

Before next class:

- **Watch videos 10.2**

Sphere

You know the formula for the volume of a sphere with radius R . Now you are able to prove it!

- (A) Write an equation for the circle with radius R centered at $(0, 0)$.
- (B) If you rotate this circle around the x -axis, it will produce a sphere. Compute its volume as an integral by slicing it like a carrot.

Pyramid

Compute the volume of a pyramid with height H and square base with side length L .

Hint: Slice the pyramid like a carrot with cuts parallel to the base.

Many axis of rotation

Let R be the region in the first quadrant bounded between the curves with equations $y = x^3$ and $y = \sqrt{32x}$.

Compute the volume of the solid of revolution obtained by rotating R around...

- (A) ... the x -axis
- (B) ... the y -axis
- (C) ... the line $y = -1$

Before next class:

- **Watch videos 11.1, 11.2**

Doughnut

Let R be the region inside the curve with equation

$$(x - 1)^2 + y^2 = 1.$$

Rotate R around the line with equation $x = 4$. The resulting solid is called a *torus*.

- (A) Draw a picture and convince yourself that a torus looks like a doughnut.
- (B) Set up the volume of the torus as an integral using x as the variable (“cylindrical shell method”). You do not need to compute the integral.
- (C) Set up the volume of the torus as an integral using y as the variable (“carrot method”). You do not need to compute the integral.

Challenge

Two cylinders have the same radius R and their axes are perpendicular. Find the volume of their intersection.

Hint: You can slice the resulting solid by parallel cuts in three different directions. One of the three makes the problem much, much simpler than the other two.