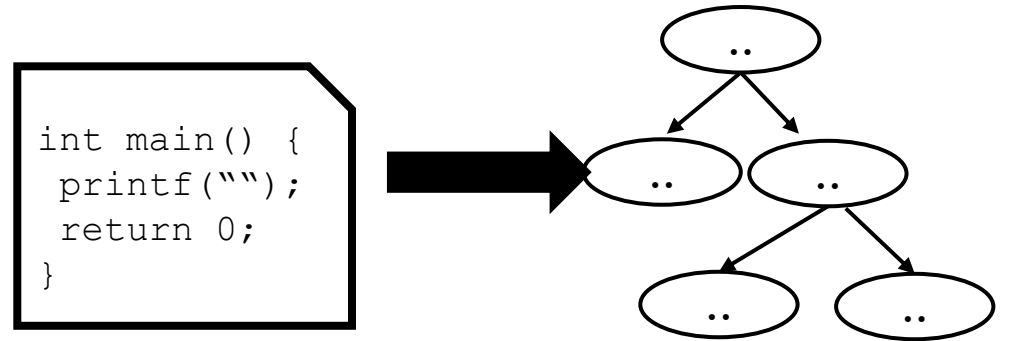


CSE110A: Compilers



Topics:

Right / Left Derivations

Some Definitions

Context Free Grammar: Formally, a context-free grammar G is a quadruple (T, NT, S, P) where: T is a set of terminals, NT is a set of non-terminals, S is a Start symbol, and P a set of Productions all for language $L(G)$.

Ambiguity: A grammar G is *ambiguous* if some sentence in $L(G)$ has more than one rightmost (or leftmost) derivation.

Sentential Form: a string of symbols that occurs as one step in a valid derivation

Derivation: a sequence of rewriting steps that begins with the grammar's start symbol and ends with a sentence in the language

Sentence: a string of symbols that can be derived from the rules of a grammar, i.e. a sentential form without non-terminals.

1	$Expr$	\rightarrow	$(Expr)$
2			$Expr Op$ name
3			name
4	Op	\rightarrow	$+$
5			$-$
6			\times
7			\div

BNF grammar for Expressions

1	$Statement$	\rightarrow	if $Expr$ then $Statement$ else $Statement$
2			if $Expr$ then $Statement$
3			$Assignment$
4			...other statements ...

Classical ambiguous grammar from Algol 60

Leftmost and Rightmost Derivations

1	$Expr$	\rightarrow	$(Expr)$
2			$Expr Op name$
3			$name$
4	Op	\rightarrow	$+$
5			$-$
6			\times
7			\div

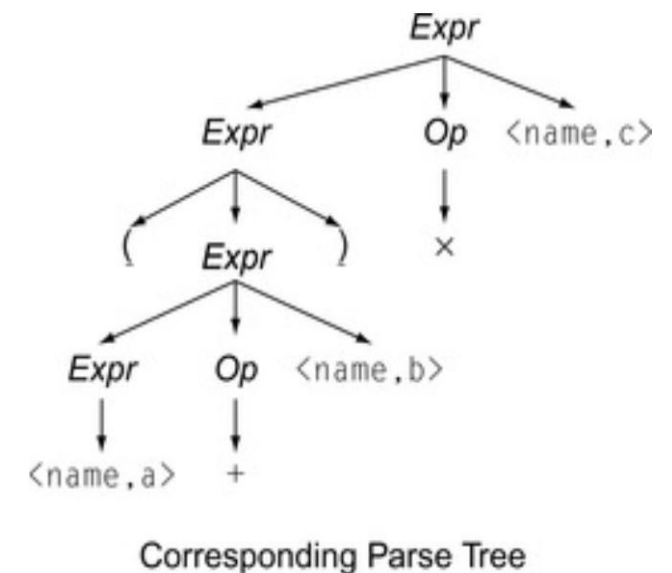
Note that leftmost derivations tend to be right associative
Rightmost derivations left associative.

Rule	Sentential Form
	$Expr$
2	$Expr Op name$
1	$(Expr) Op name$
2	$(Expr Op name) Op name$
3	$(name Op name) Op name$
4	$(name + name) Op name$
6	$(name + name) \times name$

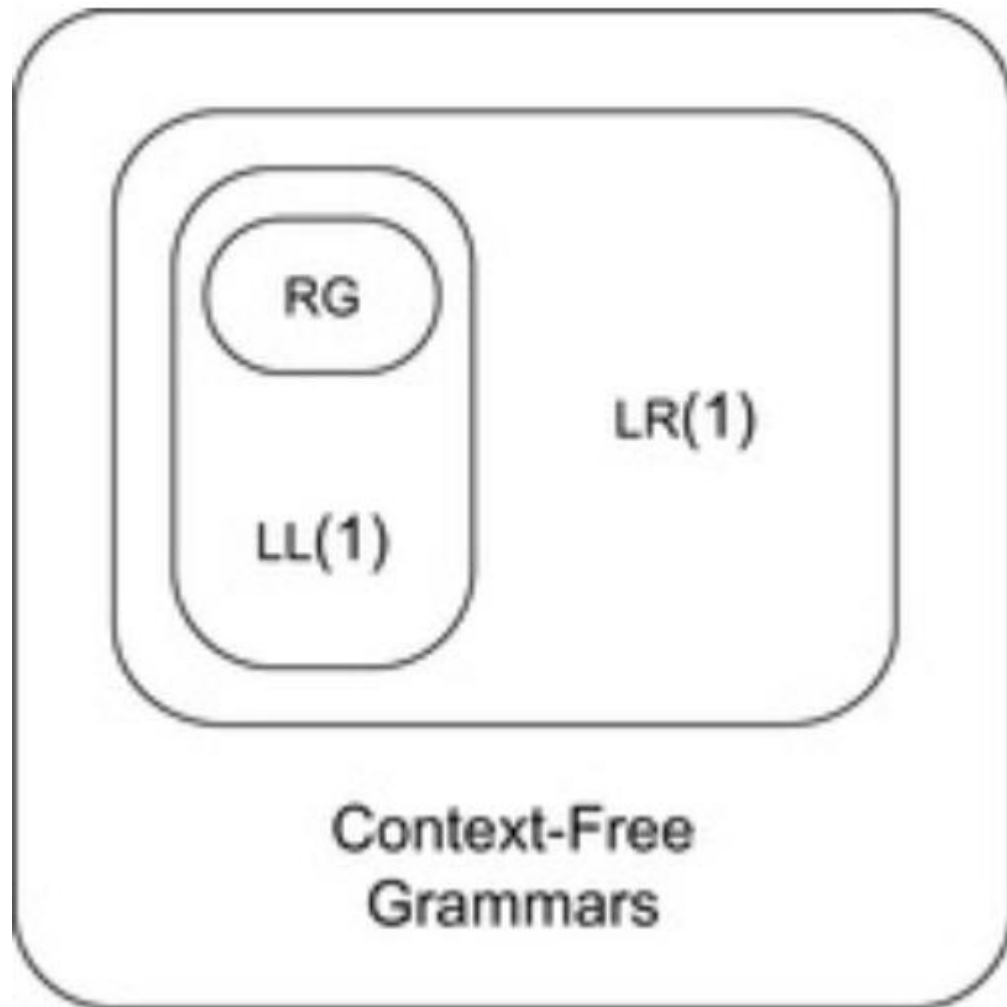
Leftmost Derivation of $(a + b) \times c$

Rule	Sentential Form
	$Expr$
2	$Expr Op name$
6	$Expr \times name$
1	$(Expr) \times name$
2	$(Expr Op name) \times name$
4	$(Expr + name) \times name$
3	$(name + name) \times name$

Rightmost Derivation of $(a + b) \times c$



CFG Hierarchy Based on Difficulty of Parsing Grammars



RG: Regular languages

LL(1): Left-to-Right Left-Derivation (Top-Down)

LR(1): Left-to-Right, Right Derivation in Reverse (Bottom-Up)

The 1 indicates 1 token look-ahead