





*n*

1

$$O(m) \quad m$$



$$\log_2(n) \qquad n$$

$$\log_2(n)$$

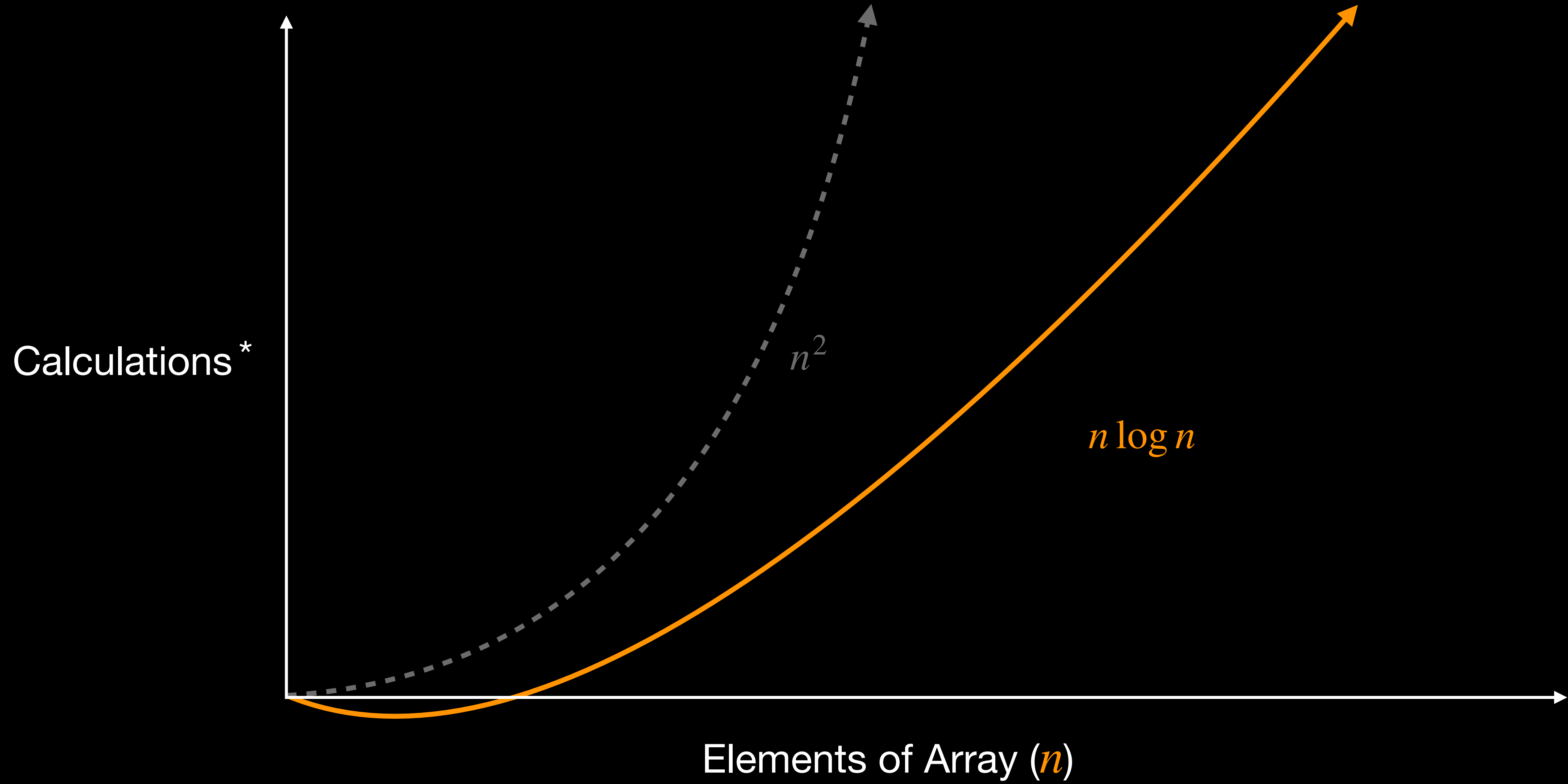
$$2n$$

$$O(n \log n)$$



# How efficient is Merge Sort?

- Let our array contain  $n$  elements. Divide the full array into equal subarrays, each with 1 element.
- Each merge operation takes  $O(m)$ , where each subarray has  $m$  elements.
- Each time we merge two subarrays, the resulting merged array is double the size of either subarray.
- We can double the size of any subarray at most  $\log_2(n)$  before the subarray is of size  $n$ .
- So, we perform  $\log_2(n)$  merges, which could each take up to  $2n$  operations.
- The overall running time is  $O(n \log n)$ .



\* Loose definition