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**Algorithms-1 - CS21003**  
**(Class Test IV)**  
**Date: 18 – November – 2021**

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Maximum marks: 30

Duration: 1 hour

**File naming convention: e.g., 18CS3004\_G3\_CT4.pdf (or any other extension for images).**

**In case of multiple files, use \_1, \_2 etc at the end.**

**Submission is via Google form only. Email submissions will NOT be accepted. Please manage your time well keeping in mind that Internet and power disruptions are a new normal!**

**No clarifications from the TAs today. You can make any assumption as long as it is rational and you clearly state the same while solving the problem.**

**Plagiarism, in any form (including Internet source) will be severely penalized.**

**Whenever pseudocodes are asked, you can write C/C++ style code/pseudocode**

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### Question 1

Design an algorithm that takes a graph  $G$  as input with two specified vertices  $s$  and  $t$  and a positive integer  $k$  and computes the number of paths containing exactly  $k$  edges. For this particular problem a path is allowed to have vertex repetitions. The algorithm should have a run time of  $O(k(|V| + |E|))$  or better for full credit. Write a C/C++ style pseudocode.

[10 marks]

### Question 2

Consider a hash table of size 7 using a hash function  $h(x) = x \bmod 7$ . Draw the hash table if the following elements are inserted in order {19, 26, 13, 48, 17} and the following collision handling techniques are used:

- (a) Chaining
- (b) Linear probing
- (c) Double hashing where the second hash function  $h_2(x) = 5 - x \bmod 5$

[1+1.5+2.5=5 marks]

### Question 3

Answer the following questions with brief justifications.

- (a) True or False: There is an algorithm to convert max heap to a BST with  $O(n)$  worst-case time complexity.
- (b) True or False: Suppose there is a nearly complete binary tree with  $l$  levels, and you have an  $O(1)$  access to the first (leftmost) element at each level. It is possible to find the second minimum element with  $O(1)$  worst-case time complexity.
- (c) You are given marks for  $n$  students. You have a simple grading scheme with 5 levels, and you want to divide the students into 5 equal sets such that all students in one set can be assigned the same grade. Assuming that the marks for each student are distinct and  $n$  is divisible by 5, can you give a worst-case linear time algorithm? Provide a brief pseudocode.
- (d) You are given marks for  $n$  students in the range 0 to  $k$ . A popular query that you face is as follows: How many students got marks in the range  $[x, y]$ ? This query may arrive multiple times and you want a worst-case  $O(1)$  solution. If you are allowed to pre-process the input in  $O(\max(n, k))$  time, is there a way you can solve this problem? Briefly explain your solution.

[2+2+3+3=10 marks]

#### Question 4

You are given a complete binary tree with  $n$  nodes. Each node of the tree stores a distinct string. You want to find out if there is a node  $u$  in the tree that comes before in the lexicographical ordering, than all its neighbors. A neighbor implies nodes connected to it via a direct edge. Assuming all nodes contain distinct strings, can you solve this problem by looking at (only using the values of)  $O(\log n)$  nodes? If yes, provide a brief C/C++ style pseudocode. If no, justify why it is not possible.

[5 marks]