

Welcome to Advanced DSA 1
module. 😊

Content For Advanced DSA Module

Arrays — 3.

Bit Manipulation — 2.

Recursion & Backtracking Basics — 3.

Contest — 1 — April 15th 7:00 AM IST

Maths — 3

OOPS — 2

Hashing — 2

Language Advanced Concept — 1

Contest — 2

Sorting — 2

Searching — 3

Two Pointers — 1

Linked List — 3

Contest — 3

Stacks — 2

Queues — 1

Trees — 5

Contest — 4

Hash Map Implementation — 1

Heaps — 2

Greedy — 1

DP — 4

Contest — 5

Graphs — 3

Contest (Complete Syllabus — 3 Hrs)

+ Mock Interview (Simulating Real DSA Interview
1 hr 2 Questions)

Q:- Given an integer array A of size N.
Find maximum subarray sum out of all subarrays.

Ex:- $\{ \overset{0}{-2}, \overset{1}{3}, \overset{2}{4}, \overset{3}{-1}, \overset{4}{5}, \overset{5}{-10}, \overset{6}{7} \}$
 $= 11.$

Ex:- $\{ \overset{0}{-3}, \overset{1}{4}, \overset{2}{6}, \overset{3}{8}, \overset{4}{-10}, \overset{5}{2}, \overset{6}{7} \}$
 $= 18.$

Quiz 1

$\{ \overset{0}{4}, \overset{1}{5}, \overset{2}{2}, \overset{3}{1}, \overset{4}{6} \}$

$= 18$

2

Quiz 2

$\{ -4, -3, -6, -9, -2 \}.$

$= -2.$

Brute Force

N^2

→ Consider all subarrays

N

→ Iterate over each subarray to calculate sum & compare with global max sum.

$O(N^3)$.

↓ $O(1)$

Using Prefix Sum →

$O(N^2)$

Optimisation

Possible cases

Case I : All elements are positive

$\{4, 2, 1, 6, 7\}$ Entire array

Case II : All elements are negative

$\{-4, -2, -1, -6, -7\}$ - Max Element.

Case III : Some positives in between negatives.

$\{-3, -2, -6, 4, 3, 6, 9, -5, -3, -1, -6\}$

Case IV : Positives & negatives on either side.

$\{-3, -2, -6, 5, 3, 4, 6\}$

Generic Case

$$\left\{ \dots +, +, +, +, \overbrace{-, -, -, -}^{-25}, +, +, + \dots \right\}$$

$20 \mid$
 $15 \rightarrow 10 \rightarrow -2$

30

Ex:- $\{-2, 3, 4, -1, 5, -10, 7\}$

$7 \quad -1 \quad 5$
 $= 11$

=

Ex:-

	0	1	2	3	4	5	6	7	8	i
{	-20	10	-20	-12	6	5	-3	8	-2	}

<u>Cur Sum</u>	0	-20	10	-10	0	-12	0	8	16
<u>max Sum</u>	INT_MIN	-20	10	16	16	16	16	16	14

Quiz 3:-

{ -2, 3, 4, -1, 5, -10, 7 }
0, 1, 2, 3, 4, 5, 6

cur Sum

0 -2 0 3 7 6 11 8

max Sum

~~INT_MIN~~ -2 3 7 11

Code

```
int maxSubarraySum (int arr, int N){
```

```
    int curSum = 0;
```

```
    int maxSum = INT_MIN;
```

```
    for (i = 0 to N-1) {
```

```
        curSum += arr[i];
```

```
        if (curSum > maxSum) {  
            maxSum = curSum;  
        }
```

```
        if (curSum < 0) {  
            curSum = 0;  
        }
```

return maxSum

}

T.C $\rightarrow O(N)$

S.C $\rightarrow O(1)$

$$\{ \overset{0}{-3}, \overset{1}{-4}, \overset{2}{-5}, \overset{3}{-2} \}_i$$

$$\text{cur Sum} = \cancel{0} \quad \cancel{-3} \quad \cancel{-4} \quad \cancel{-5} \quad \cancel{0}$$

$$\text{max Sum} = \text{INT_MIN} \quad \cancel{-3} \quad -2$$

2. Given an integer array A where every element is 0. Return the final array after performing multiple queries.

Query (i, x) : Add x to all elements from index i .

Queries

$$A = \{ \overset{0}{0}, \overset{1}{0}, \overset{2}{0}, \overset{3}{0}, \overset{4}{0}, \overset{5}{0}, \overset{6}{0} \}$$

$(1, 3)$

$(4, -2)$

$(3, 1)$

+3 +3 +3 +3 +3 +3

-2 -2 -2

+1 +1 +1 +1

$$A = \{ 0, 3, 3, 4, 2, 2, 2 \}$$

Query 4

$$A = \{ \overset{0}{0}, \overset{1}{0}, \overset{2}{0}, \overset{3}{0}, \overset{4}{0} \}$$

Queries

$(1, 3)$

$(0, 2)$

$(4, 1)$

+3 +3 +3 +3

+2 +2 +2 +2 +2

+1

$$\{ 2, 5, 5, 5, 6 \}$$

$$A = \{ \overset{0}{\cancel{0}}, \overset{2}{\cancel{1}}, \overset{5}{\cancel{2}}, \overset{5}{\cancel{3}}, \overset{5}{\cancel{4}}, \overset{6}{\cancel{5}} \}$$

$$= \{ 2, 5, 5, 5, 6 \}.$$

Queries

$$\begin{aligned} (1, 3) & \checkmark \\ (0, 2) & \checkmark \\ (4, 1) & \end{aligned}$$

Brute Force

For each query, traverse the array to update the value.

$$\underline{O(Q * N)}$$

Optimisation

$$A = \begin{matrix} & 0 & 1 & 2 & 3 & 4 \\ \{ & 0 & 0 & 0 & 0 & 0 \} \\ & +2 & \textcircled{+3} & \cdot & \cdot & \cdot \\ & & & & & +1 \end{matrix}$$

Queries

$(1, 3)$
 $(0, 2)$
 $(4, 1)$

$$A = \{ 2, 3, 0, 0, 1 \}$$

↑ ↑ ↑ ↑

$$pF = \{ 2, 5, 5, 5, 6 \}$$

↑↑
ans.

Code:

```
for (i = 0; i < Q.size(); i++) {
```

```

    index = Q[i][0];
    value = Q[i][1];
    A[index] += value;
}

```

$$\forall (i = 1; \quad i \in \mathbb{N}; \quad i++) \{$$
$$A[i] = A[i-1];$$

schon 17;

$$T.C \rightarrow O(Q+N).$$

Variation

Query $\longrightarrow (i, j, x)$
Add element x to all
the indices b/w i to j .

$A = \{ \overset{0}{0}, \overset{1}{0}, \overset{2}{0}, \overset{3}{0}, \overset{4}{0}, \overset{5}{0}, \overset{6}{0} \}$

Queries

$(1, 3, 2)$ $+2$ $+2$ $+2$
 $(2, 5, 3)$ $+3$ $+3$ $+3$ $+3$
 $(5, 6, -1)$ -1 -1

ans $\rightarrow \{ 0, 2, 5, 5, 3, 2, -1 \}$

Quiz 5

$A = \{ \overset{0}{0}, \overset{1}{0}, \overset{2}{0}, \overset{3}{0}, \overset{4}{0}, \overset{5}{0}, \overset{6}{0}, \overset{7}{0} \}$

i, j, x

$1, 4, 3$ $+3$ $+3$ $+3$ $+3$
 $0, 5, -1$ -1 -1 -1 -1 -1
 $2, 2, 4$ $+4$
 $4, 6, 3$ $+3$ $+3$ $+3$

ans $\rightarrow \{ -1, 2, 6, 2, 5, 2, 3, 0 \}$

$$A = \{ \overset{0}{0}, \overset{1}{0}, \overset{2}{0}, \overset{3}{0}, \overset{4}{0}, \overset{5}{0}, \overset{6}{0}, \overset{7}{0} \}$$

$+3 \quad +3 \quad +3 \quad +3 \quad +3 \quad +3 \quad +3$
 $-3 \quad -3 \quad -3$

$i \quad j$
1 4 3
1 1

1 7 3
1 1

$$A[i] += \text{value};$$

$$A[j+1] += -\text{value};$$

	0	1	2
Q(0)	1	4	3
Q(1)	0	5	-1
Q(2)	2	2	4

Code.

```
for (q = 0; q < Q; q++) {
```

```
    i = Q(q)[0];
    j = Q(q)[1];
    value = Q(q)[2];
```

```
    A[i] += val;
```

```
    A[j+1] += -val; // Check if
```

j+1 is
in bound.

}

```
for (i = 1; i < N; i++) {
```

```
    A[i] += A[i-1];
```

}

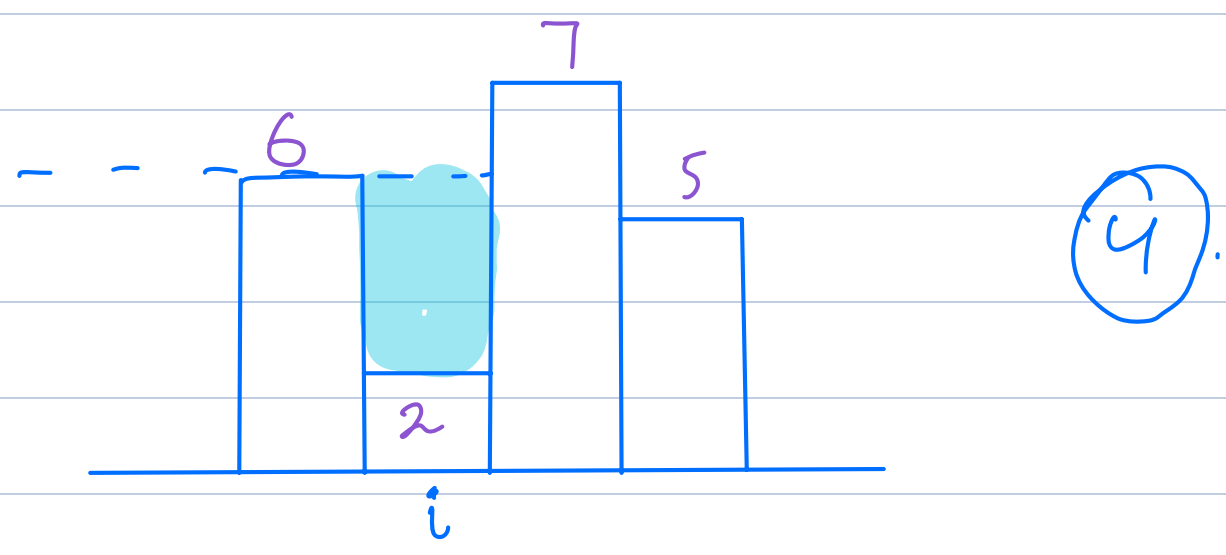
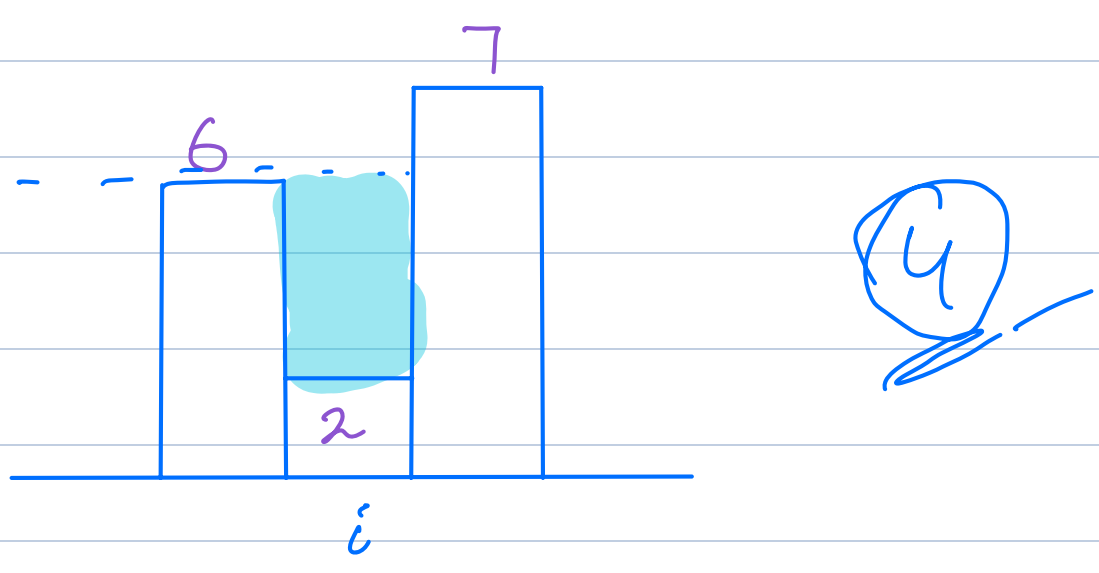
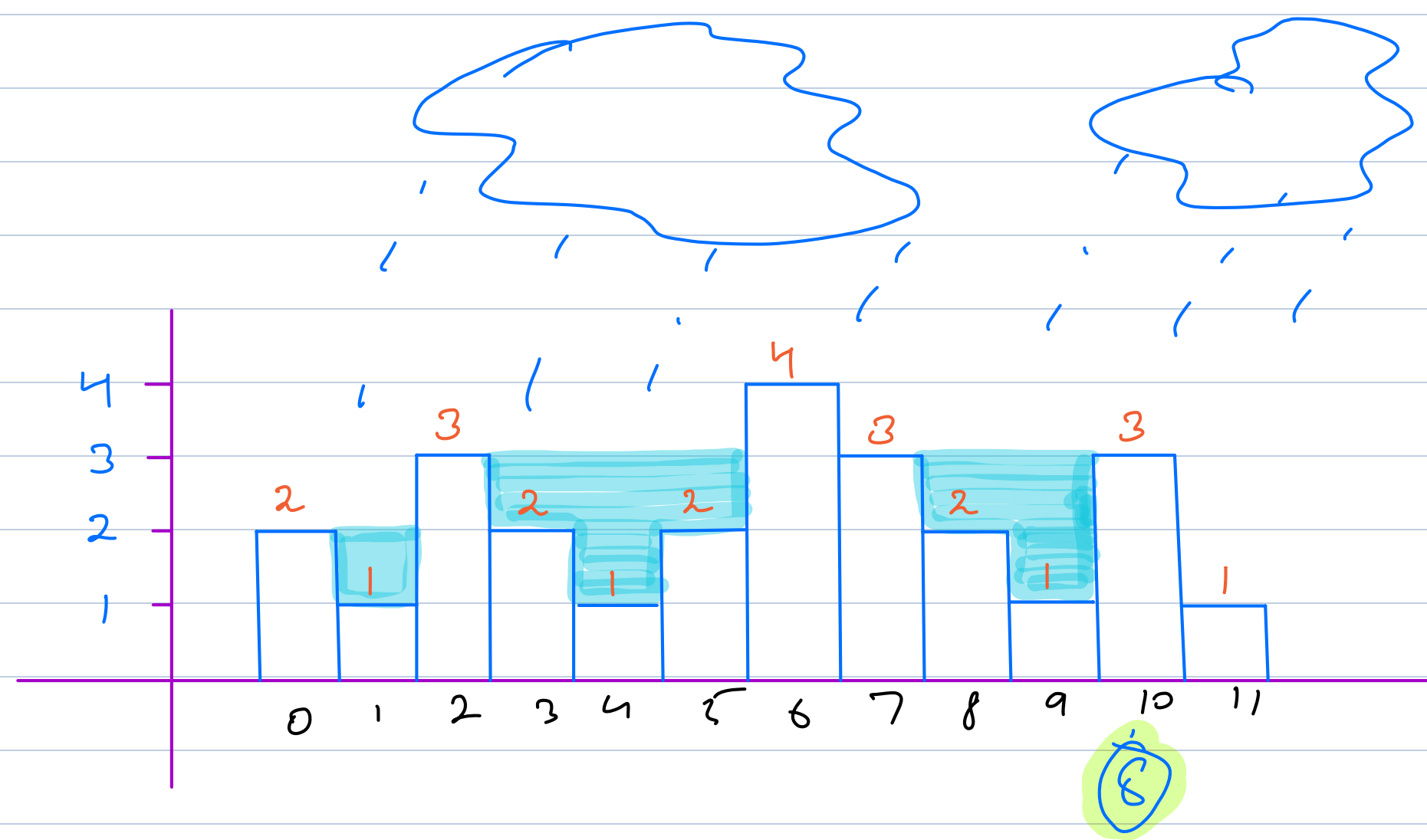
T.C $\rightarrow O(Q + N)$

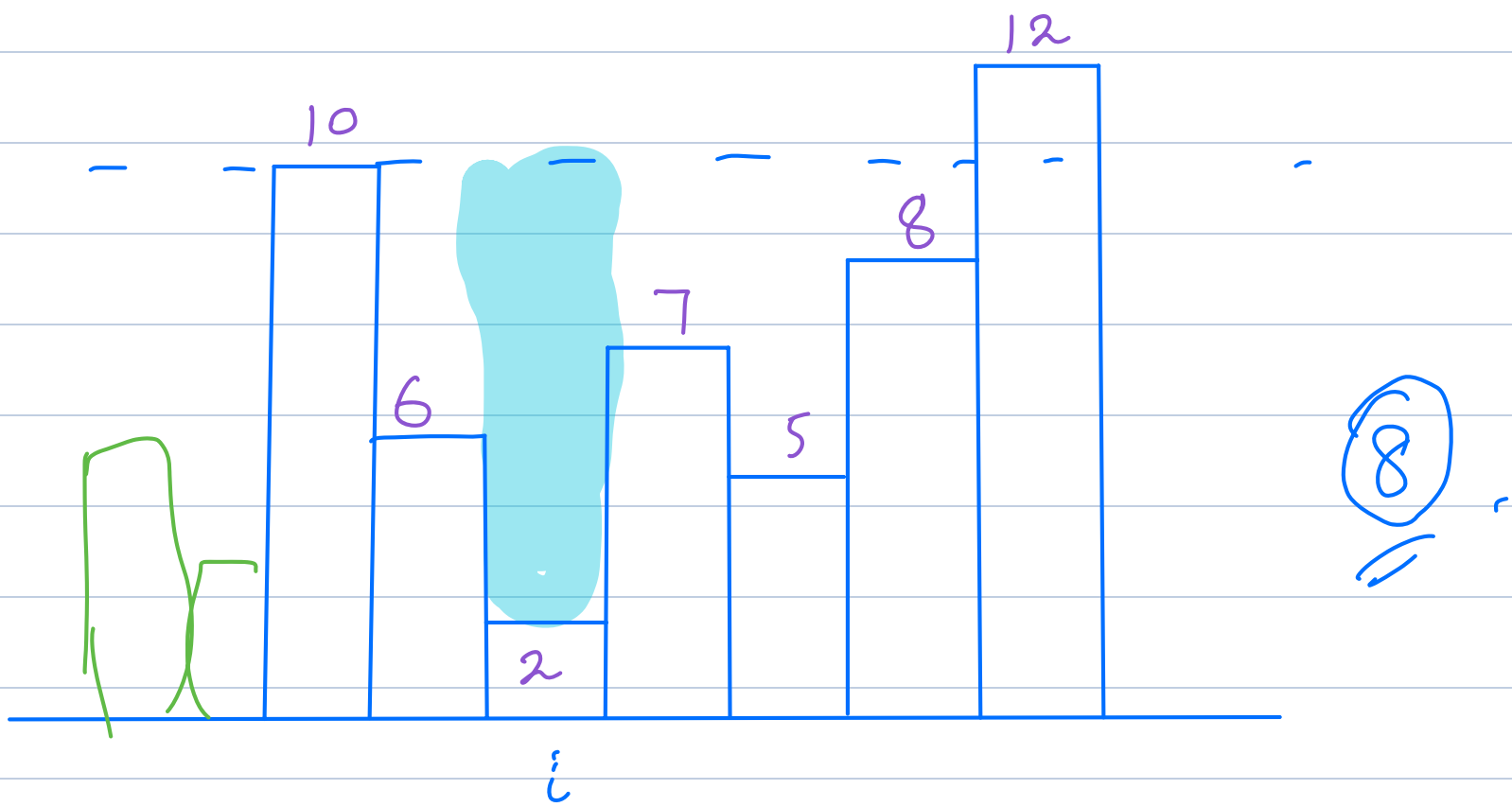
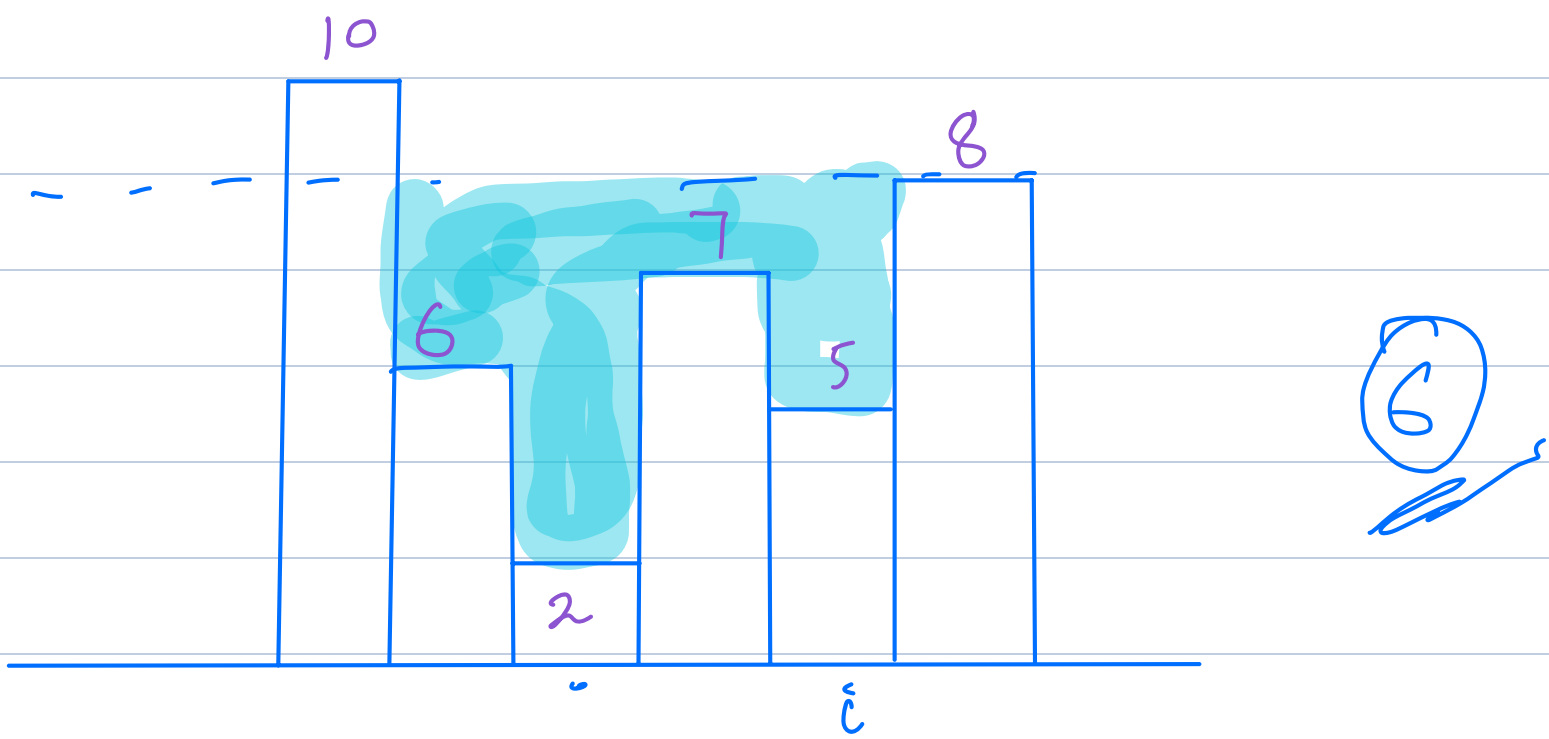
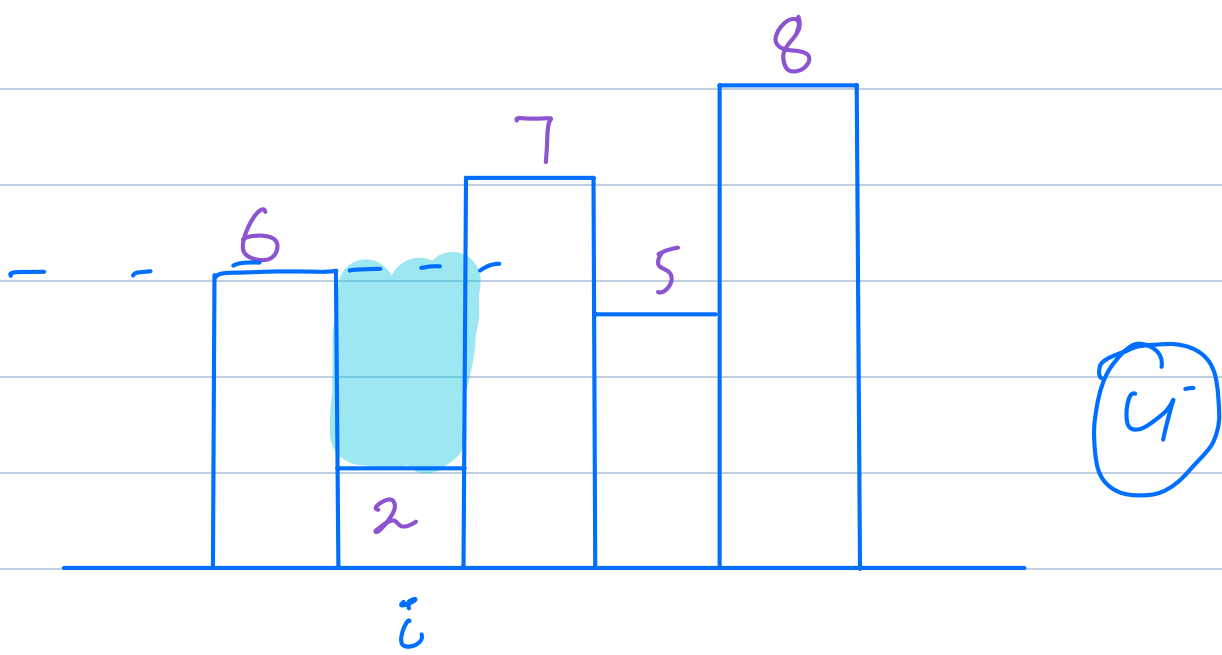
S.C $\rightarrow O(1)$

8:45:

Q:- Given N buildings with height of each building. Find the rain water trapped between the buildings.

arr[] - { 2, 1, 3, 2, 1, 2, 4, 3, 2, 1, 3, 1 }



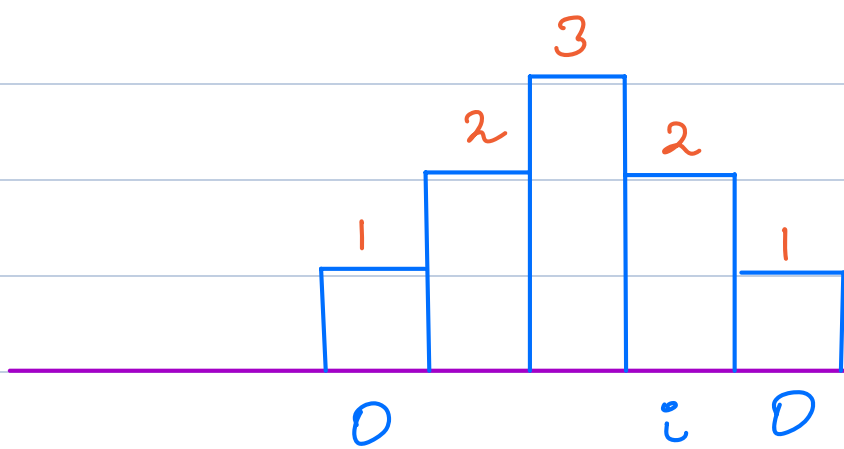


Conclusion

The amount of water that will be accumulated over building of index i = $\min(\text{maxht}(0, i-1), \text{maxht}(i+1, N-1)) - \text{ht}(i)$;

Quiz 6

ans = 0



max left = 3
max right = 1

min = 1

Brute Force

For i^{th} building we need to find max. hts on both the sides.

Code -

ans = 0;

```
for (i = 1; i < N-1; i++) {
```


N

{

maxLeft = Max. value on
0 to i-1;

maxRight = Max value on
i+1 to N-1;

level = min (maxLeft, maxRight)

if (level > ht[i]) {

1 ans += level - ht[i];

3

}

return ans;

T.C

$O(N^2)$

Optimisation

We can store the $lmax$ & $rmax$ every array approach.

$lmax[i] \rightarrow$ Max. element from index 0 to $i-1$.

$rmax[i] \rightarrow$ Max. element from index $i+1$ to $N-1$.

arr - $\{ \overset{0}{4}, \overset{1}{2}, \overset{2}{5}, \overset{3}{7}, \overset{4}{4}, \overset{5}{2}, \overset{6}{3}, \overset{7}{6}, \overset{8}{8}, \overset{9}{2}, \overset{10}{3} \}$

$lmax[] \{ 0, 4, 4, 5, 7, 7, 7, 7, 7, 8, 8 \}$
 $rmax[] \{ 8, 8, 8, 8, 8, 8, 8, 8, 3, 3, 0 \}$

$lmax[i+1] \rightarrow$ max. value from 0 to i

$lmax[i] \rightarrow$ max. value from 0 to $i-1$;

$lmax[i+1] = \max(lmax[i], arr[i]);$
 $\underbrace{\hspace{1.5cm}}_{0 \text{ to } i-1} \quad \underbrace{\hspace{1.5cm}}_i$

#

Code. $i = 0$ $lmax[N];$ $lmax[0] = 0;$ for ($i = 0; i < N-1; i++$) {| $lmax[i+1] = \max(lmax[i], a[i]);$

}

Similarly populate a $rmax$ array.① Create the $lmax$ & $rmax$ arrays. $ans = 0;$ for ($i = 1; i < N-1; i++$) {| $maxLeft = lmax[i];$ | $maxRight = rmax[i];$ | $level = \min(maxLeft, maxRight);$ | if ($level > ht[i]$) {| | $ans += level - ht[i];$

| }

}

return ans;

$$T.C \rightarrow O(N+N)$$

$$S.C \rightarrow O(N+N)$$