

Note: Your PAR (both initial and final drafts) must be typed in \LaTeX .

Problem Statement

1. Is there a linear transformation \mathcal{T} such that $\mathcal{T}(\langle 1, 1 \rangle) = \langle 1, 2 \rangle$ and $\mathcal{T}(\langle 3, 2 \rangle) = \langle 2, 4 \rangle$? Either give a matrix for such a transformation, or explain why there isn't one.
2. Is there a linear transformation \mathcal{R} such that $\mathcal{R}(\langle 1, 2 \rangle) = \langle 1, 1 \rangle$, and $\mathcal{R}(\langle 2, 4 \rangle) = \langle 3, 2 \rangle$? Either give a matrix for such a transformation, or explain why there isn't one.
3. If you answered "yes" to either of the above questions, are there other linear transformations that do the same thing? Give an example, or explain why there aren't.

Suppose $\{v_1, v_2, v_3\}$ is a linearly independent set, and $\{w_1, w_2, w_3\}$ is a linearly dependent set in \mathbb{R}^3 .

4. Is there a linear transformation \mathcal{P} such that $\mathcal{P}(v_i) = w_i$ for $i = 1, 2, 3$?
5. Is there a linear transformation \mathcal{Q} such that $\mathcal{Q}(w_i) = v_i$ for $i = 1, 2, 3$?

For problems 4 and 5, PROVE your answer! (Hint: You will need to use the definition of a linear transformation.)

\LaTeX note: To make fancy script letters, add the line `\usepackage{amsfonts}` to your preamble, and use the command `\mathcal{T}`, for example. (Once you've loaded this package, you can play around with other fun fonts like `\mathbb{b}` and `\mathfrak{f}`, too.)

Reflection

Turn the page and check off the icons for things you think you did well; circle the icons for things you would like feedback on.

Suggestions

Communication

Strengths



Show All Steps



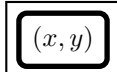
Explain Why,
Not Just What



Avoid Pronouns



Use Correct
Definitions



Define Variables,
Units, etc.

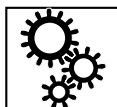


Create Diagrams

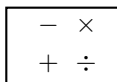
Suggestions

Accuracy

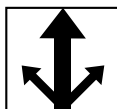
Strengths



Correct Setup



Accurate Calculations



Solve Multiple Ways



Answer Reasonable



Other
(Write Below)