

CS 6375

Machine Learning

(Qualifying Exam Section)

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- Course website: www.utdallas.edu/~nrr150130/cs6375/2018fa/
- Piazza (online forum): sign-up link on eLearning

Prerequisites



- CS 5343 (data structures & algorithms)
- “Mathematical sophistication”
 - Basic probability
 - Linear algebra
 - Eigenvalues, eigenvectors, matrices, vectors, etc.
 - Multivariate calculus
 - Derivatives, gradients, convex functions, etc.
- I’ll review some concepts as we come to them, but **you should brush up in areas that you aren’t as comfortable**

- 5-6 problem sets (50%)
 - See collaboration policy on the web
 - Mix of theory and programming (in MATLAB or Python)
 - Available and turned in on eLearning
 - Approximately one assignment every two weeks
- Midterm Exam (20%)
- Final Exam (30%)

-subject to change-

- Dimensionality reduction
 - PCA
 - Matrix Factorizations
- Learning
 - Supervised, unsupervised, active, reinforcement, ...
 - Learning theory: PAC learning, VC dimension
 - SVMs & kernel methods
 - Decision trees, k-NN, logistic regression, ...
 - Parameter estimation: Bayesian methods, MAP estimation, maximum likelihood estimation, expectation maximization, ...
 - Clustering: k-means & spectral clustering
- Probabilistic models
 - Bayesian networks
 - Naïve Bayes
- Neural networks
- Statistical methods
 - Boosting, bagging, bootstrapping
 - Sampling
- Ranking & Collaborative Filtering

What is ML?



What is ML?



“A computer program is said to learn from experience E with respect to some task T and some performance measure P , if its performance on T , as measured by P , improves with experience E .”

- Tom Mitchell

Basic Machine Learning Paradigm



- Collect data
- Build a model using “training” data
- Use model to make predictions

- **Input:** $(x^{(1)}, y^{(1)}), \dots, (x^{(M)}, y^{(M)})$
 - $x^{(m)}$ is the m^{th} data item and $y^{(m)}$ is the m^{th} **label**
- **Goal:** find a function f such that $f(x^{(m)})$ is a “good approximation” to $y^{(m)}$
 - Can use it to predict y values for previously unseen x values

Examples of Supervised Learning

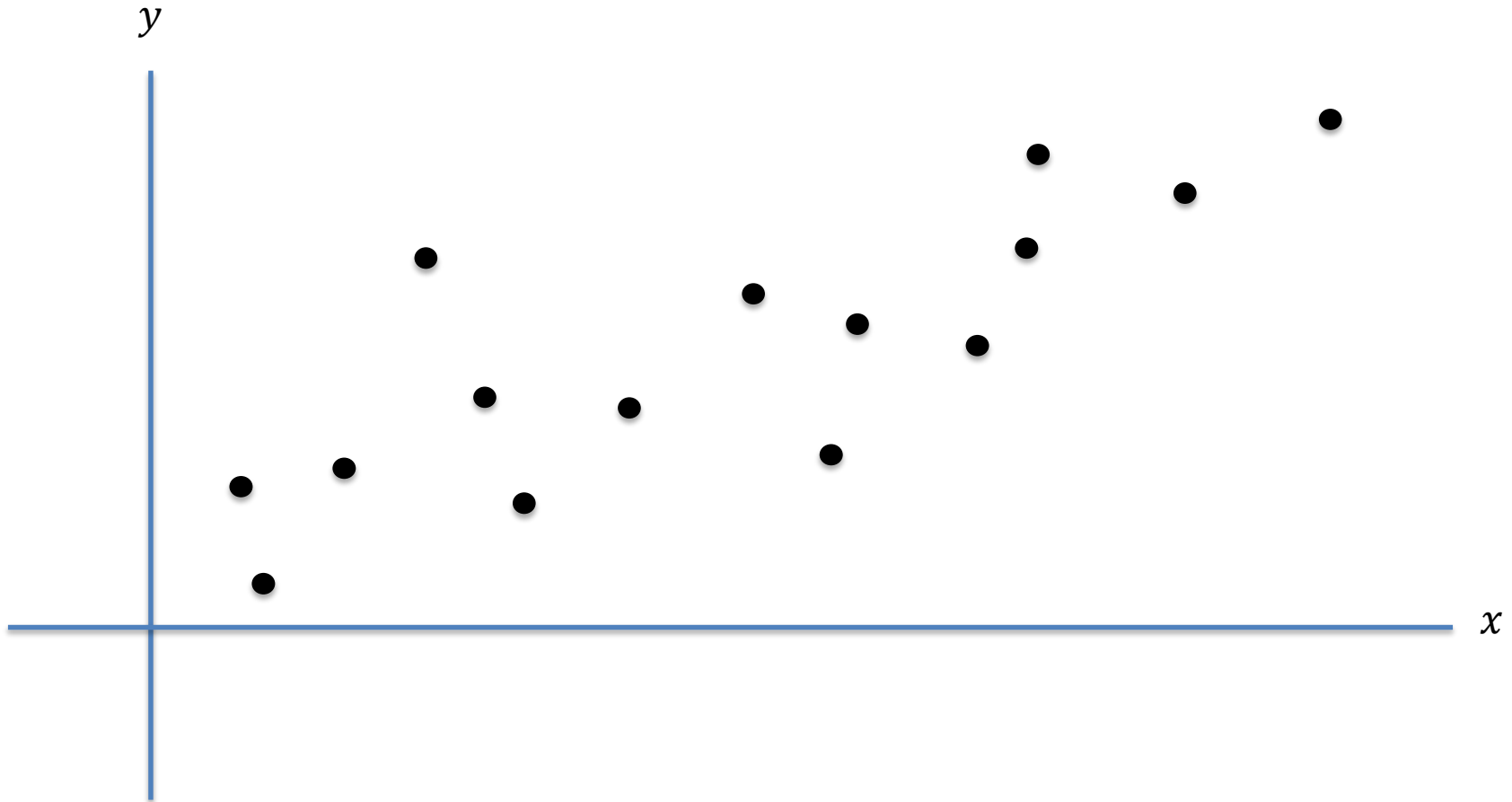


- Spam email detection
- Handwritten digit recognition
- Stock market prediction
- More?

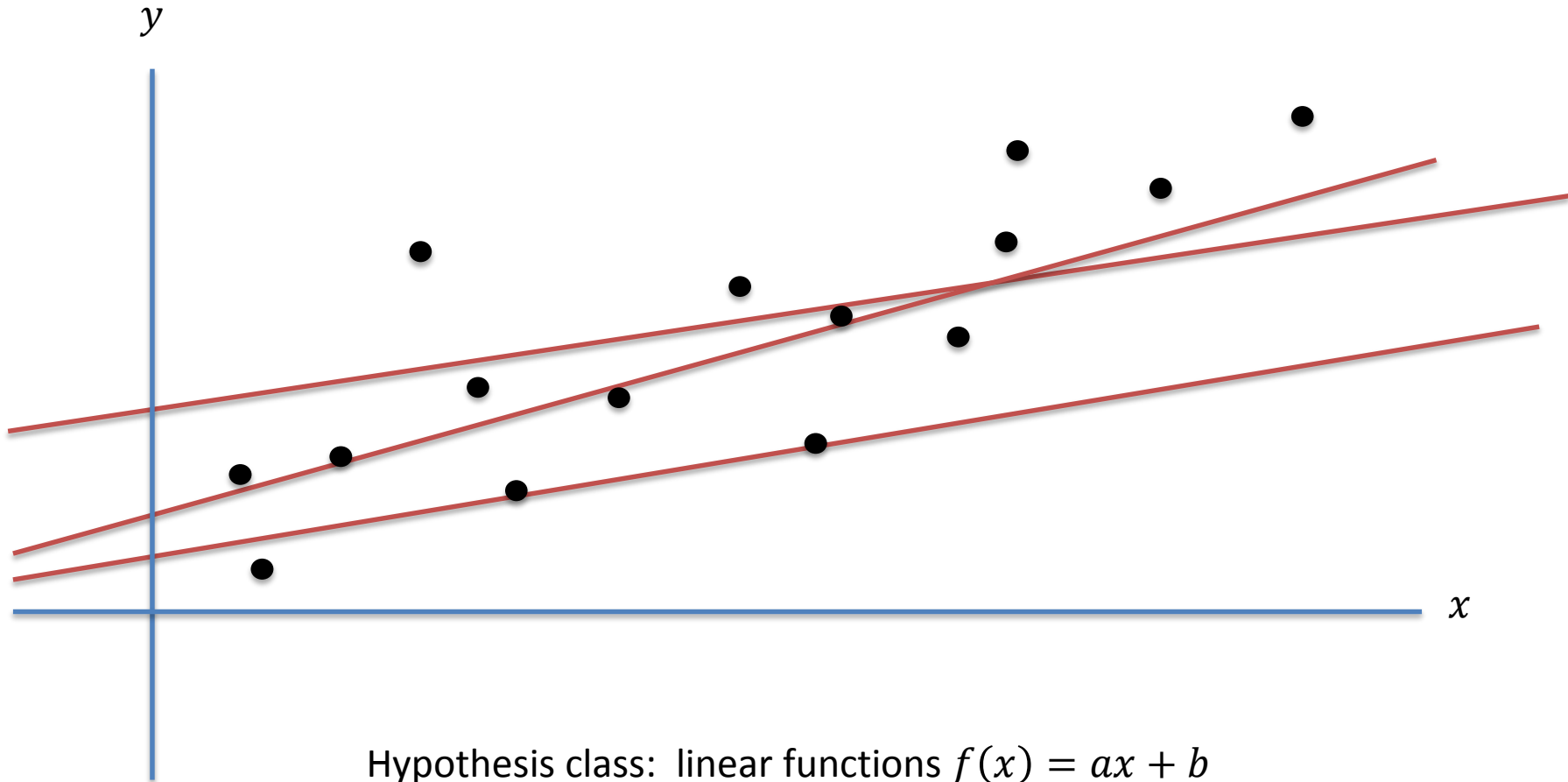
- **Hypothesis space**: set of allowable functions $f: X \rightarrow Y$
- Goal: find the “best” element of the hypothesis space
 - How do we measure the quality of f ?

- Simple linear regression
 - Input: pairs of points $(x^{(1)}, y^{(1)}), \dots, (x^{(M)}, y^{(M)})$ with $x^{(m)} \in \mathbb{R}$ and $y^{(m)} \in \mathbb{R}$
 - Hypothesis space: set of linear functions $f(x) = ax + b$ with $a, b \in \mathbb{R}$
 - Error metric: squared difference between the predicted value and the actual value

Regression



Regression



Hypothesis class: linear functions $f(x) = ax + b$

How do we compute the error of a specific hypothesis?

Linear Regression



- For any data point, x , the learning algorithm predicts $f(x)$
- In typical regression applications, measure the fit using a squared **loss function**

$$L(f) = \frac{1}{M} \sum_m (f(x^{(m)}) - y^{(m)})^2$$

- Want to minimize the average loss on the **training data**
- The optimal linear hypothesis is then given by

$$\min_{a,b} \frac{1}{M} \sum_m (ax^{(m)} + b - y^{(m)})^2$$

Linear Regression



$$\min_{a,b} \frac{1}{M} \sum_m (ax^{(m)} + b - y^{(m)})^2$$

- How do we find the optimal a and b ?

$$\min_{a,b} \frac{1}{M} \sum_m (ax^{(m)} + b - y^{(m)})^2$$

- How do we find the optimal a and b ?
 - Solution 1: take derivatives and solve (there is a closed form solution!)
 - Solution 2: use gradient descent

$$\min_{a,b} \frac{1}{M} \sum_m (ax^{(m)} + b - y^{(m)})^2$$

- How do we find the optimal a and b ?
 - Solution 1: take derivatives and solve (there is a closed form solution!)
 - Solution 2: use gradient descent
 - This approach is much more likely to be useful for general loss functions

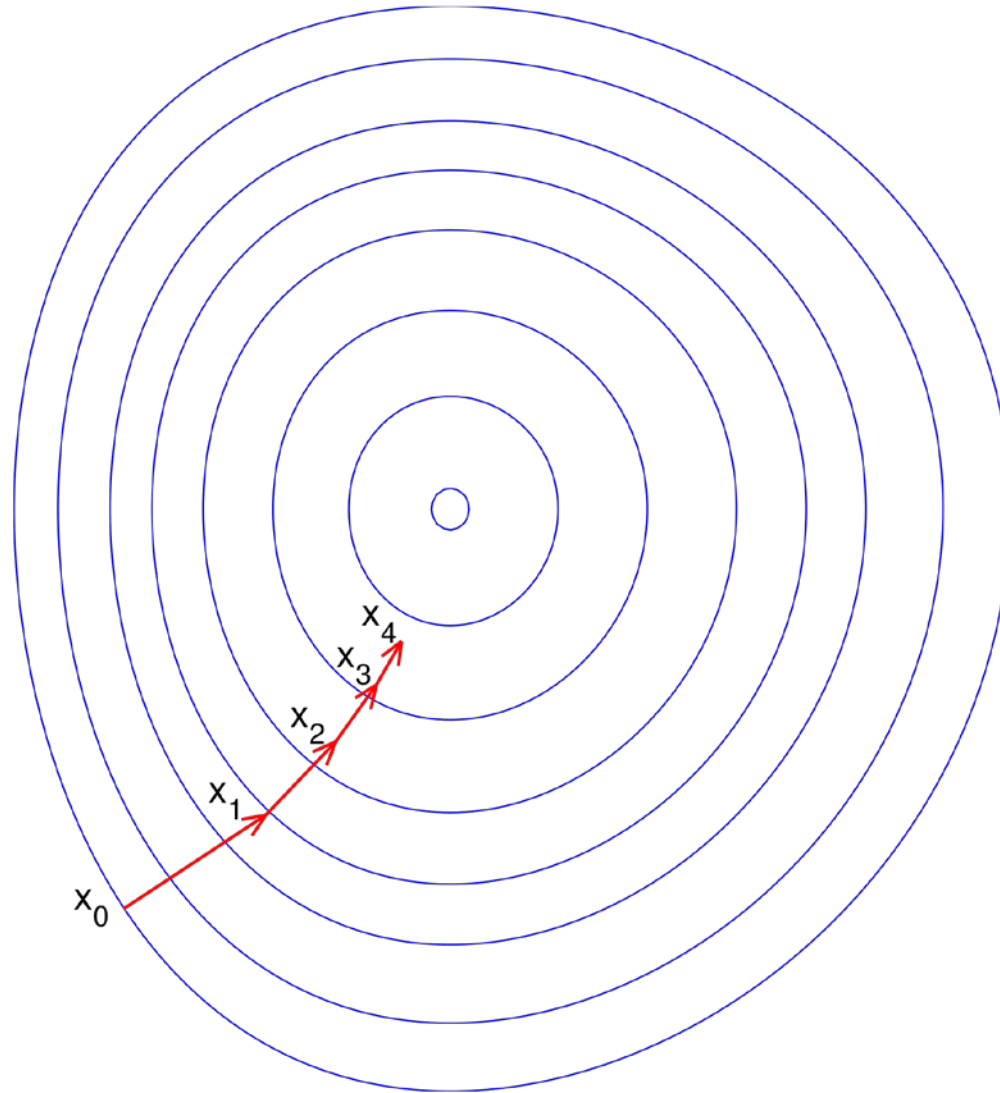
Iterative method to minimize a (convex) differentiable function f

- Pick an initial point x_0
- Iterate until convergence

$$x_{t+1} = x_t - \gamma_t \nabla f(x_t)$$

where γ_t is the t^{th} step size (sometimes called learning rate)

Gradient Descent



$$\min_{a,b} \frac{1}{M} \sum_m (ax^{(m)} + b - y^{(m)})^2$$

- What is the gradient of this function?
- What does a gradient descent iteration look like for this simple regression problem?

(on board)

- In higher dimensions, the linear regression problem is essentially the same with $x^{(m)} \in \mathbb{R}^n$

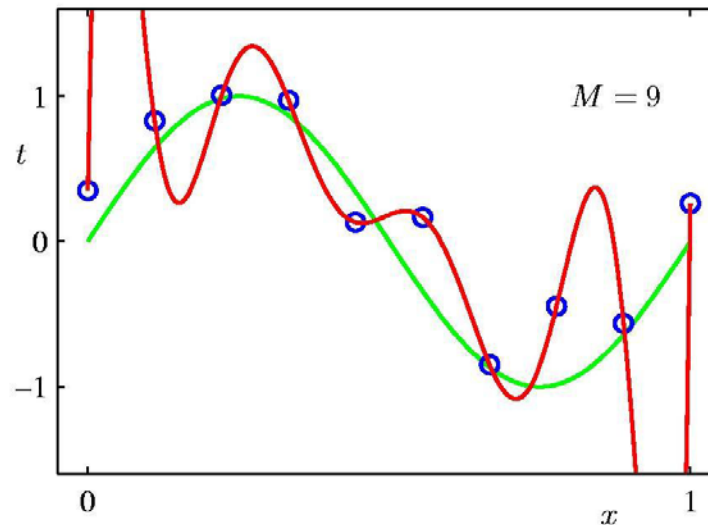
$$\min_{a \in \mathbb{R}^n, b} \frac{1}{M} \sum_m (a^T x^{(m)} + b - y^{(m)})^2$$

- Can still use gradient descent to minimize this
 - Not much more difficult than the $n = 1$ case

- Gradient descent converges under certain technical conditions on the function f and the step size γ_t
 - If f is convex, then any fixed point of gradient descent must correspond to a global optimum of f
 - In general, convergence is only guaranteed to a local optimum

- What if we enlarge the hypothesis class?
 - Quadratic functions
 - k -degree polynomials
- Can we always learn better with a larger hypothesis class?

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- Larger hypothesis space always decreases the cost function, but this does **NOT** necessarily mean better predictive performance
 - This phenomenon is known as **overfitting**
 - Ideally, we would select the **simplest** hypothesis consistent with the observed data
- In practice, we cannot simply evaluate our learned hypothesis on the training data, we want it to perform well on unseen data (otherwise, we can just memorize the training data!)
 - Report the loss on some held out **test data** (i.e., data not used as part of the training process)

Binary Classification



- Regression operates over a continuous set of outcomes
- Suppose that we want to learn a function $f: X \rightarrow \{0,1\}$
- As an example:

	x_1	x_2	x_3	y
1	0	0	1	0
2	0	1	0	1
3	1	1	0	1
4	1	1	1	0

How do we pick the hypothesis space?

How do we find the best f in this space?

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How many functions with three binary inputs and one binary output are there?

Binary Classification



	x_1	x_2	x_3	y
	0	0	0	?
1	0	0	1	0
2	0	1	0	1
	0	1	1	?
	1	0	0	?
	1	0	1	?
3	1	1	0	1
4	1	1	1	0

2^8 possible functions

2^4 are consistent with the observations

How do we choose the best one?

What if the observations are noisy?

- How to choose the right hypothesis space?
 - Number of factors influence this decision: difficulty of learning over the chosen space, how expressive the space is, ...
- How to evaluate the quality of our learned hypothesis?
 - Prefer “simpler” hypotheses (to prevent overfitting)
 - Want the outcome of learning to **generalize** to unseen data

- How do we find the best hypothesis?
 - This can be an NP-hard problem!
 - Need fast, scalable algorithms if they are to be applicable to real-world scenarios

Other Types of Learning



- Unsupervised
 - The training data does not include the desired output
- Semi-supervised
 - Some training data comes with the desired output
- Active learning
 - Semi-supervised learning where the algorithm can ask for the correct outputs for specifically chosen data points
- Reinforcement learning
 - The learner interacts with the world via allowable actions which change the state of the world and result in rewards
 - The learner attempts to maximize rewards through trial and error