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1. What is regular language? write regular definition for following:

- The set of identifiers of Java language.
- Comments consisting of a string surrounded by `/*` and `*/` without an intervening `*/`.  
Unless it appears inside the quotes `"and"`.
- All strings of 0's and 1's with even number of 0's and an odd number of 1's.

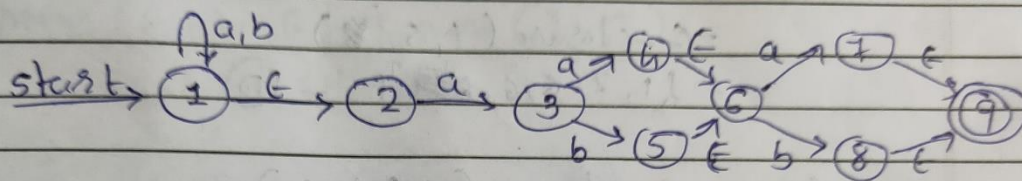
→ Regular expressions are used to denote regular languages.  
A language is regular if it can be expressed in terms of regular expression.

a.  $\text{alpha} \rightarrow a|b|\dots|z|A|B|\dots|Z|_|\$$   
 $\text{digit} \rightarrow 0|1|\dots|9$   
 $\text{alphas} \rightarrow \text{alpha}\text{alpha}^*$   
 $\text{digits} \rightarrow \text{digit}\text{digit}^*$   
 $\text{id} \rightarrow \text{alphas}(\text{digits}^*|\text{alphas}^*)^*$

(b).  $S \rightarrow /*$  (c)  $E \rightarrow (00+11)^*(01+10)$   
 $E \rightarrow */$  (3/14/2)  $C \rightarrow (00+11+0E+10E+0E)$   
 $Q \rightarrow "$   $EQ \rightarrow I(C) + (CE$   
 $EST \rightarrow [^*"]$   
 $ESL \rightarrow [^"/"]$   
 $\text{Comments} \rightarrow S(EST|^\dagger ESL) | (^\dagger(ESL)(E)(EST)^\dagger)E$

2. Construct DFA from following regular expression using Thompson's construction method.

$(ab)^* a (ab) (ab) \#$  also minimize it.



$$\epsilon\text{-closure}(1) = \{1, 2\}$$

$$\epsilon\text{-closure}(2) = \{2\}$$

$$\epsilon\text{-closure}(3) = \{3\}$$

$$\epsilon\text{-closure}(4) = \{4, 6\}$$

$$\epsilon\text{-closure}(5) = \{5, 6\}$$

$$\epsilon\text{-closure}(6) = \{6\}$$

$$\epsilon\text{-closure}(7) = \{7, 9\}$$

$$\epsilon\text{-closure}(8) = \{8, 9\}$$

$$\epsilon\text{-closure}(9) = \{9\}$$

	a	b
1	1	1
2	3	$\phi$
3	4	5
4	$\phi$	$\phi$
5	$\phi$	$\phi$
6	7	8
7	$\phi$	$\phi$
8	$\phi$	$\phi$
9	$\phi$	$\phi$

$$\therefore q_0 = \epsilon\text{-closure}(q_0')$$

$$q_0 = \{1, 2\} \text{ --- (A)}$$

$$\text{Move}(A, a) = \epsilon\text{-closure}\{\delta(1, a) \cup \delta(2, a)\}$$

$$= \epsilon\text{-closure}\{2, 3\}$$

$$= \{1, 2, 3\} \text{ --- (B)}$$



$$\begin{aligned} \text{move}(A, b) &= E\text{-closure}(\delta(1, b) \cup \delta(2, b)) \\ &= E\text{-closure}(2) \\ &= \{1, 2\} \end{aligned}$$

$$\begin{aligned} \text{move}(B, a) &= E\text{-closure}(\delta(1, a) \cup \delta(2, a) \cup \delta(3, a)) \\ &= E\text{-closure}(1, 3, 4) \\ &= \{1, 2, 3, 4, 6\} \quad \text{(C)} \end{aligned}$$

$$\begin{aligned} \text{move}(B, b) &= E\text{-closure}(\delta(1, b) \cup \delta(2, b) \cup \delta(3, b) \cup \delta(4, b) \cup \delta(6, b)) \\ &= E\text{-closure}(1, 5, 8) \\ &= \{1, 2, 5, 6, 8\} \quad \text{(D)} \end{aligned}$$

$$\begin{aligned} \text{move}(C, a) &= E\text{-closure}(1, 3, 4, 7) \\ &= \{1, 2, 3, 4, 6, 7, 9\} \quad \text{(E)} \end{aligned}$$

$$\begin{aligned} \text{move}(C, b) &= E\text{-closure}(1, 8) \\ &= \{1, 2, 8, 9, 6\} \quad \text{(F)} \end{aligned}$$

$$\begin{aligned} \text{move}(D, a) &= E\text{-closure}(1, 3, 7) \\ &= \{1, 2, 3, 7, 4\} \quad \text{(G)} \end{aligned}$$

$$\begin{aligned} \text{move}(D, b) &= E\text{-closure}(1, 8) \\ &= \{1, 2, 8, 9\} \quad \text{(H)} \end{aligned}$$

$$\begin{aligned} \text{move}(E, a) &= E\text{-closure}(1, 3, 4, 7) \\ &= \{1, 2, 3, 4, 6, 7, 9\} \end{aligned}$$

$$\begin{aligned} \text{move}(E, b) &= E\text{-closure}(1, 5, 8) \\ &= \{1, 2, 5, 6, 8, 9\} \end{aligned}$$

$$\text{move}(F, a) = G\text{-closure}(\cancel{1, 8, 7}) (1, 3, 7) \\ = \cancel{\{1, 2, 8, 7\}} = \{1, 2, 3, 7, 9\}$$

$$\text{move}(F, b) = G\text{-closure}(1, 8) \\ = \{1, 2, 8, 9\}$$

$$\text{move}(G, a) = G\text{-closure}(1, 3, 4) \\ = \{1, 2, 3, 4, 6\}$$

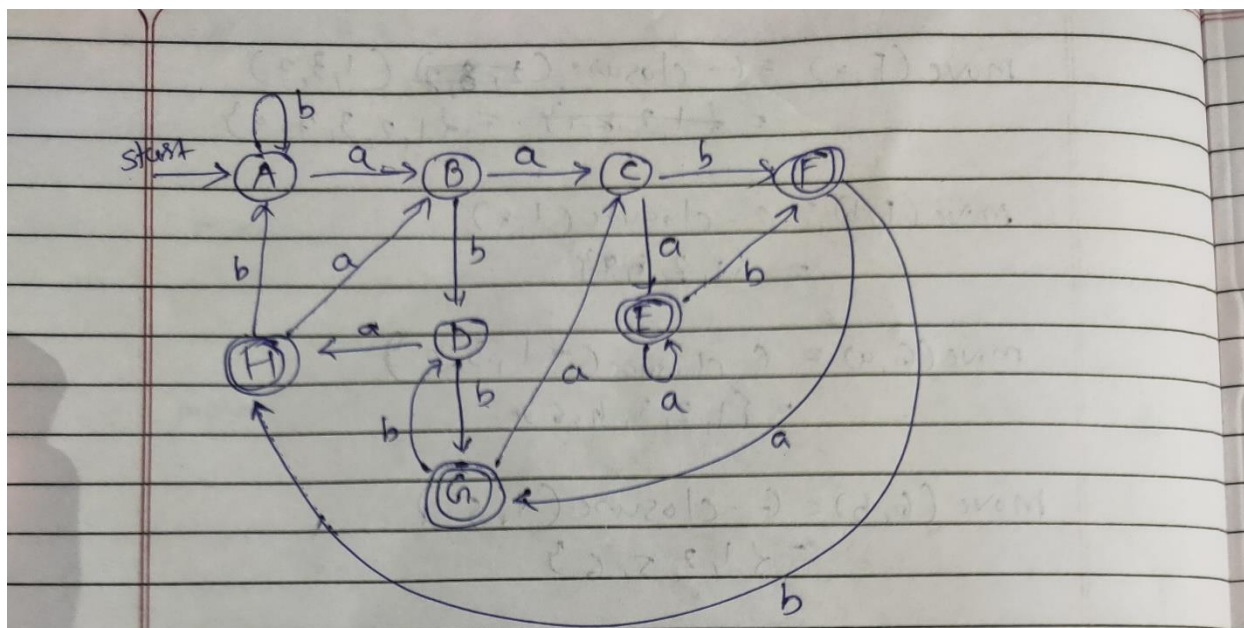
$$\text{move}(G, b) = G\text{-closure}(1, 5) \\ = \{1, 2, 5, 6\}$$

$$\text{move}(H, a) = G\text{-closure}(1, 3) \\ = \{1, 2, 3\}$$

$$\text{move}(H, b) = G\text{-closure}(1) \\ = \{1, 2\}$$

	a	b
A = {1, 2}	B	A
B = {1, 2, 3}	C	D
C = {1, 2, 3, 4, 6}	E	F
D = {1, 2, 5, 6}	G	H
Ⓔ = {1, 2, 3, 4, 6, 7, 9}	E	F
Ⓕ = {1, 2, 8, 9, 5, 6}	G	H
Ⓖ = {1, 2, 3, 7, 9}	C	D
Ⓗ = {1, 2, 8, 9}	B	A





3. ~~Construct DFA for following regular expression using syntax tree method. Also minimize~~

DFA Optimization

{A, B, C, D, E, F, G, H}

Non accepting states

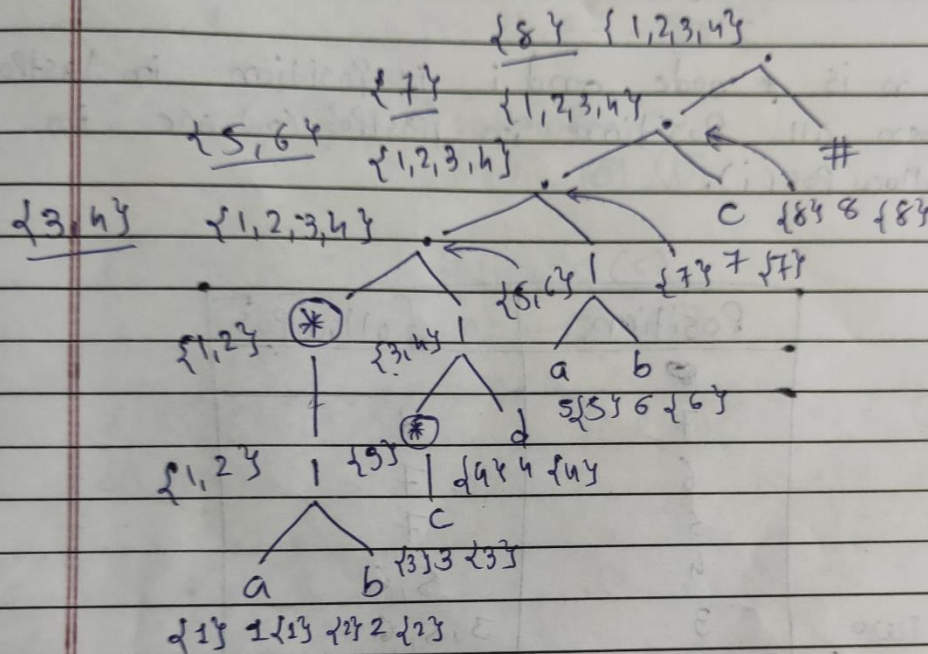
{A, B, C, D}

Accepting states

{E, F, G, H}

→ So In Non accepting states subgroups, doesn't have any states  $s$  and  $t$  such that for all input symbols  $a$ , states  $s$  and  $t$  have transitions on  $a$  states in same group. So DFA is already optimized.

3. construct DFA for following regular expression using syntax tree method also minimize it.  
 $(a|b)^*(c^*|d)(a|b)c\#$



→ Nullable node

Here \* is only nullable node

→ A leaf with position  $i = d_i$

first pos = last pos =  $d_i$

→ if last pos differ from first pos then it will be displayed with underline.



- if  $n$  is concatenation node with left child  $c1$  and right child  $c2$  and  $i$  is a position in  $\text{lastPos}(c1)$ , then all position in  $\text{firstPos}(c2)$  are in  $\text{followPos}(i)$ .
- if  $n$  is  $*$  node and  $i$  is position in  $\text{lastPos}(n)$  then all position in  $\text{firstPos}(n)$  are in  $\text{followPos}(i)$ .

Position	followPos
7	8
6	7
5	7
4	5, 6
3	3, 5, 6
2	1, 2, 3, 4
1	1, 2, 3, 4

above two rules are applied because of  $*$ !

Initial state =  $\text{firstPos of root} = \{1, 2, 3, 4\}$  - (A)

State A

$$\delta((1, 2, 3, 4), a) = \text{followPos}(2) \\ = \{1, 2, 3, 4\} - A$$

$$\delta((1, 2, 3, 4), b) = \text{followPos}(2) \\ = \{1, 2, 3, 4\} - (A)$$

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$$\delta((1,2,3,4), c) = \text{followPos}(3) = \{5,6\} - \textcircled{B}$$

$$\delta((1,2,3,4), d) = \text{followPos}(4) = \{5,6\} - \textcircled{C}$$

$$\delta((5,6), a) = \text{followPos}(5) = \{7\} - \textcircled{D}$$

$$\delta((5,6), b) = \text{followPos}(6) = \{7\} - \textcircled{D}$$

$$\delta((5,6), c) = \{7\}$$

$$\delta((5,6), d) = \{7\}$$

$$\delta(7, a) = \{7\}$$

$$\delta(7, b) = \{7\}$$

$$\delta(7, c) = \text{followPos}(7) = \{8\} - \textcircled{E}$$

$$\delta(7, d) = \{7\}$$

$$\delta((3,5,6), a) = (5) = 7 - \textcircled{D}$$

$$\delta((3,5,6), b) = (6) = 7 - \textcircled{D}$$

$$\delta((3,5,6), c) = (3) = (3,5,6) - \textcircled{B}$$

$$\delta((3,5,6), d) = \{7\}$$

State	a	b	c	d
A = {1,2,3,4}	A	A	B	<del>C</del>
B = {5,6}	D	D	B	-
C = {5,6}	D	D	<del>B</del>	-
D = {7}	-	-	E	-
E	-	-	-	-

```

graph LR
    Start(( )) --> A((A))
    A -- a,b --> A
    A -- c --> B((B))
    A -- d --> C((C))
    B -- a,b --> B
    B -- c --> D((D))
    C -- a,b --> D
    D -- c --> E((E))
    style Start fill:none,stroke:none
    
```



5. Define token. Explain how it differs from pattern and lexeme. Find token, pattern and lexeme from following expressions.

Token:

Sequence of characters having a collective meaning is known as token.

Pattern:

The set of rules called pattern associated with a token.

Lexemes:

The sequence of characters in a source program matched with a pattern for a token is called lexeme.

→ A lexeme is a string of characters that is a smallest-level syntactic unit in the programming language.

b).  $total = sum + 12.5$

Token	Lexeme	Pattern
identifier 1	total	letter followed by letter digit
operator 1	=	<= or <= or = or <> or =>
identifier 2	sum	letter followed by digit or letter
operator 2	+	for - or * or / or %
constant 1	12.5	only numeric constant

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a) `if (x <= 5)`

Token	Lexem	Pattern
Identifier 1	if	if
Operator 1	(	(
Identifier 2	x	letter followed by letter or digit
Operator 2	<=	< or > or <= or >= or < >
Constant 1	5	Numeric constant
Operator 3	)	)

b. Construct a DFA from recognizing the unsigned integers & unsigned real numbers with fraction.

```

graph LR
    start((start)) -- d --> 1((1))
    1 -- d --> 2((2))
    2 -- d --> 2
    2 -- "." --> 3((3))
    3 -- d --> 4((4))
    4 -- d --> 4
    4 -- "E" --> 5((5))
    5 -- "+, -" --> 6((6))
    6 -- d --> 7((7))
    7 -- d --> 7
    style start fill:none,stroke:none
    style 7 fill:#fff,stroke:#000,stroke-width:2px
  
```

digit = d  $\rightarrow$  0 | 1 | ... | 9  
 digits  $\rightarrow$  d d\*

optional fraction  $\rightarrow$  . digits |  $\epsilon$   
 optional exponent  $\rightarrow$  (E (+ | -) digits) |  $\epsilon$   
 num  $\rightarrow$  digits optional fraction optional exponent