

# Introduction to **Information Retrieval**

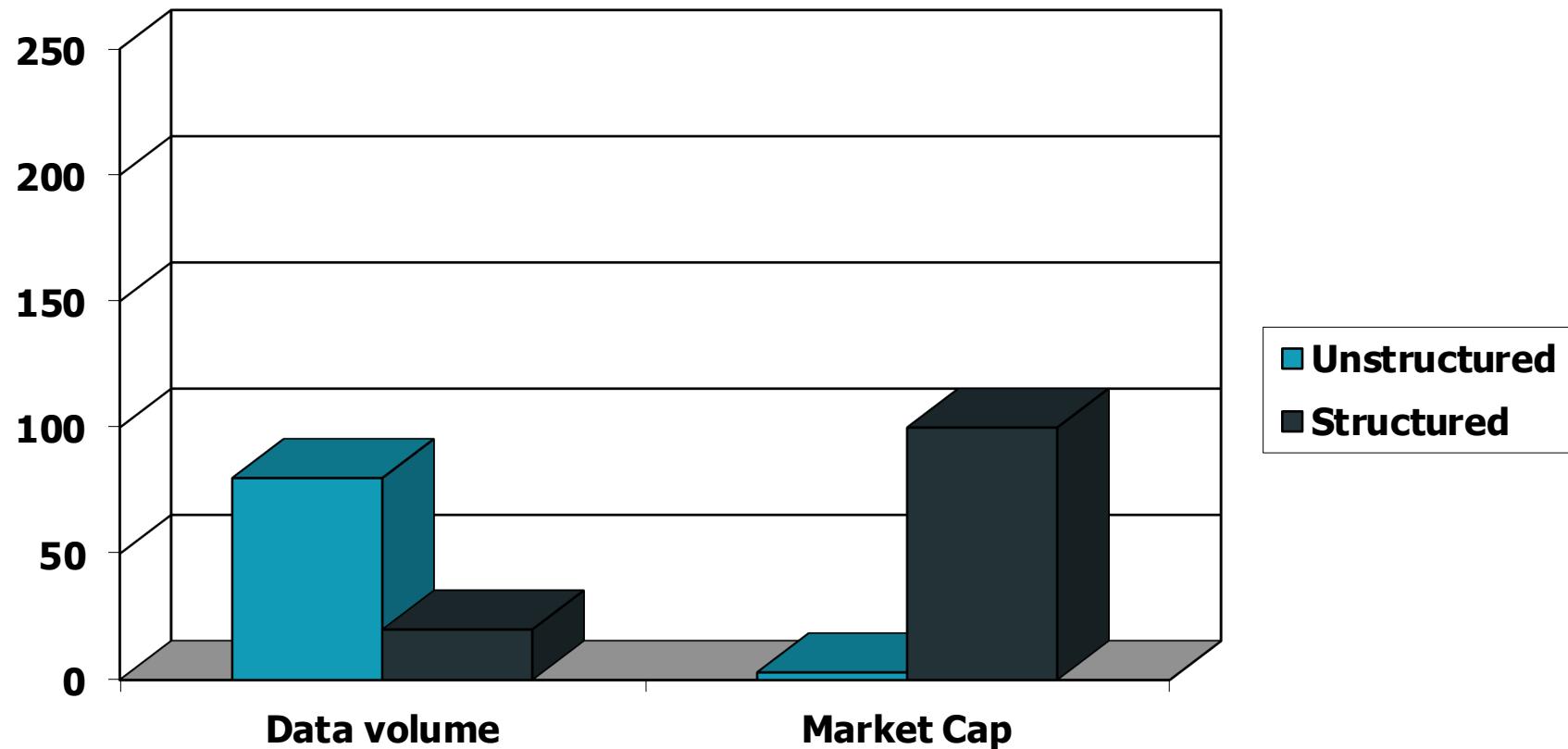
Introducing Information Retrieval  
and Web Search

# Information Retrieval

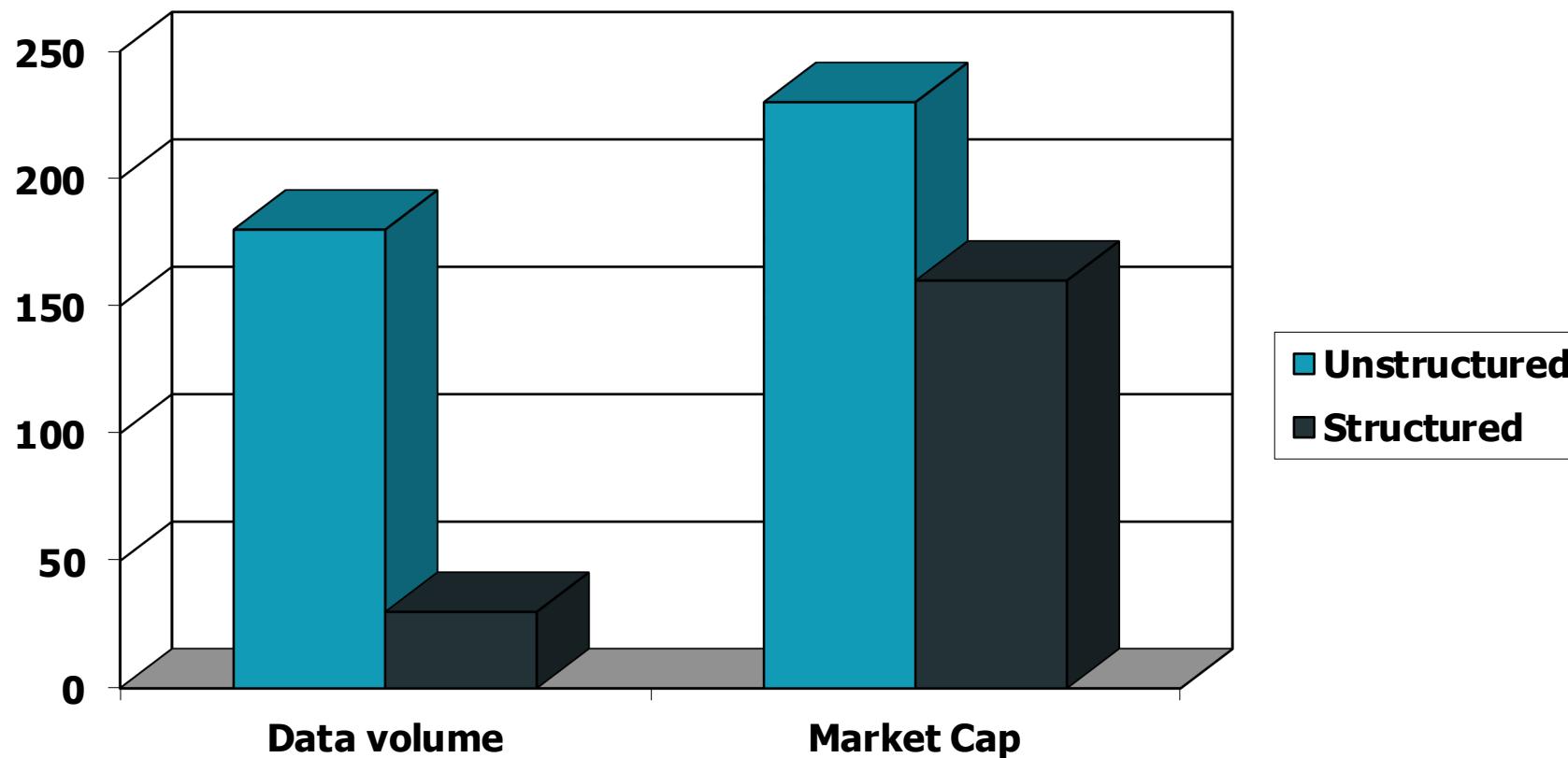
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- Information Retrieval (IR) is **finding material** (usually documents) of an **unstructured nature** (usually text) that satisfies an **information need** from within **large collections** (usually stored on computers).
- These days we frequently think first of **web search**, but there are many other cases:
  - E-mail search
  - Searching your laptop
  - Corporate knowledge bases
  - Legal information retrieval

# Unstructured (text) vs. structured (database) data in the mid-nineties



# Unstructured (text) vs. structured (database) data today

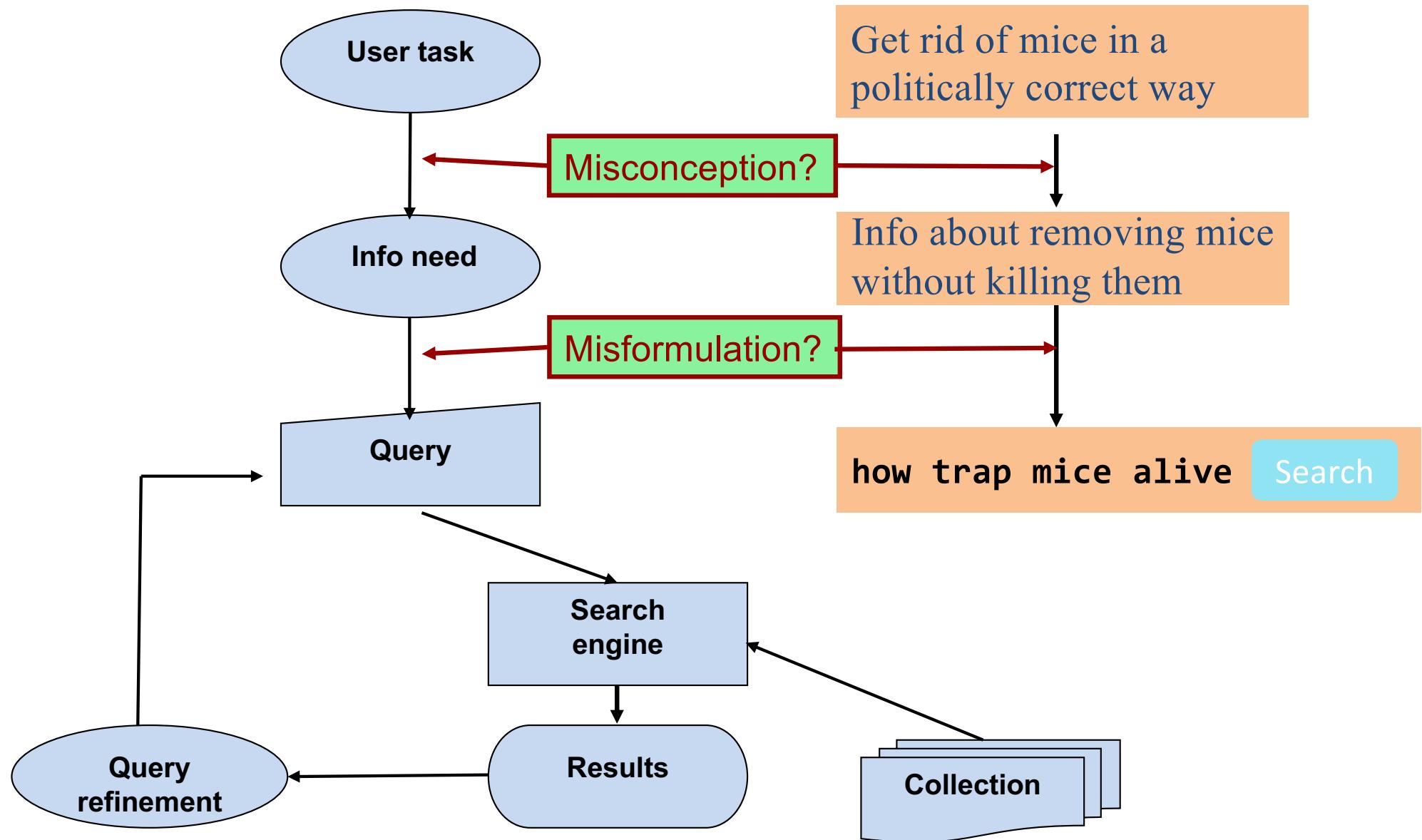


# Basic assumptions of Information Retrieval

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- **Collection:** A set of documents
  - Assume it is a static collection for the moment
- **Goal:** Retrieve documents with information that is **relevant** to the user's **information need** and helps the user complete a **task**

# The classic search model



# How good are the retrieved docs?

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- *Precision* : Fraction of retrieved docs that are relevant to the user's **information need**
- *Recall* : Fraction of relevant docs in collection that are retrieved
  - More precise definitions and measurements to follow later

# Introduction to **Information Retrieval**

Term-document incidence matrices

# Unstructured data in 1620

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- Which plays of Shakespeare contain the words ***Brutus*** AND ***Caesar*** but ***NOT Calpurnia***?
- One could grep all of Shakespeare's plays for ***Brutus*** and ***Caesar***, then strip out lines containing ***Calpurnia***?
- Why is that not the answer?
  - Slow (for large corpora)
  - **NOT *Calpurnia*** is non-trivial
  - Other operations (e.g., find the word ***Romans*** near ***countrymen***) not feasible
  - Ranked retrieval (best documents to return)
    - Later lectures

# Term-document incidence matrices

	Antony and Cleopatra	Julius Caesar	The Tempest	Hamlet	Othello	Macbeth
Antony	1	1	0	0	0	1
Brutus	1	1	0	1	0	0
Caesar	1	1	0	1	1	1
Calpurnia	0	1	0	0	0	0
Cleopatra	1	0	0	0	0	0
mercy	1	0	1	1	1	1
worser	1	0	1	1	1	0

*Brutus AND Caesar BUT NOT  
Calpurnia*

1 if play contains  
word, 0 otherwise

# Incidence vectors

- So we have a 0/1 vector for each term.
- To answer query: take the vectors for ***Brutus***, ***Caesar*** and ***Calpurnia*** (complemented) → bitwise AND.
  - 110100 AND
  - 110111 AND
  - 101111 =
  - **100100**

	Antony and Cleopatra	Julius Caesar	The Tempest	Hamlet	Othello	Macbeth
<b>Antony</b>	1	1	0	0	0	1
<b>Brutus</b>	1	1	0	1	0	0
<b>Caesar</b>	1	1	0	1	1	1
<b>Calpurnia</b>	0	1	0	0	0	0
<b>Cleopatra</b>	1	0	0	0	0	0
<b>mercy</b>	1	0	1	1	1	1
<b>worser</b>	1	0	1	1	1	0

# Answers to query

- Antony and Cleopatra, Act III, Scene ii

*Agrippa* [Aside to DOMITIUS ENOBARBUS]: Why, Enobarbus,  
When Antony found Julius **Caesar** dead,  
He cried almost to roaring; and he wept  
When at Philippi he found **Brutus** slain.

- Hamlet, Act III, Scene ii

*Lord Polonius*: I did enact Julius **Caesar** I was killed i' the  
Capitol; **Brutus** killed me.



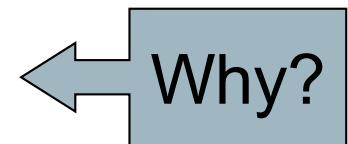
# Bigger collections

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- Consider  $N = 1$  million documents, each with about 1000 words.
- Avg 6 bytes/word including spaces/punctuation
  - 6GB of data in the documents.
- Say there are  $M = 500K$  *distinct* terms among these.

# Can't build the matrix

- 500K x 1M matrix has half-a-trillion 0's and 1's.
- But it has no more than one billion 1's.
  - matrix is extremely sparse.
- What's a better representation?
  - We only record the 1 positions.

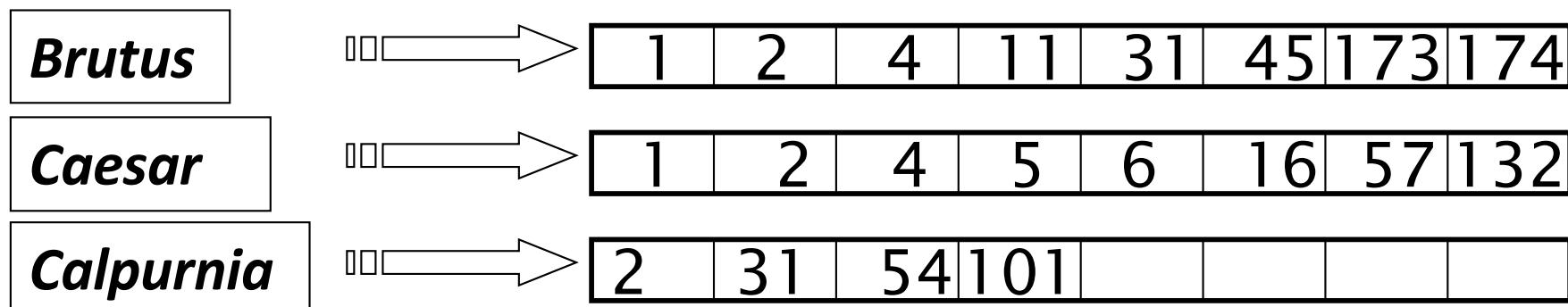


# Introduction to **Information Retrieval**

The Inverted Index  
The key data structure underlying modern IR

# Inverted index

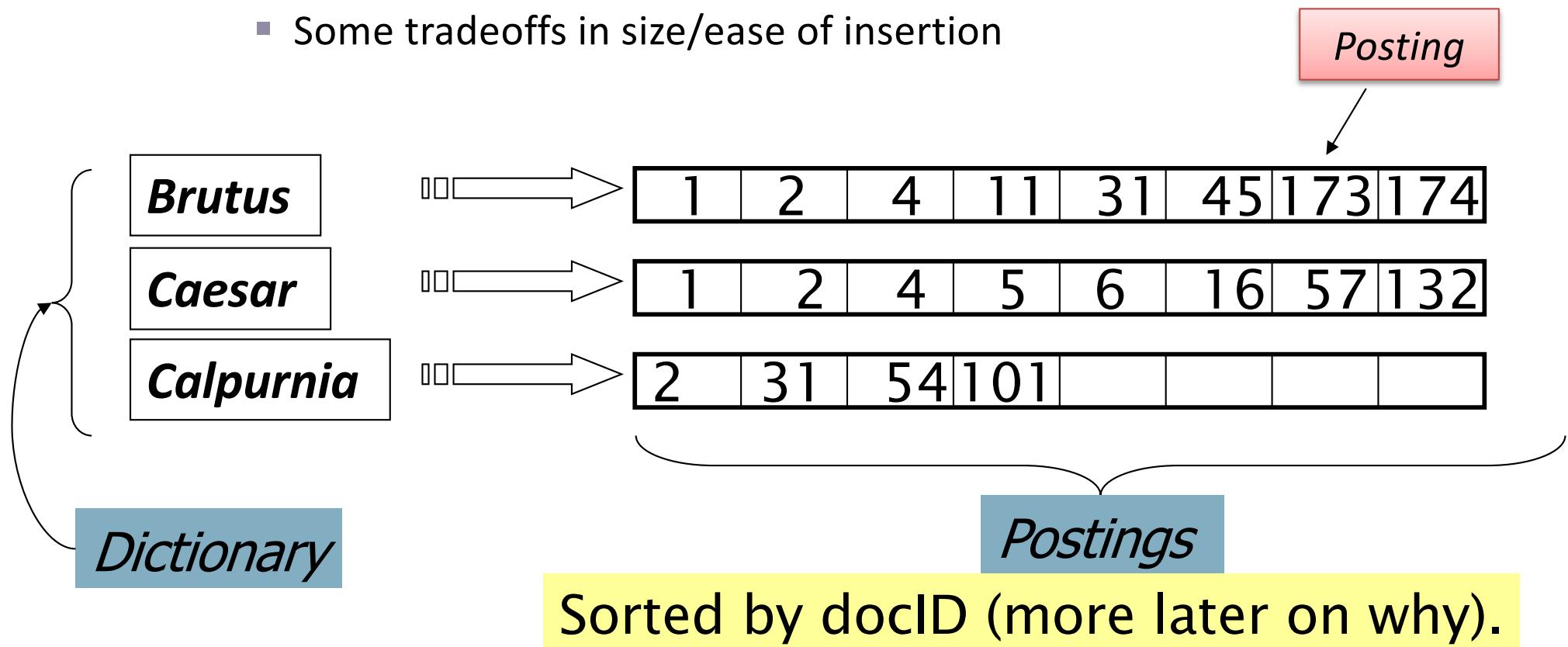
- For each term  $t$ , we must store a list of all documents that contain  $t$ .
  - Identify each doc by a **docID**, a document serial number
- Can we used fixed-size arrays for this?



What happens if the word **Caesar** is added to document 14?

# Inverted index

- We need variable-size **postings lists**
  - On disk, a continuous run of postings is normal and best
  - In memory, can use linked lists or variable length arrays
    - Some tradeoffs in size/ease of insertion



# Inverted index construction

Documents to be indexed



Friends, Romans, countrymen.  
⋮

Tokenizer

Token stream

Friends

Romans

Countrymen

Linguistic modules

Modified tokens

friend

roman

countryman

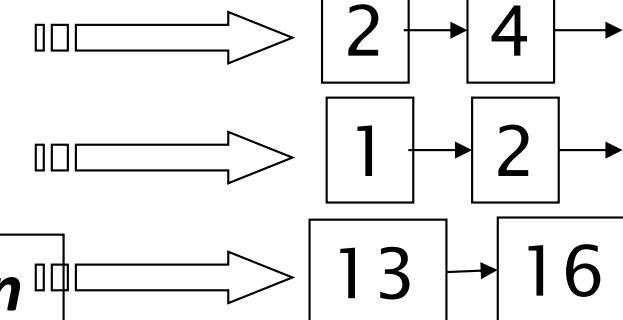
Indexer

Inverted index

*friend*

*roman*

*countryman*



# Initial stages of text processing

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- Tokenization
  - Cut character sequence into word tokens
    - Deal with “*John’s*”, *a state-of-the-art solution*
- Normalization
  - Map text and query term to same form
    - You want *U.S.A.* and *USA* to match
- Stemming
  - We may wish different forms of a root to match
    - *authorize, authorization*
- Stop words
  - We may omit very common words (or not)
    - *the, a, to, of*

# Indexer steps: Token sequence

- Sequence of (Modified token, Document ID) pairs.

Doc 1

I did enact Julius  
Caesar I was killed  
i' the Capitol;  
Brutus killed me.

Doc 2

So let it be with  
Caesar. The noble  
Brutus hath told you  
Caesar was ambitious



Term	docID
I	1
did	1
enact	1
julius	1
caesar	1
I	1
was	1
killed	1
i'	1
the	1
capitol	1
brutus	1
killed	1
me	1
so	2
let	2
it	2
be	2
with	2
caesar	2
the	2
noble	2
brutus	2
hath	2
told	2
you	2
caesar	2
was	2
ambitious	2

# Indexer steps: Sort

- Sort by terms
  - At least conceptually
    - And then docID

Core indexing step

Term	docID
I	1
did	1
enact	1
julius	1
caesar	1
I	1
was	1
killed	1
i'	1
the	1
capitol	1
brutus	1
killed	1
me	1
so	2
let	2
it	2
be	2
with	2
caesar	2
the	2
noble	2
brutus	2
hath	2
told	2
you	2
caesar	2
was	2
ambitious	2

Term	docID
ambitious	2
be	2
brutus	1
brutus	2
capitol	1
caesar	1
caesar	2
caesar	2
did	1
enact	1
hath	1
I	1
I	1
i'	1
it	2
julius	1
killed	1
killed	1
let	2
me	1
noble	2
so	2
the	1
the	2
told	2
you	2
caesar	2
was	1
was	2
with	2

# Indexer steps: Dictionary & Postings

- Multiple term entries in a single document are merged.
- Split into Dictionary and Postings
- Doc. frequency information is added.

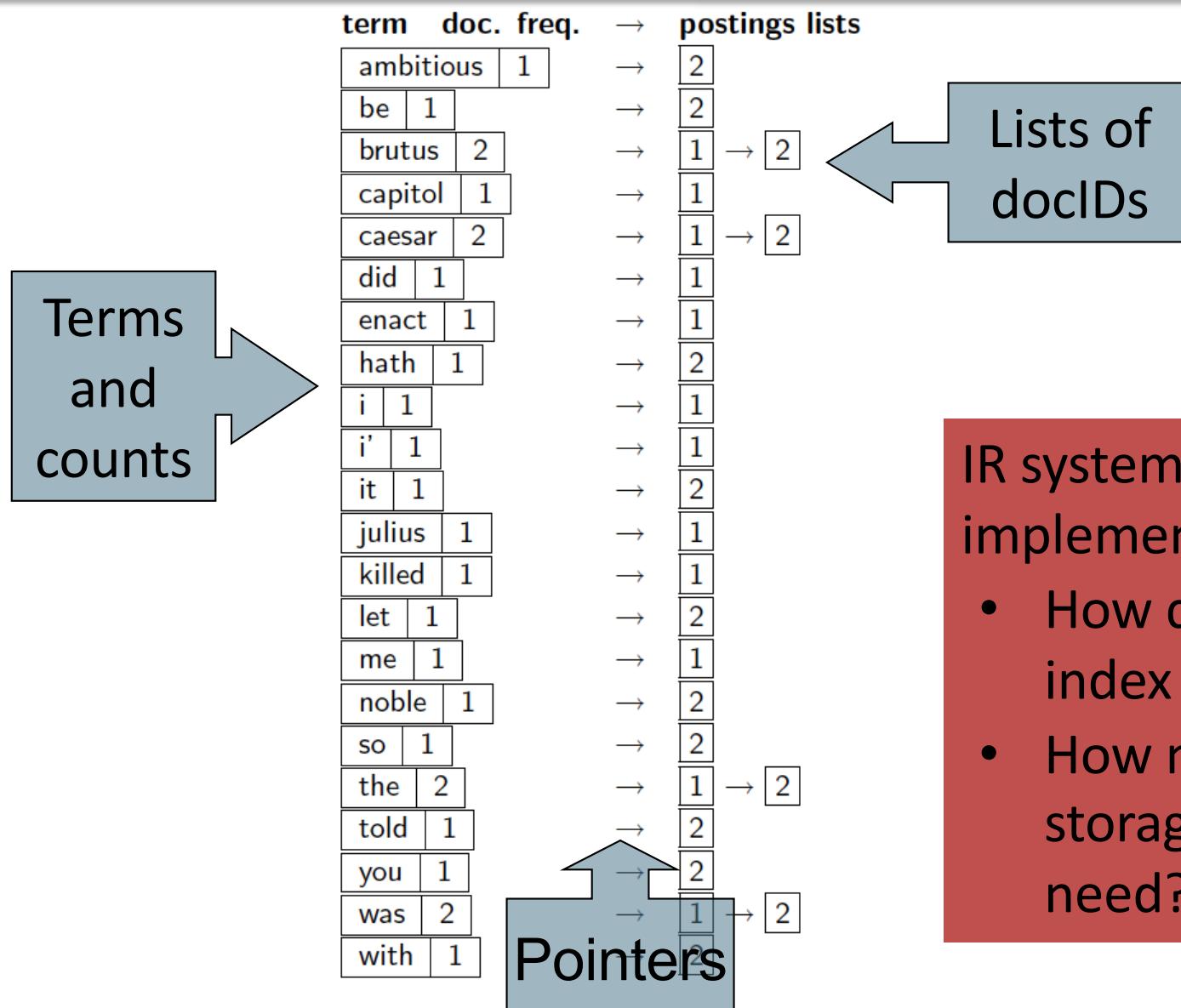
Why frequency?  
Will discuss later.

Term	docID
ambitious	2
be	2
brutus	1
brutus	2
capitol	1
caesar	1
caesar	2
caesar	2
did	1
enact	1
hath	1
I	1
I	1
i'	1
it	2
julius	1
killed	1
killed	1
let	2
me	1
noble	2
so	2
the	1
the	2
told	2
you	2
was	1
was	2
with	2

→

term	doc. freq.	→	postings lists
ambitious	1	→	2
be	1	→	2
brutus	2	→	1 → 2
capitol	1	→	1
caesar	2	→	1 → 2
did	1	→	1
enact	1	→	1
hath	1	→	2
i	1	→	1
i'	1	→	1
it	1	→	2
julius	1	→	1
killed	1	→	1
let	1	→	2
me	1	→	1
noble	1	→	2
so	1	→	2
the	2	→	1 → 2
told	1	→	2
you	1	→	2
was	2	→	1 → 2
with	1	→	2

# Where do we pay in storage?



# IR system implementation

- How do we index efficiently?
  - How much storage do we need?

# Introduction to **Information Retrieval**

Query processing with an inverted index

# The index we just built

- How do we process a query?
  - Later – what kinds of queries can we process?

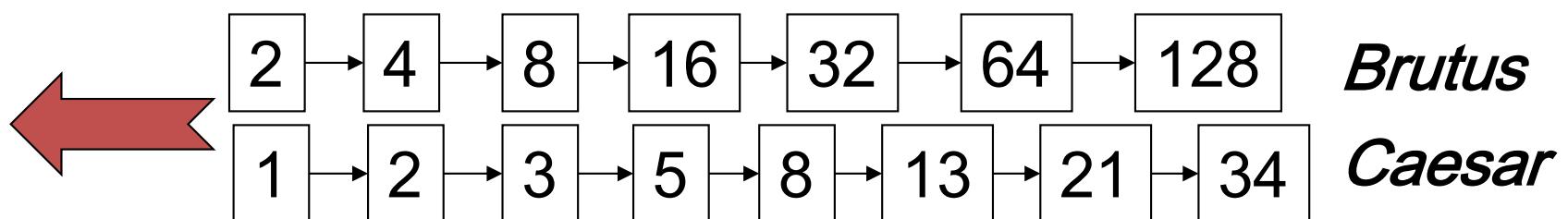


# Query processing: AND

- Consider processing the query:

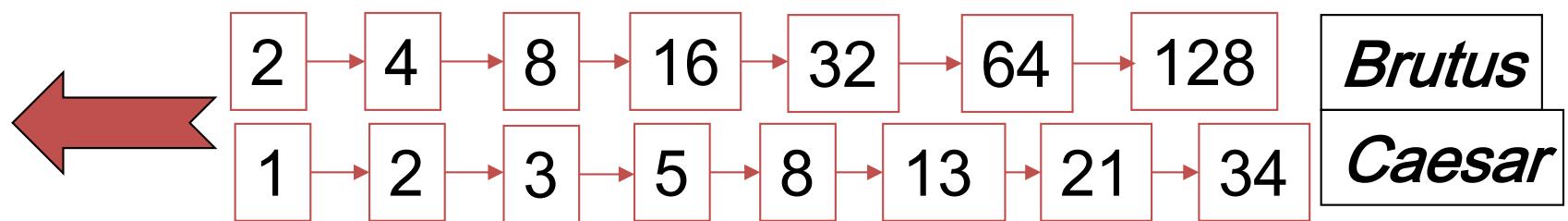
***Brutus AND Caesar***

- Locate ***Brutus*** in the Dictionary;
  - Retrieve its postings.
- Locate ***Caesar*** in the Dictionary;
  - Retrieve its postings.
- “Merge” the two postings (intersect the document sets):



# The merge

- Walk through the two postings simultaneously, in time linear in the total number of postings entries



If the list lengths are  $x$  and  $y$ , the merge takes  $O(x+y)$  operations.

Crucial: postings sorted by docID.

# Intersecting two postings lists (a “merge” algorithm)

INTERSECT( $p_1, p_2$ )

```
1  answer ← ⟨ ⟩  
2  while  $p_1 \neq \text{NIL}$  and  $p_2 \neq \text{NIL}$   
3  do if  $\text{docID}(p_1) = \text{docID}(p_2)$   
4      then ADD(answer,  $\text{docID}(p_1)$ )  
5           $p_1 \leftarrow \text{next}(p_1)$   
6           $p_2 \leftarrow \text{next}(p_2)$   
7      else if  $\text{docID}(p_1) < \text{docID}(p_2)$   
8          then  $p_1 \leftarrow \text{next}(p_1)$   
9          else  $p_2 \leftarrow \text{next}(p_2)$   
10 return answer
```

# Introduction to **Information Retrieval**

The Boolean Retrieval Model  
& Extended Boolean Models

# Boolean queries: Exact match

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- The Boolean retrieval model is being able to ask a query that is a Boolean expression:
  - Boolean Queries are queries using *AND*, *OR* and *NOT* to join query terms
    - Views each document as a set of words
    - Is precise: document matches condition or not.
  - Perhaps the simplest model to build an IR system on
- Primary commercial retrieval tool for 3 decades.
- Many search systems you still use are Boolean:
  - Email, library catalog, macOS Spotlight

# Example: WestLaw <http://www.westlaw.com/>

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- Largest commercial (paying subscribers) legal search service (started 1975; ranking added 1992; new federated search added 2010)
- Tens of terabytes of data; ~700,000 users
- Majority of users *still* use boolean queries
- Example query:
  - What is the statute of limitations in cases involving the federal tort claims act?
  - **LIMIT! /3 STATUTE ACTION /S FEDERAL /2 TORT /3 CLAIM**
    - /3 = within 3 words, /S = in same sentence

# Example: WestLaw <http://www.westlaw.com/>

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- Another example query:
  - Requirements for disabled people to be able to access a workplace
  - **disabl! /p access! /s work-site work-place (employment /3 place**
- Note that SPACE is disjunction, not conjunction!
- Long, precise queries; proximity operators; incrementally developed; not like web search
- Many professional searchers still like Boolean search
  - You know exactly what you are getting
- But that doesn't mean it actually works better...

# Boolean queries:

## More general merges

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- Exercise: Adapt the merge for the queries:  
***Brutus AND NOT Caesar***  
***Brutus OR NOT Caesar***
- Can we still run through the merge in time  $O(x+y)$ ?  
What can we achieve?

# Merging

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What about an arbitrary Boolean formula?

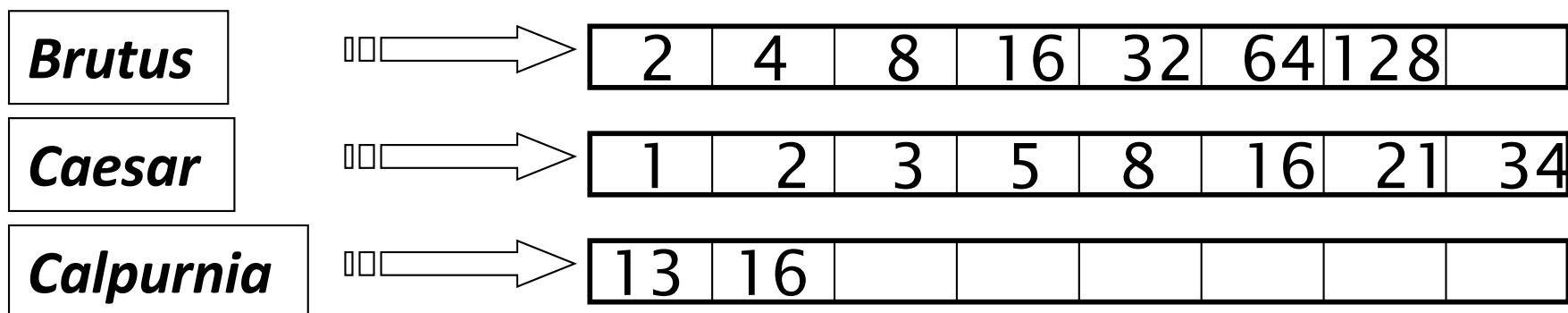
***(Brutus OR Caesar) AND NOT***

***(Antony OR Cleopatra)***

- Can we always merge in “linear” time?
  - Linear in what?
- Can we do better?

# Query optimization

- What is the best order for query processing?
- Consider a query that is an *AND* of  $n$  terms.
- For each of the  $n$  terms, get its postings, then *AND* them together.



**Query:** *Brutus AND Calpurnia AND Caesar*

# Query optimization example

- Process in order of increasing freq:
  - *start with smallest set, then keep cutting further.*

This is why we kept  
document freq. in dictionary

<b>Brutus</b>	⇒	2   4   8   16   32   64   128
<b>Caesar</b>	⇒	1   2   3   5   8   16   21   34
<b>Calpurnia</b>	⇒	13   16

Execute the query as (**Calpurnia AND Brutus**) AND **Caesar**.

# Exercise

- Recommend a query processing order for

*(tangerine OR trees) AND  
(marmalade OR skies) AND  
(kaleidoscope OR eyes)*

- Which two terms should we process first?

Term	Freq
eyes	213312
kaleidoscope	87009
marmalade	107913
skies	271658
tangerine	46653
trees	316812

# More general optimization

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- e.g., **(madding OR crowd) AND (ignoble OR strife)**
- Get doc. freq.'s for all terms.
- Estimate the size of each *OR* by the sum of its doc. freq.'s (conservative).
- Process in increasing order of *OR* sizes.

# Query processing exercises

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- **Exercise:** If the query is *friends AND romans AND (NOT countrymen)*, how could we use the freq of *countrymen*?
- **Exercise:** Extend the merge to an arbitrary Boolean query. Can we always guarantee execution in time linear in the total postings size?
- **Hint:** Begin with the case of a Boolean *formula* query: in this, each query term appears only once in the query.

# Exercise

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- Try the search feature at  
<http://www.rhymezone.com/shakespeare/>
- Write down five search features you think it could do better

Introduction to  
**Information Retrieval**

Phrase queries and positional indexes

# Phrase queries

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- We want to be able to answer queries such as “***stanford university***” – as a phrase
- Thus the sentence “*I went to university at Stanford*” is not a match.
  - The concept of phrase queries has proven easily understood by users; one of the few “advanced search” ideas that works
  - Many more queries are *implicit phrase queries*
- For this, it no longer suffices to store only  $\langle \text{term} : \text{docs} \rangle$  entries

# A first attempt: Biword indexes

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- Index every consecutive pair of terms in the text as a phrase
- For example the text “Friends, Romans, Countrymen” would generate the biwords
  - *friends romans*
  - *romans countrymen*
- Each of these biwords is now a dictionary term
- Two-word phrase query-processing is now immediate.

# Longer phrase queries

- Longer phrases can be processed by breaking them down
- ***stanford university palo alto*** can be broken into the Boolean query on biwords:

***stanford university AND university palo AND palo alto***

Without the docs, we cannot verify that the docs matching the above Boolean query do contain the phrase.

Can have false positives!

# Issues for biword indexes

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- False positives, as noted before
- Index blowup due to bigger dictionary
  - Infeasible for more than biwords, big even for them
- Biword indexes are not the standard solution (for all biwords) but can be part of a compound strategy

## Solution 2: Positional indexes

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- In the postings, store, for each ***term*** the position(s) in which tokens of it appear:

<***term***, number of docs containing ***term***;

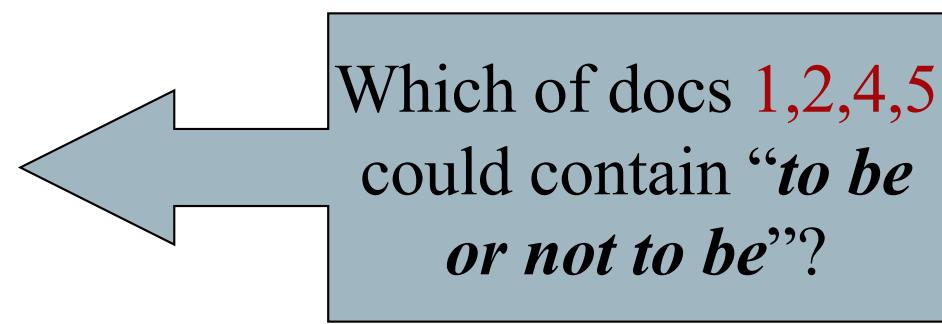
*doc1*: position1, position2 ... ;

*doc2*: position1, position2 ... ;

etc.>

# Positional index example

<**be**: 993427;  
**1**: 7, 18, 33, 72, 86, 231;  
**2**: 3, 149;  
**4**: 17, 191, 291, 430, 434;  
**5**: 363, 367, ...>



Which of docs **1,2,4,5**  
could contain “**to be**  
or **not to be**”?

- For phrase queries, we use a merge algorithm recursively at the document level
- But we now need to deal with more than just equality

# Processing a phrase query

- Extract inverted index entries for each distinct term:  
***to, be, or, not.***
- Merge their *doc:position* lists to enumerate all positions with “***to be or not to be***”.
  - ***to:***
    - 2:1,17,74,222,551; **4:8,16,190,429,433;** 7:13,23,191; ...
  - ***be:***
    - 1:17,19; **4:17,191,291,430,434;** 5:14,19,101; ...
- Same general method for proximity searches

# Proximity queries

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- **LIMIT! /3 STATUTE /3 FEDERAL /2 TORT**
  - Again, here,  $/k$  means “within  $k$  words of”.
- Clearly, positional indexes can be used for such queries; biword indexes cannot.
- Exercise: Adapt the linear merge of postings to handle proximity queries. Can you make it work for any value of  $k$ ?
  - This is a little tricky to do correctly and efficiently
  - See Figure 2.12 of *IIR*

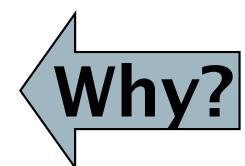
# Positional index size

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- A positional index expands postings storage *substantially*
  - Even though indices can be compressed
- Nevertheless, a positional index is now standardly used because of the power and usefulness of phrase and proximity queries ... whether used explicitly or implicitly in a ranking retrieval system.

# Positional index size

- Need an entry for each occurrence, not just once per document
- Index size depends on average document size
  - Average web page has <1000 terms
  - SEC filings, books, even some epic poems ... easily 100,000 terms
- Consider a term with frequency 0.1%



Document size	Postings	Positional postings
1000	1	1
100,000	1	100

# Rules of thumb

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- A positional index is 2–4 as large as a non-positional index
- Positional index size 35–50% of volume of original text
  - Caveat: all of this holds for “English-like” languages

# Combination schemes

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- These two approaches can be profitably combined
  - For particular phrases (“*Michael Jackson*”, “*Britney Spears*”) it is inefficient to keep on merging positional postings lists
    - Even more so for phrases like “*The Who*”
- Williams et al. (2004) evaluate a more sophisticated mixed indexing scheme
  - A typical web query mixture was executed in  $\frac{1}{4}$  of the time of using just a positional index
  - It required 26% more space than having a positional index alone