

Author:

- Sidharth
- 2K18/ MC/ 114

Objective:

Demonstrate the Renewal Process. WAP to find the expected waiting time until the n th renewal in case of a renewal process with renewal cycle length distributed

1. normally with mean μ and standard deviation σ , ($\mu > 3\sigma$)
2. exponentially with parameter λ .

Demonstrate it by taking suitable values for (a) and (b) both.

Theory:

A Renewal Process is a general case of Poisson Process in which the inter arrival time of the process or the time between failures does not necessarily follow the exponential distribution. A counting process $N(t)$ that represents the total number of occurrences of an event in the time interval $(0,t)$ is called a renewal process. If the time between failures are independent and identically distributed random variables.

The probability that there are exactly n failures occurring by time t can be written as,

$$P\{N(t) = n\} = P\{N(t) \geq n\} - P\{N(t) > n\}$$

And,

$$T_k = W_k + W_{k-1}$$

▼ Code & Output:

❶. Normally with mean μ and standard deviation σ , ($\mu > 3\sigma$)

```
n = int(input('Enter value of n: '))
mu = int(input('Enter value of  $\mu$ : '))
sigma = input('Enter value of  $\sigma$ : ')
ans = n*mu
print('Expected waiting time until the', n, 'th renewal = ', ans)
```

```
☞ Enter value of n: 87
Enter value of  $\mu$ : 3
Enter value of  $\sigma$ : 0.6
Expected waiting time until the 87 th renewal = 261
```

❷. Exponentially with parameter λ

```
n = int(input('Enter value of n: '))
l = float(input('Enter value of  $\lambda$ : '))
ans = n/l
print('Expected waiting time until the', n, 'th renewal = ', ans)
```

```
☞ Enter value of n: 122
Enter value of  $\lambda$ : 0.245
Expected waiting time until the 122 th renewal = 497.9591836734694
```

Result:

Demonstrated the Renewal Process and calculated the expected waiting time until the nth renewal.

Discussion:

Calculation of the expected waiting time until the nth renewal in case of a renewal process with renewal cycle length distributed normally with mean μ and standard deviation σ and exponentially with parameter λ are being calculated through above formula.

