

Jets, Substructure, and Searching for Dark Matter at the Large Hadron Collider

by

Siddharth Madhavan Narayanan

Submitted to the Department of Physics
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Author
Department of Physics
August 32, 2018

Certified by.....
Christoph M. E. Paus
Professor of Physics
Thesis Supervisor

Accepted by
Somebody
Chairman, Department Committee on Graduate Theses

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Abstract

Astrophysical observations of gravitational interactions provide strong evidence for the existence of dark matter (DM). Many theories propose and experiments test the hypothesis that DM may have a particle physics origin, but this remains unproven. One such experiment is the Compact Muon Solenoid (CMS) at the Large Hadron Collider (LHC). If DM couples to particles present in protons, it is possible that DM is produced in collisions at the LHC. Because DM, by its very nature, is effectively invisible to CMS, we must look for collisions in which DM is produced in association with one or more Standard Model (SM) particles. This thesis describes three different scenarios for the SM particle hypothesis: a single top quark, a single Higgs boson, or two light quarks. All three cases result in complicated detector signatures due to the hadronization of final-state quarks. Improved jet substructure techniques to identify these unique signatures are presented. Since the observed data is consistent with SM backgrounds in all three searches, we translate this result into the most stringent constraints to date on the relevant beyond-SM models.

Thesis Supervisor: Christoph M. E. Paus
Title: Professor of Physics

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Thank you to Professor Markus Klute for nice barbecues.

Contents

1	The Search for $t + p_{\text{T}}^{\text{miss}}$	15
1.1	Signal selection	19
1.1.1	Online trigger selection	20
1.1.2	Offline signal selection	21
1.2	Background estimation	24
1.2.1	Visible final states to constrain invisible final states	24
1.2.2	Theoretically-limited extrapolations	38
1.3	Results	44
1.3.1	Constraints on mono-top models	48
2	The Search for Invisible Decays of the Higgs Boson	53
2.1	Signal selection	54
2.1.1	Online trigger selection	54
2.1.2	EW and QCD production of electroweak bosons	56
2.1.3	Sensitivity optimization	56
2.2	Background estimation	56
2.3	Results	56
2.3.1	Constraints on Higgs production and decay parameters	56
2.3.2	Constraints on scalar production of DM	56

List of Figures

1.1	Production of mono-top in the SM, in which a top quark is produced in addition to a Z boson and bottom quark. The Z decays to neutrinos, providing large p_T^{miss}	16
1.2	Possible DM production at the LHC, assuming a simplified spin-1 extension to the SM.	17
1.3	Possible DM production at the LHC, assuming the existence of a charged, color scalar that couples to DM and the top quark.	18
1.4	Spectra of DM (missing) momentum under various signal hypothesis.	18
1.5	Comparison of missing and jet momenta in various backgrounds and signal models.	19
1.6	Efficiency of the p_T^{miss} trigger measured in single-muon events.	21
1.7	p_T^{miss} distributions in the two mono-top signal regions. The bottom section of each figure shows the ratio of the data and the prediction. The only uncertainties plotted in these figures are those arising from Poisson fluctuations in data (black bars) and MC (grey band).	22
1.8	Schematic representation of two Z decay modes: to neutrinos (as in the SR) and to muons (as in the CRs). Note that in both cases, U is sensitive to the same effects arising from the measurement of the jet recoiling against the Z boson, whereas $p_T^{\mu\mu}$ is largely independent of the jet.	25
1.9	Various kinematic distributions in the two mono-top $\mu\mu$ CRs. Note the clearly discernable peak in the $m_{\mu\mu}$ distribution near m_Z	26
1.10	Shape uncertainties affecting $T_i^{\mu\mu}$ in both categories, as a function of U	29

1.11	The transfer factors $T_{Z,i}^{\mu\mu}$ as a function of recoil and BDT score. The vertical black bars represent the Poisson uncertainties in the MC simulation, while the grey bands represent the sum of Poisson uncertainties and other, systematic, uncertainties. All uncertainties are represented as one standard deviation.	30
1.12	Various kinematic distributions in the two mono-top ee CRs.	31
1.13	The transfer factors T_i^{ee} as a function of recoil and BDT score. The vertical black bars represent the Poisson uncertainties in the MC simulation, while the grey bands represent the sum of Poisson uncertainties and other, systematic, uncertainties. All uncertainties are represented as one standard deviation.	31
1.14	Schematic representation of the W and $t\bar{t}$ SM processes. In both cases, $U \approx p_T^W$. Furthermore, if the charged lepton is lost, $U = p_T^{\text{miss}} \approx p_T^W$	32
1.15	Various kinematic distributions in the two mono-top $b\mu$ CRs.	34
1.16	Various kinematic distributions in the two mono-top μ CRs.	34
1.17	The transfer factors $\mathbf{T}_{t\bar{t}}^{b\mu}$, \mathbf{T}_W^μ , and $\mathbf{T}_{t\bar{t}}^\mu$; and corresponding shape uncertainties.	35
1.18	Various kinematic distributions in the mono-top be CRs (top) and e CRs (bottom).	36
1.19	The transfer factors $\mathbf{T}_{t\bar{t}}^{be}$, \mathbf{T}_W^e , and $\mathbf{T}_{t\bar{t}}^e$	37
1.20	Theoretical predictions for p_T^Z in Z +jet events and the corresponding k -factors. No detector simulation is applied in these figures; all quantities are directly from MC simulation of the physics process. “LO QCD uncertainty” refers to an estimate of the effect of the QCD renormalization and factorization scales on the LO simulation. The grey band in the ratio is the quadrature sum of the QCD and statistical uncertainties.	40
1.21	Differential k -factors for each of the V +jet processes.	40
1.22	Various kinematic distributions in the two mono-top γ CRs.	41
1.23	The transfer factors \mathbf{T}_γ^γ and $\mathbf{T}_{Z/W}^{\text{SR}}$; and corresponding shape uncertainties.	43

1.24	Data validation of CR-to-CR transfer factors in the loose category. Only ratios with theoretically-limited systematic uncertainties are shown.	45
1.25	Comparison of pre- and post-fit results in the SRs, after simultaneously fitting all channels. The fit is performed having fixed $\mu = 0$.	45
1.26	Comparison of pre- and post-fit results in the single-lepton CRs, after simultaneously fitting all channels. The fit is performed having fixed $\mu = 0$.	46
1.27	Comparison of pre- and post-fit results in the di-lepton and photon CRs, after simultaneously fitting all channels. The fit is performed having fixed $\mu = 0$.	47
1.28	95% CLs upper limits on the cross section of the production of ϕ , where the resonance mass m_ϕ is scanned. Values of m_ϕ for which $\sigma_{95\% \text{ CLs}} < \sigma_{\text{theory}}$ are excluded at 95% confidence level. The dashed black line represents the median expected exclusion, with the green and yellow bands representing the 1 and 2 standard deviation envelopes on the expected exclusion. The red band represents the 1 standard deviation of the uncertainty on the theory cross section (driven by higher-order QCD terms).	48
1.29	95% CLs upper limits on the signal strength ($\mu = \sigma/\sigma_{\text{theory}}$) of the flavor-violating process $pp \rightarrow t\chi\bar{\chi}$ as a function of m_V and m_χ . Two hypotheses are tested: assuming $g_\chi^V, g_q^V \neq 0$ (vector-like) and assuming $g_\chi^A, g_q^A \neq 0$ (axial vector-like).	49
1.30	95% CLs upper limits on the signal strength ($\mu = \sigma/\sigma_{\text{theory}}$) of the flavor-violating process $pp \rightarrow t\chi\bar{\chi}$ as a function of m_V , g_q , and g_χ . Two hypotheses are tested: assuming $g_\chi^V, g_q^V \neq 0$ (vector-like) and assuming $g_\chi^A, g_q^A \neq 0$ (axial vector-like). The DM mass m_χ is fixed at 1 GeV.	50
1.31	Maximum excluded value of m_V for each set of couplings, assuming vector-only couplings.	51

2.1	Diagrams that contribute to the production of the SM Higgs boson at the LHC, with the subsequent decay to DM candidates. The shown diagrams are all chosen to generate large p_T^{miss} through the presence of one or more SM particles in the final state.	54
2.2	Candidate VBF $H \rightarrow \chi\bar{\chi}$ event with two energetic forward jets ($p_T = 180, 107$ GeV) and large p_T^{miss} (360 GeV). Red (blue) towers represent deposits in the hadronic (electromagnetic) calorimeter. Green lines are tracks reconstructed from hits of charged particles in the tracker. The blue arrow represents the direction and magnitude of the p_T^{miss}	55

List of Tables

1.1	Criteria used to select events for the mono-top search signal regions. Note that two SRs are defined, based on the BDT score.	23
1.2	Criteria used to select events for the mono-top $Z \rightarrow \mu\mu$ CR. As with the SR, the region is further split based on the jet BDT score.	27
1.3	Uncertainties affecting the $\mu\mu \leftrightarrow \nu\nu$ extrapolation. “Shape” uncertain- ties have different priors for each bin, but are assumed to be correlated across bins.	29
1.4	Criteria used to select events for the mono-top $b\mu$ CR. As with the SR, the region is further split based on the jet BDT score.	33
1.5	Criteria used to select events for the mono-top μ CR. As with the SR, the region is further split based on the jet BDT score.	33
1.6	Uncertainties affecting the various single-muon extrapolations. “Shape” uncertainties have different priors for each bin, but are assumed to be correlated across bins.	34
1.7	Criteria used to select events for the mono-top γ CR. As with the SR, the region is further split based on the jet BDT score.	41

Chapter 1

The Search for $t + p_{\text{T}}^{\text{miss}}$

In this chapter, we discuss the search for dark matter produced in association with a single top quark (“mono-top”). Since the initial state of pp collisions do not contain any appreciable contribution from top quarks, any process that produces a single top quark must involve some flavor violation. In the Standard Model, any such process is heavily suppressed by off-diagonal elements of the CKM matrix. The SM production mechanism for the mono-top signature (Figure 1.1) involves a b quark in the final state, and thus does not couple the third generation with the first or second. True production of mono-top must introduce some such coupling as an extension to the SM, in addition to one (or more) invisible particle to serve as a DM candidate.

To illustrate how beyond-SM physics can produce this final state, we introduce two DM models: a flavor-changing neutral current V and a charged, colored scalar ϕ . These models will also be used to benchmark the sensitivity of the analysis. However, it should be emphasized that the search is motivated and designed agnostically, without reliance on any specific model; the assumption is that the mono-top final state alone is indicative of new physics, regardless of the specific production mechanism.

The FCNC V is assumed to couple to a fermionic DM candidate χ . A partial Lagrangian of the interaction terms is given by:

$$\mathcal{L}_{\text{int}} = V_{\mu} \bar{\chi} \gamma^{\mu} (g_{\chi}^V + g_{\chi}^A \gamma_5) \chi + \bar{q}_u \gamma^{\mu} (g_u^V + g_u^A \gamma_5) q_u V_{\mu} + \bar{q}_d \gamma^{\mu} (g_d^V + g_d^A \gamma_5) q_d V_{\mu} + \text{h.c.}, \quad (1.1)$$

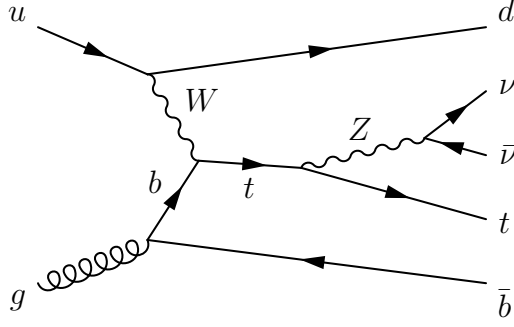


Figure 1.1: Production of mono-top in the SM, in which a top quark is produced in addition to a Z boson and bottom quark. The Z decays to neutrinos, providing large p_T^{miss} .

The model comes with 22 free parameters, broadly organized in three sets:

- The masses m_V and m_χ . (2)
- The couplings g_χ^V and g_χ^A . These, respectively, control the strength of the vector and axial interactions between V and χ . (2)
- The four coupling matrices g_q^X , where $q = u, d$ and $X = V, A$. As before, X determines the type of spin-1 interaction. In principle, different coupling strengths can be permitted for up- and down-type quarks, so this indexed by q . Each g_q^X is a 3×3 matrix, cross-coupling the three quark generations. To preserve $\text{SU}(2)_L$ symmetry, we require $g_u^V - g_u^A = g_d^V - g_d^A$. ($3 \times 6 = 18$)

It is the $g_{u,d}^{V,A}$ matrices that determine whether the model can produce mono-top, or mono-bottom, or mono-up, etc. If $g_{u,d}$ is strongly diagonal (i.e. strongest couplings are within generations), then mono-light quark production will dominate, resulting in the mono-jet final state (Figure 1.2a). On the other hand, if we assume the only non-zero elements are those that couple the first and third generations, then mono-top production at the LHC is the best way to probe this model (Figure 1.2b). It is this latter choice that will be made in the rest of this chapter; other choices are best probed using a combination of multiple DM channels, which is left as future work. Furthermore, to respect $\text{SU}(2)_L$ symmetry, we make the assumption that $g_u^V = g_d^V$ and $g_u^A = g_d^A$.

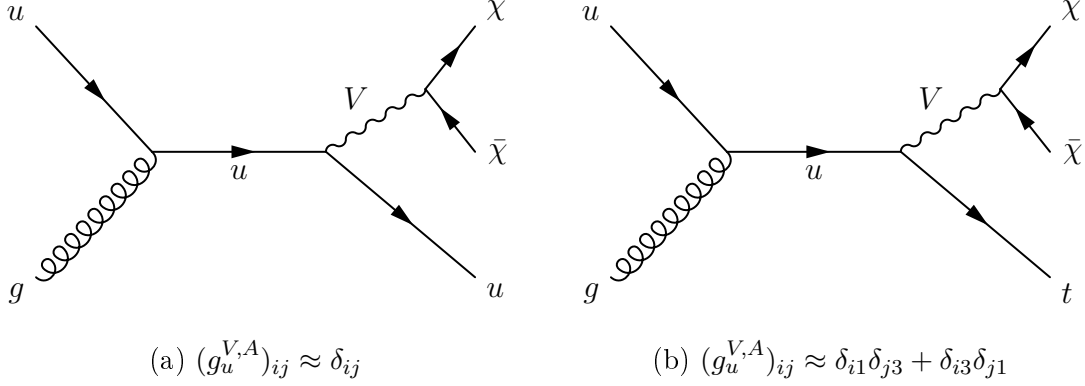


Figure 1.2: Possible DM production at the LHC, assuming a simplified spin-1 extension to the SM.

In the second benchmark model, the charged, colored scalar ϕ couples to down-type quarks, or to a fermionic DM candidate ψ and a top quark. The interaction terms of the Lagrangian is given by:

$$\mathcal{L}_{\text{int}} = \phi \bar{d}_i^C [(a_q)^{ij} + (b_q)^{ij} \gamma^5] d_j + \phi \bar{t} [a_\psi + b_\psi \gamma^5] \psi + \text{h.c.} \quad (1.2)$$

There are 16 free parameters in this model, broadly organized in three categories:

- The masses m_ϕ and m_ψ . (2)
- The couplings at the $\phi \bar{t} \psi$ vertex a_ψ and b_ψ , which respectively control the strength of the scalar and pseudoscalar interactions. (2)
- The couplings at the $\phi \bar{d}_i d_j$ vertex a_q^{ij} and b_q^{ij} where $i, j = 1, 2, 3$. Again, a and b refer the scalar and pseudoscalar couplings, respectively. (12)

In this model, mono-top production primarily occurs through the resonant decay of ϕ to ψ and t , as shown in Figure 1.3.

The two benchmark models show markedly different spectra in Figure 1.4, motivating their use to test different modes of mono-top production. The FCNC produces a falling p_T^{miss} distribution, whereas the scalar resonance produces a p_T^{miss} distribution peaking at approximately $m_\phi/2$.

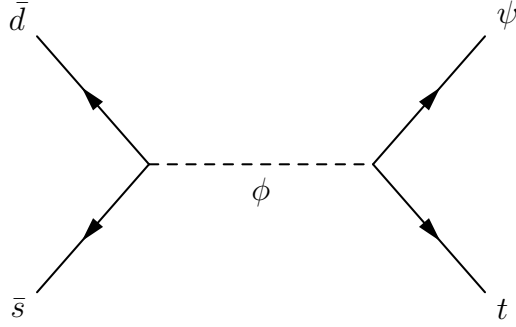


Figure 1.3: Possible DM production at the LHC, assuming the existence of a charged, color scalar that couples to DM and the top quark.

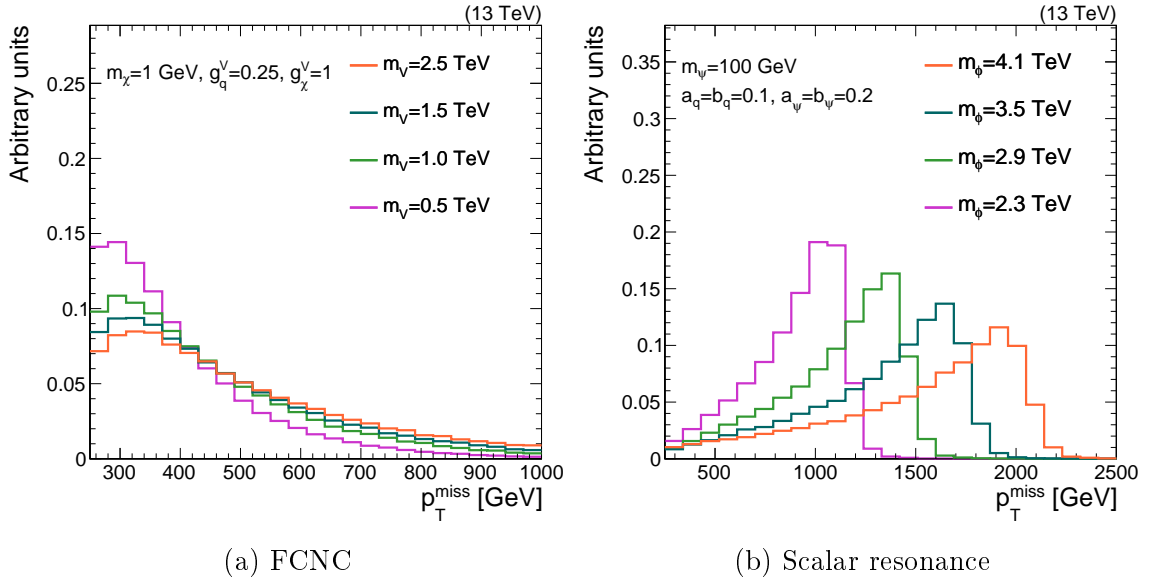


Figure 1.4: Spectra of DM (missing) momentum under various signal hypothesis.

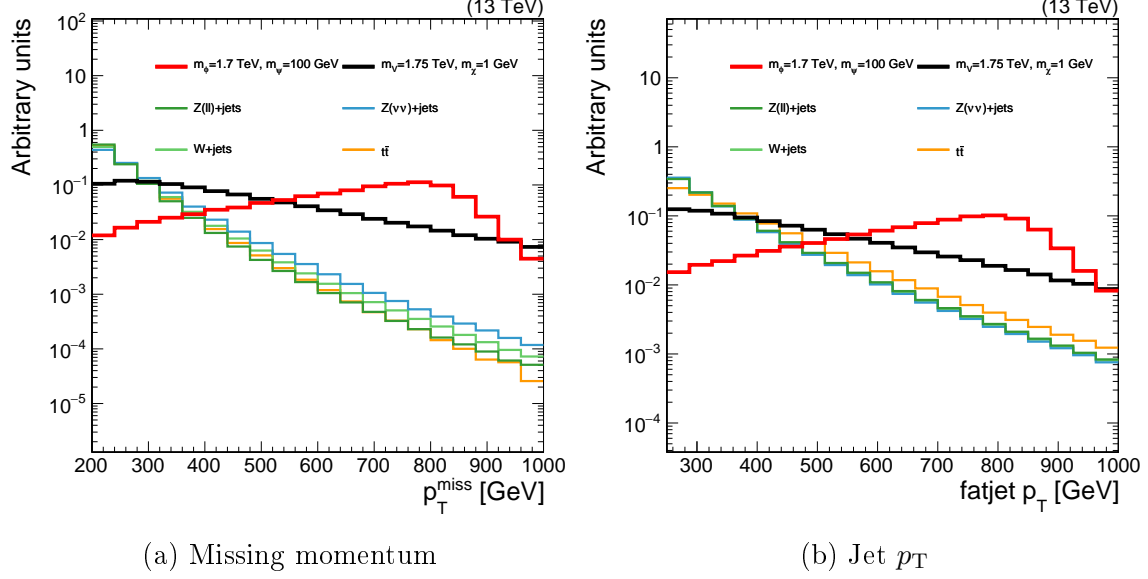


Figure 1.5: Comparison of missing and jet momenta in various backgrounds and signal models.

1.1 Signal selection

When looking at events that pass a simple set of criteria (moderate p_T^{miss} and one CA15 jet), it is clear (Figure 1.5) that the highest signal sensitivity is found in regions of high p_T^{miss} and jet p_T . The three primary background processes are:

- $Z \rightarrow \nu\nu$. When the Z is produced in association with one or more jets, the jet system can (with low probability) pass the criteria used to select a top jet. The neutrinos manifest as p_T^{miss} .
- $W \rightarrow \ell\nu$. As in the case of the Z , additional jets can mimic the signature of a top jet. Typically, the charged lepton in the final state is vetoed, but if it is out of acceptance (e, μ) or fails ID criteria (τ_h), then it is not identified.
- $t\bar{t} \rightarrow bq\bar{q}' + \bar{b}\ell\nu$. As in the case of the W , a charged lepton in the final state may not be properly identified. Unlike the previous two processes, a semi-leptonic $t\bar{t}$ event contains a real hadronic top quark decay.

1.1.1 Online trigger selection

Data events are first selected by the L1 trigger system by requiring $p_{\text{T,L1}}^{\text{miss}} > 70$ GeV, where:

$$p_{\text{T,L1}}^{\text{miss}} = - \left(\sum_{i \in C} \vec{p}_i \right)_{\text{T}}, \quad C = \{\text{calorimeter deposits with } |\eta| < 3.0\} \quad (1.3)$$

Events that pass this selection are sent to the HLT system, where we place requirements on the both the missing momentum ($p_{\text{T,HLT}}^{\text{miss}}$) and the missing hadronic momentum ($H_{\text{T,HLT}}^{\text{miss}}$). These are defined as:

$$p_{\text{T,HLT}}^{\text{miss}} = - \left(\sum_{i \in \text{particles}} \vec{p}_i \right)_{\text{T}}, \quad \text{all particles except muons} \quad (1.4)$$

$$H_{\text{T,HLT}}^{\text{miss}} = - \left(\sum_{i \in \text{jets}} \vec{p}_i \right)_{\text{T}}, \quad \text{jets passing noise-rejection ID} \quad (1.5)$$

The HLT decides to keep an event if $\min(p_{\text{T,HLT}}^{\text{miss}}, H_{\text{T,HLT}}^{\text{miss}})$ is higher than a specified threshold. Over the course of the data-taking period considered in this chapter, this threshold varied from 90 to 120 GeV.

Note that in all of the trigger decisions, muons are implicitly (in the L1) or explicitly (in the HLT) excluded from the missing momentum calculations. This means that an event which produces high-momentum muons can be selected using these triggers. This flexibility will be exploited in Section 1.2.

Since the online environment and reconstruction are significantly limited as compared to the offline reconstruction of U , we do not expect the trigger decision to be a step function at $U = 120$ GeV. Therefore, we define and measure a trigger efficiency:

$$\epsilon_{\text{trig}}(U) = \frac{N_{\text{pass trig}}(U)}{N(U)} \quad (1.6)$$

This is measured using $W \rightarrow \mu\nu$ events containing one or more high- p_{T} jets. The events are triggered using single- μ triggers (which have lower thresholds and efficiencies ~ 1 in this phase space). We then require events have exactly one well-identified

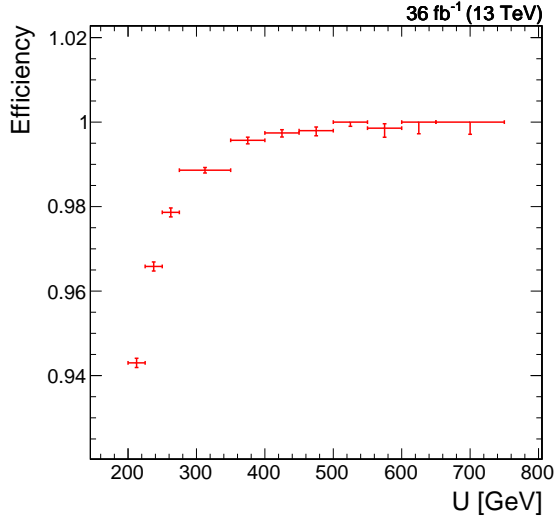


Figure 1.6: Efficiency of the p_T^{miss} trigger measured in single-muon events.

muon and at least one jet with $p_T > 100$ GeV. Figure 1.6 shows the efficiency as a function of U . To avoid the steeply-rising part of the curve, we choose a threshold of $U > 250$ GeV in the analysis.

1.1.2 Offline signal selection

Events in the signal regions (SRs) are then selected according to Table 1.1, chosen to be consistent with the signal topology while mitigating the aforementioned SM backgrounds. As described in Section ??, two working points (WPs) are defined for the top ID BDT. The signal events (passing all other selection criteria) are partitioned into a “loose” SR and a “tight” SR on the basis of which WP the top candidate jet satisfies.

Figure 1.7 shows the p_T^{miss} distributions, as predicted by MC and as observed in collected data, in the two signal regions.

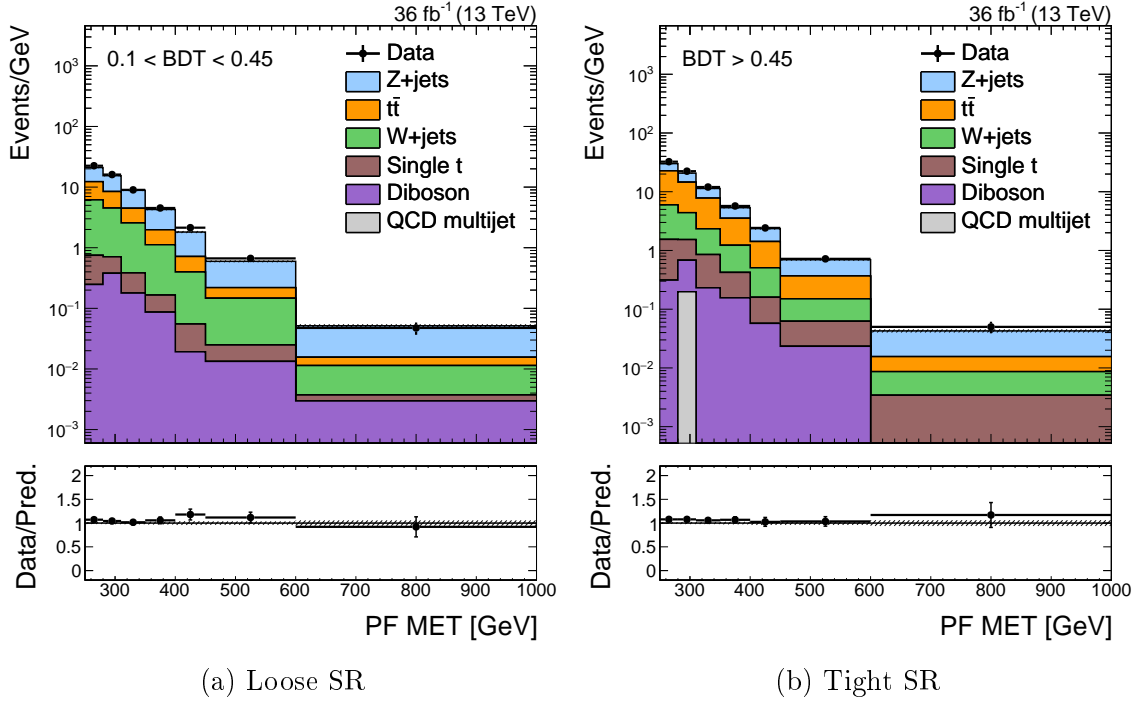


Figure 1.7: p_T^{miss} distributions in the two mono-top signal regions. The bottom section of each figure shows the ratio of the data and the prediction. The only uncertainties plotted in these figures are those arising from Poisson fluctuations in data (black bars) and MC (grey band).

Table 1.1: Criteria used to select events for the mono-top search signal regions. Note that two SRs are defined, based on the BDT score.

Criterion	Notes
$p_T^{\text{miss}} > 250 \text{ GeV}$	Signal events should have large missing momentum. Exact threshold is chosen to maximize online trigger efficiency.
1 CA15 jet with $p_T > 250 \text{ GeV}$	Top quark candidate. Recoils against p_T^{miss} , so threshold is set at 250 GeV.
CA15 jet $110 < m_{\text{SD}} < 210 \text{ GeV}$	Consistency with top quark mass.
At least one b -tagged sub-jet	Identifying B hadron produced from top decay/hadronization.
No b -tagged narrow jets	Rejecting semi-leptonic $t\bar{t}$ decays.
No identified e, μ, τ_h	Suppress W +jet and $t\bar{t}$ processes.
No identified γ	Suppress γ +jet processes.
$\min_{\text{jets}} \Delta\phi(\text{jet}, p_T^{\text{miss}}) > 0.5$	Remove events with large p_T^{miss} caused by mismeasured jets.
CA15 jet BDT	Identifying top decay structure. If the jet passes the tight WP, it is placed in the “tight” SR. Otherwise, if it only passes the loose WP, it is placed in the “loose” SR.

1.2 Background estimation

Searching for DM amounts to looking for an excess of data events over the SM prediction at large values of p_T^{miss} . Therefore, the p_T^{miss} distribution of the three primary SM backgrounds described in Section 1.1 must be predicted with small uncertainty. The MC simulation provides a reasonable description of the data, but the theoretical uncertainties inherent in the MC (primarily due to higher-order QCD effects) can range up to 20%. To reduce the prediction uncertainty further, a “data-driven” approach is used to estimate the SM processes in the SR. In this context, “data-driven” refers to the use of control data (i.e. data that cannot contain signal) to directly estimate or supplement the estimation of SM processes in the SR.

1.2.1 Visible final states to constrain invisible final states

As a starting point, let us tackle the estimation of $Z \rightarrow \nu\nu$ in the SR. Since the momentum imbalance (up to experimental effects) in a $Z \rightarrow \nu\nu$ event is just the transverse momentum of the Z boson (p_T^Z), we must estimate p_T^Z . To good approximation, the p_T^Z distribution is independent of the decay mode of the Z boson. Therefore, it is natural to estimate $p_T^{\text{miss}}(Z \rightarrow \nu\nu)$ by measuring $p_T^Z(Z \rightarrow \mu\mu)$, as muons are easily identifiable and reconstructible.

However, there is one important distinction between $\nu\nu$ and $\mu\mu$ events. In the latter, p_T^Z can be directly measured, whereas in the former it must be inferred through a momentum imbalance. Effects like jet energy scale and acceptance can impact p_T^{miss} , but not $p_T^{\mu\mu}$. Therefore, instead of directly measuring $p_T^{\mu\mu}$ in $\mu\mu$ events, we define and use the hadronic recoil U :

$$\vec{U} = \vec{p}_T^{\text{miss}} + \sum_{\mu} \vec{p}_T^{\mu} + \sum_e \vec{p}_T^e + \sum_{\gamma} \vec{p}_T^{\gamma} \quad (1.7)$$

In the SR (where there are no e, μ, γ), $U = p_T^{\text{miss}}$. In $Z \rightarrow \mu\mu$ events, U mimics the momentum imbalance, if we had pretended the identified muons did not exist when computing p_T^{miss} . Therefore, U is an exact analogy for p_T^{miss} in the SR. Figure 1.8

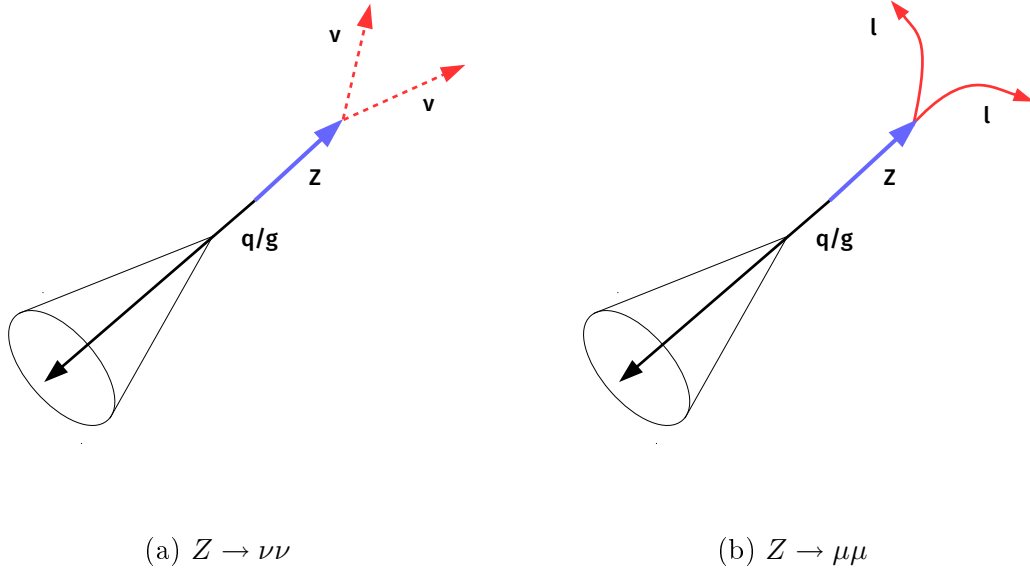


Figure 1.8: Schematic representation of two Z decay modes: to neutrinos (as in the SR) and to muons (as in the CRs). Note that in both cases, U is sensitive to the same effects arising from the measurement of the jet recoiling against the Z boson, whereas $p_T^{\mu\mu}$ is largely independent of the jet.

makes the same argument in a schematic fashion.

Table 1.2 describes the criteria used to define events in the “ $\mu\mu$ ” control regions (CRs). Figure 1.9 shows the distribution of U in these CRs, as well as the $m_{\mu\mu}$ and p_T^μ distributions.

The control data is used to constrain the SR prediction by means of “transfer factors” $T_{Y,i}^X$, where X refers to a particular CR (e.g. $\mu\mu$), Y refers to a particular process (e.g. Z), and i refers to a particular bin in the CR (e.g. $200 < U < 250$ GeV in the tight category). Formally:

$$T_{Z,i}^{\mu\mu} = \frac{N_i^{\text{SR}}(Z \rightarrow \nu\nu)}{N_i^{\mu\mu}(Z \rightarrow \mu\mu)} \quad (1.8)$$

The transfer factors are estimated using MC simulation. To encode the effects of

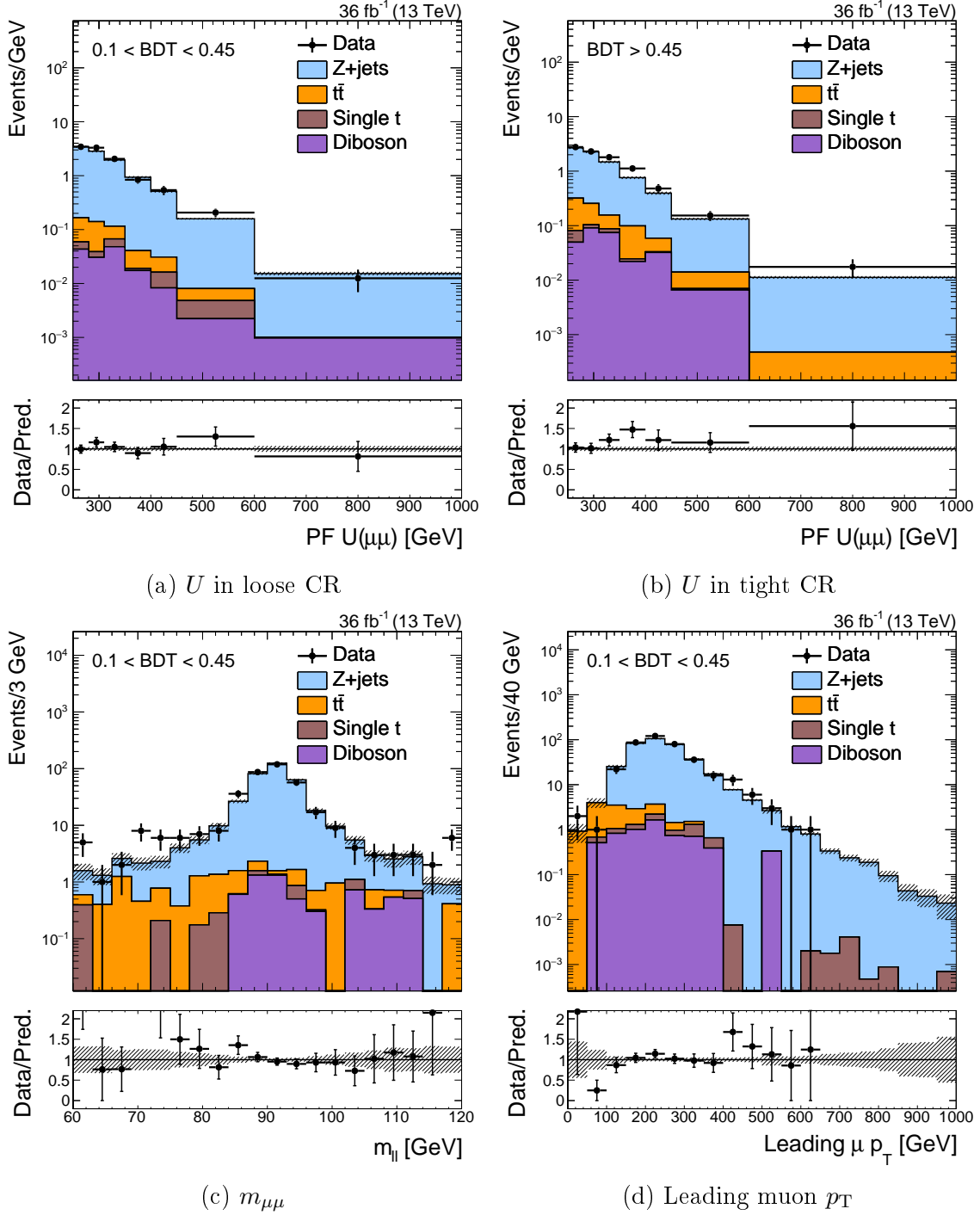


Figure 1.9: Various kinematic distributions in the two mono-top $\mu\mu$ CRs. Note the clearly discernable peak in the $m_{\mu\mu}$ distribution near m_Z

Table 1.2: Criteria used to select events for the mono-top $Z \rightarrow \mu\mu$ CR. As with the SR, the region is further split based on the jet BDT score.

Criterion	Notes
$U > 250$ GeV	Mimicking the selection in the SR; also constrained by trigger thresholds.
1 CA15 jet with $p_T > 250$ GeV	Same as SR
CA15 jet $110 < m_{SD} < 210$ GeV	Same as SR
Well-identified μ^-, μ^+ pair, with $ m_{\mu\mu} - m_Z < 30$ GeV	Identifying the $Z \rightarrow \mu\mu$ resonance.
No identified e, τ_h	Same as SR.
No identified γ	Same as SR
$\min_{\text{jets}} \Delta\phi(\text{jet}, U) > 0.5$	Same as SR
CA15 jet BDT	Same as SR

various uncertainties, we introduce nuisance parameters $\boldsymbol{\theta}$. That is:

$$T_{Y,i}^X \rightarrow T_{Y,i}^X(\boldsymbol{\theta}) \equiv T_{Y,i}^X \times \prod_{j=0}^{n_\theta} (1 + \theta_j) \quad (1.9)$$

$$\theta_j \sim p_j(\theta_j) \quad (1.10)$$

where n_θ is the number of nuisance parameters and $p_j(\theta_j)$ is some prior distribution for each nuisance (see below for how the priors are used). The priors are typically chosen to have a central value (e.g. mean, median) at 0, with a finite variance that encodes the uncertainty. In this chapter, we assume p_j is either a normal distribution centered at 0 or a log-normal distribution (in cases where negative values are undesirable). We will use the terms “uncertainty” and “nuisance parameter” interchangeably.

Let $\text{Pois}(d|\lambda)$ refer to the Poisson probability of observing d with an expected mean of λ . In terms of these transfer factors, the likelihood for the data observed in the signal and $\mu\mu$ control regions is:

$$\begin{aligned} \mathcal{L}(\mathbf{d} \mid \mu, \boldsymbol{\mu}_{\text{SR}}^{Z \rightarrow \nu\nu}, \boldsymbol{\theta}) = \prod_{i \in \text{bins}} & \left[\text{Pois}(d_i^{\text{SR}} \mid \mu S_i^{\text{SR}}(\boldsymbol{\theta}) + \mu_{\text{SR},i}^{Z \rightarrow \nu\nu} + B_i^{\text{SR}}(\boldsymbol{\theta})) \right. \\ & \left. \times \text{Pois}\left(d_i^{\mu\mu} \mid \frac{\mu_{\text{SR},i}^{Z \rightarrow \nu\nu}}{T_{Z,i}^{\mu\mu}(\boldsymbol{\theta})} + B_i^{\mu\mu}(\boldsymbol{\theta})\right) \right] \times \prod_{j=0}^{n_\theta} p_j(\theta_j) \quad (1.11) \end{aligned}$$

where the following notation is used:

d_i^X : The data observed in bin i of region X . For now, $X = \text{SR}, \mu\mu$.

S_i^{SR} : The predicted number of signal events in bin i of the SR, under some fixed signal hypothesis.

μ : The “signal strength”. Essentially an unconstrained nuisance parameter that scales up or down the total signal yield.

$\mu_{\text{SR},i}^P$: The expected number of events from process P in bin i of the SR. This is also an unconstrained nuisance parameter.

B_i^X : The predicted number of “minor” background events in bin i of region X . Here, “minor” refers to all SM processes that are not the signal and are not estimated using a data-driven method.

The signal and background yields \mathbf{S} and \mathbf{B} are estimated using MC. Note that the inclusion of the priors in the likelihood constrains the nuisance parameters to be close to their “nominal” values; moving a θ_j to fit the data incurs a large cost from the prior.

If we set $B_i = \mu = 0$ (the null hypothesis, ignoring small minor backgrounds), a simple picture emerges of how the likelihood is maximized. The parameters $\boldsymbol{\mu}_{\text{SR}}^{Z \rightarrow \nu\nu}$ float freely to satisfy $d_{\text{SR},i} \sim \mu_{\text{SR},i}^{Z \rightarrow \nu\nu}$ and $d_{\mu\mu,i} \sim \mu_{\text{SR},i}^{Z \rightarrow \nu\nu} / T_{Z,i}^{\mu\mu}(\boldsymbol{\theta})$. If both constraints cannot be satisfied simultaneously by scaling $\boldsymbol{\mu}_{\text{SR}}^{Z \rightarrow \nu\nu}$, the (constrained) nuisance parameters $\boldsymbol{\theta}$ modify the transfer factor $\mathbf{T}_Z^{\mu\mu}$. Table 1.6 shows the relevant uncertainties for $\mathbf{T}_Z^{\mu\mu}$, and Figure 1.10 shows the shape of uncertainties that evolve as a function of U .

The transfer factors are shown in Figure 1.11. The exact values of $\mathbf{T}_Z^{\mu\mu}(\boldsymbol{\theta})$ have two salient features:

1. The values are strictly greater than one. This is due to (a) $\mathcal{B}(Z \rightarrow \nu\nu) > \mathcal{B}(Z \rightarrow \mu\mu)$ and (b) a non-100% efficiency in reconstructing and identifying muons. This implies that the constraining power of the $\mu\mu$ CR is less than that of the SR, especially at high U (i.e. the Poisson uncertainties are larger).

Table 1.3: Uncertainties affecting the $\mu\mu \leftrightarrow \nu\nu$ extrapolation. “Shape” uncertainties have different priors for each bin, but are assumed to be correlated across bins.

Uncertainty	1 s.d.	Notes
μ ID	2%	
μ track	1%	
τ_h veto	3%	
Z +heavy flavor	3%	
Trigger	0-2%	Shape
b -tag	$\sim 0.5\%$	Shape
$udcsg$ -mistag	3-4%	Shape

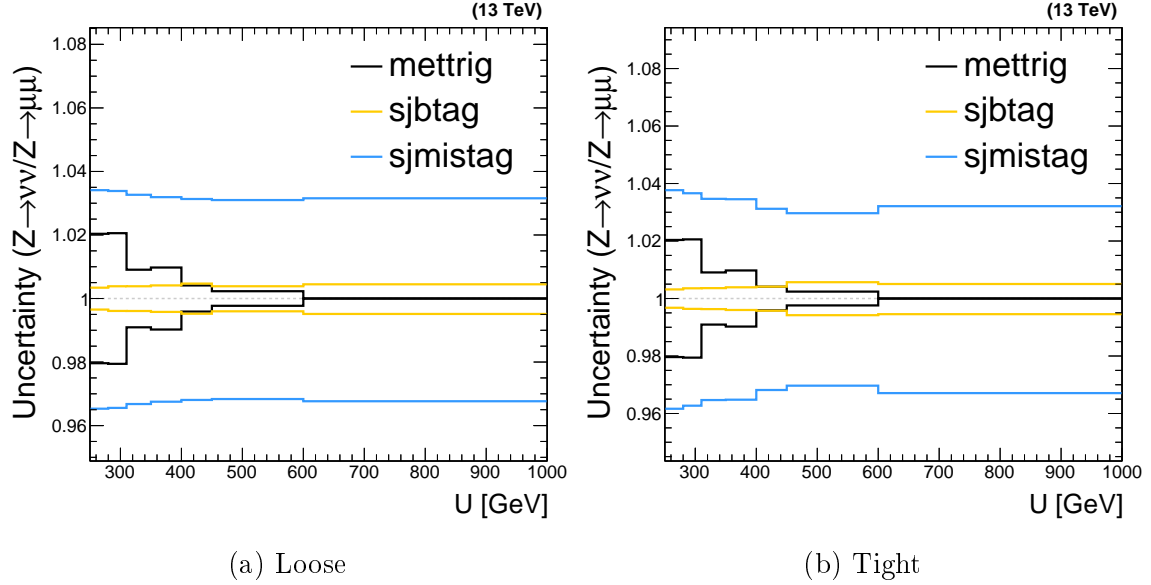


Figure 1.10: Shape uncertainties affecting $T_i^{\mu\mu}$ in both categories, as a function of U .

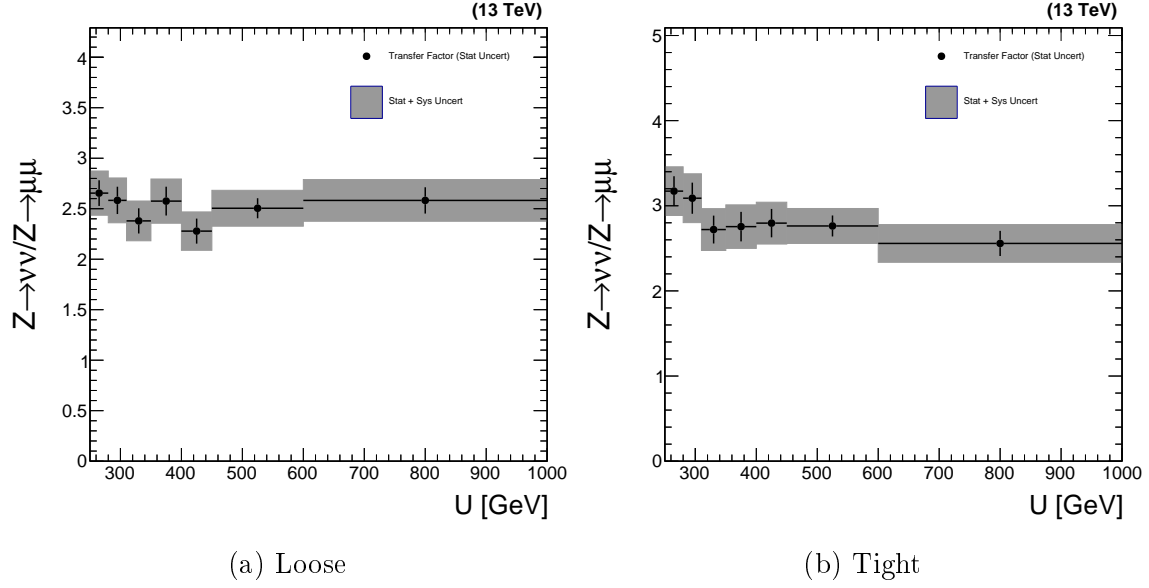


Figure 1.11: The transfer factors $T_{Z,i}^{\mu\mu}$ as a function of recoil and BDT score. The vertical black bars represent the Poisson uncertainties in the MC simulation, while the grey bands represent the sum of Poisson uncertainties and other, systematic, uncertainties. All uncertainties are represented as one standard deviation.

2. The one standard deviation variation of all uncertainties that impact $T_{Z,i}^{\mu\mu}$ are contained within a 10% envelope. This is already a factor of two smaller than the inherent $\sim 20\%$ uncertainties in the MC simulation.

To account for point (1), we can simply add more control data by also looking at $Z \rightarrow ee$ decays. Essentially all of the arguments used for the $\mu\mu$ CRs applies to the ee CRs. Figures 1.12-1.13 show the data/simulation agreement and the transfer factors for the new dielectron regions. A further set of statistical constraints to improve the estimate at high U (which is where the signals are most enhanced) is described in Section 1.2.2.

Similar methods are used to predict the W +jets and $t\bar{t}$ contributions in the SRs; these three backgrounds comprise at least 95% of the SM processes. In both cases, the momentum imbalance in the SR is a proxy for the momentum of the W boson, since the charged lepton is lost. A sketch of the event topologies is shown in Figure 1.14. Following the same arguments as used for the $Z \rightarrow \ell\ell$ CRs, we can use the hadronic recoil U in CRs that measure visible final states of W and $t\bar{t}$.

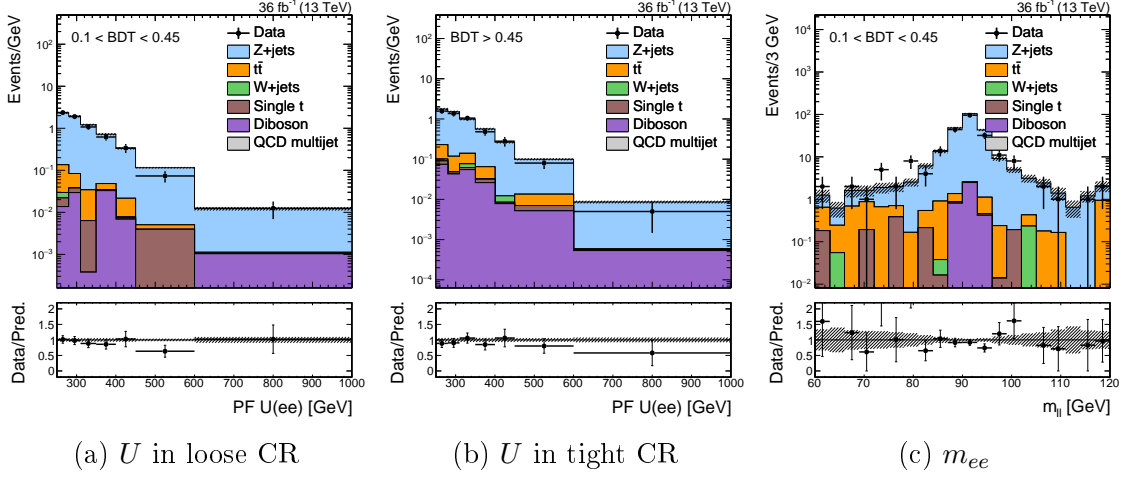


Figure 1.12: Various kinematic distributions in the two mono-top ee CRs.

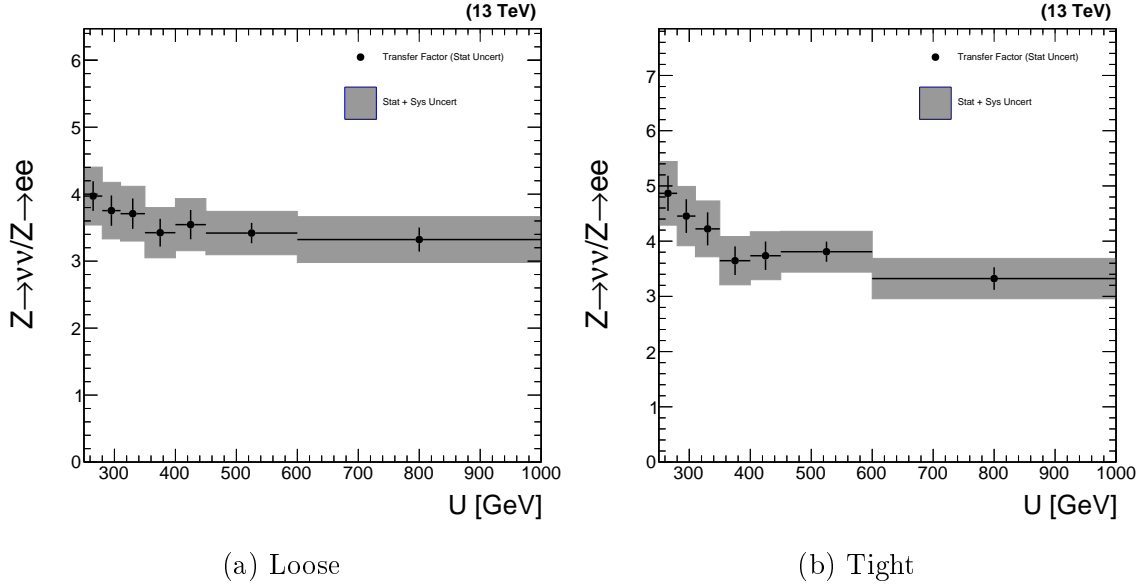


Figure 1.13: The transfer factors T_i^{ee} as a function of recoil and BDT score. The vertical black bars represent the Poisson uncertainties in the MC simulation, while the grey bands represent the sum of Poisson uncertainties and other, systematic, uncertainties. All uncertainties are represented as one standard deviation.

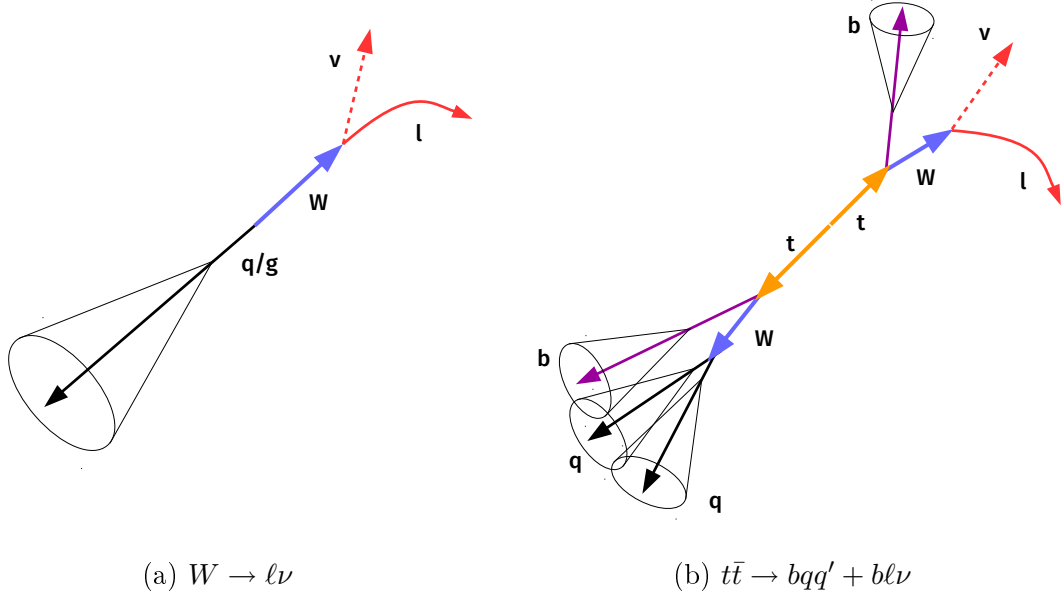


Figure 1.14: Schematic representation of the W and $t\bar{t}$ SM processes. In both cases, $U \approx p_T^W$. Furthermore, if the charged lepton is lost, $U = p_T^{\text{miss}} \approx p_T^W$.

Starting with muon final states (electrons will follow naturally), we define two sets of CRs based on the number of identified B hadrons. The selection for the $b\mu$ CRs (to measure $t\bar{t}$) is shown in Table 1.4. The selection for the μ CRs (to measure W) is shown in Table 1.5. Figures 1.15-1.16 show various kinematic distributions in these regions.

Each CR gets a set of transfer factors to constrain the targetted process in the SR: $\mathbf{T}_{t\bar{t}}^{b\mu}$ and \mathbf{T}_W^μ . In the tight μ CR (Figures 1.16b-1.16c), the stringent top ID requirement enhances the $t\bar{t}$ and suppresses the W contribution. Since we cannot create a pure W in the tight category, we introduce an additional set of transfer factors $\mathbf{T}_{t\bar{t}}^\mu$. This extra constraint uses the $b\mu$ CRs to estimate the $t\bar{t}$ component in the μ CRs, thereby leaving only one large degree of freedom in the μ CRs. These three sets of transfer factors, and the corresponding uncertainties, are shown in Figure 1.17.

As we added the ee CRs to complement the $\mu\mu$ CRs, we also add be (e) CRs to augment the statistical power of the $b\mu$ (μ) CRs, especially at high recoil. Figures 1.18 and 1.19 respectively show some kinematic distributions and the transfer factors corresponding to these electron constraints.

Table 1.4: Criteria used to select events for the mono-top $b\mu$ CR. As with the SR, the region is further split based on the jet BDT score.

Criterion	Notes
$U > 250$ GeV	Mimicking the selection in the SR; also constrained by trigger thresholds.
1 CA15 jet with $p_T > 250$ GeV	Same as SR
CA15 jet $110 < m_{SD} < 210$ GeV	Same as SR
At least one b -tagged sub-jet	Identifying B hadron produced from hadronic top decay.
Exactly one b -tagged narrow jet	Identifying B hadron produced from leptonic top decay.
Exactly one well-identified μ	Produced from $W \rightarrow \mu\nu$
No identified e, τ_h	Same as SR.
No identified γ	Same as SR
$\min_{\text{jets}} \Delta\phi(\text{jet}, U) > 0.5$	Same as SR
CA15 jet BDT	Same as SR

Table 1.5: Criteria used to select events for the mono-top μ CR. As with the SR, the region is further split based on the jet BDT score.

Criterion	Notes
$U > 250$ GeV	Mimicking the selection in the SR; also constrained by trigger thresholds.
1 CA15 jet with $p_T > 250$ GeV	Same as SR
CA15 jet $110 < m_{SD} < 210$ GeV	Same as SR
No b -tagged sub-jets	Suppressing semi-leptonic $t\bar{t}$ decays
No b -tagged narrow jets	Suppressing semi-leptonic $t\bar{t}$ decays
Exactly one well-identified μ	Produced from $W \rightarrow \mu\nu$
No identified e, τ_h	Same as SR.
No identified γ	Same as SR
$\min_{\text{jets}} \Delta\phi(\text{jet}, U) > 0.5$	Same as SR
CA15 jet BDT	Same as SR

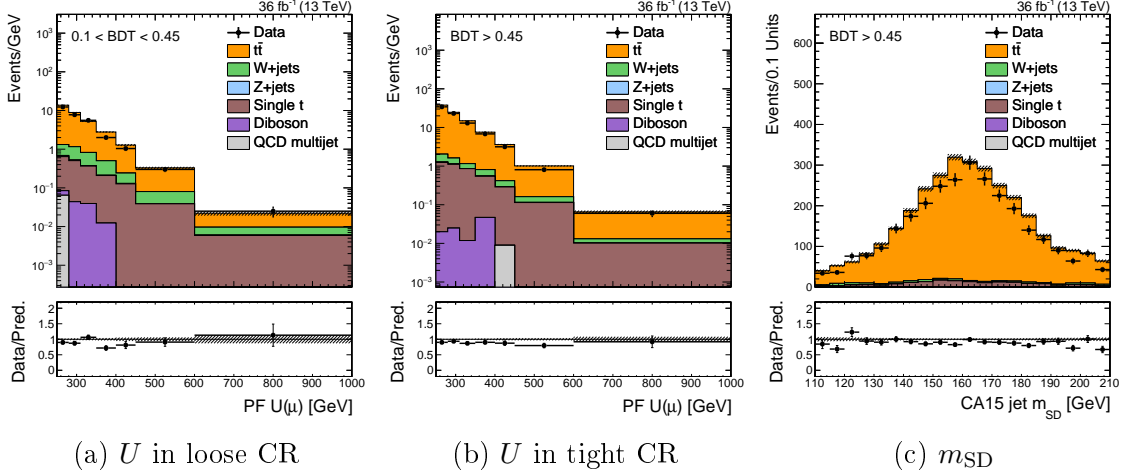


Figure 1.15: Various kinematic distributions in the two mono-top $b\mu$ CRs.

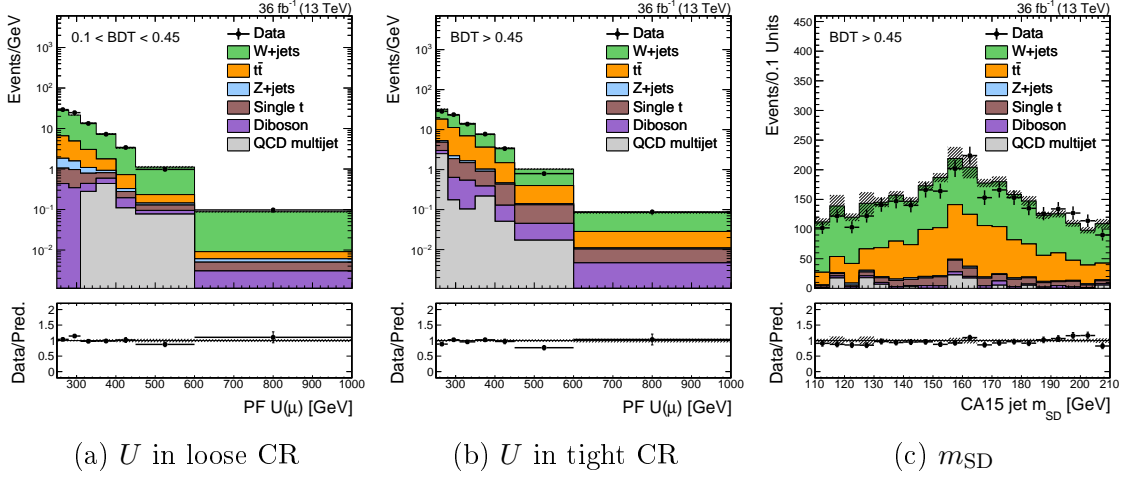


Figure 1.16: Various kinematic distributions in the two mono-top μ CRs.

Table 1.6: Uncertainties affecting the various single-muon extrapolations. “Shape” uncertainties have different priors for each bin, but are assumed to be correlated across bins.

Uncertainty	1 s.d. ($T_{t\bar{t}}^{b\mu}$)	1 s.d. (T_W^μ)	1 s.d. ($T_{t\bar{t}}^\mu$)	Notes
μ ID	1%	1%	1%	
μ track	0.5%	0.5%	0.5%	
τ_h veto	3%	3%	3%	
W +heavy flavor		3%		
Trigger	0-2%	0-2%	0-2%	Shape
b -tag	2%	$\sim 0.5\%$	3-6%	Shape
$udcsg$ -mistag	1%	5%	1%	Shape

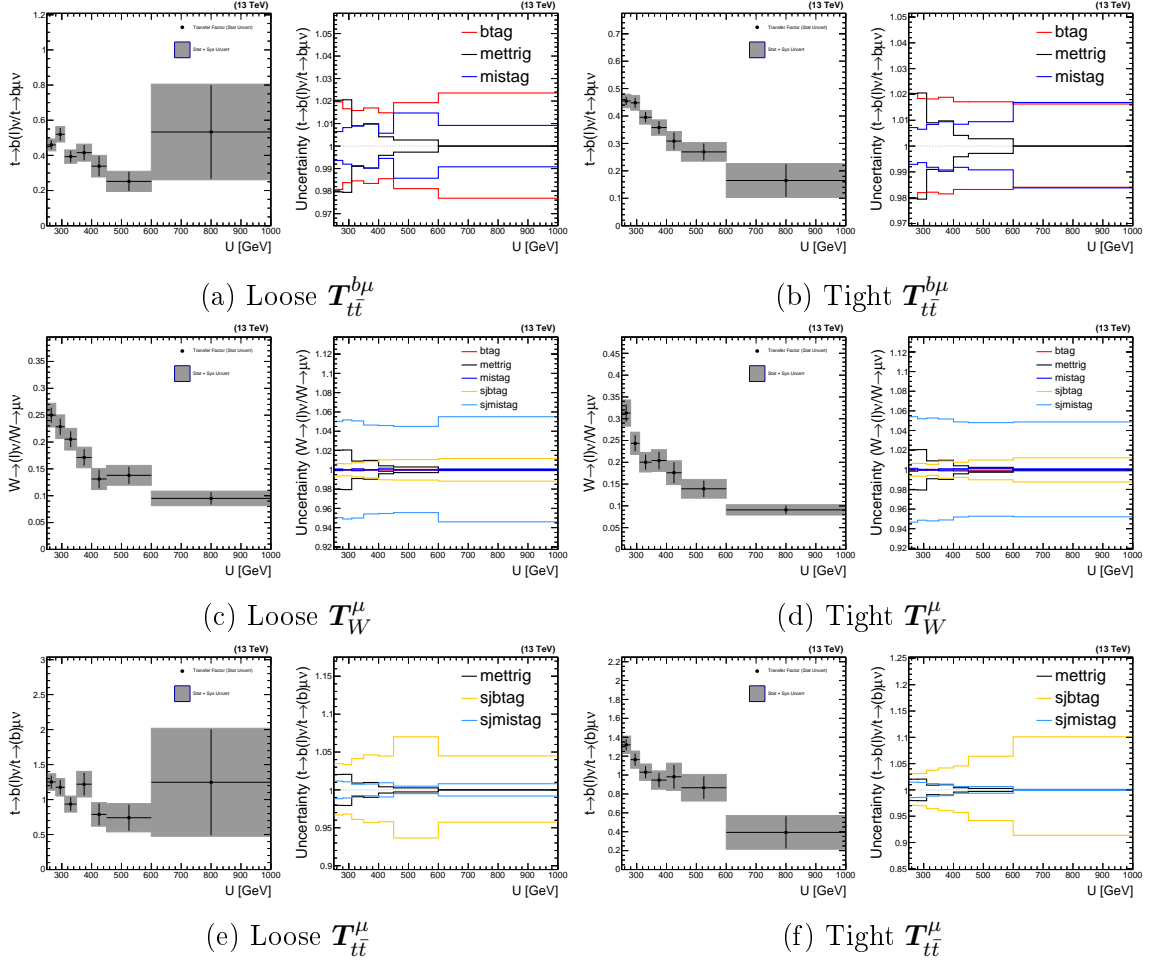


Figure 1.17: The transfer factors $T_{tt}^{b\mu}$, T_W^μ , and T_{tt}^μ ; and corresponding shape uncertainties.

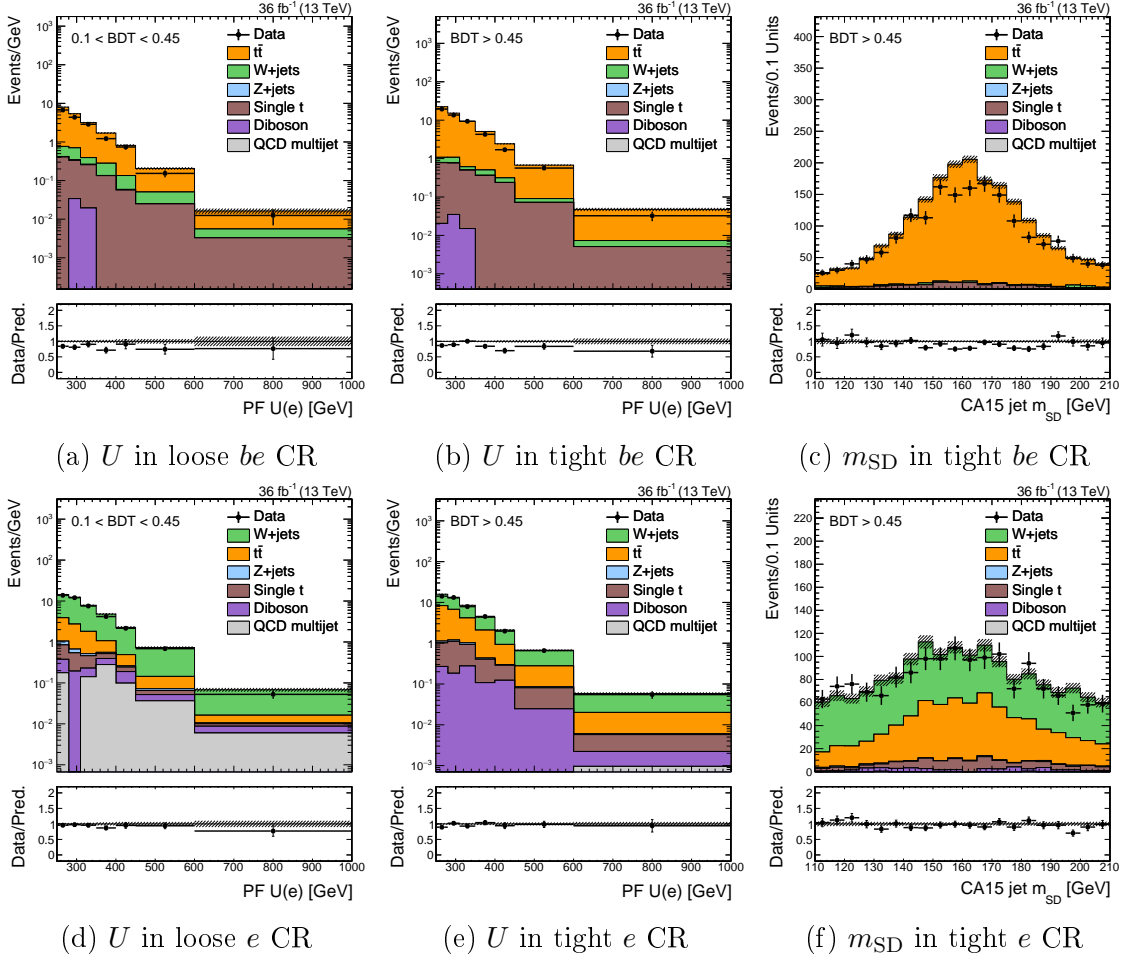


Figure 1.18: Various kinematic distributions in the mono-top be CRs (top) and e CRs (bottom).

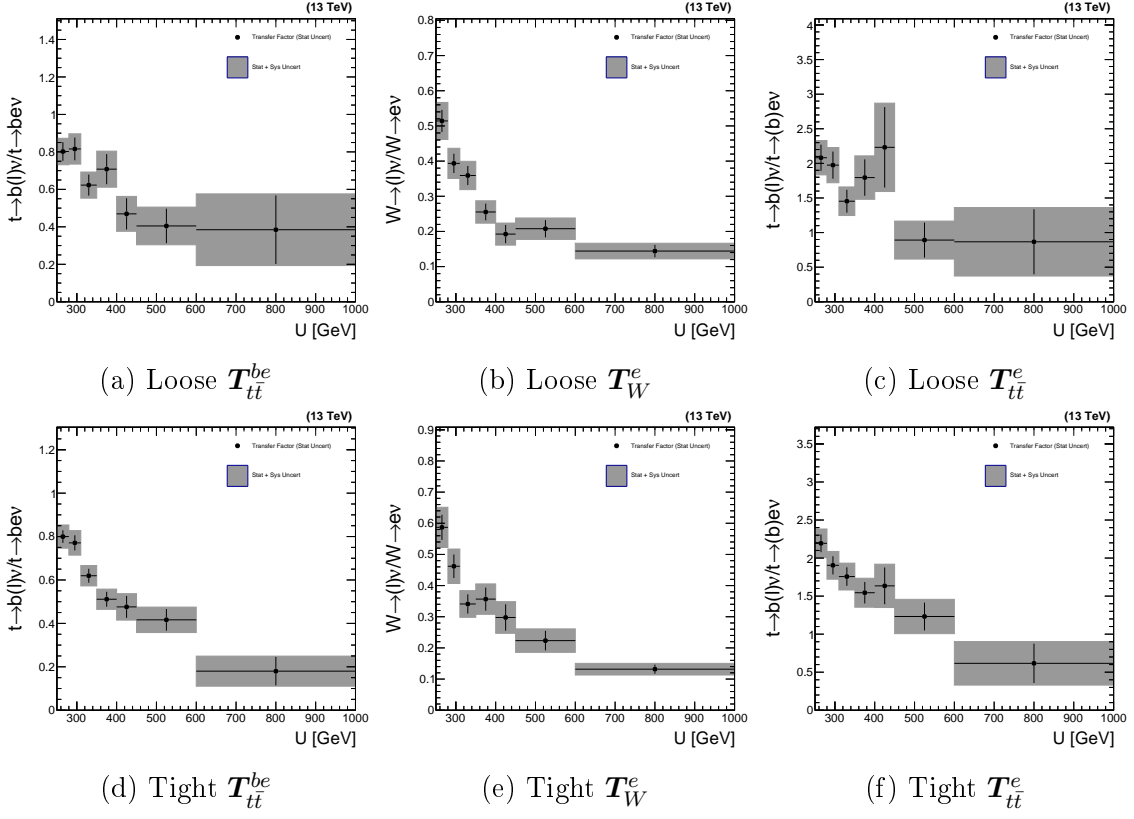


Figure 1.19: The transfer factors T_{tt}^{be} , T_W^e , and T_{tt}^e

Having defined (almost all of) the CRs and transfer factors, we can write down a complete likelihood for the mono-top search:

$$\begin{aligned}
\mathcal{L}(\mathbf{d} \mid \mu, \boldsymbol{\mu}_{\text{SR}}^{Z \rightarrow \nu\nu}, \boldsymbol{\mu}_{\text{SR}}^{W \rightarrow \ell\nu}, \boldsymbol{\mu}_{\text{SR}}^{t\bar{t}}, \boldsymbol{\theta}) = & \\
\prod_{i \in \text{bins}} \left[\text{Pois} \left(d_i^{\text{SR}} \mid \mu S_i^{\text{SR}}(\boldsymbol{\theta}) + \mu_{\text{SR},i}^{Z \rightarrow \nu\nu} + \mu_{\text{SR},i}^{W \rightarrow \ell\nu} + \mu_{\text{SR},i}^{t\bar{t}} + B_i^{\text{SR}}(\boldsymbol{\theta}) \right) \right. & \\
\times \prod_{X=\mu\mu, ee} \text{Pois} \left(d_i^X \mid \frac{\mu_{\text{SR},i}^{Z \rightarrow \nu\nu}}{T_{Z,i}^X(\boldsymbol{\theta})} + B_i^X(\boldsymbol{\theta}) \right) & \\
\times \prod_{X=b\mu, be} \text{Pois} \left(d_i^X \mid \frac{\mu_{\text{SR},i}^{t\bar{t}}}{T_{t\bar{t},i}^X(\boldsymbol{\theta})} + B_i^X(\boldsymbol{\theta}) \right) & \\
\times \left. \prod_{X=\mu, e} \text{Pois} \left(d_i^X \mid \frac{\mu_{\text{SR},i}^{W \rightarrow \ell\nu}}{T_{W,i}^X(\boldsymbol{\theta})} + \frac{\mu_{\text{SR},i}^{t\bar{t}}}{T_{t\bar{t},i}^X(\boldsymbol{\theta})} + B_i^X(\boldsymbol{\theta}) \right) \right] \times \prod_{j=0}^{n_\theta} p_j(\theta_j) \quad (1.12)
\end{aligned}$$

1.2.2 Theoretically-limited extrapolations

Despite the combination of the $\mu\mu$ and ee regions, there are still large statistical uncertainties in the estimate of $Z \rightarrow \nu\nu$ at high U . This is apparent in Figure 1.12, in which exactly one event is observed in the last bin of the tight CR. The dilepton CRs are limited by $\sigma(pp \rightarrow Z \rightarrow \nu\nu) > \sigma(pp \rightarrow Z \rightarrow \ell^+\ell^-)$; accordingly, to alleviate this limitation, we look to a process with a much bigger cross-section. In similar regions of final-state phase space, $\sigma(pp \rightarrow \gamma + \text{jets}) \sim 30 \times \sigma(pp \rightarrow Z(\rightarrow \nu\nu) + \text{jets})$. Therefore, it is natural to use the γ +jet production spectrum as a way to estimate the Z +jet spectrum. As before, let us define another transfer factor:

$$T_{\gamma,i}^\gamma = \frac{N_i^{\text{SR}}(Z \rightarrow \nu\nu)}{N_i^\gamma(\gamma)} \quad (1.13)$$

However, unlike the \mathbf{T}_Y^X we have discussed so far (which correlate similar processes, e.g. $Z \rightarrow \nu\nu/Z \rightarrow \mu\mu$), \mathbf{T}_γ^γ is highly sensitive to the theoretical predictions of the Z and γ spectra.

To reduce the impact of higher-order effects on \mathbf{T}_γ^γ , we ensure that the numerator and denominator are predicted to as high an order as possible. Leading-order MC is used to simulate V +jet processes, because higher-order simulations are much more

computationally intensive. We therefore choose to produce a less accurate LO simulation, as opposed to a more accurate, but statistically-limited, NLO simulation. While producing sufficient NLO simulation for the analysis is prohibitive, we can compute certain inclusive distributions at NLO. Since $U \approx p_T^V$ is the quantity of interest in this analysis, we want to ensure this distribution is accurately predicted. It is clear from Figure 1.20 that adding an additional QCD order induces large corrections, both at low and high p_T^V . In the LO simulation, we can obtain an estimate of the uncertainty due to NLO effects by varying the renormalization and factorization scales (μ_R, μ_F) by factors of two. This is represented by the red envelope and grey band in Figure 1.20 and clearly is insufficient to cover NLO effects. Therefore, we compute a simple correction for the NLO QCD effects, known as a k -factor:

$$k_{Z,\text{QCD}}(p_T^Z) = \frac{d\sigma_{\text{NLO QCD}}(Z)/dp_T^Z}{d\sigma_{\text{LO}}(Z)/dp_T^Z} \quad (1.14)$$

We include another k -factor, k_{EWK} , to correct for higher-order EWK effects. Unlike k_{QCD} , k_{EWK} is derived using a theoretical calculation [7, 8, 11] instead of NLO simulation. k_{EWK} covers NLO EWK terms, as well as large Sudakov logarithms that appear at high p_T^V in the NNLO expansion (NLL).

Figure 1.21 compares the k -factors for all three V +jet processes. While there are similar trends as a function of p_T^V , it is clear that the corrections are quite different for each process. Therefore, transfer factors like \mathbf{T}_γ^γ are strongly sensitive to NLO effects, i.e.:

$$T_{\gamma,i}^\gamma = \frac{N_i^{\text{SR}}(Z \rightarrow \nu\nu)}{N_i^\gamma(\gamma)} \neq \frac{N_i^{\text{SR,LO}}(Z \rightarrow \nu\nu)}{N_i^{\gamma,\text{LO}}(\gamma)} \quad (1.15)$$

The distributions in Sections 1.1-1.2 are all corrected using these k -factors. Figure 1.22 shows the equivalent for CRs that target γ +jet events, and Table 1.7 describes the selection used to define these CRs.

Now that we can describe \mathbf{T}_γ^γ at NLO, we must assess the impact of unknown higher-order terms on the transfer factors. We account for variations caused by uncertainties in the PDF model by taking the RMS of the 100 parameter variations prescribed for the NNPDF3.0 set [1]. By varying μ_F and μ_R by factors of 0.5 and

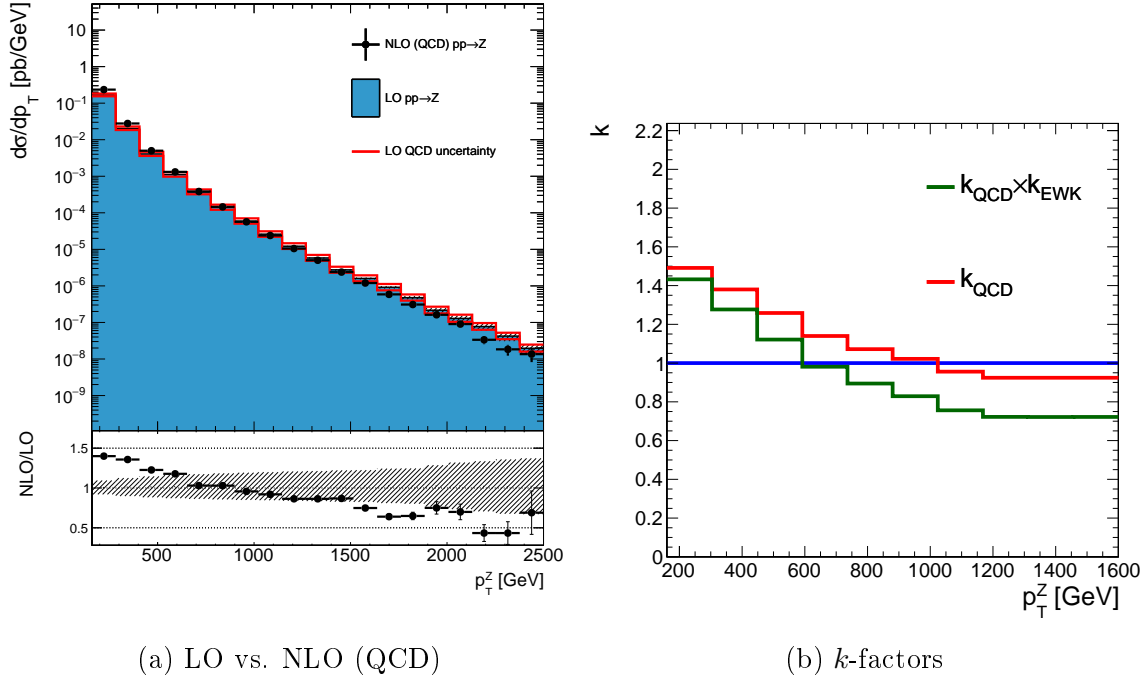


Figure 1.20: Theoretical predictions for p_T^Z in Z +jet events and the corresponding k -factors. No detector simulation is applied in these figures; all quantities are directly from MC simulation of the physics process. “LO QCD uncertainty” refers to an estimate of the effect of the QCD renormalization and factorization scales on the LO simulation. The grey band in the ratio is the quadrature sum of the QCD and statistical uncertainties.

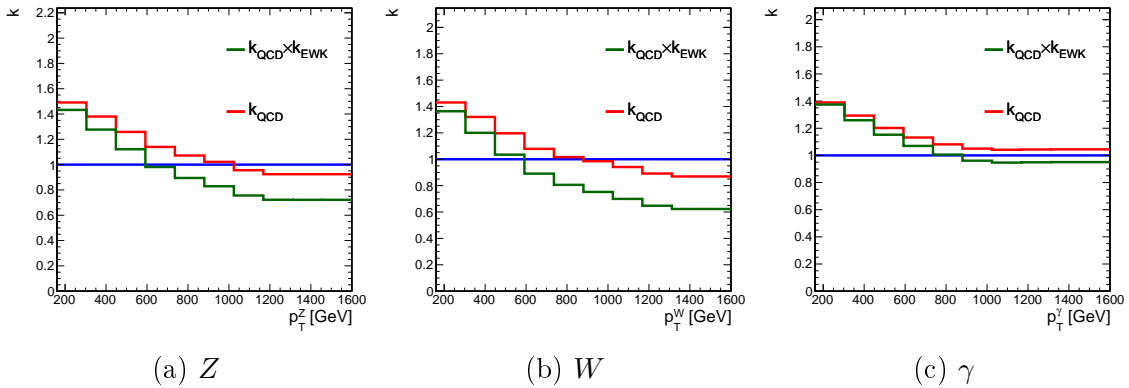
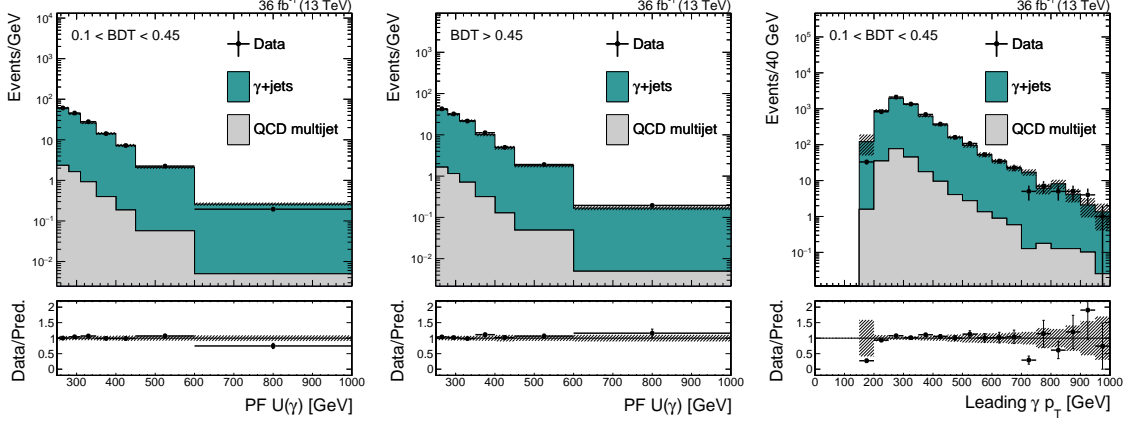


Figure 1.21: Differential k -factors for each of the V +jet processes.



(a) U in loose CR

(b) U in tight CR

(c) p_T^γ

Figure 1.22: Various kinematic distributions in the two mono-top γ CRs.

Table 1.7: Criteria used to select events for the mono-top γ CR. As with the SR, the region is further split based on the jet BDT score.

Criterion	Notes
$U > 250$ GeV	Mimicking the selection in the SR
1 CA15 jet with $p_T > 250$ GeV	Same as SR
CA15 jet $110 < m_{SD} < 210$ GeV	Same as SR
No identified μ, e, τ_h	Same as SR.
Well-identified γ with $p_T^\gamma > 175$ GeV	High- p_T photon, set by trigger threshold
$\min_{\text{jets}} \Delta\phi(\text{jet}, U) > 0.5$	Same as SR
CA15 jet BDT	Same as SR

2, we assess the effect of the integration scale choices on \mathbf{T} . These scale and PDF uncertainties cover all unknown QCD effects on the production of electroweak bosons. To be conservative, they are assumed to be uncorrelated between processes. However, the uncertainties are correlated between all bins (i.e. as a function of p_T^V). A second set of uncertainties is included for higher-order EWK effects, following what is suggested in References [3, 4, 5, 7, 8, 9, 10, 11, 12] and agreed upon in the LHC Dark Matter Working Group. These EWK uncertainties break down into three categories:

- Unknown Sudakov logarithms in the NLL correction. These uncertainties are correlated across processes (Z, W, γ).
- Missing NNLO EWK effects not covered by the NLL correction. These are not correlated across processes.
- The full difference between the NLL correction and an exponentiation of the NLO correction; also not correlated across processes.

It should be stressed that while these uncertainties apply to the prediction of each V +jet processes, they do not affect transfer factors that correlate processes differing only in decay mode or acceptance. This is simply because these uncertainties primarily deal with the initial state or the production of an electroweak boson, which is not related to the description of the decay to leptons or the experimental identification of leptons and b -jets. That is:

$$T_{Z,i}^{\mu\mu} = \frac{N_i^{\text{SR}}(Z \rightarrow \nu\nu)}{N_i^{\mu\mu}(Z \rightarrow \mu\mu)} \approx \frac{N_i^{\text{SR,LO}}(Z \rightarrow \nu\nu)}{N_i^{\mu\mu,\text{LO}}(Z \rightarrow \mu\mu)} \quad (1.16)$$

Now that we have tools to construct transfer factors of the form $N(V)/N(V')$ with reasonably small uncertainties (i.e. smaller than the statistical uncertainty of the data), it is natural to add another transfer factor to our toolbox:

$$T_{Z/W,i}^{\text{SR}} = \frac{N_i^{\text{SR}}(Z \rightarrow \nu\nu)}{N_i^{\text{SR}}(W \rightarrow \ell\nu)} \quad (1.17)$$

This allows us to use the e, μ CRs (which target W +jet production) to further reduce

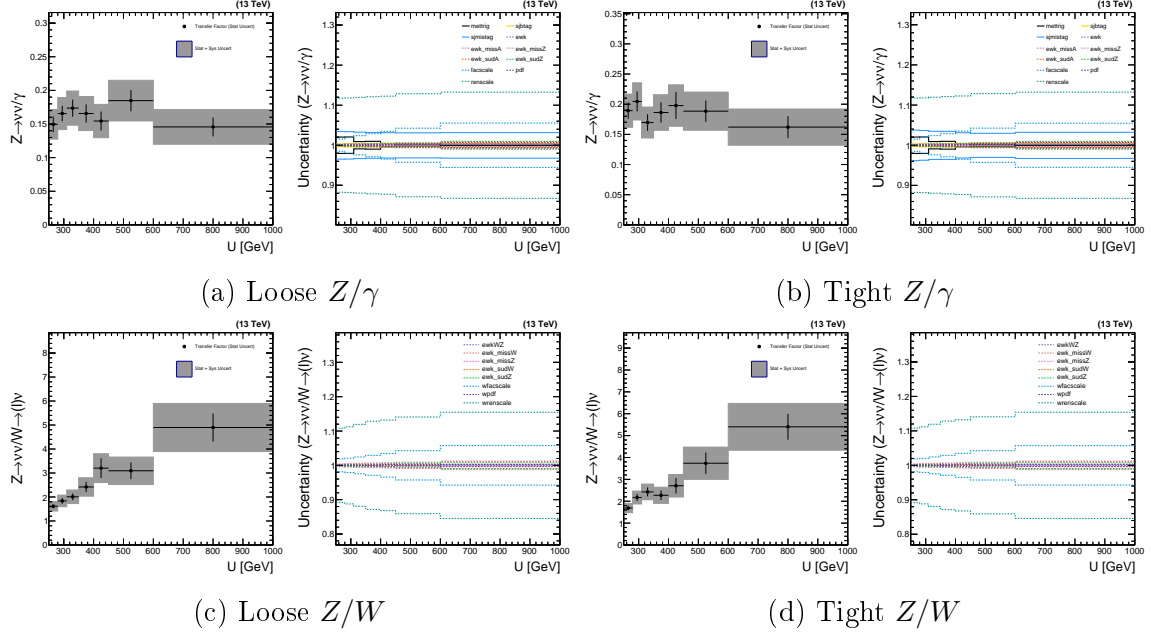


Figure 1.23: The transfer factors \mathbf{T}_γ and $\mathbf{T}_{Z/W}^{\text{SR}}$; and corresponding shape uncertainties.

the uncertainty in the estimation of $Z \rightarrow \nu\nu$ in the SR. For technical reasons, the transfer factor is defined as the ratio Z/W in the SR. However, the SR and the μ CR are connected through a product of transfer factors:

$$N_i^{\text{SR}}(Z \rightarrow \nu\nu) = T_{Z/W,i}^{\text{SR}}(\hat{\boldsymbol{\theta}}) \times T_{W,i}^\mu(\hat{\boldsymbol{\theta}}) \times N_i^\mu(W \rightarrow \ell\nu) \quad (1.18)$$

where $\hat{\boldsymbol{\theta}}$ is the maximum-likelihood estimate of $\boldsymbol{\theta}$.

Figure 1.23 shows these additional transfer factors and their shape uncertainties. It is clear from inspection that $\mathbf{T}_\gamma \ll 1$, and the same holds for the effective transfer factor $\mathbf{T}_{Z/W}^{\text{SR}} \times \mathbf{T}_W^\mu$. This indicates that the CR data to which the transfer factor is linked has greater statistical power than the SR data.

Having included all of these components, the likelihood can be written as:

$$\begin{aligned}
\mathcal{L}(\mathbf{d} \mid \mu, \boldsymbol{\mu}_{\text{SR}}^{Z \rightarrow \nu\nu}, \boldsymbol{\mu}_{\text{SR}}^{t\bar{t}}, \boldsymbol{\theta}) = & \\
& \prod_{i \in \text{bins}} \left[\text{Pois} \left(d_i^{\text{SR}} \mid \mu S_i^{\text{SR}}(\boldsymbol{\theta}) + \mu_{\text{SR},i}^{Z \rightarrow \nu\nu} + \frac{\mu_{\text{SR},i}^{Z \rightarrow \nu\nu}}{T_{Z/W,i}^{\text{SR}}(\boldsymbol{\theta})} + \mu_{\text{SR},i}^{t\bar{t}} + B_i^{\text{SR}}(\boldsymbol{\theta}) \right) \right. \\
& \times \prod_{X=\mu\mu, ee} \text{Pois} \left(d_i^X \mid \frac{\mu_{\text{SR},i}^{Z \rightarrow \nu\nu}}{T_{Z,i}^X(\boldsymbol{\theta})} + B_i^X(\boldsymbol{\theta}) \right) \\
& \times \prod_{X=b\mu, be} \text{Pois} \left(d_i^X \mid \frac{\mu_{\text{SR},i}^{t\bar{t}}}{T_{t\bar{t},i}^X(\boldsymbol{\theta})} + B_i^X(\boldsymbol{\theta}) \right) \\
& \times \prod_{X=\mu, e} \text{Pois} \left(d_i^X \mid \frac{\mu_{\text{SR},i}^{Z \rightarrow \nu\nu}}{T_{W,i}^X(\boldsymbol{\theta}) T_{Z/W,i}^{\text{SR}}(\boldsymbol{\theta})} + \frac{\mu_{\text{SR},i}^{t\bar{t}}}{T_{t\bar{t},i}^X(\boldsymbol{\theta})} + B_i^X(\boldsymbol{\theta}) \right) \\
& \left. \times \text{Pois} \left(d_i^\gamma \mid \frac{\mu_{\text{SR},i}^{Z \rightarrow \nu\nu}}{T_{\gamma,i}^\gamma(\boldsymbol{\theta})} \right) \right] \times \prod_{j=0}^{n_\theta} p_j(\theta_j) \tag{1.19}
\end{aligned}$$

The discussion in this section has largely relied on arguments from simulation and calculation. We can, however, validate that our estimates of \mathbf{T} and the corresponding uncertainties are reasonable by using CR data and appropriate proxies. For example, to test $\mathbf{T}_\gamma^\gamma \sim N(Z \rightarrow \nu\nu)/N(\gamma)$, we can look at $N(Z \rightarrow \mu\mu)/N(\gamma)$. Up to differences in branching ratio and muon identification, these ratios are identical. Figure 1.24 shows some examples of these proxy ratios. In particular, we see that the Z/γ , Z/W and W/γ ratios are well-described the MC, especially as compared to the systematic uncertainties that are assigned.

1.3 Results

Having built this likelihood, we perform a maximum likelihood fit to the data in all regions simultaneously. The results of a ML fit under a background-only hypothesis (i.e. setting $\mu = 0$) is shown in Figures

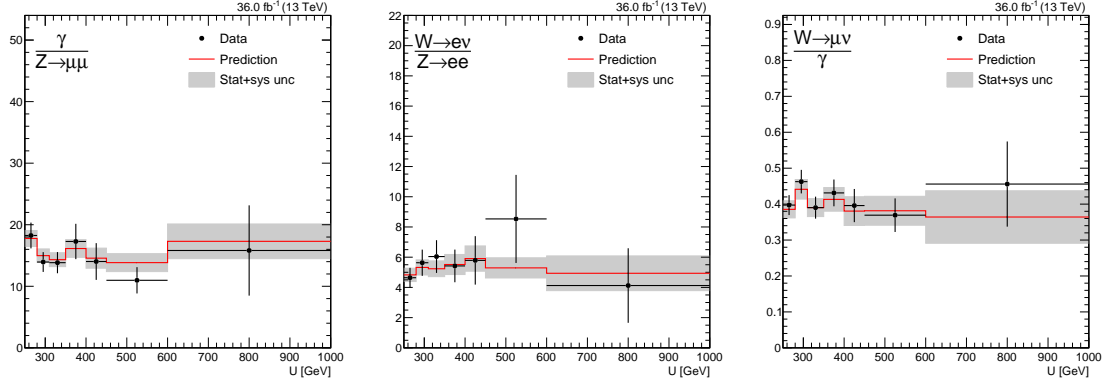


Figure 1.24: Data validation of CR-to-CR transfer factors in the loose category. Only ratios with theoretically-limited systematic uncertainties are shown.

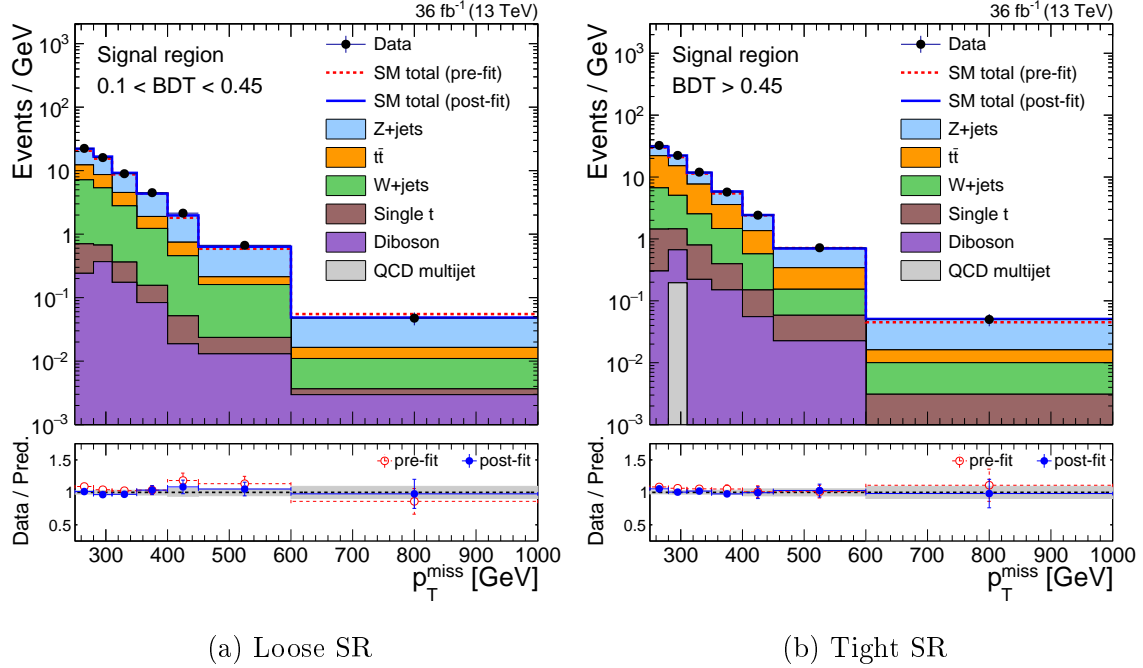


Figure 1.25: Comparison of pre- and post-fit results in the SRs, after simultaneously fitting all channels. The fit is performed having fixed $\mu = 0$.

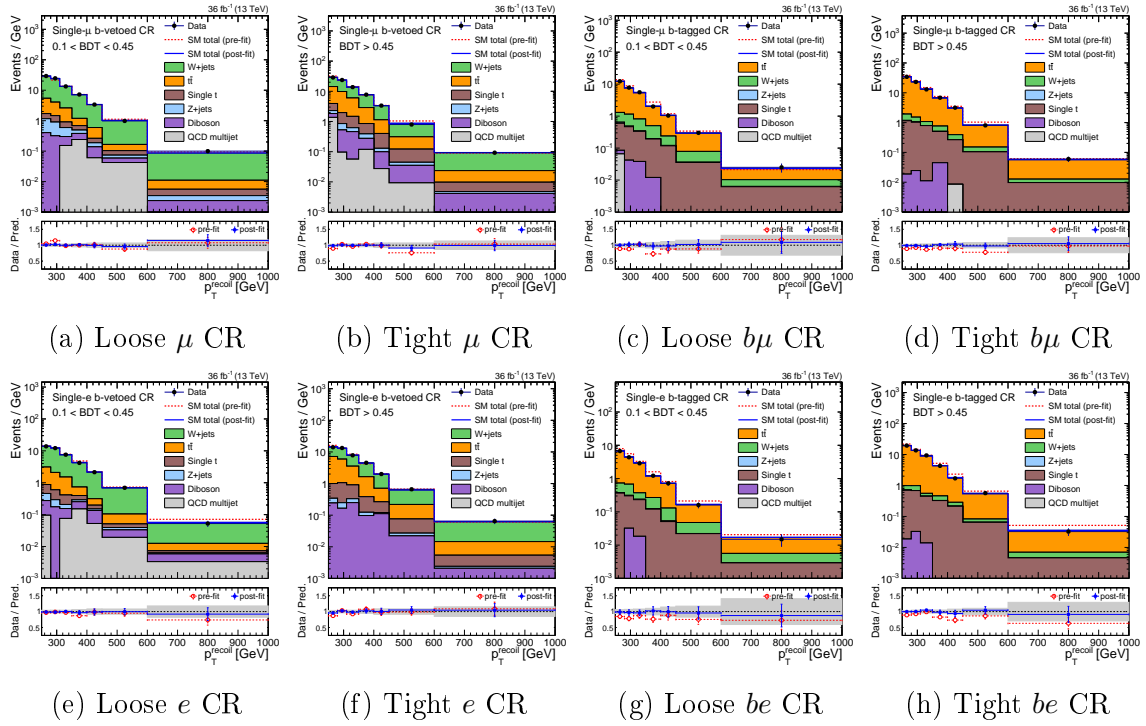


Figure 1.26: Comparison of pre- and post-fit results in the single-lepton CRs, after simultaneously fitting all channels. The fit is performed having fixed $\mu = 0$.

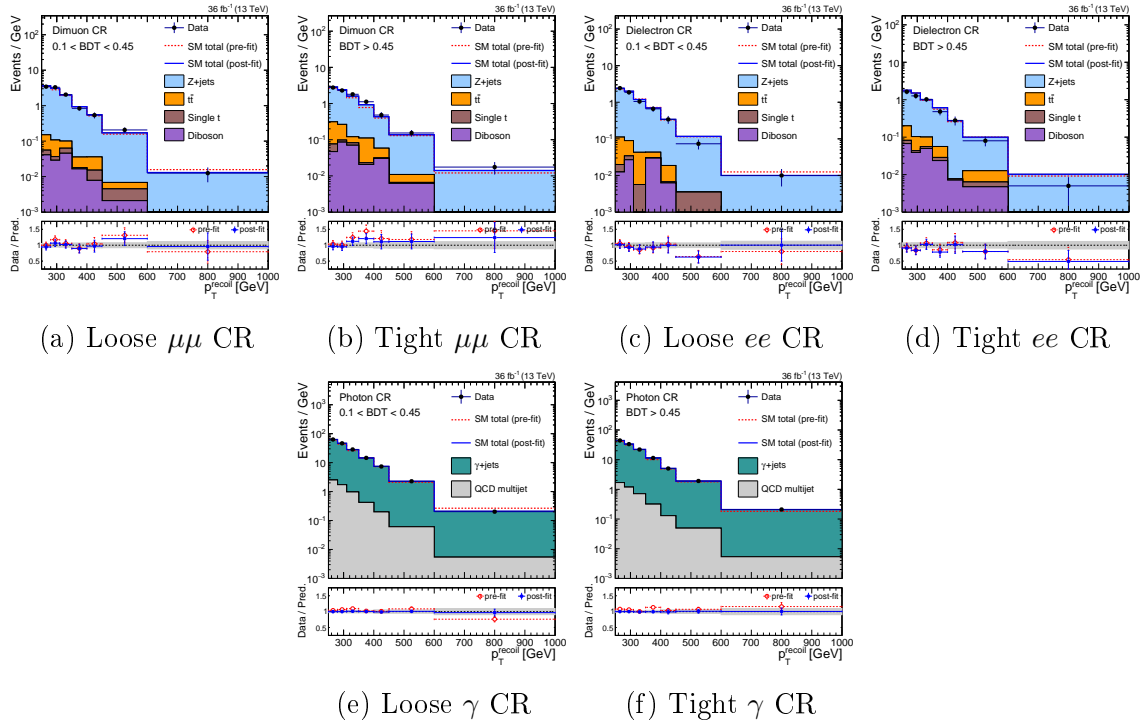


Figure 1.27: Comparison of pre- and post-fit results in the di-lepton and photon CRs, after simultaneously fitting all channels. The fit is performed having fixed $\mu = 0$.

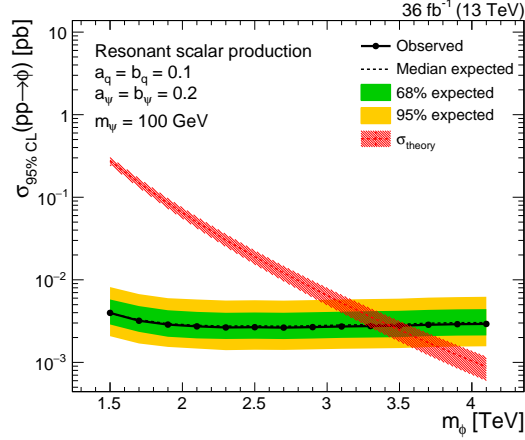


Figure 1.28: 95% CLs upper limits on the cross section of the production of ϕ , where the resonance mass m_ϕ is scanned. Values of m_ϕ for which $\sigma_{95\% \text{ CLs}} < \sigma_{\text{theory}}$ are excluded at 95% confidence level. The dashed black line represents the median expected exclusion, with the green and yellow bands representing the 1 and 2 standard deviation envelopes on the expected exclusion. The red band represents the 1 standard deviation of the uncertainty on the theory cross section (driven by higher-order QCD terms).

1.3.1 Constraints on mono-top models

The results of the previous section show that the background-only (B-only) model is able to describe the data. To quantify the preference of the B-only model to a signal+background model (S+B), we compute 95% CLs upper limits on the signal strength μ for each signal hypothesis. A description of CLs upper limits and the asymptotic profile likelihood method is given in Section [?].

We begin with the simpler of the two models: the resonant scalar. Figure 1.28 shows the upper limit on the cross section of ϕ production as a function of m_ϕ . A fixed value of m_ψ is chosen such that $m_\psi \ll m_\phi$. In this regime, the exact value of m_ψ does not strongly affect the kinematics or cross section; in the opposite regime, the decay $\phi \rightarrow t\psi$ is strongly suppressed. The values of the couplings a_q, b_q and a_ψ, b_ψ are similarly fixed to reasonable values. The cross section (and therefore the signal strength μ) roughly scales as $(a_q + b_q)^2$ and $(a_\psi + b_\psi)^2$. Given these assumptions, the observed data excludes scalars with mass $m_\phi < 3.4$ TeV. This can be compared to the expected exclusion, which is also 3.4 TeV.

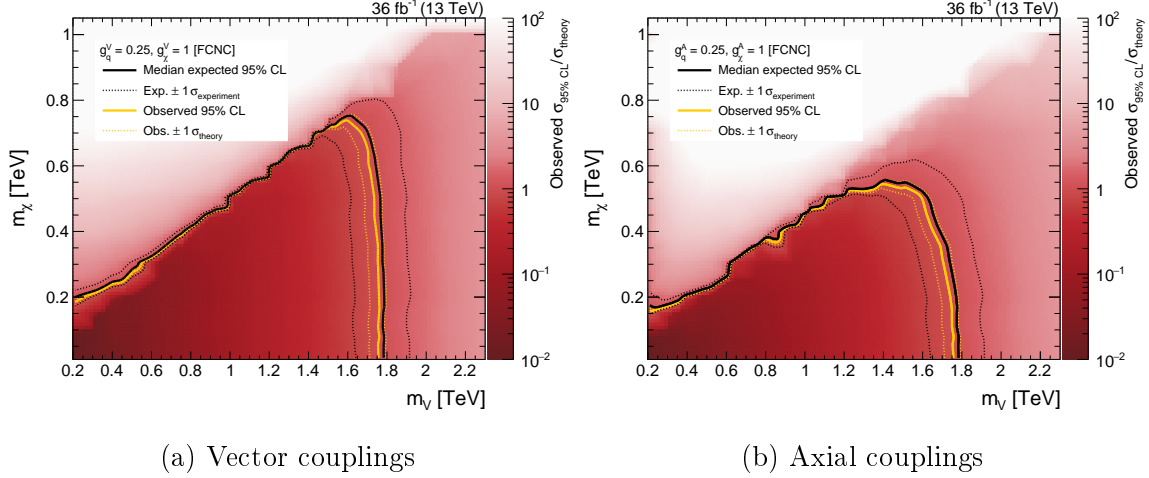


Figure 1.29: 95% CLs upper limits on the signal strength ($\mu = \sigma/\sigma_{\text{theory}}$) of the flavor-violating process $pp \rightarrow t\chi\bar{\chi}$ as a function of m_V and m_χ . Two hypotheses are tested: assuming $g_\chi^V, g_q^V \neq 0$ (vector-like) and assuming $g_\chi^A, g_q^A \neq 0$ (axial vector-like).

The FCNC model contains many more non-trivial parameters, and so we do not simply fix all but one. First, fixing the couplings (at values agreed upon by the LHC Dark Matter Working Group in Reference [6]), we show the upper limits as a function of (m_V, m_χ) in Figure 1.29. Both vector-like and axial vector-like couplings are probed independently. In either scenario, assuming $m_\chi < 50$ GeV, we are able to exclude $0.2 < m_V < 1.75$ TeV. The lower bound arises from measurements of m_t and Γ_t ; allowing $m_V \lesssim 200$ GeV modifies Γ_t beyond measured bounds as the $t^{(*)} \rightarrow Vu$ channel opens. As m_χ crosses the $m_V/2$ boundary, σ_{theory} drops off rapidly, reducing the strength of the exclusion. In the vector case, this defines a clear exclusion triangle bounded by $m_V < 1.75$ TeV and $2m_\chi < m_V$. In the axial-vector case, Γ_V is much narrower, modifying the transition to the off-shell region. On the entire plane, the observed exclusion is consistent with the median expected exclusion within one standard deviation.

Sticking to two-dimensional projections of the parameter space, Figure 1.30 shows the excluded regions as a function of mediator mass m_V and all four free couplings $g_q^V, g_q^A, g_\chi^V, g_\chi^A$. As the DM mass is fixed to be strictly on-shell regardless of m_V , there are no visible differences between the vector and axial-vector scenarios. Assuming

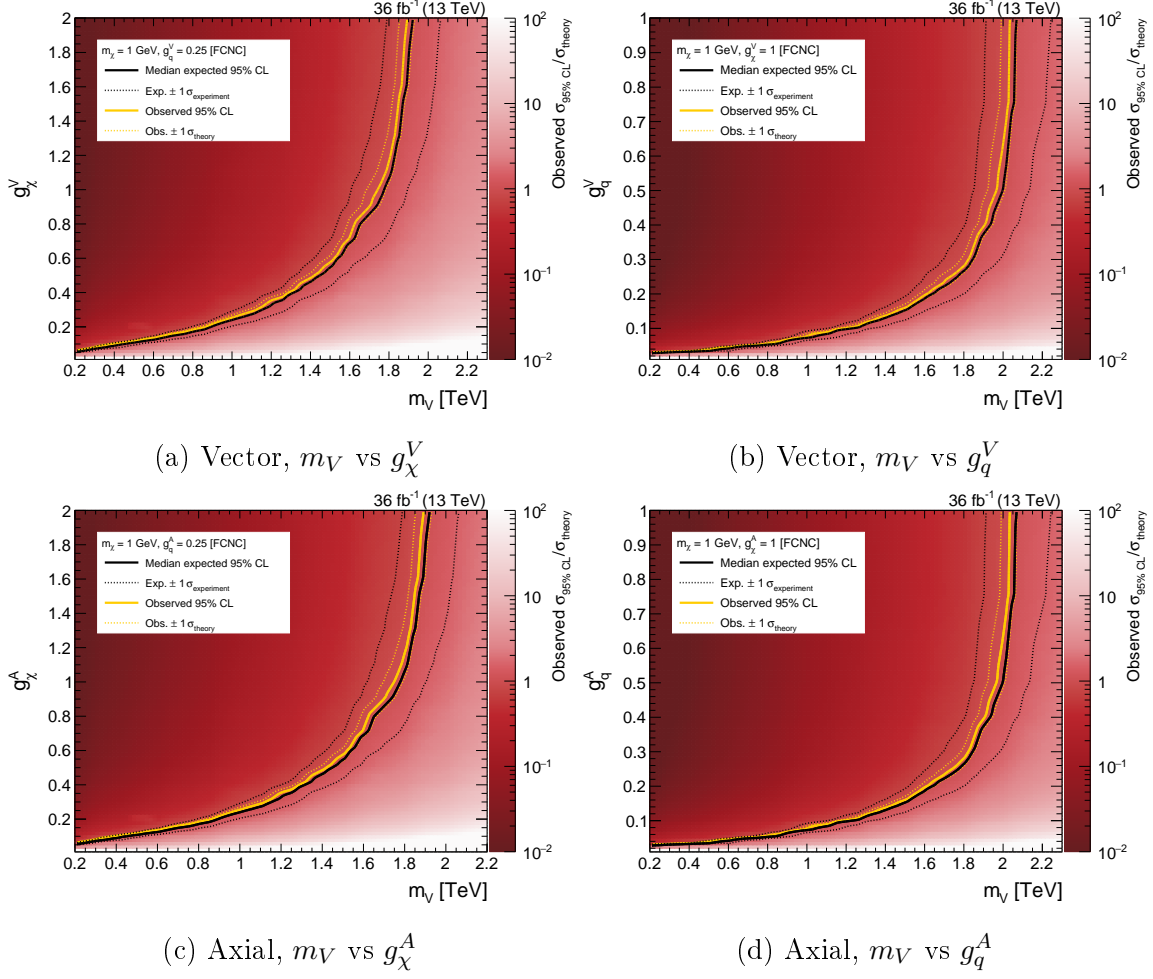


Figure 1.30: 95% CLs upper limits on the signal strength ($\mu = \sigma/\sigma_{\text{theory}}$) of the flavor-violating process $pp \rightarrow t\chi\bar{\chi}$ as a function of m_V , g_q , and g_χ . Two hypotheses are tested: assuming $g_\chi^V, g_q^V \neq 0$ (vector-like) and assuming $g_\chi^A, g_q^A \neq 0$ (axial vector-like). The DM mass m_χ is fixed at 1 GeV.

sufficiently low masses (still corresponding to viable hypotheses), we exclude couplings as weak as $g_q \cdot g_\chi \sim 0.01$.

It is difficult to fully visualize more than two dimensions of the parameter space at a time. Figure 1.31 shows the largest mediator mass that is excluded as a function of g_q^V, g_χ^V (assuming $g_q^A = g_\chi^A = 0$). Given sufficiently large couplings, we exclude FCNCs as massive as 2.5 TeV, while only assuming that $2m_\chi < m_V$.

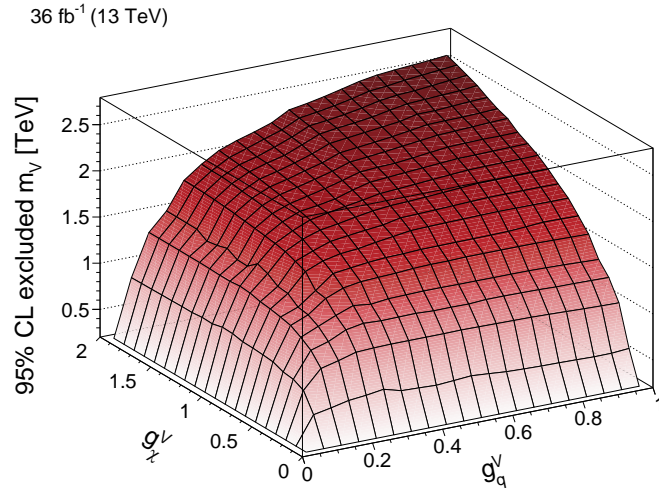


Figure 1.31: Maximum excluded value of m_V for each set of couplings, assuming vector-only couplings.

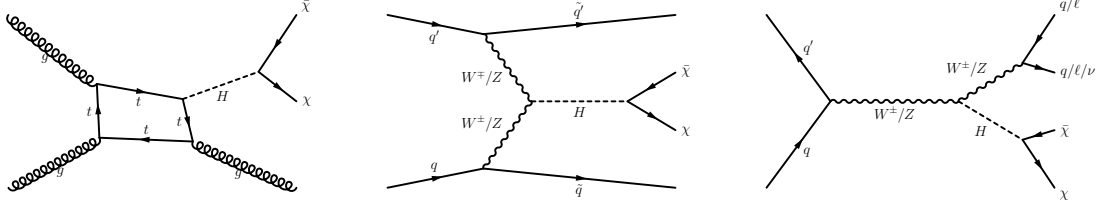
Chapter 2

The Search for Invisible Decays of the Higgs Boson

The discovery of the SM Higgs boson [??] involved multiple production modes. Gluon fusion has the largest cross section (49 pb) at the LHC because of the large gluon PDF, followed by vector boson fusion (VBF) (3.8 pb), WH (1.4 pb), and ZH (0.89 pb) [2]. While gluon fusion is the most frequent mode, the unique detector signatures of the other production modes can be combined the various Higgs decay signatures to define a signal topology with few backgrounds.

Many DM models [??] allow for DM fermions or scalars to acquire mass through the Higgs mechanism, coupling to the SM Higgs boson. If the DM candidate χ satisfies $2m_\chi < m_H$, then we expect to observe $H \rightarrow \chi\bar{\chi}$. From measurements of the visible branching fractions, we can indirectly place an upper bound of $\mathcal{B}(H \rightarrow \chi\bar{\chi}) < 0.2$ [??]. In this chapter, we describe a direct search for $H \rightarrow \chi\bar{\chi}$ decays.

As with the case of the mono-top search, the $H \rightarrow \chi\bar{\chi}$ process manifests as p_T^{miss} . Each of the aforementioned Higgs production modes translates into a $p_T^{\text{miss}} + X$ signature, where X refers to one or more SM particles. Figure 2.1 shows each of the signatures; in this chapter, we will focus on the VBF production mode, as the unique final state topology provides the best sensitivity to $H \rightarrow \chi\bar{\chi}$.



(a) $gg \rightarrow H(\rightarrow \chi\bar{\chi}) + \text{jet(s)}$ (b) $qq' \rightarrow H(\rightarrow \chi\bar{\chi}) + \text{jet(s)}$ (c) $qq' \rightarrow VH(\rightarrow \chi\bar{\chi})$

Figure 2.1: Diagrams that contribute to the production of the SM Higgs boson at the LHC, with the subsequent decay to DM candidates. The shown diagrams are all chosen to generate large $p_{\text{T}}^{\text{miss}}$ through the presence of one or more SM particles in the final state.

2.1 Signal selection

VBF $H \rightarrow \chi\bar{\chi}$ events are characterized by large $p_{\text{T}}^{\text{miss}}$ and two jets. These jets are typically:

- Fairly forward in the detector
- Far apart from each other in η
- Highly energetic (large E , moderate p_{T})
- Close together in ϕ

A candidate VBF $H \rightarrow \chi\bar{\chi}$ event displaying these properties is shown in a CMS event display in Figure 2.2.

2.1.1 Online trigger selection

The same trigger decisions (L1 and HLT) as described in Section 1.1.1 are used to select events in this analysis. However, the L1 seeds for the 2016 data run were designed with mono-top-like analyses in mind; i.e., searches where the momentum imbalance is created by central objects. To avoid noise and resolution issues in the forward calorimeters, the L1 seed only considers energy deposits in the region $|\eta| <$

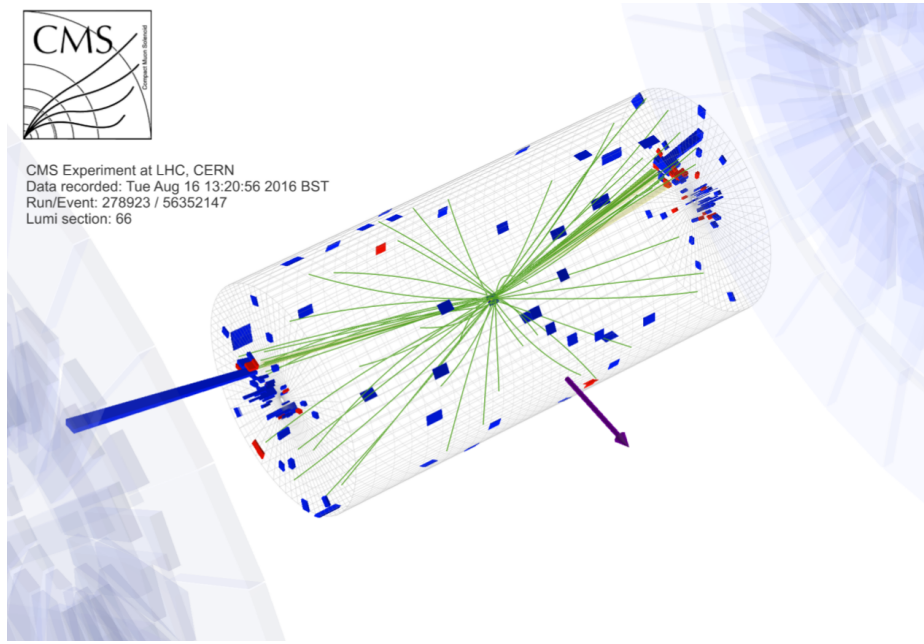


Figure 2.2: Candidate VBF $H \rightarrow \chi\bar{\chi}$ event with two energetic forward jets ($p_T = 180, 107$ GeV) and large p_T^{miss} (360 GeV). Red (blue) towers represent deposits in the hadronic (electromagnetic) calorimeter. Green lines are tracks reconstructed from hits of charged particles in the tracker. The blue arrow represents the direction and magnitude of the p_T^{miss} .

3. Therefore, VBF events in which both jets are in the forward region will not be triggered.

2.1.2 EW and QCD production of electroweak bosons

2.1.3 Sensitivity optimization

2.2 Background estimation

2.3 Results

2.3.1 Constraints on Higgs production and decay parameters

2.3.2 Constraints on scalar production of DM

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