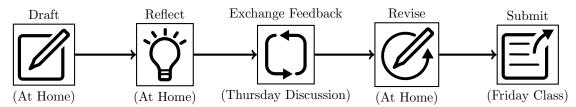
## The PAR Process



Note: Your PAR (both initial and final drafts) must be typed in IATEX.

## **Problem Statement**

Recall the setup from PAR 1. The newly-appointed queen of a newly-discovered land hires three explorers to map her territory: Emily, Jack, and Lila. The explorers have their own equipment and their own quirks.

Jack Jack has a miscalibrated compass—it is off by 45°. When Jack thinks he's walking east, he is actually walking due northeast. When Jack walks in what he thinks is a cardinal direction, he measures distance accurately.

Emily Emily is a careful explorer with an accurate compass. When Emily measures distance in a cardinal direction, it too is accurate.

Lila Lila is an excitable explorer. Her compass is accurate, but when she walks north, she skips and twirls. As a consequence, when Lila walks north, the distance she thinks she travels is *half* the distance she actually traveled.

Further, each explorer only walks in what they think are cardinal directions (i.e., north, east, south, and west). The queen declares that her palace is the center of the nation and that all measurements be made relative to her palace. She then sends the explorers on their way.

With the framework of linear transformations and bases, we have a more powerful framework to analyze this problem.

- 1. Find transformations  $S_J$ ,  $S_E$  and  $S_L$  that convert Jack, Emily, and Lila's coordinates into true coordinates. Are these transformations linear transformations?
  - Hint 1: remember, a transformation is a function from vectors to vectors. A matrix can give a transformation, but a matrix by itself is not the same thing as a transformation. Make sure you explain what your transformation is in each case.
  - Hint 2: you cannot use a matrix to represent a transformation until **after** you either show the transformation is linear, or find an explicit formula for it that coincides with matrix multiplication.
- 2. Jack and Lila are best friends and love to trade coordinates with each other. However, they both know they need to tweak their coordinates to suit the other. Jack invents a function  $T_J: \mathbb{R}^2 \to \mathbb{R}^2$  which takes Jack's coordinates as input and outputs the same position in Lila's coordinates. Lila has a similar transformation  $T_L: \mathbb{R}^2 \to \mathbb{R}^2$ . Are  $T_J$  and  $T_L$  linear transformations? How do they relate to each other?
- 3. Jack, Lila, and Emily got into a fight over whose coordinates are *right*. Each of them claims since they can compute distances accurately (based on formulas from PAR 1) and can convert their coordinates to each other's, that their coordinates should be the *Official Royal Coordinates*. Using the language of linear algebra, and in particular the idea of basis, explain what's going on to Jack, Lila, and Emily.

Feedback Provided By:\_



Show All Steps



Explain Why, Not Just What



Avoid Pronouns



Use Correct Definitions



Define Variables, Units, etc.



Create Diagrams

Suggestions Accuracy Strengths



Correct Setup



Accurate Calculations



Solve Multiple Ways



Answer Reasonable



Other (Write Below)