

# Introduction to Information Retrieval

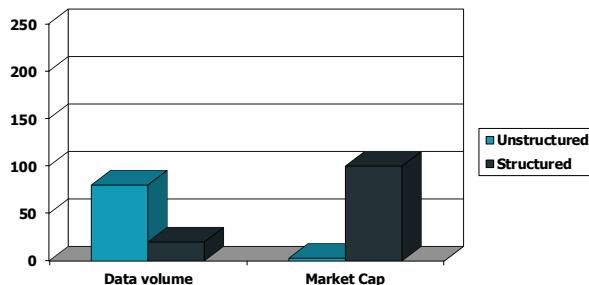
Introducing Information Retrieval  
and Web Search

## Information Retrieval

- Information Retrieval (IR) is **finding material** (usually documents) of an **unstructured** nature (usually text) that satisfies an **information need** from within **large collections** (usually stored on computers).
- These days we frequently think first of **web search**, but there are many other cases:
  - E-mail search
  - Searching your laptop
  - Corporate knowledge bases
  - Legal information retrieval

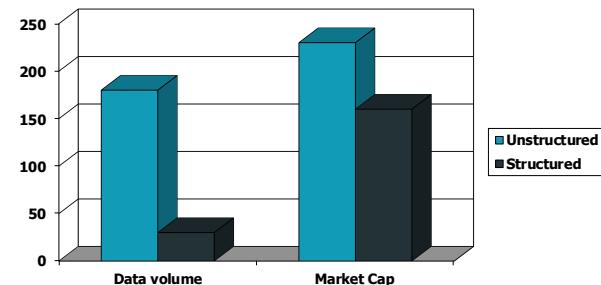
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### Unstructured (text) vs. structured (database) data in the mid-nineties



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### Unstructured (text) vs. structured (database) data today



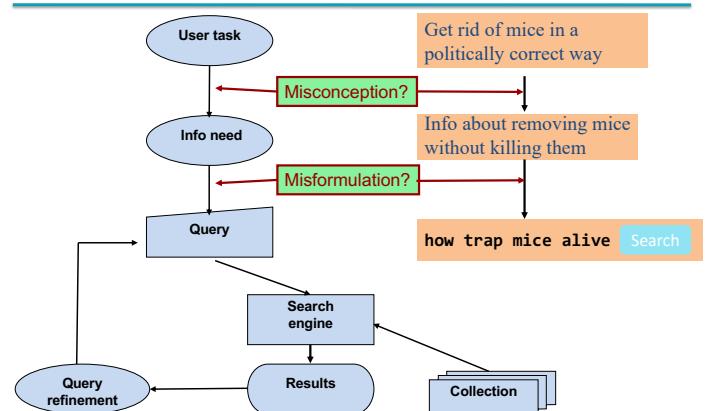
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### Basic assumptions of Information Retrieval

- Collection:** A set of documents
  - Assume it is a static collection for the moment
- Goal:** Retrieve documents with information that is **relevant** to the user's **information need** and helps the user complete a **task**

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### The classic search model



## How good are the retrieved docs?

- **Precision** : Fraction of retrieved docs that are relevant to the user's information need
- **Recall** : Fraction of relevant docs in collection that are retrieved
- More precise definitions and measurements to follow later

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# Introduction to Information Retrieval

Term-document incidence matrices

## Unstructured data in 1620

- Which plays of Shakespeare contain the words ***Brutus AND Caesar*** but NOT ***Calpurnia***?
- One could grep all of Shakespeare's plays for ***Brutus*** and ***Caesar***, then strip out lines containing ***Calpurnia***?
- Why is that not the answer?
  - Slow (for large corpora)
  - ***NOT Calpurnia*** is non-trivial
  - Other operations (e.g., find the word ***Romans*** near ***countrymen***) not feasible
- Ranked retrieval (best documents to return)
  - Later lectures

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## Incidence vectors

- So we have a 0/1 vector for each term.
- To answer query: take the vectors for ***Brutus***, ***Caesar*** and ***Calpurnia*** (complemented) → bitwise AND.
  - 110100 AND
  - 110111 AND
  - 101111 =
  - **100100**

	Antony and Cleopatra	Julius Caesar	The Tempest	Hamlet	Othello	Macbeth
Antony	1	1	0	0	0	1
Brutus	1	1	0	1	0	0
Caesar	1	1	0	1	1	1
Calpurnia	0	1	0	0	0	0
Cleopatra	1	0	0	0	0	0
mercy	1	0	1	1	1	1
worser	1	0	1	1	1	0

## Term-document incidence matrices

	Antony and Cleopatra	Julius Caesar	The Tempest	Hamlet	Othello	Macbeth
Antony	1	1	0	0	0	1
Brutus	1	1	0	1	0	0
Caesar	1	1	0	1	1	1
Calpurnia	0	1	0	0	0	0
Cleopatra	1	0	0	0	0	0
mercy	1	0	1	1	1	1
worser	1	0	1	1	1	0

Brutus AND Caesar BUT NOT  
Calpurnia1 if play contains  
word, 0 otherwise

## Answers to query

- **Antony and Cleopatra, Act III, Scene ii**

Agrippa [Aside to DOMITIUS ENOBARBUS]: Why, Enobarbus,  
When Antony found Julius ***Caesar*** dead,  
He cried almost to roaring; and he wept  
When at Philippi he found ***Brutus*** slain.

- **Hamlet, Act III, Scene ii**

Lord Polonius: I did enact Julius ***Caesar*** I was killed i' the  
Capitol; ***Brutus*** killed me.



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## Bigger collections

- Consider  $N = 1$  million documents, each with about 1000 words.
- Avg 6 bytes/word including spaces/punctuation
  - 6GB of data in the documents.
- Say there are  $M = 500K$  distinct terms among these.

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## Can't build the matrix

- 500K x 1M matrix has half-a-trillion 0's and 1's.
- But it has no more than one billion 1's.
  - matrix is extremely sparse.
- What's a better representation?
  - We only record the 1 positions.



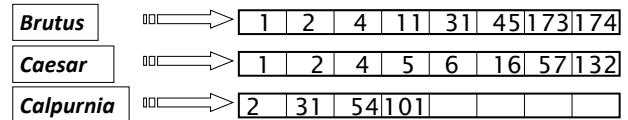
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## Introduction to Information Retrieval

The Inverted Index  
The key data structure underlying modern IR

## Inverted index

- For each term  $t$ , we must store a list of all documents that contain  $t$ .
  - Identify each doc by a **docID**, a document serial number
- Can we use fixed-size arrays for this?

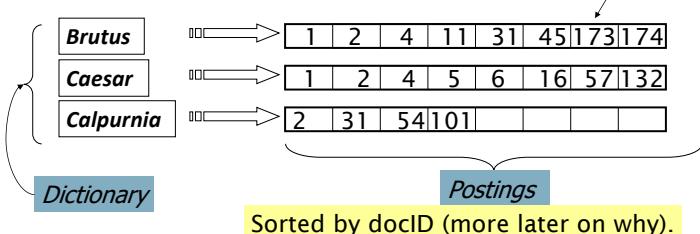


What happens if the word **Caesar** is added to document 14?

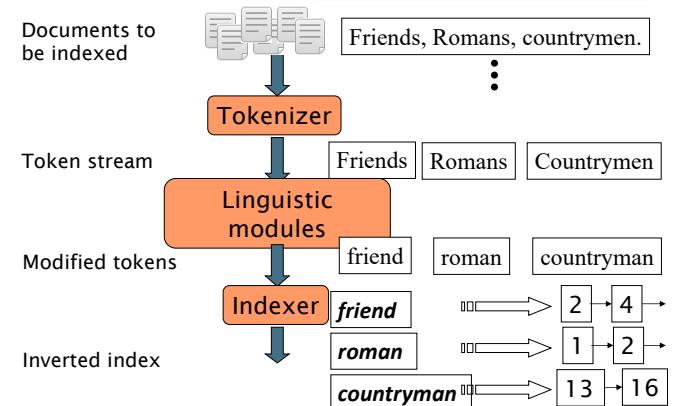
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## Inverted index

- We need variable-size **postings lists**
  - On disk, a continuous run of postings is normal and best
  - In memory, can use linked lists or variable length arrays
    - Some tradeoffs in size/ease of insertion



## Inverted index construction



## Initial stages of text processing

- Tokenization
    - Cut character sequence into word tokens
      - Deal with "*John's*", a state-of-the-art solution
  - Normalization
    - Map text and query term to same form
      - You want *U.S.A.* and *USA* to match
  - Stemming
    - We may wish different forms of a root to match
      - *authorize*, *authorization*
  - Stop words
    - We may omit very common words (or not)
      - *the*, *a*, *to*, *of*

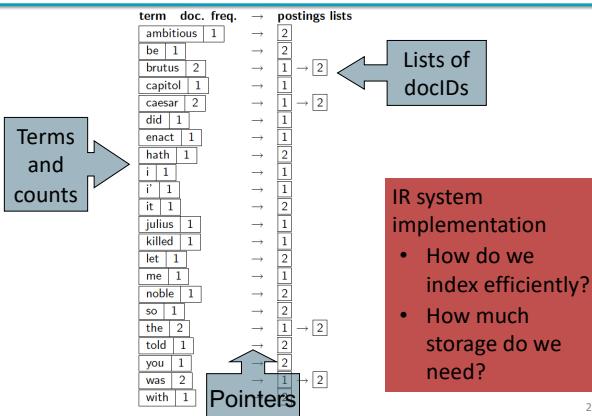
## Indexer steps: Sort

- Sort by terms
    - At least conceptually
      - And then docID



Term	docID	Term	docID
I	1	ambitious	2
did	1	be	2
enact	1	brutus	1
julius	1	brute	2
caesar	1	capitol	1
I	1	caesar	2
was	1	caesar	2
killed	1	caesar	2
I'	1	did	1
the	1	enact	1
capitol	1	hath	1
brutus	1	I	1
killed	1	I	1
me	1	it	2
so	2	julius	1
let	2	killed	1
be	2	Julius	1
with	2	let	2
caesar	2	me	1
the	2	noble	2
noble	2	so	2
brutus	2	the	1
two	2	told	2
told	2	told	2
you	2	you	2
caesar	2	was	1
was	2	was	2
ambitious	2	with	2

## Where do we pay in storage?



## Indexer steps: Dictionary & Postings

- Multiple term entries in a single document are merged.
  - Split into Dictionary and Postings
  - Doc. frequency information is added.

Why frequency?  
Will discuss later

Term	docID	term	doc	freq.	→	postings	lists
ambitious	2	ambitious	[1]		→	[2]	
be	2	be	[1]		→	[2]	
brutus	1	brutus	[2]		→	[1]	→ [2]
brutus	2				→	[1]	
capitol	2	capitol	[1]		→	[1]	
caesar	1				→	[1]	→ [2]
caesar	2	caesar	[2]		→	[1]	
caesar	2	did	[1]		→	[1]	
did	1	enact	[1]		→	[1]	
enact	1	hath	[1]		→	[2]	
hath	1	i	[1]		→	[1]	
i	1	i'	[1]		→	[1]	
r	1	it	[1]		→	[2]	
s	2						
julius	1	julius	[1]		→	[1]	
killed	1	killed	[1]		→	[1]	
killed	1						
let	2	let	[1]		→	[2]	
me	1	me	[1]		→	[1]	
noble	2	noble	[1]		→	[2]	
so	2	so	[1]		→	[2]	
the	1	the	[2]		→	[1]	→ [2]
the	2	told	[1]		→	[2]	
told	2	you	[1]		→	[2]	
you	2	was	[2]		→	[1]	→ [2]
was	2	with	[1]		→	[2]	
with	2						

# Introduction to **Information Retrieval**

## The index we just built

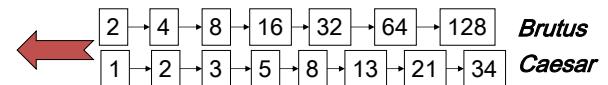
- How do we process a query?
  - Later – what kinds of queries can we process?

Our focus

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## Query processing: AND

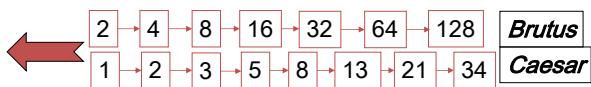
- Consider processing the query:  
***Brutus AND Caesar***
  - Locate ***Brutus*** in the Dictionary;
  - Retrieve its postings.
  - Locate ***Caesar*** in the Dictionary;
  - Retrieve its postings.
  - “Merge” the two postings (intersect the document sets):



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## The merge

- Walk through the two postings simultaneously, in time linear in the total number of postings entries



If the list lengths are  $x$  and  $y$ , the merge takes  $O(x+y)$  operations.

Crucial: postings sorted by docID.

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## Intersecting two postings lists (a “merge” algorithm)

```

INTERSECT( $p_1, p_2$ )
1  $answer \leftarrow \langle \rangle$ 
2 while  $p_1 \neq NIL$  and  $p_2 \neq NIL$ 
3 do if  $docID(p_1) = docID(p_2)$ 
4   then ADD( $answer, docID(p_1)$ )
5      $p_1 \leftarrow next(p_1)$ 
6      $p_2 \leftarrow next(p_2)$ 
7   else if  $docID(p_1) < docID(p_2)$ 
8     then  $p_1 \leftarrow next(p_1)$ 
9   else  $p_2 \leftarrow next(p_2)$ 
10 return  $answer$ 

```

# Introduction to Information Retrieval

The Boolean Retrieval Model  
& Extended Boolean Models

## Boolean queries: Exact match

- The **Boolean retrieval model** is being able to ask a query that is a Boolean expression:
  - Boolean Queries are queries using ***AND***, ***OR*** and ***NOT*** to join query terms
    - Views each document as a set of words
    - Is precise: document matches condition or not.
  - Perhaps the simplest model to build an IR system on
  - Primary commercial retrieval tool for 3 decades.
  - Many search systems you still use are Boolean:
    - Email, library catalog, macOS Spotlight

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## Example: WestLaw <http://www.westlaw.com/>

- Largest commercial (paying subscribers) legal search service (started 1975; ranking added 1992; new federated search added 2010)
- Tens of terabytes of data; ~700,000 users
- Majority of users *still* use boolean queries
- Example query:
  - What is the statute of limitations in cases involving the federal tort claims act?
  - **LIMIT! /3 STATUTE ACTION /S FEDERAL /2 TORT /3 CLAIM**
  - /3 = within 3 words, /S = in same sentence

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## Example: WestLaw <http://www.westlaw.com/>

- Another example query:
  - Requirements for disabled people to be able to access a workplace
  - **disabl! /p access! /s work-site work-place (employment /3 place**
- Note that SPACE is disjunction, not conjunction!
- Long, precise queries; proximity operators; incrementally developed; not like web search
- Many professional searchers still like Boolean search
  - You know exactly what you are getting
- But that doesn't mean it actually works better....

## Boolean queries: More general merges

- Exercise: Adapt the merge for the queries:  
**Brutus AND NOT Caesar**  
**Brutus OR NOT Caesar**
- Can we still run through the merge in time  $O(x+y)$ ?  
 What can we achieve?

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## Merging

What about an arbitrary Boolean formula?

**(Brutus OR Caesar) AND NOT**

**(Antony OR Cleopatra)**

- Can we always merge in “linear” time?
  - Linear in what?
- Can we do better?

## Query optimization

- What is the best order for query processing?
- Consider a query that is an *AND* of  $n$  terms.
- For each of the  $n$  terms, get its postings, then *AND* them together.

<b>Brutus</b>	⇒	[ 2   4   8   16   32   64   128 ]
<b>Caesar</b>	⇒	[ 1   2   3   5   8   16   21   34 ]
<b>Calpurnia</b>	⇒	[ 13   16   ]

Query: **Brutus AND Calpurnia AND Caesar**

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## Query optimization example

- Process in order of increasing freq:
  - start with smallest set, then keep cutting further.

This is why we kept  
document freq. in dictionary

<b>Brutus</b>	⇒	[ 2   4   8   16   32   64   128 ]
<b>Caesar</b>	⇒	[ 1   2   3   5   8   16   21   34 ]
<b>Calpurnia</b>	⇒	[ 13   16   ]

Execute the query as **(Calpurnia AND Brutus) AND Caesar**.

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## Exercise

- Recommend a query processing order for

*(tangerine OR trees) AND (marmalade OR skies) AND (kaleidoscope OR eyes)*

- Which two terms should we process first?

Term	Freq
eyes	213312
kaleidoscope	87009
marmalade	107913
skies	271658
tangerine	46653
trees	316812

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## More general optimization

- e.g., *(madding OR crowd) AND (ignoble OR stripe)*
- Get doc. freq.'s for all terms.
- Estimate the size of each *OR* by the sum of its doc. freq.'s (conservative).
- Process in increasing order of *OR* sizes.

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## Query processing exercises

- **Exercise:** If the query is *friends AND romans AND (NOT countrymen)*, how could we use the freq of *countrymen*?
- **Exercise:** Extend the merge to an arbitrary Boolean query. Can we always guarantee execution in time linear in the total postings size?
- **Hint:** Begin with the case of a Boolean *formula* query: in this, each query term appears only once in the query.

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## Exercise

- Try the search feature at <http://www.rhymezone.com/shakespeare/>
- Write down five search features you think it could do better

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Introduction to  
**Information Retrieval**

Phrase queries and positional indexes

## Phrase queries

- We want to be able to answer queries such as *"stanford university"* – as a phrase
- Thus the sentence *"I went to university at Stanford"* is not a match.
  - The concept of phrase queries has proven easily understood by users; one of the few “advanced search” ideas that works
  - Many more queries are *implicit phrase queries*
- For this, it no longer suffices to store only *<term : docs>* entries

## A first attempt: Biword indexes

- Index every consecutive pair of terms in the text as a phrase
- For example the text “Friends, Romans, Countrymen” would generate the biwords
  - *friends romans*
  - *romans countrymen*
- Each of these biwords is now a dictionary term
- Two-word phrase query-processing is now immediate.

## Longer phrase queries

- Longer phrases can be processed by breaking them down
- ***stanford university palo alto*** can be broken into the Boolean query on biwords:  
***stanford university AND university palo AND palo alto***

Without the docs, we cannot verify that the docs matching the above Boolean query do contain the phrase.

 Can have false positives!

## Issues for biword indexes

- False positives, as noted before
- Index blowup due to bigger dictionary
  - Infeasible for more than biwords, big even for them
- Biword indexes are not the standard solution (for all biwords) but can be part of a compound strategy

## Solution 2: Positional indexes

- In the postings, store, for each ***term*** the position(s) in which tokens of it appear:

```
<term, number of docs containing term;
doc1: position1, position2 ... ;
doc2: position1, position2 ... ;
etc.>
```

## Positional index example

```
<be: 993427;
  1: 7, 18, 33, 72, 86, 231;
  2: 3, 149;
  4: 17, 191, 291, 430, 434;
  5: 363, 367, ...>
```

Which of docs 1,2,4,5 could contain “*to be or not to be*”?

- For phrase queries, we use a merge algorithm recursively at the document level
- But we now need to deal with more than just equality

## Processing a phrase query

- Extract inverted index entries for each distinct term: ***to, be, or, not***.
- Merge their *doc:position* lists to enumerate all positions with “***to be or not to be***”.
  - ***to:***
    - 2:1,17,74,222,551; 4:8,16,190,429,433; 7:13,23,191; ...
  - ***be:***
    - 1:17,19; 4:17,191,291,430,434; 5:14,19,101; ...
- Same general method for proximity searches

## Proximity queries

- **LIMIT! /3 STATUTE /3 FEDERAL /2 TORT**
  - Again, here,  $/k$  means “within  $k$  words of”.
- Clearly, positional indexes can be used for such queries; biword indexes cannot.
- Exercise: Adapt the linear merge of postings to handle proximity queries. Can you make it work for any value of  $k$ ?
  - This is a little tricky to do correctly and efficiently
  - See Figure 2.12 of IIR

## Positional index size

- A positional index expands postings storage *substantially*
  - Even though indices can be compressed
- Nevertheless, a positional index is now standardly used because of the power and usefulness of phrase and proximity queries ... whether used explicitly or implicitly in a ranking retrieval system.

## Positional index size

- Need an entry for each occurrence, not just once per document
- Index size depends on average document size 
- Average web page has <1000 terms
- SEC filings, books, even some epic poems ... easily 100,000 terms
- Consider a term with frequency 0.1%

Document size	Postings	Positional postings
1000	1	1
100,000	1	100

## Rules of thumb

- A positional index is 2–4 as large as a non-positional index
- Positional index size 35–50% of volume of original text
- Caveat: all of this holds for “English-like” languages

## Combination schemes

- These two approaches can be profitably combined
  - For particular phrases (**“Michael Jackson”, “Britney Spears”**) it is inefficient to keep on merging positional postings lists
    - Even more so for phrases like **“The Who”**
- Williams et al. (2004) evaluate a more sophisticated mixed indexing scheme
  - A typical web query mixture was executed in  $\frac{1}{4}$  of the time of using just a positional index
  - It required 26% more space than having a positional index alone