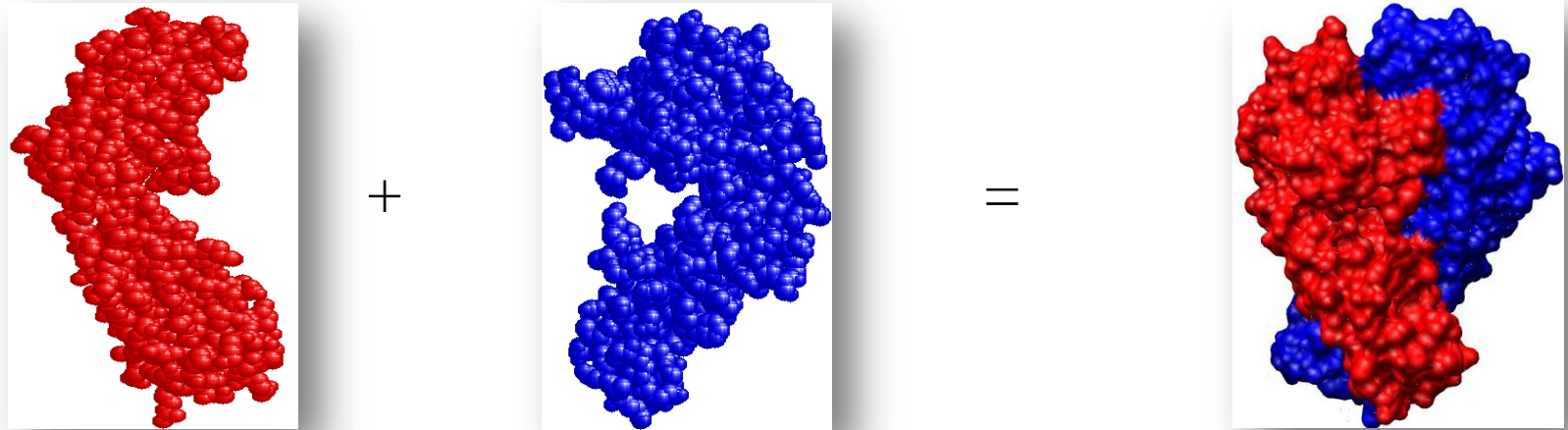


Lecture 13

Protein-protein Docking

Protein-Protein Docking

Ab initio **Protein-protein docking** is the determination of the molecular structure of *complexes* formed by two or more proteins without the need for *experimental* measurement.

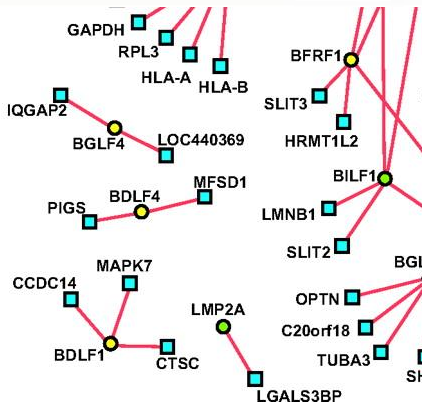
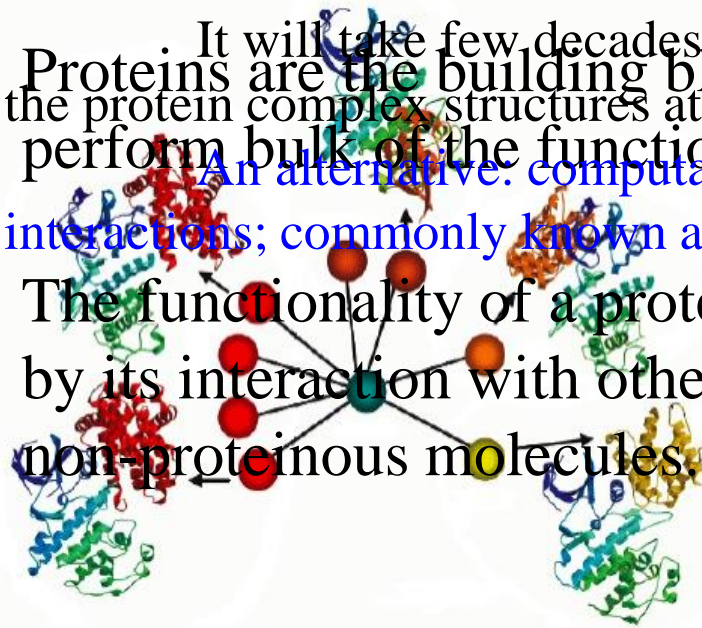


Background

It will take few decades to experimentally determine all the protein complex structures at atomic level resolution.

An alternative: computational modeling of protein-protein interactions; commonly known as protein-protein docking.

The functionality of a protein is determined by its interaction with other proteinous or non-proteinous molecules.



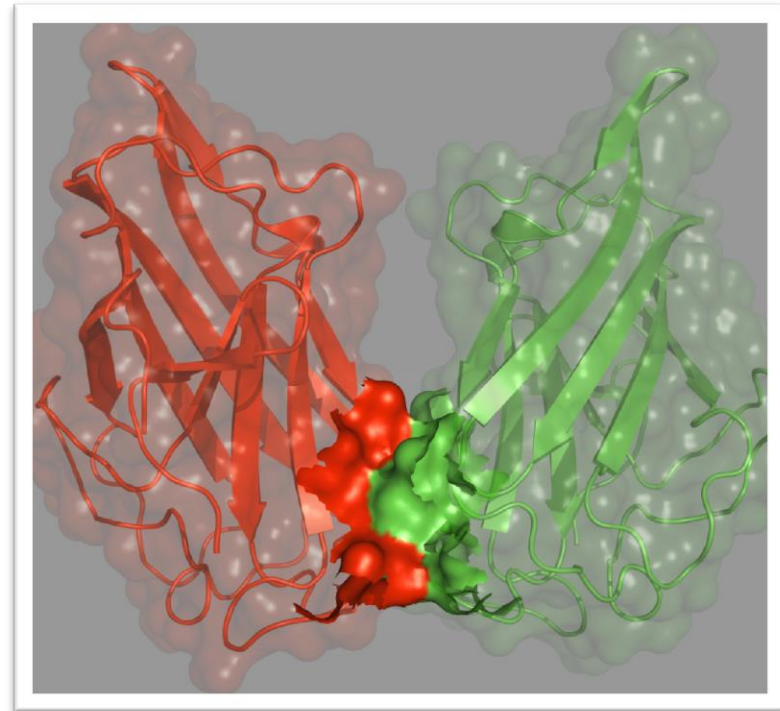
Epstein-Barr virus(

Aloy et al. (2004). *Nat. Biotechnology*

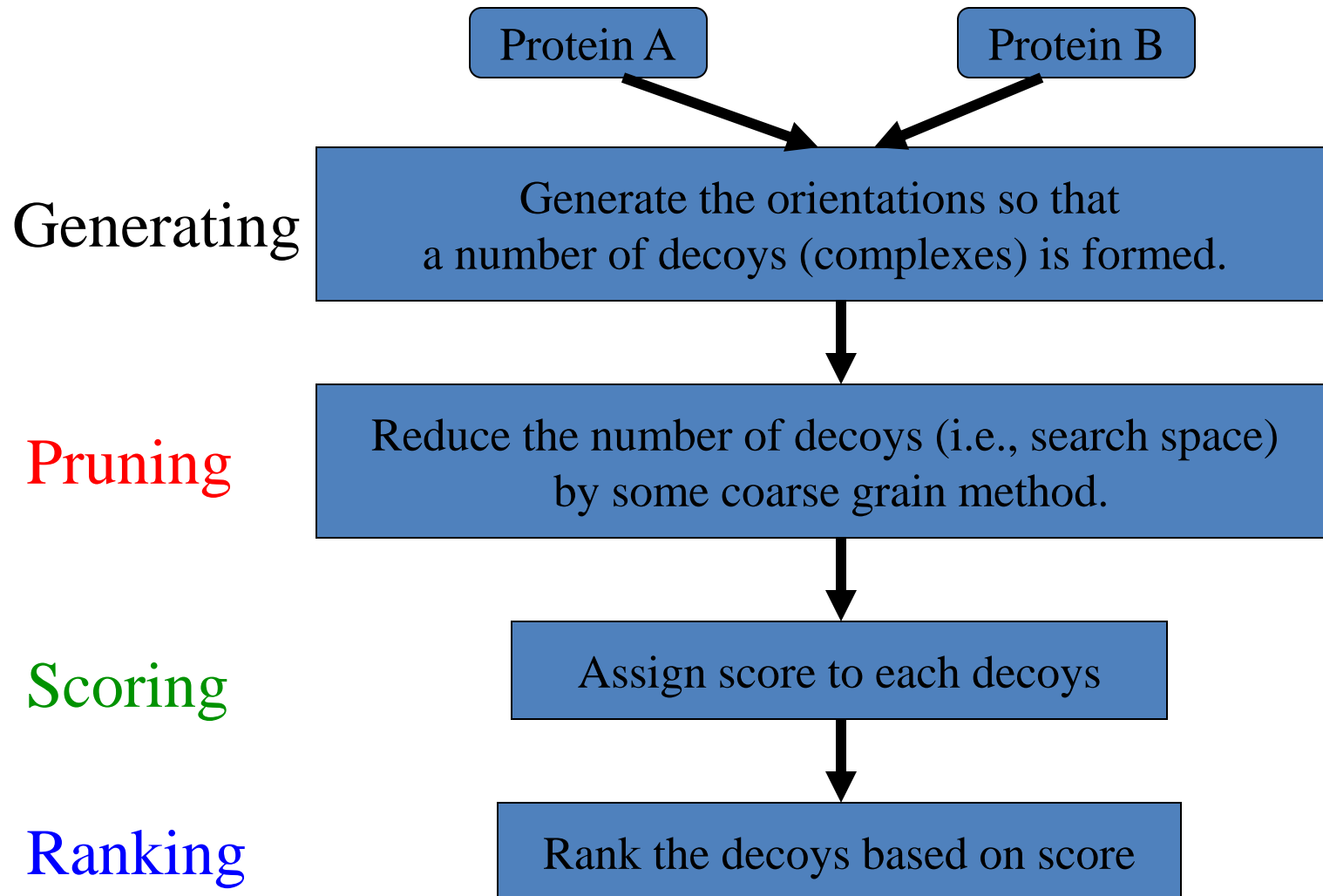
Calderwood M A et al. (2007) *PNAS* **104**, 7606-7611.

Protein Interaction

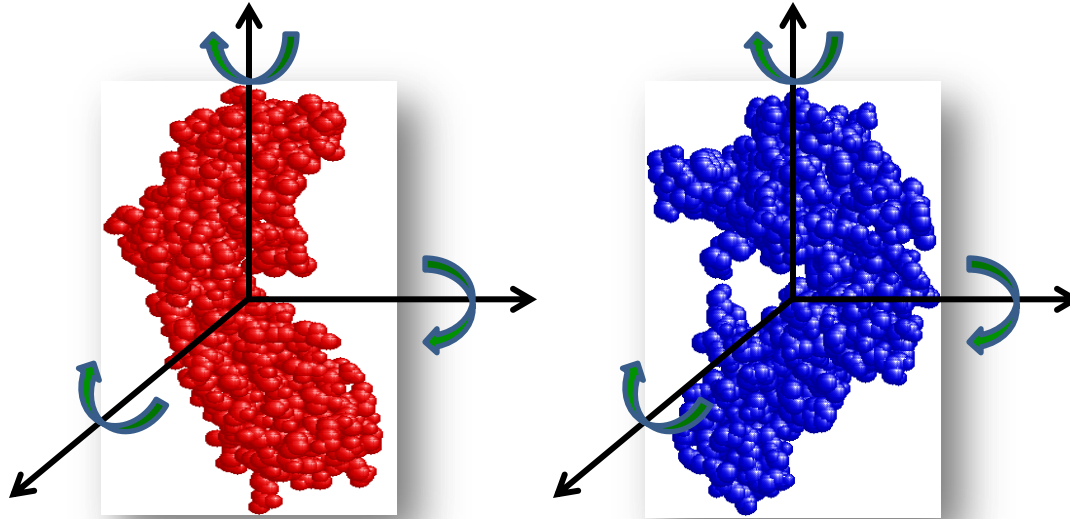
- Identify the interacting surface for two given protein molecules.
 - To model the protein complex structure formed out of two protein molecules – protein-protein docking



Docking Strategy



Generation methods



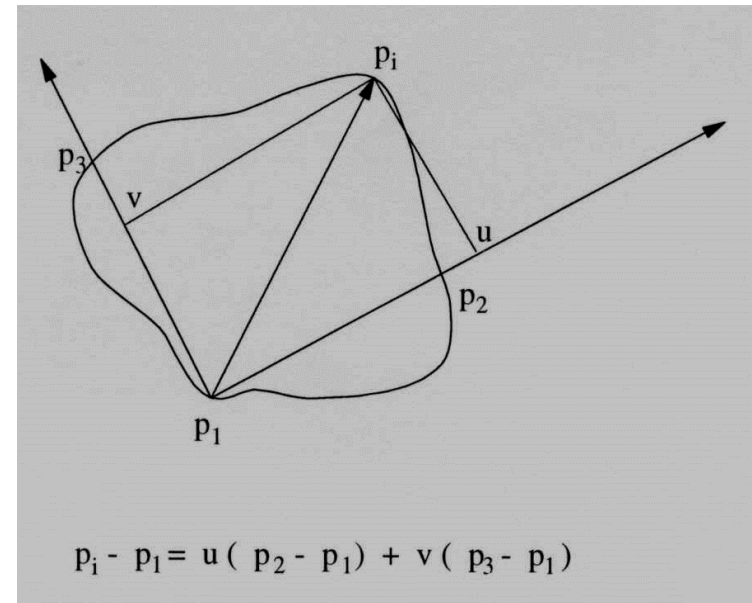
- Tagline – “Higher the decoys; better the possibility of having a hit”
- How many is good?
- Move to discrete space

Geometric Hashing

- Models are represented in a redundant affine invariant way and stored in a table (off-line).
- Hashing is used for organizing and searching the table.

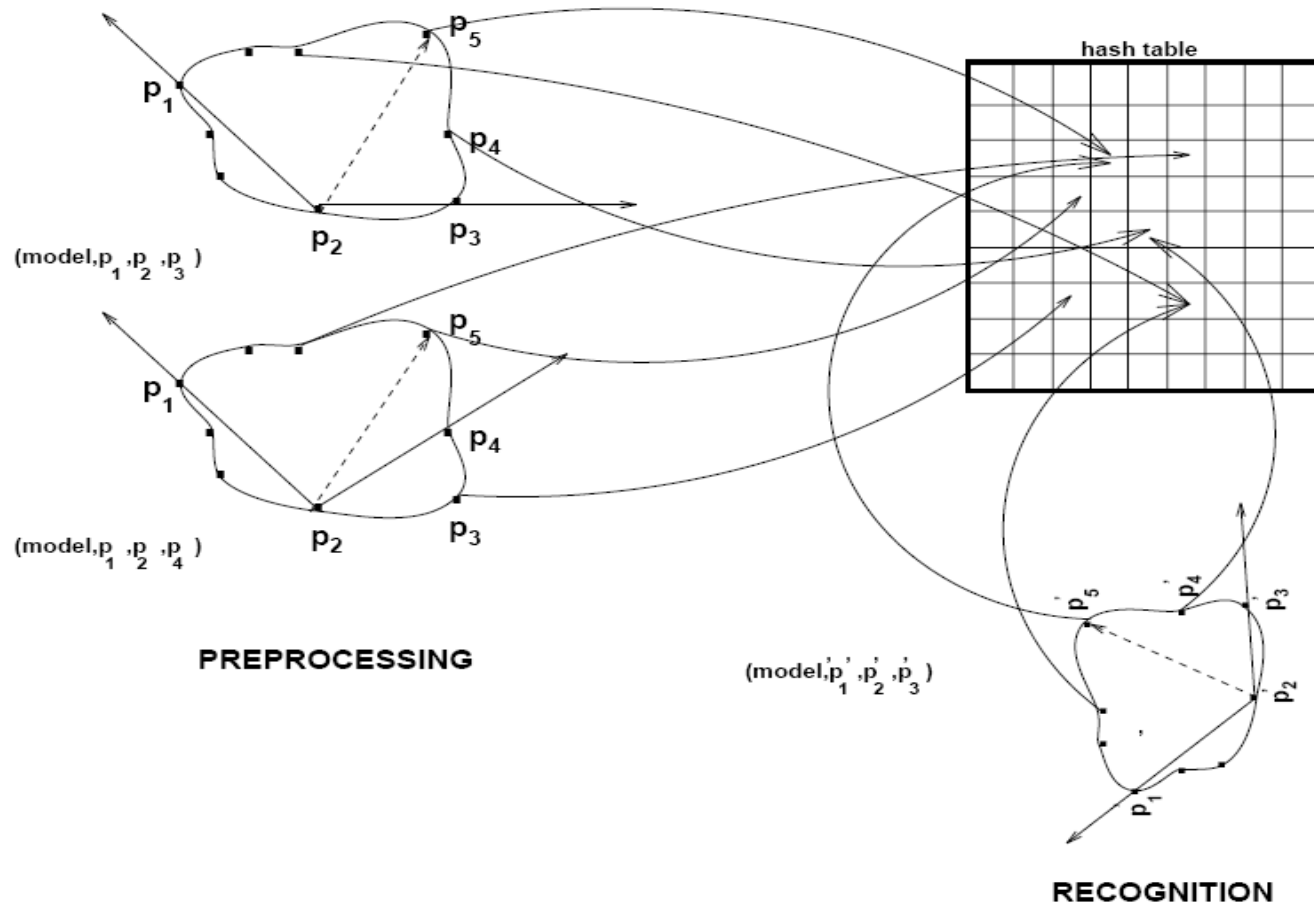
Affine Invariants

- Each triplet of non-collinear model points forms a basis of a coordinate system that is invariant under affine transformations.
- Represent model points in an affine invariant way by rewriting them in terms of this coordinate system.

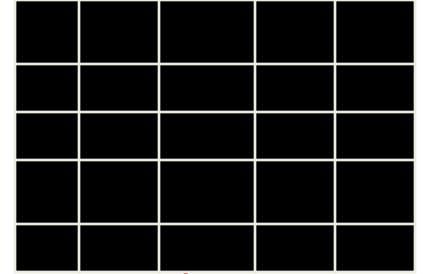


(u, v) are affine invariant!

Preprocessing and Recognition



Preprocessing Step

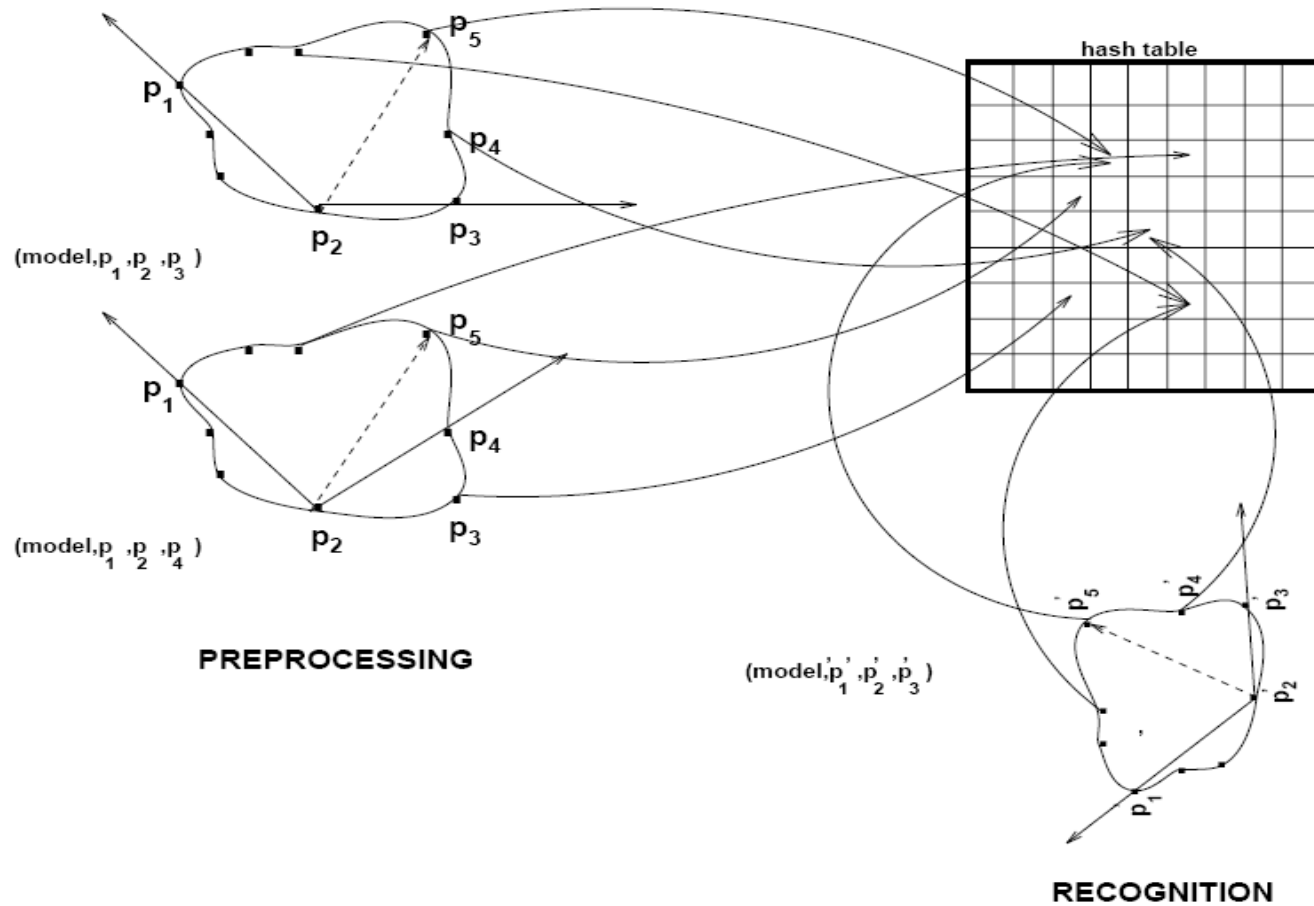


For each model do:

- (1) Extract model's point features.
- (2) For each ordered set of three, non-collinear, points (p_1, p_2, p_3)
 - (a) Compute the coordinates (u, v) of the remaining features in the coordinate frame defined by the model basis (p_1, p_2, p_3)
 - (b) After a proper quantization, use the computed coordinates (u, v) as an index to a two dimensional hash table, and record in the corresponding hash table bin the information $(\text{model}, (p_1, p_2, p_3))$

Hash Function: $h(Q(u), Q(v)) \rightarrow$

Preprocessing and Recognition



Recognition Step

- (1) Extract the image point features
- (2) Choose an arbitrary ordered pair (p'_1, p'_2, p'_3)
- (3) Compute the coordinates (u', v') , of the remaining feature points in the coordinate frame defined by the image basis (p'_1, p'_2, p'_3)
- (4) After quantization, use the computed coordinates as an index to the hash table. For every entry $(\text{model}, (p_1, p_2, p_3))$ found in the corresponding bin, cast a vote.

Recognition Step (cont'd)

(5) Histogram all the hash table entries that received one or more votes. Determine those entries that received more than a certain number of votes -- each such entry corresponds to a potential match (*hypothesis generation*).

(6) For each potential match, consider all the model-image feature pairs which voted for a particular entry, and recover the affine transformation **A** that results in the best least-squares match between all the corresponding feature points.

Recognition Step (cont'd)

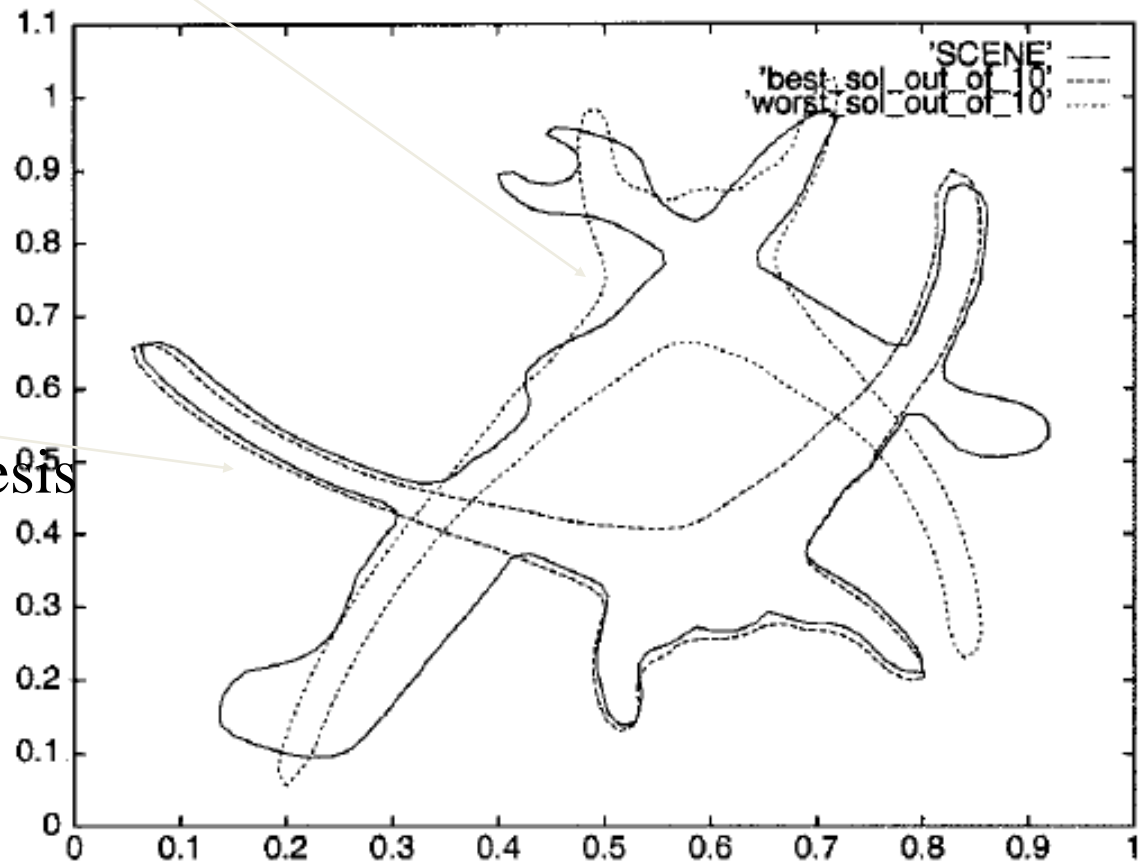
(7) Map the model onto the image using the computed transform and compare the model edges with the image edges (verification step).

(8) If the verification fails for all the models computed in step (5), go back to step (2) and repeat the procedure using a different image basis.

Recognition Example

Bad hypothesis

Good hypothesis



Complexity

- Preprocessing Step:

$$O(Mm^4)$$

- Recognition Step:

worst case: $O(i^4Mm^4)$

(M: #models, m: #model points, i: #scene points)

Geometric Hashing

❖ Pro:

- ❖ Faster

❖ Con:

- ❖ Storage requirement is very high and increases with the increase in object points.
- ❖ Proper identification of object points are crucial for the success.