

A *random vector* in \mathbb{R}^n is a vector whose components (when written in the standard basis) are independently and uniformly chosen random numbers in the interval $[0, 1]$.

Random Vector Theorem: Let $\mathcal{V} \subset \mathbb{R}^n$ be a subspace of \mathbb{R}^n of dimension $m < n$ and let $\vec{x} \in \mathbb{R}^n$ be a random vector. The probability that $\vec{x} \in \mathcal{V}$ is zero.

Problem Statement

Let $\vec{x}_1, \dots, \vec{x}_n \in \mathbb{R}^n$ be n random vectors.¹ Prove that there is a 100% chance that $\{\vec{x}_1, \dots, \vec{x}_n\}$ form a basis for \mathbb{R}^n .

Hint: the random vector theorem is your friend. Use it!

Reflection

Turn the page and check off the icons for things you think you did well; circle the icons for things you would like feedback on.

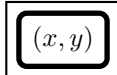
¹If you are familiar with probability theory, $\vec{x}_1, \dots, \vec{x}_n$ are independent random variables—which is a distinct concept from linear independence.

Suggestions**Communication****Strengths**

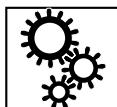
Show All Steps

Explain Why,
Not Just What

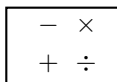
Avoid Pronouns

Use Correct
DefinitionsDefine Variables,
Units, etc.

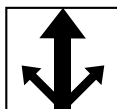
Create Diagrams

Suggestions**Accuracy****Strengths**

Correct Setup



Accurate Calculations



Solve Multiple Ways



Answer Reasonable

Other
(Write Below)