sets it to zero.

  # ================================================================ #
  # YOUR CODE HERE:
  #   Implement the momentum update formula.  Return the updated weights
  #   as next_w, and the updated velocity as v.
  # ================================================================ #

  v = config['momentum'] * v - config['learning_rate'] * dw
  next_w = w + v

  # ================================================================ #
  # END YOUR CODE HERE
  # ================================================================ #

  config['velocity'] = v

  return next_w, config

def sgd_nesterov_momentum(w, dw, config=None):
  """
  Performs stochastic gradient descent with Nesterov momentum.

  config format:
  - learning_rate: Scalar learning rate.
  - momentum: Scalar between 0 and 1 giving the momentum value.
    Setting momentum = 0 reduces to sgd.
  - velocity: A numpy array of the same shape as w and dw used to store a moving
    average of the gradients.
  """
  if config is None: config = {}
  config.setdefault('learning_rate', 1e-2)
  config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
  v = config.get('velocity', np.zeros_like(w))   # gets velocity, else sets it to zero.

  # ================================================================ #
  # YOUR CODE HERE:
  #   Implement the momentum update formula.  Return the updated weights
  #   as next_w, and the updated velocity as v.
  # ================================================================ #

  v_o = v
  v = config['momentum'] * v - config['learning_rate'] * dw
  w += v + config['momentum'] * (v - v_o)
  next_w = w


  # ================================================================ #
  # END YOUR CODE HERE
  # ================================================================ #

  config['velocity'] = v

  return next_w, config

def rmsprop(w, dw, config=None):
  """
  Uses the RMSProp update rule, which uses a moving average of squared gradient
  values to set adaptive per-parameter learning rates.

  config format:
  - learning_rate: Scalar learning rate.
  - decay_rate: Scalar between 0 and 1 giving the decay rate for the squared
    gradient cache.
  - epsilon: Small scalar used for smoothing to avoid dividing by zero.
  - beta: Moving average of second moments of gradients.
  """
  if config is None: config = {}
  config.setdefault('learning_rate', 1e-2)
  config.setdefault('decay_rate', 0.99)
  config.setdefault('epsilon', 1e-8)
  config.setdefault('a', np.zeros_like(w))

  next_w = None

  # ================================================================ #
  # YOUR CODE HERE:
  #   Implement RMSProp.  Store the next value of w as next_w.  You need
  #   to also store in config['a'] the moving average of the second
  #   moment gradients, so they can be used for future gradients. Concretely,
  #   config['a'] corresponds to "a" in the lecture notes.
  # ================================================================ #

  config['a'] = config['decay_rate']*config['a'] + (1-config['decay_rate'])*(dw**2)
  next_w = w - config['learning_rate']*dw/(np.sqrt(config['a'])+config['epsilon'])

  # ================================================================ #
  # END YOUR CODE HERE
  # ================================================================ #

  return next_w, config


def adam(w, dw, config=None):
  """
  Uses the Adam update rule, which incorporates moving averages of both the
  gradient and its square and a bias correction term.

  config format:
  - learning_rate: Scalar learning rate.
  - beta1: Decay rate for moving average of first moment of gradient.
  - beta2: Decay rate for moving average of second moment of gradient.
  - epsilon: Small scalar used for smoothing to avoid dividing by zero.
  - m: Moving average of gradient.
  - v: Moving average of squared gradient.
  - t: Iteration number.
  """
  if config is None: config = {}
  config.setdefault('learning_rate', 1e-3)
  config.setdefault('beta1', 0.9)
  config.setdefault('beta2', 0.999)
  config.setdefault('epsilon', 1e-8)
  config.setdefault('v', np.zeros_like(w))
  config.setdefault('a', np.zeros_like(w))
  config.setdefault('t', 0)

  next_w = None

  # ================================================================ #
  # YOUR CODE HERE:
  #   Implement Adam.  Store the next value of w as next_w.  You need
  #   to also store in config['a'] the moving average of the second
  #   moment gradients, and in config['v'] the moving average of the
  #   first moments.  Finally, store in config['t'] the increasing time.
  # ================================================================ #

  beta1 = config['beta1']
  beta2 = config['beta2']
  t = config['t'] + 1

  v = beta1 * config['v'] + (1 - beta1) * dw
  a = beta2 * config['a'] + (1 - beta2) * (dw**2)
  v_corrected = v/(1 - beta1**t)
  a_corrected = a/(1 - beta2**t)
  next_w = w - config['learning_rate'] * v_corrected / (np.sqrt(a_corrected) + config['epsilon'])

  config['v'] = v
  config['a'] = a
  config['t'] = t

  # ================================================================ #
  # END YOUR CODE HERE
  # ================================================================ #

  return next_w, config
```