TakeHomeAug4

2024-07-23

Take-home #1 (Chapter 2 #10)

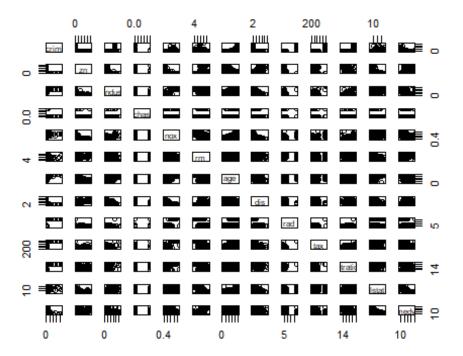
Part A

```
#Access Boston Data
library(ISLR2)
my_data = Boston
#Dimensions of table
rows_columns = dim(my_data)
#Print dimensions
nrow(Boston)
## [1] 506
ncol(Boston)
## [1] 13
```

Answer: 506 rows and 13 variables

Part B

```
#Convert the 'chas' and 'rad' column to numeric type
my_data$chas <- as.numeric(my_data$chas)
my_data$rad <- as.numeric(my_data$rad)
# Create a scatterplot matrix of the variables in the my_data dataframe
pairs(my_data)</pre>
```



Answer: The plot itself doesn't really help us reach any conclusions. What it does tell us is that some variables may be correlated. For example, we can see that crim and dis may seems to have a relationship.

Part C

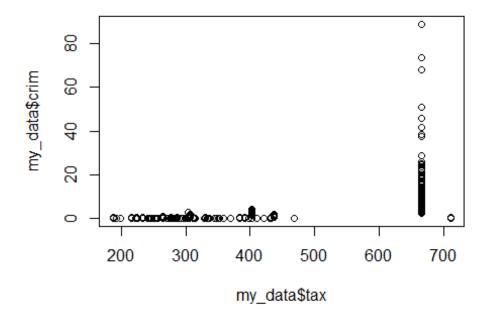
```
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
#Initialize empty lists to store results
i <- character()</pre>
j <- character()</pre>
cor <- numeric()</pre>
p <- numeric()</pre>
#Loop through each variable in the my data
for (var in names(my_data)) {
if (var != "crim") {
```

```
# Calculate correlation and p-value
    test <- cor.test(my_data$crim, my_data[[var]])</pre>
    # Store results
    i <- c(i, "crim")</pre>
    j <- c(j, var)</pre>
    cor <- c(cor, test$estimate)</pre>
    p <- c(p, test$p.value)</pre>
  }
}
#Combine results into a my data
results <- data.frame(i, j, cor, p)
#Display the results
print(results)
##
                           cor
## 1 crim
                zn -0.20046922 5.506472e-06
## 2 crim indus 0.40658341 1.450349e-21
## 3 crim chas -0.05589158 2.094345e-01
## 4 crim
             nox 0.42097171 3.751739e-23
## 5 crim
               rm -0.21924670 6.346703e-07
## 6 crim
## 7 crim
               age 0.35273425 2.854869e-16
               dis -0.37967009 8.519949e-19
## 8 crim
               rad 0.62550515 2.693844e-56
## 9 crim
               tax 0.58276431 2.357127e-47
## 10 crim ptratio 0.28994558 2.942922e-11
## 11 crim
             lstat 0.45562148 2.654277e-27
## 12 crim
              medv -0.38830461 1.173987e-19
```

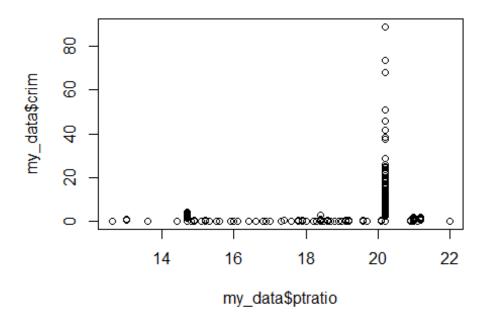
Answer: To see the relationships between the variables and crime rate, I made a correlation matrix with p-values. The correlation matrix shows that there is indeed a relationship between the predictors and crime rate. For example, rad and crim has a correlation coefficient of 0.625 and a really low p-value indicating a strong relationship. Some variables demonstrate a negative correlation too.

Part D

```
#Scatter Plots for tax and ptration against crime
plot(my_data$tax,my_data$crim)
```



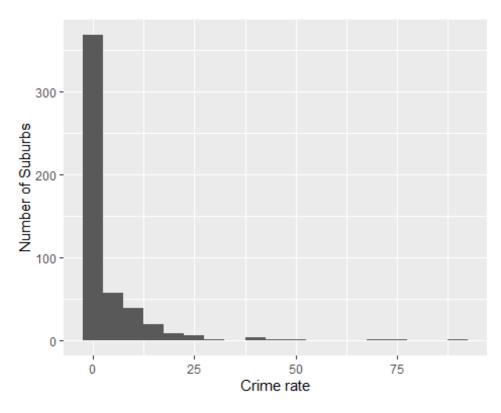
plot(my_data\$ptratio,my_data\$crim)



```
#Ranges Displayed for
range(my_data$tax)
## [1] 187 711
range(my_data$ptratio)
## [1] 12.6 22.0
```

- The range for tax is 187 711 and The range for ptratio is 12.6 22.0
- Particularly the census tracts where tax is 666 and ptratio is 20.2, we see a spike in the range of crime rate. However this does not mean that the areas with the highest tax rate have the highest crime rates. Perhaps because some properties at nicer places have higher tax rates for example comparing NY city to the Hamptons.

```
#Plot Histogram for Crime Rate Across Different Suburbs
library(ggplot2)
qplot(my_data$crim, binwidth=5, xlab= "Crime rate", ylab= "Number of Suburbs")
## Warning: `qplot()` was deprecated in ggplot2 3.4.0.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was ## generated.
```



• From the above figure, we can see that while some neighborhoods have low crime rates, others have extremely high rates. Additionally, given that the median crime

rate is 0.26% and the maximum is 89%, it is evident that certain neighborhoods experience alarmingly high crime rates.

Part E

```
# Census tracts in this data set bound the Charles river
sum(my_data$chas)
## [1] 35
```

Answer: Number of Census Tracts that bound Charles River is 35

Part F

```
#Median pupil-teacher ratio
median(my_data$ptratio)
## [1] 19.05
```

Answer: Median PT ratio is 19.05

Part G

```
#Find the census tract with lowest median value of owner occupied homes
ordered_by_medv <- my_data[order(my_data$medv),]</pre>
ordered_by_medv [1, ]
##
         crim zn indus chas
                                               dis rad tax ptratio lstat
                              nox
                                     rm age
medv
## 399 38.3518 0 18.1
                          0 0.693 5.453 100 1.4896
                                                    24 666
                                                              20.2 30.59
#Find Summary of all columns of data set so we can compare
summary(ordered_by_medv)
##
        crim
                                           indus
                                                            chas
                            zn
## Min.
          : 0.00632
                      Min.
                             : 0.00
                                       Min.
                                              : 0.46
                                                       Min.
                                                              :0.00000
## 1st Qu.: 0.08205
                      1st Qu.: 0.00
                                       1st Qu.: 5.19
                                                       1st Qu.:0.00000
## Median : 0.25651
                      Median: 0.00
                                       Median: 9.69
                                                       Median :0.00000
## Mean
         : 3.61352
                      Mean
                            : 11.36
                                       Mean
                                              :11.14
                                                       Mean
                                                              :0.06917
                                       3rd Qu.:18.10
##
   3rd Qu.: 3.67708
                      3rd Qu.: 12.50
                                                       3rd Ou.:0.00000
## Max.
           :88.97620
                             :100.00
                                              :27.74
                                                       Max.
                                                              :1.00000
                      Max.
                                       Max.
##
                                                          dis
        nox
                          rm
                                         age
## Min.
                                    Min.
           :0.3850
                    Min.
                           :3.561
                                           : 2.90
                                                     Min.
                                                            : 1.130
   1st Ou.:0.4490
                    1st Ou.:5.886
                                    1st Ou.: 45.02
                                                     1st Ou.: 2.100
##
##
   Median :0.5380
                    Median :6.208
                                    Median : 77.50
                                                     Median : 3.207
                                           : 68.57
## Mean
          :0.5547
                    Mean
                           :6.285
                                    Mean
                                                     Mean : 3.795
##
   3rd Qu.:0.6240
                    3rd Qu.:6.623
                                    3rd Qu.: 94.08
                                                     3rd Qu.: 5.188
## Max.
          :0.8710
                    Max.
                           :8.780
                                    Max.
                                           :100.00
                                                     Max.
                                                            :12.127
##
        rad
                         tax
                                       ptratio
                                                        lstat
## Min.
          : 1.000
                           :187.0
                                    Min.
                                         :12.60
                                                         : 1.73
                    Min.
                                                    Min.
## 1st Qu.: 4.000
                    1st Qu.:279.0
                                    1st Qu.:17.40
                                                    1st Qu.: 6.95
## Median : 5.000
                    Median :330.0
                                                    Median :11.36
                                    Median :19.05
## Mean : 9.549
                    Mean :408.2
                                    Mean :18.46
                                                    Mean :12.65
```

```
## 3rd Ou.:24.000
                   3rd Ou.:666.0
                                 3rd Ou.:20.20
                                                3rd Ou.:16.95
                   Max. :711.0
                                 Max. :22.00
## Max.
        :24.000
                                                Max.
                                                      :37.97
       medv
##
## Min. : 5.00
## 1st Qu.:17.02
## Median :21.20
## Mean :22.53
## 3rd Qu.:25.00
## Max. :50.00
```

- Crime is very high(38.35) falling even higher than the third quartile(3.67) when compared to overall range.
- No residential land zones for lots over 25,000 sq.ft.
- Proprotion of non-retail business acres per town is very high falling at just on the third quartile when compared to overall range.
- Suburb 399 does not bound the Charles River.
- Nox is very high (0.693) falling even higher than third third quartile (0.6240) when compared to overall range.
- Rooms per dwelling metric falls under the lower category (5.443), lower than the 1st quartile (5.886).
- One of the highest undefined proportion of owner occupied unit sbuilt prior to 1940 (100).
- Weighted mean of distances to five Boston employment centres falls at one of the lowest (1.486), lower than the 1st quartile (17.02).
- Index of accessibility to radial highways is the highest when compared to the range of the entire data set.
- Full-value property tax rate per \$10,000 is quit high sitting right o the third quartile (666)
- Pupil teacher ration by town is quite high of 20.2 falling on the third quurtile.
- Lower status of population is quite high (30.59), falling above the third quartiel (16.95).
- Median value of owner occupied homes in \$1000s is the lowest in the range (5.00).

Part H

```
#Do Summation given conditions for rooms per dwelling.
sum(my_data$rm > 7) #64
## [1] 64
```

```
sum(my_data$rm > 8) #13
## [1] 13
```

Answer:

- 64 suburbs with rooms per dwelling > 7.
- 13 suburbs with roombs per dwelling > 8.

```
#Find summary for suburbs where rooms per dwelling is greater than 8
summary(filter(my_data, my_data$rm > 8))
##
         crim
                                           indus
                             zn
                                                              chas
##
    Min.
           :0.02009
                      Min.
                              : 0.00
                                       Min.
                                              : 2.680
                                                         Min.
                                                                :0.0000
##
    1st Qu.:0.33147
                      1st Qu.: 0.00
                                       1st Qu.: 3.970
                                                         1st Qu.:0.0000
##
    Median :0.52014
                      Median : 0.00
                                       Median : 6.200
                                                         Median :0.0000
## Mean
           :0.71879
                      Mean
                              :13.62
                                       Mean : 7.078
                                                         Mean
                                                                :0.1538
                                       3rd Qu.: 6.200
##
    3rd Qu.:0.57834
                      3rd Qu.:20.00
                                                         3rd Qu.:0.0000
##
    Max.
           :3.47428
                                              :19.580
                                                         Max.
                      Max.
                              :95.00
                                       Max.
                                                                :1.0000
                                                            dis
##
         nox
                            rm
                                           age
                                                              :1.801
##
    Min.
           :0.4161
                     Min.
                             :8.034
                                      Min.
                                             : 8.40
                                                       Min.
    1st Qu.:0.5040
                     1st Qu.:8.247
                                      1st Qu.:70.40
                                                       1st Qu.:2.288
##
##
   Median :0.5070
                     Median :8.297
                                      Median :78.30
                                                       Median :2.894
##
   Mean
           :0.5392
                     Mean
                             :8.349
                                      Mean
                                              :71.54
                                                       Mean
                                                              :3.430
##
    3rd Ou.:0.6050
                      3rd Ou.:8.398
                                      3rd Ou.:86.50
                                                       3rd Qu.:3.652
##
   Max.
           :0.7180
                     Max.
                             :8.780
                                      Max.
                                              :93.90
                                                       Max.
                                                              :8.907
##
         rad
                           tax
                                         ptratio
                                                           1stat
                                                                            medv
## Min.
                                              :13.00
                                                              :2.47
           : 2.000
                     Min.
                             :224.0
                                      Min.
                                                       Min.
                                                                      Min.
:21.9
## 1st Qu.: 5.000
                     1st Qu.:264.0
                                      1st Qu.:14.70
                                                       1st Qu.:3.32
                                                                      1st
Ou.:41.7
## Median : 7.000
                     Median :307.0
                                      Median :17.40
                                                       Median :4.14
                                                                      Median
:48.3
## Mean
           : 7.462
                     Mean
                             :325.1
                                      Mean
                                              :16.36
                                                       Mean
                                                              :4.31
                                                                      Mean
:44.2
## 3rd Qu.: 8.000
                      3rd Qu.:307.0
                                      3rd Qu.:17.40
                                                       3rd Qu.:5.12
                                                                      3rd
Ou.:50.0
## Max.
           :24.000
                     Max.
                             :666.0
                                      Max.
                                              :20.20
                                                       Max.
                                                              :7.44
                                                                      Max.
:50.0
```

- Mean crime rates when compared to the entire data set is much lower when number of dwellings is more than 8.
- There is a low pupil teacher ratio.
- These properties seem to farther away from the highways perhaps because they are not as near to the the centre of the city. Additionally, there are not a lot of non-retail businesses showing that these areas are residential.
- They are older houses.

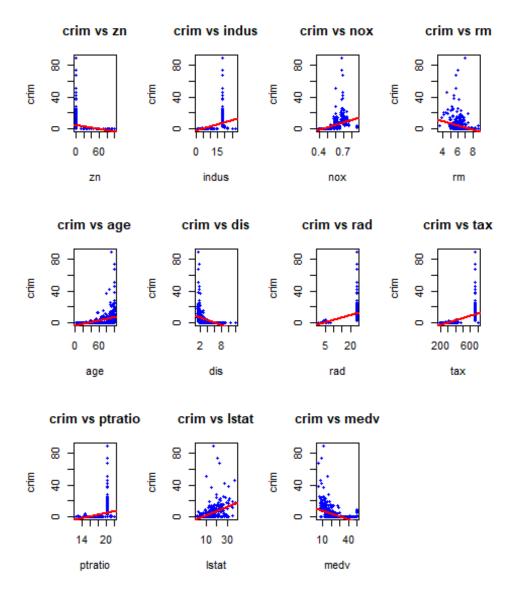
Take-home #2 (Chapter 2 #10)

```
#Access Boston Data
library(ISLR2)
p2_data = Boston
```

Part A

```
#List of all predictors in the dataset except for crim
predictors <- names(Boston)[names(Boston) != "crim"]</pre>
#Initialize an empty list to store the model summaries
model summaries <- list()</pre>
#Fit simple linear regression models for each predictor
for (predictor in predictors) {
  formula <- as.formula(paste("crim ~", predictor))</pre>
  model <- lm(formula, data = Boston)</pre>
  model summaries[[predictor]] <- summary(model)</pre>
}
#Extract significant and non-significant predictors
significant_predictors <- list()</pre>
non_significant_predictors <- list()</pre>
for (predictor in predictors) {
  coef_summary <- coef(model_summaries[[predictor]])</pre>
  p_value <- coef_summary[2, 4] # p-value of the predictor</pre>
  if (p value < 0.05) {
    significant_predictors <- c(significant_predictors, predictor)</pre>
  } else {
    non significant predictors <- c(non significant predictors, predictor)
  }
}
#Display significant and non-significant predictors
significant_predictors
## [[1]]
## [1] "zn"
##
## [[2]]
## [1] "indus"
##
## [[3]]
## [1] "nox"
##
## [[4]]
## [1] "rm"
##
```

```
## [[5]]
## [1] "age"
##
## [[6]]
## [1] "dis"
##
## [[7]]
## [1] "rad"
## [[8]]
## [1] "tax"
##
## [[9]]
## [1] "ptratio"
##
## [[10]]
## [1] "lstat"
##
## [[11]]
## [1] "medv"
non_significant_predictors
## [[1]]
## [1] "chas"
#Set up plot area
par(mfrow = c(2, 4))
#Plot for each significant predictor
for (predictor in significant_predictors) {
  formula <- as.formula(paste("crim ~", predictor))</pre>
  model <- lm(formula, data = Boston)</pre>
  plot(Boston[[predictor]], Boston$crim, main = paste("crim vs", predictor),
       xlab = predictor, ylab = "crim", pch = 20, col = "blue")
  abline(model, col = "red", lwd = 2)
}
```



#Comments: According to the simple regression model the only predictor that does not have a statistically significant relationship with crime is chas (if tract bounds river or not). All other variables seem to have a relationship. The linear lines are present however, it is

clear that it is not a very accurate representation of what is going on because of the residuals.

Part B

```
#Multiple Regression Model with a target variable of Crime
lm.all = lm(crim ~ ., data=p2 data)
summary(lm.all)
##
## Call:
## lm(formula = crim ~ ., data = p2_data)
## Residuals:
##
     Min
            10 Median
                        3Q
                             Max
## -8.534 -2.248 -0.348 1.087 73.923
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 13.7783938 7.0818258 1.946 0.052271
## zn
            0.0457100 0.0187903 2.433 0.015344 *
            -0.0583501 0.0836351 -0.698 0.485709
## indus
## chas
            -0.8253776 1.1833963 -0.697 0.485841
            -9.9575865 5.2898242 -1.882 0.060370 .
## nox
             0.6289107 0.6070924 1.036 0.300738
## rm
## age
            -0.0008483 0.0179482 -0.047 0.962323
## dis
            ## rad
## tax
            -0.0037756   0.0051723   -0.730   0.465757
## ptratio
           0.1388006 0.0757213 1.833 0.067398 .
## lstat
             -0.2200564 0.0598240 -3.678 0.000261 ***
## medv
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 6.46 on 493 degrees of freedom
## Multiple R-squared: 0.4493, Adjusted R-squared: 0.4359
## F-statistic: 33.52 on 12 and 493 DF, p-value: < 2.2e-16
```

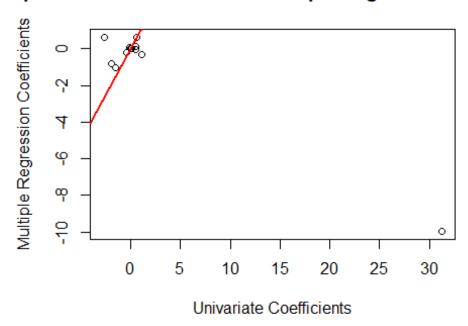
#Comment: According to the table with he p-values listed for each predictor zn, dis, rad, and medv have a p-value lower than 0.05, meaning they are the only variables that demonstrate a statistically significant relationship within the multiple regression model.

Part C

```
#List of all predictors in the dataset except for crim
predictors <- names(Boston)[names(Boston) != "crim"]
#Initialize vectors to store coefficients
univariate_coeffs <- c()</pre>
```

```
#Fit simple linear regression models for each predictor and extract
coefficients
for (predictor in predictors) {
  formula <- as.formula(paste("crim ~", predictor))</pre>
  model <- lm(formula, data = Boston)</pre>
  univariate_coeffs <- c(univariate_coeffs, coef(model)[2])</pre>
}
#Display univariate coefficients
univariate_coeffs
##
            zn
                     indus
                                   chas
                                                nox
                                                                         age
## -0.07393498 0.50977633 -1.89277655 31.24853120 -2.68405122
                                                                  0.10778623
           dis
                       rad
                                            ptratio
                                                           lstat
                                                                        medv
                                    tax
## -1.55090168 0.61791093 0.02974225 1.15198279 0.54880478 -0.36315992
#Fit a multiple regression model including all predictors
multi model <- lm(crim ~ ., data = Boston)</pre>
#Extract coefficients for all predictors (excluding intercept)
multi_coeffs <- coef(multi_model)[-1]</pre>
#Display multiple regression coefficients
multi coeffs
##
                         indus
                                         chas
                                                         nox
##
    0.0457100386 -0.0583501107 -0.8253775522 -9.9575865471 0.6289106622
                                                                   ptratio
##
             age
                            dis
                                          rad
                                                         tax
## -0.0008482791 -1.0122467382 0.6124653115 -0.0037756465 -0.3040727572
##
           lstat
                          medv
  0.1388005968 -0.2200563590
#Plot univariate vs multiple regression coefficients
plot(univariate coeffs, multi coeffs,
     xlab = "Univariate Coefficients",
     ylab = "Multiple Regression Coefficients",
     main = "Comparison of Univariate and Multiple Regression Coefficients")
#Add 45-degree reference line
abline(0, 1, col = "red", lwd = 2)
```

nparison of Univariate and Multiple Regression Coef



Comment: The plot shows that most predictors have similar coefficients in univariate and multiple regression models. However, "nox" (nitrogen oxides concentration (parts per 10 million)) is the only variable that exhibits a large discrepancy. This discrepancy likely results from multicollinearity with other predictors, as indicated by its extreme difference in coefficients.

Part D

```
# List of all predictors in the dataset except for crim
predictors <- names(Boston)[names(Boston) != "crim"]

# Initialize a list to store significant cubic terms
significant_cubic <- list()

# Fit polynomial regression models for each predictor and check for cubic
terms
for (predictor in predictors) {
   formula <- as.formula(paste("crim ~", predictor, "+ I(", predictor, "^2) +
I(", predictor, "^3)"))
   poly_model <- lm(formula, data = Boston)
   coef_summary <- summary(poly_model)$coefficients

# Check if the model includes the cubic term
if (nrow(coef_summary) >= 4) {
    # Extract the p-value for the cubic term (4th row)
    p_value_cubic <- coef_summary[4, 4]</pre>
```

```
if (p value cubic < 0.05) {</pre>
      significant_cubic <- c(significant_cubic, predictor)</pre>
    }
  }
}
# Display predictors with significant cubic terms
significant_cubic
## [[1]]
## [1] "indus"
##
## [[2]]
## [1] "nox"
##
## [[3]]
## [1] "age"
##
## [[4]]
## [1] "dis"
##
## [[5]]
## [1] "ptratio"
##
## [[6]]
## [1] "medv"
```

#"indus", "nox", "age", "dis", "ptratio", "medv" are all the variables that show a non-linear relationship with crime given the cubic polynomial model.

Take-home #3 (Chapter 6 #11)

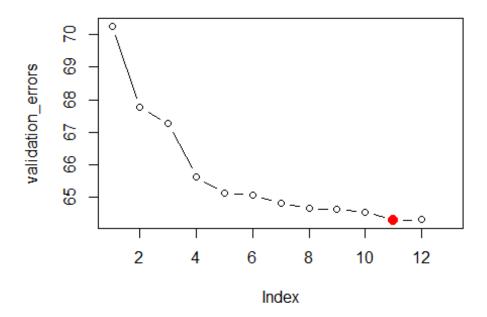
```
#Access Boston Data
library(ISLR2)
p3_data = Boston
summary(p3_data)
##
                                           indus
                                                            chas
        crim
                            zn
                             : 0.00
                                                       Min.
## Min.
          : 0.00632
                      Min.
                                       Min.
                                             : 0.46
                                                               :0.00000
##
   1st Qu.: 0.08205
                      1st Qu.:
                                0.00
                                       1st Qu.: 5.19
                                                       1st Qu.:0.00000
## Median : 0.25651
                      Median : 0.00
                                       Median: 9.69
                                                       Median :0.00000
## Mean
         : 3.61352
                      Mean
                            : 11.36
                                       Mean
                                              :11.14
                                                       Mean
                                                              :0.06917
##
   3rd Qu.: 3.67708
                       3rd Qu.: 12.50
                                        3rd Qu.:18.10
                                                       3rd Qu.:0.00000
           :88.97620
                                              :27.74
                                                       Max.
## Max.
                      Max.
                              :100.00
                                       Max.
                                                               :1.00000
        nox
                                                          dis
##
                           rm
                                         age
## Min.
           :0.3850
                    Min.
                           :3.561
                                    Min.
                                           : 2.90
                                                     Min.
                                                            : 1.130
##
   1st Qu.:0.4490
                     1st Qu.:5.886
                                     1st Qu.: 45.02
                                                     1st Qu.: 2.100
## Median :0.5380
                    Median :6.208
                                    Median : 77.50
                                                     Median : 3.207
```

```
## Mean :0.5547
                   Mean :6.285
                                 Mean : 68.57
                                                Mean : 3.795
## 3rd Qu.:0.6240
                   3rd Qu.:6.623
                                 3rd Qu.: 94.08
                                                 3rd Qu.: 5.188
                                                Max. :12.127
## Max. :0.8710
                  Max.
                         :8.780
                                 Max. :100.00
##
                                    ptratio
                                                   lstat
       rad
                       tax
## Min. : 1.000
                  Min.
                         :187.0
                                 Min.
                                       :12.60
                                               Min. : 1.73
## 1st Qu.: 4.000
                  1st Qu.:279.0
                                 1st Qu.:17.40
                                               1st Qu.: 6.95
## Median : 5.000
                  Median :330.0
                                 Median :19.05
                                               Median :11.36
## Mean : 9.549
                  Mean
                         :408.2
                                 Mean
                                       :18.46
                                               Mean
                                                      :12.65
## 3rd Qu.:24.000
                  3rd Qu.:666.0
                                 3rd Qu.:20.20
                                                3rd Qu.:16.95
## Max.
         :24.000
                  Max. :711.0
                                 Max. :22.00
                                               Max. :37.97
##
       medv
         : 5.00
## Min.
## 1st Qu.:17.02
## Median :21.20
## Mean
        :22.53
## 3rd Qu.:25.00
## Max. :50.00
```

Part A

Linear Model Regularization Method: Best Subset Selection

```
library(leaps)
set.seed(1)
train_set <- sample(1:nrow(p3_data), 0.80 * nrow(p3_data))</pre>
test_set <- setdiff(1:nrow(p3_data), train_set)</pre>
crim_test <- p3_data$crim[test_set]</pre>
#Perform best subset selection on training set
subset_fit <- regsubsets(crim ~ ., data = p3_data, subset = train_set, nvmax</pre>
subset summary <- summary(subset fit)</pre>
#Create the test matrix
test_mat <- model.matrix(crim ~ ., data = p3_data[test_set, ])</pre>
validation errors <- rep(NA, 13)
#Calculate validation errors for each model
for (idx in 1:12) {
    coefficients <- coef(subset_fit, id = idx)</pre>
    predictions <- test mat[, names(coefficients)] %*% coefficients</pre>
    validation_errors[idx] <- mean((p3_data$crim[test_set] - predictions)^2)</pre>
}
#Identify the best model
optimal model <- which.min(validation errors)</pre>
plot(validation_errors, type = 'b')
points(optimal_model, validation_errors[optimal_model], col = "red", cex = 2,
pch = 20
```

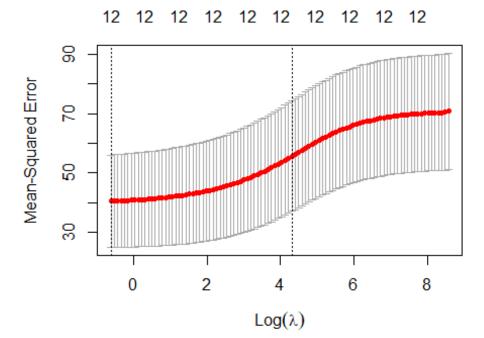


```
subset_mse <- validation_errors[optimal_model]</pre>
subset_rmse <- sqrt(subset_mse)</pre>
#Refit the best subset model on the entire dataset
full_subset_fit <- regsubsets(crim ~ ., data = p3_data, nvmax = 11)</pre>
full_model_coeffs <- coef(full_subset_fit, optimal_model)</pre>
#Display results
cat("Optimal number of predictors:", optimal_model, "\n")
## Optimal number of predictors: 11
cat("Coefficients of the best model:\n")
## Coefficients of the best model:
print(full_model_coeffs)
##
     (Intercept)
                                         indus
                                                         chas
                             zn
##
    13.801555544
                    0.045818028
                                 -0.058345869
                                                -0.828283847 -10.022404078
##
                            dis
                                                          tax
                                                                    ptratio
              rm
                                           rad
##
     0.623650191
                   -1.008539667
                                  0.612822152 -0.003782956 -0.304784434
##
           lstat
                           medv
##
     0.137698956
                   -0.220092318
cat("MSE of the best model:", subset mse, "\n")
## MSE of the best model: 64.2848
```

```
cat("RMSE of the best model:", subset_rmse, "\n")
## RMSE of the best model: 8.01778
```

Linear Model Regularization Method: Ridge Regression

```
library(glmnet)
## Loading required package: Matrix
## Loaded glmnet 4.1-8
#Set seed for reproducibility
set.seed(1)
#Prepare the data
X <- model.matrix(crim ~ ., p3_data)[, -1] # Design matrix (features)</pre>
Y <- p3_data$crim # Response vector (target variable)
# Split the data into training and testing sets
set.seed(4)
training_indices <- sample(1:nrow(p3_data), 0.80 * nrow(p3_data))</pre>
testing_indices <- setdiff(1:nrow(p3_data), training_indices)</pre>
#Fit the Ridge Regression model on the training set
ridge_model <- glmnet(X[training_indices, ], Y[training_indices], alpha = 0)</pre>
#Perform cross-validation to find the best lambda
cv_ridge_model <- cv.glmnet(X[training_indices, ], Y[training_indices], alpha</pre>
= 0)
plot(cv_ridge_model)
```



```
#Optimal Lambda value
optimal_lambda <- cv_ridge_model$lambda.min
cat("Best lambda value for Ridge Regression:", optimal_lambda, "\n")
## Best lambda value for Ridge Regression: 0.5360017</pre>
```

Note that I chose to do cross-validation to optimize hyper-parameter lamda.

```
#Predict on the test set using optimal lambda
ridge_predictions <- predict(ridge_model, s = optimal_lambda, newx =
X[testing_indices, ])
ridge_mse <- mean((ridge_predictions - Y[testing_indices])^2)
ridge_rmse <- sqrt(ridge_mse)

#Display the Ridge Regression Erro Values
cat("MSE for Ridge Regression:", ridge_mse, "\n")

## MSE for Ridge Regression: 51.27786

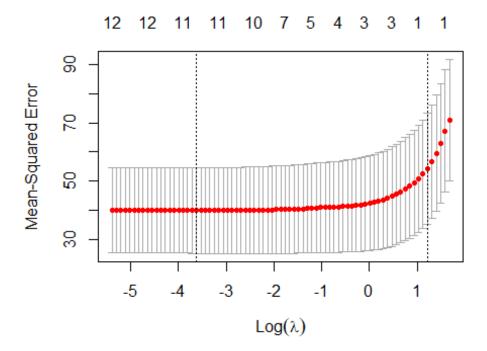
cat("RMSE for Ridge Regression:", ridge_rmse, "\n")

## RMSE for Ridge Regression: 7.160856</pre>
```

Linear Model Regularization Method: Lasso Regression

```
#Fit the Lasso Regression on training set
lasso_model <- glmnet(X[training_indices, ], Y[training_indices], alpha = 1)</pre>
```

```
#Perform cross-validation to find optimal lambda
cv_lasso_model <- cv.glmnet(X[training_indices, ], Y[training_indices], alpha
= 1)
plot(cv_lasso_model)</pre>
```



```
#Optimal Lambda value
optimal_lambda <- cv_lasso_model$lambda.min</pre>
cat("Best lambda value for Lasso Regression:", optimal_lambda, "\n")
## Best lambda value for Lasso Regression: 0.02667693
#Predict on the test set using optimal lambda
lasso_predictions <- predict(lasso_model, s = optimal_lambda, newx =</pre>
X[testing_indices, ])
lasso mse <- mean((lasso predictions - Y[testing indices])^2)</pre>
lasso_rmse <- sqrt(lasso_mse)</pre>
#Get coefficients of the best model
lasso_coefficients <- predict(lasso_model, type = "coefficients", s =</pre>
optimal lambda)[1:13,]
#Results
cat("MSE for Lasso Regression:", lasso_mse, "\n")
## MSE for Lasso Regression: 50.83944
cat("RMSE for Lasso Regression:", lasso rmse, "\n")
```

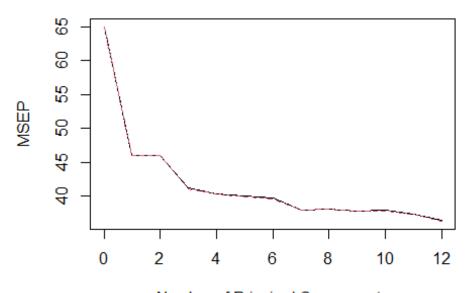
```
## RMSE for Lasso Regression: 7.130178
cat("Number of non-zero coefficients in the best model:",
length(lasso_coefficients[lasso_coefficients != 0]), "\n")
## Number of non-zero coefficients in the best model: 12
cat("Non-zero coefficients in the best model:\n")
## Non-zero coefficients in the best model:
print(lasso coefficients[lasso coefficients != 0])
                                indus
                                            chas
##
  (Intercept)
                       zn
                                                         nox
rm
## 12.179494455 0.041259779 -0.053172489 -0.400995114 -7.128511511
0.376115516
##
                                                       1stat
          dis
                      rad
                                  tax
                                          ptratio
0.206121819
```

Linear Model Regularization Method: Principal Component Regression

```
library(pls)
##
## Attaching package: 'pls'
## The following object is masked from 'package:stats':
##
##
       loadings
#Fit the PCR model on the training set
pcr_model <- pcr(crim ~ ., data = p3_data, subset = train_set, scale = TRUE,</pre>
validation = "CV")
#Summary of PCR model
summary(pcr_model)
## Data:
            X dimension: 404 12
## Y dimension: 404 1
## Fit method: svdpc
## Number of components considered: 12
##
## VALIDATION: RMSEP
## Cross-validated using 10 random segments.
##
          (Intercept) 1 comps 2 comps 3 comps 4 comps 5 comps
                                                                      6 comps
## CV
                8.062
                         6.783
                                   6.782
                                            6.416
                                                     6.351
                                                               6.320
                                                                        6.297
## adjCV
                8.062
                         6.781
                                   6.779
                                            6.411
                                                     6.344
                                                               6.317
                                                                        6.293
##
          7 comps
                   8 comps 9 comps
                                     10 comps 11 comps 12 comps
## CV
                     6.167
                              6.145
                                         6.151
                                                   6.111
                                                              6.029
            6.162
## adjCV
            6.157
                              6.140
                                         6.146
                                                   6.105
                                                              6.022
                     6.163
```

```
##
## TRAINING: % variance explained
         1 comps 2 comps 3 comps 4 comps 5 comps 6 comps 7 comps 8
##
comps
## X
           50.37
                    64.05
                             73.18
                                      80.30
                                               86.59
                                                        90.14
                                                                  92.71
94.86
## crim
           29.85
                    30.02
                             37.77
                                      38.96
                                               39.64
                                                                 42.82
                                                        40.17
43.05
##
         9 comps
                  10 comps 11 comps
                                      12 comps
## X
           96.71
                     98.23
                               99.44
                                        100.00
## crim
           43.45
                     43.53
                               44.50
                                         46.03
validationplot(pcr_model, val.type = "MSEP", main = "PCR Validation", xlab =
"Number of Principal Components")
```

PCR Validation



Number of Principal Components

```
#Make predictions on the test set using the model with 12 components
pcr_predictions <- predict(pcr_model, p3_data[test_set,], ncomp = 12)
pcr_mse <- mean((pcr_predictions - p3_data$crim[test_set])^2)
pcr_rmse <- sqrt(pcr_mse)

#Display the PCR results
cat("MSE for PCR:", pcr_mse, "\n")

## MSE for PCR: 64.30352

cat("RMSE for PCR:", pcr_rmse, "\n")

## RMSE for PCR: 8.018948</pre>
```

Part B

Comparison of Model Errors



Summary of Results Among the 4 models Specified:

```
MSE of the best model: 64.2848 RMSE of the best model: 8.01778

MSE for Ridge Regression: 51.27786 RMSE for Ridge Regression: 7.160856

MSE for Lasso Regression: 50.83944 RMSE for Lasso Regression: 7.130178

MSE for PCR: 64.30352 RMSE for PCR: 8.018948
```

Among the four models considered, Lasso Regression yielded the lowest RMSE, making it the best-performing model for predicting the per capita crime rate in the Boston dataset. The lasso model demonstrated that it can perform variable selection and regularization.

The lower RMSE as compared to the other models shows that it can better manage multicollinearity and prevent overfitting, leading to improved predictive accuracy. Additionaly, this particular model used cross-validation to optimise the hyper-parameter lambda which helped reduce overfitting and improved the robustness of the model. It is to note that Ridge was not very far off and used a similar cross-validation method.

Part C

The Lasso Regression model selected 11 features and the intercept term, excluding age. This may have reduced the complexity of the model to improve interpretability and predictive accuracy by focusing on the more important variables.

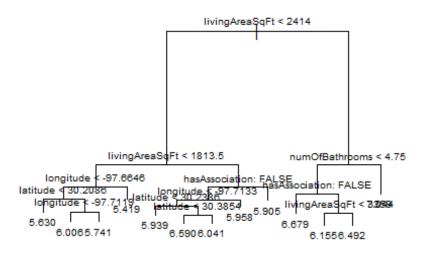
Take-home #4 (Chapter 8 #8)

```
# Load necessary libraries
library(readr)
library(dplyr)
library(tree)
library(rpart)
library(rpart.plot)
library(randomForest)
## randomForest 4.7-1.1
## Type rfNews() to see new features/changes/bug fixes.
## Attaching package: 'randomForest'
## The following object is masked from 'package:ggplot2':
##
##
       margin
## The following object is masked from 'package:dplyr':
##
##
       combine
library(caret)
## Loading required package: lattice
##
## Attaching package: 'caret'
## The following object is masked from 'package:pls':
##
##
       R2
library(BART)
## Loading required package: nlme
```

```
##
## Attaching package: 'nlme'
## The following object is masked from 'package:dplyr':
##
##
       collapse
## Loading required package: survival
##
## Attaching package: 'survival'
## The following object is masked from 'package:caret':
##
##
       cluster
# Load the dataset
#Load in the Austin Housing Data
austin_data <- read_csv('austinhouses.csv',rt)</pre>
## Rows: 6785 Columns: 34
## — Column specification
## Delimiter: ","
## chr (34): X1, X2, X3, X4, X5, X6, X7, X8, X9, X10, X11, X12, X13, X14,
X15, ...
##
## i Use `spec()` to retrieve the full column specification for this data.
## i Specify the column types or set `show_col_types = FALSE` to quiet this
message.
#Set the first row as column names
colnames(austin_data) <- austin_data[1, ]</pre>
austin_data <- austin_data[-1, ]</pre>
rownames(austin data) <- NULL</pre>
# Convert relevant columns to numeric and handle non-numeric values
austin_data <- austin_data %>%
  mutate(
    latestPrice = as.numeric(latestPrice),
    latitude = as.numeric(latitude),
    longitude = as.numeric(longitude),
    hasAssociation = as.factor(hasAssociation), # Assuming this is a
categorical variable
    livingAreaSqFt = as.numeric(livingAreaSqFt),
    numOfBathrooms = as.numeric(numOfBathrooms),
    numOfBedrooms = as.numeric(numOfBedrooms)
  )
```

```
# Check for and handle any NA values
austin_data <- austin_data %>%
  filter(
    !is.na(latestPrice) &
    !is.na(latitude) &
    !is.na(longitude) &
    !is.na(hasAssociation) &
    !is.na(livingAreaSqFt) &
    !is.na(numOfBathrooms) &
    !is.na(numOfBedrooms)
  )
# Add column for log(latestPrice)
austin data <- austin data %>%
  mutate(log latestPrice = log(latestPrice))
# Initialize a data frame to store MSE and RMSE values
results <- data.frame(</pre>
  Model = character(),
 MSE = numeric(),
 RMSE = numeric(),
  stringsAsFactors = FALSE
)
Part A
#Split the data
set.seed(1)
train <- sample(1:nrow(austin_data), 0.8*nrow(austin_data))</pre>
austin_data.train <- austin_data[train, ]</pre>
austin_data.test <- austin_data[-train, ]</pre>
Part B
#Fit regression tree
tree.austin <- tree(log_latestPrice ~ latitude + longitude + hasAssociation +</pre>
livingAreaSqFt + numOfBathrooms + numOfBedrooms,
                     data = austin data.train)
#PLot
plot(tree.austin)
```

text(tree.austin, pretty = 0, cex = 0.6, xpd = NA, offset = 0.5)



```
#Predict on test set
predictions <- predict(tree.austin, newdata = austin_data.test)

#Convert predictions back to price scale
predicted_prices <- exp(predictions)
actual_prices <- austin_data.test$latestPrice

#Calculate MSE and RMSE
tree_mse <- mean((predicted_prices - actual_prices)^2)
tree_rmse <- sqrt(tree_mse)

cat("Test MSE: ", tree_mse, "\n")

## Test MSE: 71405.56

cat("Test RMSE: ", tree_rmse, "\n")

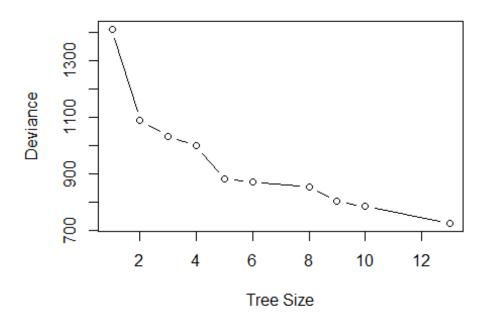
## Test RMSE: 267.2182</pre>
```

Part C

```
#Perform cross-validation to determine the optimal level of tree complexity
cv.austin <- cv.tree(tree.austin, FUN = prune.tree)

#Plot cross-validation results
plot(cv.austin$size, cv.austin$dev, type = "b", xlab = "Tree Size", ylab =
"Deviance", main = "Cross-Validation Results")</pre>
```

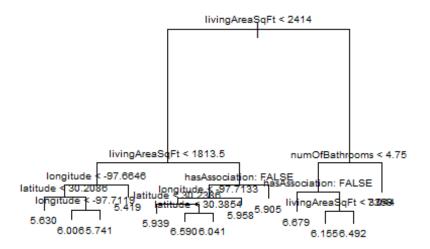
Cross-Validation Results



```
#Find the optimal size for pruning
optimal_size <- cv.austin$size[which.min(cv.austin$dev)]

#Prune the tree to the optimal size
pruned.austin <- prune.tree(tree.austin, best = optimal_size)

#Plot the pruned tree
plot(pruned.austin)
text(pruned.austin, pretty = 0, cex = 0.6, xpd = NA, offset = 0.5)</pre>
```



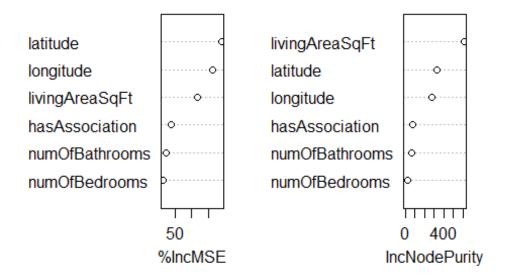
```
#MSE and RMSE for Tree before CV and Pruning
mse original <- mean((predicted prices - actual prices)^2)</pre>
rmse_original <- sqrt(mse_original)</pre>
cat("Original Tree Test MSE: ", tree_mse, "\n")
## Original Tree Test MSE: 71405.56
cat("Original Tree Test RMSE: ", tree_rmse, "\n")
## Original Tree Test RMSE: 267.2182
#Predict on test set using the pruned tree
pruned_yhat <- predict(pruned.austin, newdata = austin_data.test)</pre>
pruned_predicted_prices <- exp(pruned_yhat) # Convert back to price scale</pre>
#Calculate MSE and RMSE for the pruned tree
mse_pruned <- mean((pruned_predicted_prices - actual_prices)^2)</pre>
rmse pruned <- sqrt(mse pruned)</pre>
cat("Pruned Tree Test MSE: ", mse_pruned, "\n")
## Pruned Tree Test MSE: 71405.56
cat("Pruned Tree Test RMSE: ", rmse_pruned, "\n")
## Pruned Tree Test RMSE: 267.2182
```

#Pruning does not improve the TEST MSE. It remains the same.

Part D

```
library(randomForest)
set.seed(1)
bag.austin <- randomForest(log_latestPrice ~ latitude + longitude +</pre>
hasAssociation + livingAreaSqFt + numOfBathrooms + numOfBedrooms,
                            data = austin_data.train,
                            mtry = 6, # Number of predictors
                            importance = TRUE)
#Predict on test set using the bagging model
yhat.bag <- predict(bag.austin, newdata = austin_data.test)</pre>
predicted_prices_bag <- exp(yhat.bag) # Convert back to price scale</pre>
actual_prices <- austin_data.test$latestPrice</pre>
#Calculate MSE and RMSE for the bagging model
mse bag <- mean((predicted prices bag - actual prices)^2)</pre>
rmse_bag <- sqrt(mse_bag)</pre>
#Determine the importance of each variable
importance values <- importance(bag.austin)</pre>
varImpPlot(bag.austin)
```

bag.austin



Comments:

1. **Latitude and Longitude**: - Both latitude and longitude have high %IncMSE and IncNodePurity values, indicating that they are very important predictors in the model. The geographical location of a property significantly impacts its price.

2. Living Area (SqFt):

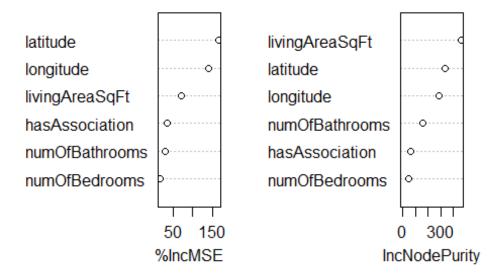
 livingAreaSqFt has the highest IncNodePurity, showing its substantial contribution to reducing node impurity. It's also quite important in terms of %IncMSE, suggesting that larger living areas are closely associated with higher property prices.

Part E

```
#Fit random forest model
set.seed(1)
rf.austin <- randomForest(log latestPrice ~ latitude + longitude +
hasAssociation + livingAreaSqFt + numOfBathrooms + numOfBedrooms,
                          data = austin_data.train,
                          mtry = 3,
                           importance = TRUE)
#Summary
print(rf.austin)
##
## Call:
## randomForest(formula = log latestPrice ~ latitude + longitude +
hasAssociation + livingAreaSqFt + numOfBathrooms + numOfBedrooms,
                                                                         data =
austin_data.train, mtry = 3, importance = TRUE)
##
                  Type of random forest: regression
                        Number of trees: 500
##
## No. of variables tried at each split: 3
##
##
             Mean of squared residuals: 0.07695819
##
                       % Var explained: 70.39
#Predict on test set using the random forest model
yhat.rf <- predict(rf.austin, newdata = austin data.test)</pre>
predicted_prices_rf <- exp(yhat.rf) # Convert back to price scale</pre>
actual prices <- austin data.test$latestPrice</pre>
#Calculate MSE and RMSE for the random forest model
mse_rf <- mean((predicted_prices_rf - actual_prices)^2)</pre>
rmse_rf <- sqrt(mse_rf)</pre>
cat("Random Forest Model Test MSE: ", mse_rf, "\n")
## Random Forest Model Test MSE: 40398.32
cat("Random Forest Model Test RMSE: ", rmse rf, "\n")
## Random Forest Model Test RMSE: 200.9933
```

```
#Determine the importance of each variable
importance values rf <- importance(rf.austin)</pre>
print(importance_values_rf)
##
                    %IncMSE IncNodePurity
## latitude
                  165.12645
                                 332.67981
## longitude
                  139.50568
                                 286.19302
## hasAssociation 36.09719
                                  61.72757
## livingAreaSqFt 69.85699
                                 462.43869
## numOfBathrooms 28.80979
                                 162.82788
## numOfBedrooms
                   17.06917
                                  50.41653
#Plot variable importance
varImpPlot(rf.austin)
```

rf.austin

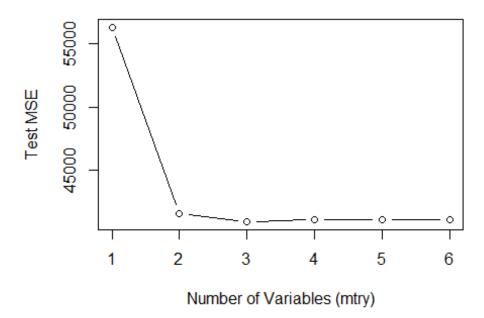


Comments: Geographical location (latitude and longitude) and the living area are the most significant predictors of property prices in Austin. The presence of a homeowners' association and the number of bathrooms also contribute but to a lesser extent. The number of bedrooms is the least important predictor among the variables considered.

```
#Test different values of mtry
set.seed(1)
mtry_values <- c(1, 2, 3, 4, 5, 6)
mse_values <- c()

for (m in mtry_values) {
   rf_model <- randomForest(log_latestPrice ~ latitude + longitude +</pre>
```

Effect of mtry on Test MSE



mytry = 3

Seeing the plot and comparing the RMSE's for mytry = 6 and 3, at mtry = 3, we find the lowest RMSE. This means that the model performed better with a smaller number but only specifically at mytry = 3 of features selected at each node which is interesting. This can improve model accuracy.

```
mytry = 6
Random Forest Model Test MSE: 41019.49 Random Forest Model Test RMSE:
202.5327
```

Random Forest Model Test MSE: 40398.32 Random Forest Model Test RMSE: 200.9933

Part F

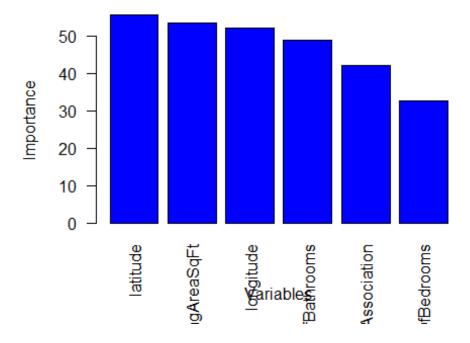
```
#Preparing Data for BART
#Install Bart Package
if (!requireNamespace("BART", quietly = TRUE)) {
  install.packages("BART")
}
#Load Libraries
library(readr)
library(dplyr)
library(BART)
#Load Data
austin_data <- read_csv('austinhouses.csv', rt)</pre>
## Rows: 6785 Columns: 34
## — Column specification
## Delimiter: ","
## chr (34): X1, X2, X3, X4, X5, X6, X7, X8, X9, X10, X11, X12, X13, X14,
X15, ...
##
## i Use `spec()` to retrieve the full column specification for this data.
## i Specify the column types or set `show_col_types = FALSE` to quiet this
message.
#Data set Cleaning
colnames(austin_data) <- austin_data[1, ]</pre>
austin_data <- austin_data[-1, ]</pre>
rownames(austin_data) <- NULL</pre>
austin_data <- austin_data %>%
  mutate(
    latestPrice = as.numeric(latestPrice),
    latitude = as.numeric(latitude),
    longitude = as.numeric(longitude),
    hasAssociation = as.numeric(as.factor(hasAssociation)), # Convert factor
to numeric
    livingAreaSqFt = as.numeric(livingAreaSqFt),
    numOfBathrooms = as.numeric(numOfBathrooms),
    numOfBedrooms = as.numeric(numOfBedrooms)
  )
austin_data <- austin_data %>%
  filter(
    !is.na(latestPrice) &
  !is.na(latitude) &
```

```
!is.na(longitude) &
    !is.na(hasAssociation) &
    !is.na(livingAreaSqFt) &
    !is.na(numOfBathrooms) &
    !is.na(numOfBedrooms)
  )
# Add column for log(latestPrice)
austin_data <- austin_data %>%
  mutate(log_latestPrice = log(latestPrice))
# Split the data according to 80/20 split (80 train 20 test) + set seed to 1
to ensure reproducibility
set.seed(1)
train <- sample(1:nrow(austin_data), 0.8 * nrow(austin_data))</pre>
austin data.train <- austin data[train, ]</pre>
austin_data.test <- austin_data[-train, ]</pre>
# Prepare the data for BART
xtrain <- austin data.train %>% select(latitude, longitude, hasAssociation,
livingAreaSqFt, numOfBathrooms, numOfBedrooms)
ytrain <- austin_data.train$log_latestPrice</pre>
xtest <- austin_data.test %>% select(latitude, longitude, hasAssociation,
livingAreaSqFt, numOfBathrooms, numOfBedrooms)
ytest <- austin_data.test$log_latestPrice</pre>
# Ensure the data is in the correct format
xtrain <- as.data.frame(lapply(xtrain, as.numeric))</pre>
xtest <- as.data.frame(lapply(xtest, as.numeric))</pre>
# Fit the BART model
set.seed(1)
bartfit <- gbart(xtrain, ytrain, x.test = xtest)</pre>
## *****Calling gbart: type=1
## *****Data:
## data:n,p,np: 5427, 6, 1357
## y1,yn: 0.455933, -0.105536
## x1,x[n*p]: 30.341196, 2.000000
## xp1,xp[np*p]: 30.488775, 3.000000
## *****Number of Trees: 200
## *****Number of Cut Points: 100 ... 8
## *****burn,nd,thin: 100,1000,1
## *****Prior:beta,alpha,tau,nu,lambda,offset:
2,0.95,0.130101,3,0.027687,6.05878
## ****sigma: 0.377010
## *****w (weights): 1.000000 ... 1.000000
## *****Dirichlet:sparse,theta,omega,a,b,rho,augment: 0,0,1,0.5,1,6,0
## *****printevery: 100
##
## MCMC
```

```
## done 0 (out of 1100)
## done 100 (out of 1100)
## done 200 (out of 1100)
## done 300 (out of 1100)
## done 400 (out of 1100)
## done 500 (out of 1100)
## done 600 (out of 1100)
## done 700 (out of 1100)
## done 800 (out of 1100)
## done 900 (out of 1100)
## done 1000 (out of 1100)
## time: 61s
## trcnt, tecnt: 1000, 1000
# Print the model summary
summary(bartfit)
##
                   Length Class
                                     Mode
                                     numeric
## sigma
                      1100 -none-
## yhat.train
                  5427000 -none-
                                     numeric
                1357000 -none-
## yhat.test
                                     numeric
                 6000 -none-
## varcount
                                     numeric
## varprob
                    6000 -none-
                                     numeric
## treedraws
                         2 -none-
                                     list
## proc.time
                         5 proc time numeric
                         1 -none-
                                     logical
## hostname
## yhat.train.mean 5427 -none-
                                     numeric
## sigma.mean
                         1 -none-
                                     numeric
## LPML
                         1 -none-
                                     numeric
## yhat.test.mean 1357 -none-
                                     numeric
## ndpost
                       1 -none-
                                     numeric
## offset
                       1 -none-
                                     numeric
## varcount.mean
                       6 -none-
                                     numeric
## varprob.mean
                         6 -none-
                                     numeric
## rm.const
                         6 -none-
                                     numeric
#Predict on test set using BART
yhat.bart <- bartfit$yhat.test.mean</pre>
predicted_prices_bart <- exp(yhat.bart) # Convert back to price scale</pre>
actual_prices <- exp(ytest) # Convert back to price scale</pre>
#MSE and RMSE
mse_bart <- mean((predicted_prices_bart - actual_prices)^2)</pre>
rmse_bart <- sqrt(mse_bart)</pre>
cat("BART Model Test MSE: ", mse_bart, "\n")
## BART Model Test MSE: 42308.27
cat("BART Model Test RMSE: ", rmse bart, "\n")
```

```
## BART Model Test RMSE: 205.6897
#Importance
ord <- order(bartfit$varcount.mean, decreasing = TRUE)</pre>
variable_importance <- bartfit$varcount.mean[ord]</pre>
#Print Statement
cat("Variable Importance (sorted): \n")
## Variable Importance (sorted):
print(variable_importance)
##
         latitude livingAreaSqFt
                                       longitude numOfBathrooms hasAssociation
##
           55.591
                          53.406
                                          52.052
                                                          48.882
##
   numOfBedrooms
           32.624
##
# Plot variable importance
barplot(variable_importance, main = "Variable Importance for BART Model",
        xlab = "Variables", ylab = "Importance",
        names.arg = names(variable_importance), las = 2, col = "blue")
```

Variable Importance for BART Model



Take-home #5 (Chapter 8 #8)

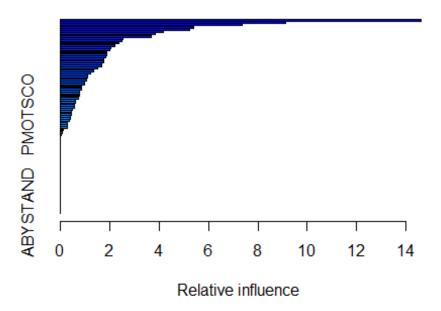
Part A

```
#Load Libraries
library(ISLR)
##
## Attaching package: 'ISLR'
## The following objects are masked from 'package:ISLR2':
##
      Auto, Credit
##
library(dplyr)
p5_data <- Caravan
#Data Cleaning and Adjustments
p5_data <- p5_data %>%
  mutate(Purchase = ifelse(Purchase == "Yes", 1, 0))
# Create a training set consisting of the first 1,000 observations
p5_train <- p5_data %>% slice(1:1000)
# Create a test set consisting of the remaining observations
p5 test <- p5 data %>% slice(1001:n())
```

Part B

```
library('gbm')
## Loaded gbm 2.2.2
## This version of gbm is no longer under development. Consider transitioning
to gbm3, https://github.com/gbm-developers/gbm3

boost_model <- gbm(Purchase ~ ., data = p5_train, distribution = "bernoulli",
n.trees = 1000, shrinkage = 0.01)
## Warning in gbm.fit(x = x, y = y, offset = offset, distribution =
distribution,
## : variable 50: PVRAAUT has no variation.
## Warning in gbm.fit(x = x, y = y, offset = offset, distribution =
distribution,
## : variable 71: AVRAAUT has no variation.
summary(boost_model)[1:10, ]</pre>
```



```
##
                 var
                       rel.inf
## PPERSAUT PPERSAUT 14.608460
## MKOOPKLA MKOOPKLA 9.124212
## MOPLHOOG MOPLHOOG 7.357535
## MBERMIDD MBERMIDD 5.409960
## PBRAND
              PBRAND 5.239352
## MGODGE
              MGODGE 4.192046
## ABRAND
              ABRAND 3.850228
## MINK3045 MINK3045
                     3.704873
## MOSTYPE
            MOSTYPE 2.536196
## PWAPART
            PWAPART
                     2.514622
```

Comment: The table shows the top 10 predictors with the highest relative influence of different for predicting the Purchase. PPERSAUT is at the top with a 14.48 relative influence.

Part C

```
#Predict the response on test data
predicted_probabilities <- predict(boost_model, p5_test, n.trees = 1000, type
= "response")
predicted_labels <- ifelse(predicted_probabilities > 0.2, 1, 0)

#Confusion matrix
confusion_matrix_boost <- table(p5_test$Purchase, predicted_labels)
#Calculate precision for boosting model
precision_boost <- confusion_matrix_boost[2, 2] /</pre>
```

```
sum(confusion matrix boost[, 2])
#Calculate sensitivity for boosting model
sensitivity_boost <- confusion_matrix_boost[2, 2] /</pre>
sum(confusion_matrix_boost[2, ])
print(confusion matrix boost)
##
      predicted labels
##
##
             112
     0 4421
     1 257
##
              32
cat("Boosting Model Precision:", precision_boost, "\n")
## Boosting Model Precision: 0.2222222
cat("Boosting Model Sensitivity:", sensitivity_boost, "\n")
## Boosting Model Sensitivity: 0.1107266
#Fit logistic regression model for comparison
logistic_model <- glm(Purchase ~ ., data = p5_train, family = binomial)</pre>
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
#Predict response on test data using logistic regression
logistic_probabilities <- predict(logistic_model, p5_test, type = "response")</pre>
## Warning in predict.lm(object, newdata, se.fit, scale = 1, type = if (type
## prediction from rank-deficient fit; attr(*, "non-estim") has doubtful
cases
logistic_labels <- ifelse(logistic_probabilities > 0.2, 1, 0)
#Create confusion matrix for logistic regression
confusion_matrix_logistic <- table(p5_test$Purchase, logistic_labels)</pre>
#Calculate precision for logistic regression
precision_logistic <- confusion_matrix_logistic[2, 2] /</pre>
sum(confusion_matrix_logistic[, 2])
#Calculate sensitivity for logistic regression
sensitivity logistic <- confusion matrix logistic[2, 2] /
sum(confusion_matrix_logistic[2, ])
print(confusion_matrix_logistic)
##
      logistic labels
##
     0 4183 350
##
     1 231
##
              58
```

```
cat("Logistic Regression Precision:", precision_logistic, "\n")
## Logistic Regression Precision: 0.1421569
cat("Logistic Regression Sensitivity:", sensitivity_logistic, "\n")
## Logistic Regression Sensitivity: 0.200692
```

Comments:

Boosting model has higher precision (21.12%) and lower sensitivity (11.76%) compared to logistic regression with lower precision (14.22%) and higher sensitivity (20.07%). Boosting model is more accurate when it predicts a purchase, but the logistic regression model is better at identifying actual purchasers. There is a trade off in this case because the choice between models depends on whether minimizing false positives (boosting) or maximizing the detection of actual purchasers where logistic regression may apply better.

Group Project Contribution:

In the group project, I was responsible for building the KNN classification model. Aside from this I also did a little bit of exploratory analysis to find out what variables were correlated with each other – I helped with the heat map. Besides programming, I was present in the meetings and maintained communication over slack and the groupchat.