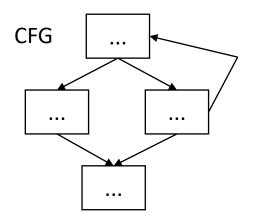
### CSE110A: Compilers

# ... AST

#### **Topics**:

- Module 3: Intermediate representations
  - Type checking
  - Error Checking and Type Conversions: 38



3 address code

```
store i32 0, ptr %2
%3 = load i32, ptr %1
%4 = add nsw i32 %3, 1,
store i32 %4, ptr %1
%5 = load i32, ptr %2
```

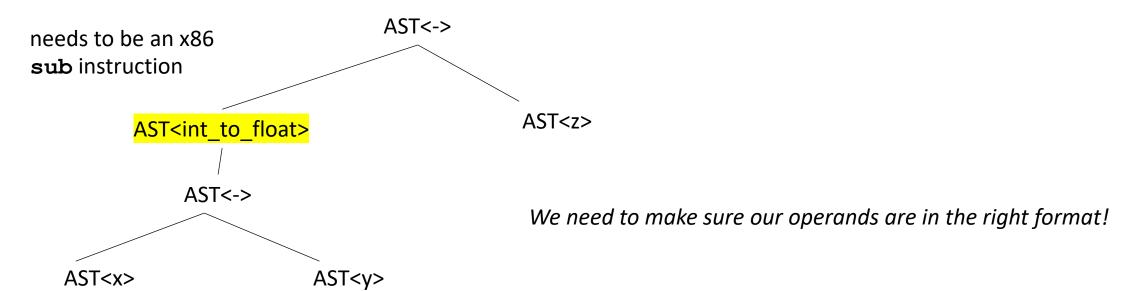
## Topic: Type Systems

### Evaluate an AST by doing a post order traversal

```
Expr ::= NUM Expr2
Expr2 ::= MINUS NUM Expr2
```

```
int x;
int y;
float z;
float w;
w = x - y - z
```

needs to be an x86 **subss** instruction



### Type systems

- Given a language a type system defines:
  - The primitive (base) types in the language
  - How the types can be converted to other types
    - implicitly or explicitly
  - How the user can define new types

### Type checking and inference

Check a program to ensure that it adheres to the type system

Especially interesting for compilers as a program given in the type system for the input language must be translated to a type system for lower-level program

### Type systems

#### Considerations:

- Base types:
  - ints
  - chars
  - strings
  - floats
  - bool
- How to combine types in expressions:
  - int and float?
  - int and char?
  - int and bool?

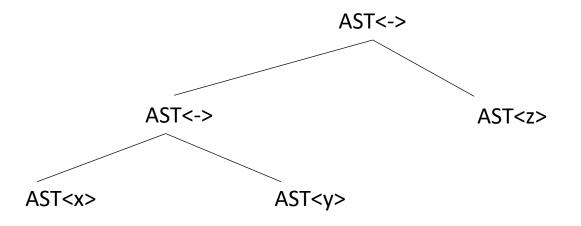
### Type checking

#### Two components

- Type inference
  - Determines a type for each AST node
  - Modifies the AST into a type-safe form
- Catches type-related errors

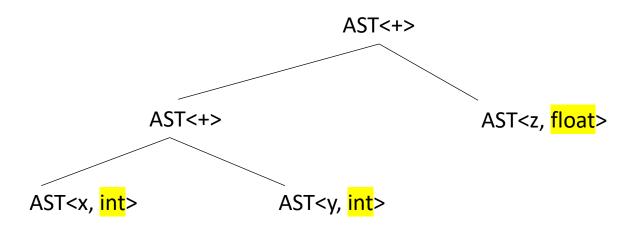
```
int x;
int y;
float z;
float w;
w = x - y - z
```

each node additionally gets a type



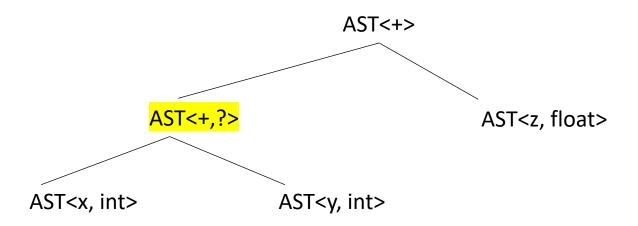
```
int x;
int y;
float z;
float w;
w = x - y - z
```

each node additionally gets a type we can get this from the symbol table for the leaves or based on the input (e.g. 5 vs 5.0)



```
int x;
int y;
float z;
float w;
w = x - y - z
```

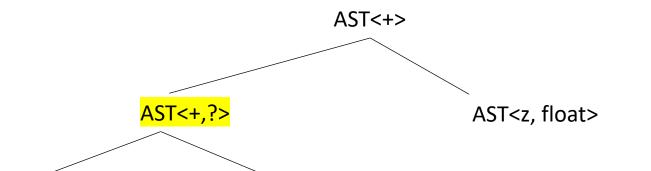
How do we get the type for this one?



```
int x;
int y;
float z;
float w;
w = x - y - z
```

AST<x, int>

How do we get the type for this one?

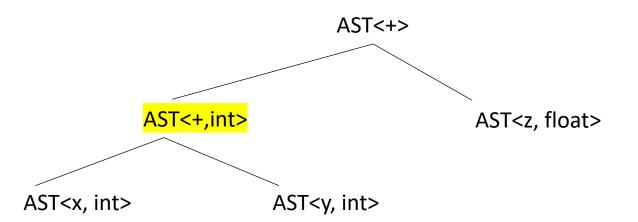


AST<y, int>

first	second	result
int	int	int
int	float	float
float	int	float
float	float	float

```
int x;
int y;
float z;
float w;
w = x - y - z
```

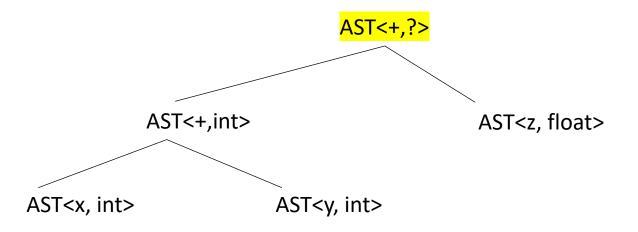
How do we get the type for this one?



first	second	result
int	<mark>int</mark>	<mark>int</mark>
int	float	float
float	int	float
float	float	float

```
int x;
int y;
float z;
float w;
w = x - y - z
```

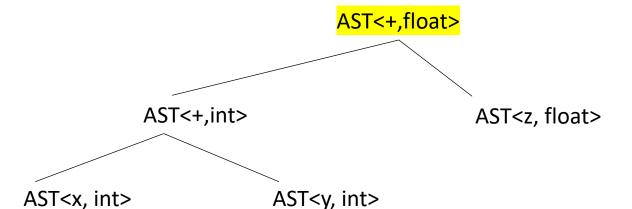
How do we get the type for this one?



first	second	result
int	int	int
int	float	float
float	int	float
float	float	float

```
int x;
int y;
float z;
float w;
w = x - y - z
```

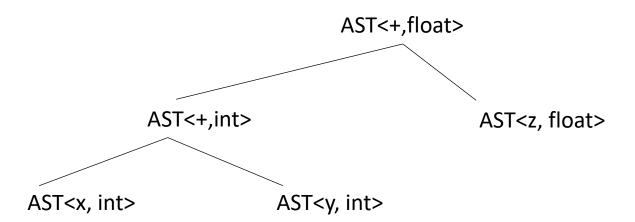
How do we get the type for this one?



first	second	result
int	int	int
<mark>int</mark>	float	float
float	int	float
float	float	float

```
int x;
int y;
float z;
float w;
w = x + y + z
```

How do we get the type for this one?



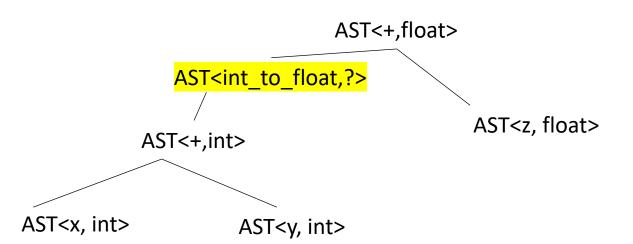
#### inference rules for addition:

first	second	result
int	int	int
int	float	float
float	int	float
float	float	float

what else?

```
int x;
int y;
float z;
float w;
w = x + y + z
```

How do we get the type for this one?



inference rules for addition:

first	second	result
int	int	int
int	float	float
float	int	float
float	float	float

what else? need to convert the int to a float

```
class ASTNode():
    def __init__(self):
        pass
```

```
class ASTLeafNode(ASTNode):
  def __init__(self, value):
    self.value = value
class ASTNumNode(ASTLeafNode):
  def ___init___(self, value):
    super(). init (value)
class ASTIDNode(ASTLeafNode):
  def __init__(self, value):
    super().__init__(value)
```

```
class ASTBinOpNode(ASTNode):
  def __init__(self, | child, r child):
    self.l child = l child
    self.r child = r child
class ASTPlusNode(ASTBinOpNode):
  def __init__(self, | child, r child):
    super().__init__(l_child,r_child)
class ASTMultNode(ASTBinOpNode):
  def __init__(self, | child, r child):
    super().__init__(l_child,r_child)
```

```
from enum import Enum

class Types(Enum):
    INT = 1
    FLOAT = 2
```

#### Our base AST Node needs a type

```
class ASTNode():
    def __init__(self):
        self.node_type = None
        pass

def set_type(self, t):
        self.node_type = t

def get_type(self):
    return self.node_type
```

Now we need to set the types for the leaf nodes

```
from enum import Enum

class Types(Enum):
    INT = 1
    FLOAT = 2
```

#### Our base AST Node needs a type

```
class ASTNode():
    def __init__(self):
        self.node_type = None
        pass

def set_type(self, t):
        self.node_type = t

def get_type(self):
    return self.node_type
```

#### Now we need to set the types for the leaf nodes

```
class ASTNumNode(ASTLeafNode):
    def __init__(self, value):
        super(). __init__(value)
    if is_int(value):
        self.set_type(Types.INT)
    else:
        self.set_type(Types.FLOAT)
```

```
from enum import Enum

class Types(Enum):
    INT = 1
    FLOAT = 2
```

#### Our base AST Node needs a type

```
class ASTNode():
    def __init__(self):
        self.node_type = None
        pass

def set_type(self, t):
        self.node_type = t

def get_type(self):
    return self.node_type
```

#### Now we need to set the types for the leaf nodes

```
class ASTNumNode(ASTLeafNode):
    def __init__(self, value):
        super().__init__(value)
    if is_int(value):
        self.set_type(Types.INT)
    else:
        self.set_type(Types.FLOAT)
```

```
class ASTIDNode(ASTLeafNode):
    def __init__(self, value, value_type):
        super().__init__(value)
        self.set_type(value_type)
```

Where can we get the value type for an ID?

### Symbol Table

Say we are matched the statement: int x;

```
• SymbolTable ST;
              (TYPE, 'int') (ID, 'x')
declare statement ::= TYPE ID SEMI
  eat (TYPE)
  id name = self.to match.value
  eat(ID)
  ST.insert(id name, None)
  eat (SEMI)
```

in homework 2 and 3 we didn't record any information in the symbol table

### Symbol Table

Say we are matched the statement: int x;

• SymbolTable ST; (TYPE, 'int') (ID, 'x')declare statement ::= TYPE ID SEMI value type = self.to match.value eat (TYPE) id name = self.to match.value eat(ID) ST.insert(id name, value type) eat (SEMI)

previously we weren't saving any information about the ID

record the type in the symbol table

```
from enum import Enum

class Types(Enum):
    INT = 1
    FLOAT = 2
```

#### Our base AST Node needs a type

```
class ASTNode():
    def __init__(self):
        self.node_type = None
        pass

def set_type(self, t):
        self.node_type = t

def get_type(self):
    return self.node_type
```

Now we need to set the types for the leaf nodes

```
class ASTNumNode(ASTLeafNode):
    def __init__(self, value):
        super().__init__(value)
    if is_int(value):
        self.set_type(Types.INT)
    else:
        self.set_type(Types.FLOAT)
```

```
class ASTIDNode(ASTLeafNode):
    def __init__(self, value, value_type):
        super().__init__(value)
        self.set_type(value_type)
```

Where can we get the value type for an ID?

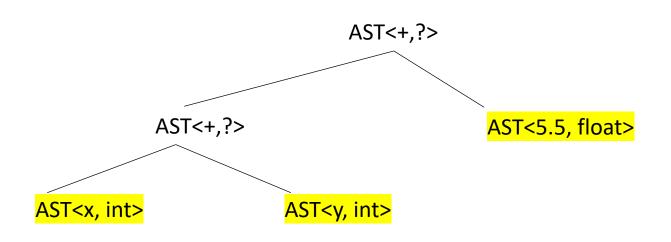
But that doesn't get us here yet...

### add the type at parse time

```
Unit ::= ID | NUM
```

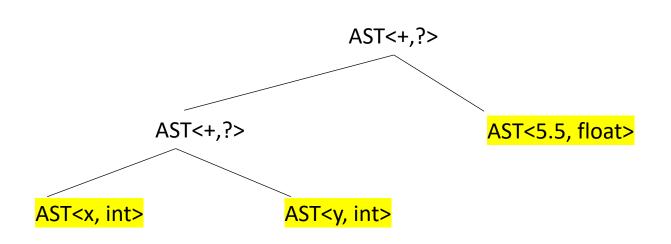
```
def parse_unit(self, lhs_node):
    # ... for applying the first production rule (ID)
    value = self.next_word.value
    # ... Check that value is in the symbol table
    node = ASTIDNode(value, ST[value])
    return node
```

We now have the types for the leaf nodes



```
int x;
int y;
float w;
w = x + y + 5.5
```

We now have the types for the leaf nodes



Next steps:

we do a post order traversal on the AST and do a type inference

def type\_inference(n):

Given a node n: find its type and the types of any of its children

```
def type_inference(n):

  case split on n:

  if n is a leaf node:
    return n.get_type()

  if n is a plus node:
    ...
```

Given a node n: find its type and the types of any of its children

```
def type_inference(n):
                                   Given a node n: find its type and the types of any of its children
 case split on n:
 if n is a leaf node:
   return n.get_type()
                               lookup the rule for plus
 if n is a plus node:
    return lookup type from table
```

#### inference rules for plus

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

```
def type_inference(n):
                                   Given a node n: find its type and the types of any of its children
 case split on n:
 if n is a leaf node:
   return n.get type()
                               lookup the rule for plus
 if n is a plus node:
    return lookup type from table
```

#### inference rules for plus

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

but we're missing a few things

```
def type_inference(n):
                                  Given a node n: find its type and the types of any of its children
 case split on n:
 if n is a leaf node:
                                 we need to make sure the
   return n.get_type()
                                 children have types!
 if n is a plus node:
     do type inference on children
     return lookup type from table
```

#### inference rules for plus

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

```
def type_inference(n):
                                 Given a node n: find its type and the types of any of its children
 case split on n:
 if n is a leaf node:
                                we should record our type
   return n.get_type()
 if n is a plus node:
    do type inference on children
    t = lookup type from table
    set n type to t
    return t
```

#### inference rules for plus

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

```
def type_inference(n):
                                 Given a node n: find its type and the types of any of its children
 case split on n:
 if n is a leaf node:
   return n.get type()
 if n is a plus node:
    do type inference on children
    t = lookup type from table
    set n type to t
    return t
```

is this just for plus?

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

def type\_inference(n):

Given a node n: find its type and the types of any of its children

most language promote types, e.g. ints to float for expression operators

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

set n type to t

return t

def type\_inference(n):

Given a node n: find its type and the types of any of its children

most language promote types, e.g. ints to float for expression operators

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

```
def type_inference(n):

   case split on n:

   if n is a leaf node:
      return n.get_type()

   if n is a bin op node:
      do type inference on children
      t = lookup type from table
      set n type to t
      return t
```

#### What about for assignments?

```
int x; cout << (x = 5.5) << endl;
```

#### What does this return?

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

```
def type_inference(n):

   case split on n:

   if n is a leaf node:
     return n.get_type()

   if n is a bin op node:
     do type inference on children
     t = lookup type from table
     set n type to t
     return t
```

#### What about for assignments?

```
int x; cout << (x = 5.5) << endl;
```

#### What does this return?

left	right	result
int	int	<mark>int</mark>
int	float	<mark>int</mark>
float	int	float
float	float	float

#### whatever the left is

# Type checking

Checking for errors

```
def type_inference(n):
                                 Given a node n: find its type and the types of any of its children
 case split on n:
 if n is a leaf node:
                                we should record our type
   return n.get type()
 if n is a plus node:
    do type inference on children
    t = lookup type from table
    if t is None:
       throw type exception
    set n type to t
    return t
```

#### inference rules for plus

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

```
def type_inference(n):
                                 Given a node n: find its type and the types of any of its children
 case split on n:
 if n is a leaf node:
                                we should record our type
   return n.get type()
 if n is a plus node:
    do type inference on children
    t = lookup type from table
    if t is None:
       throw type exception
    set n type to t
    return t
```

#### inference rules for plus

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float
string	int	<mark>None</mark>

like in Python

What other examples would throw an error?

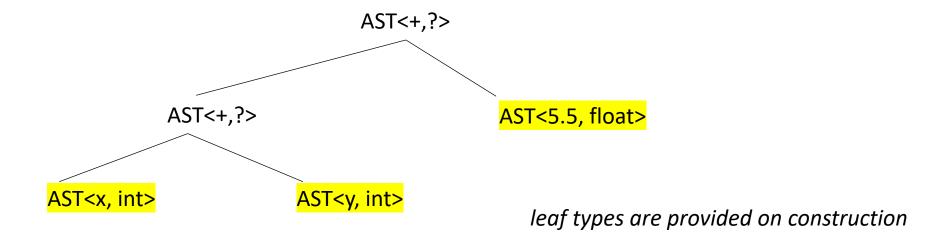
```
def type_inference(n):
                                 Given a node n: find its type and the types of any of its children
 case split on n:
 if n is a leaf node:
                                we should record our type
   return n.get type()
 if n is a plus node:
    do type inference on children
    t = lookup type from table
    if t is None:
       throw type exception
    set n type to t
    return t
```

#### inference rules for plus

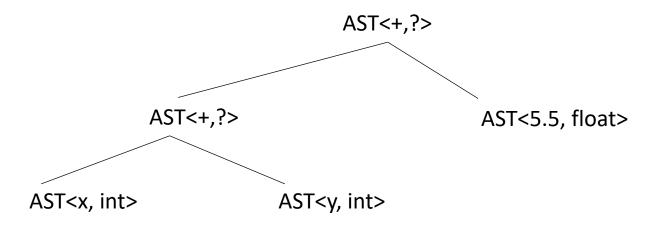
left	right	result
int	int	int
int	float	float
float	int	float
float	float	float
string	int	<mark>None</mark>

like in Python

```
int x;
int y;
float w;
w = x + y + 5.5
```



```
int x;
int y;
float w;
w = x + y + 5.5
```

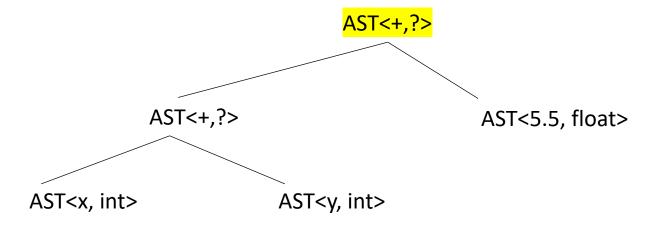


#### def type\_inference(n):

if n is a leaf node:
 return n.get\_type()

if n is a bin op node:
 do type inference on children
 t = lookup type from table
 set n type to t
 return t.

```
int x;
int y;
float w;
w = x + y + 5.5
start on top
```



#### def type\_inference(n):

```
case split on type of n:

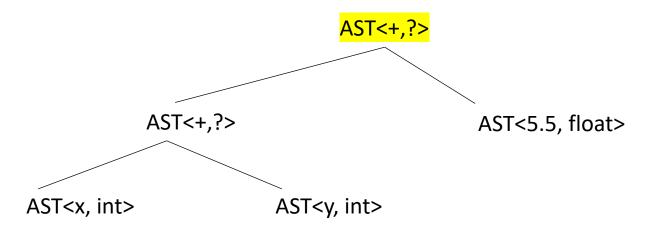
if n is a leaf node:
   return n.get_type()

if n is a bin op node:
   do type inference on children
   t = lookup type from table
   set n type to t
   return t
```

### def type\_inference(n):

```
int x;
int y;
float w;
w = x + y + 5.5
```

it's a binary op



case split on type of n:
if n is a leaf node:
 return n.get\_type()

if n is a bin op node:
 do type inference on children
 t = lookup type from table
 set n type to t
 return t

```
int x;
int y;
float w;
w = x + y + 5.5
```

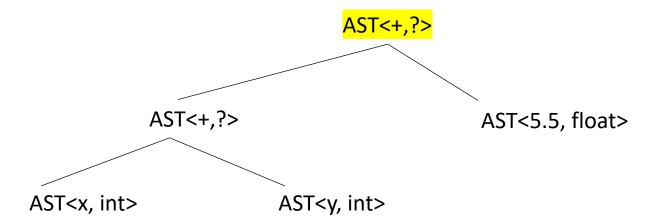
### def type\_inference(n):

recursion

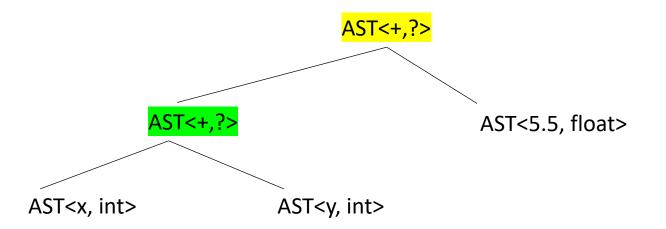
```
case split on type of n:

if n is a leaf node:
   return n.get_type()

if n is a bin op node:
   do type inference on children
   t = lookup type from table
   set n type to t
   return t
```



```
int x;
int y;
float w;
w = x + y + 5.5
```



#### def type\_inference(n):

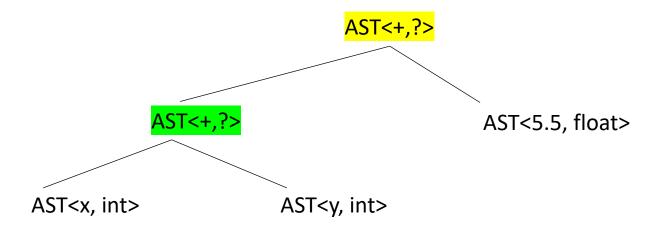
```
if n is a leaf node:
   return n.get_type()

if n is a bin op node:
   do type inference on children
   t = lookup type from table
   set n type to t
   return t
```

### def type\_inference(n):

```
int x;
int y;
float w;
w = x + y + 5.5
```

it's a binary op



case split on type of n:
if n is a leaf node:
 return n.get\_type()

#### if n is a bin op node:

do type inference on children
t = lookup type from table
set n type to t
return t

```
int x;
int y;
float w;
```

w = x + y + 5.5

#### recursion

```
AST<+,?>
AST<+,?>
AST<5.5, float>
AST<x, int>
AST<y, int>
```

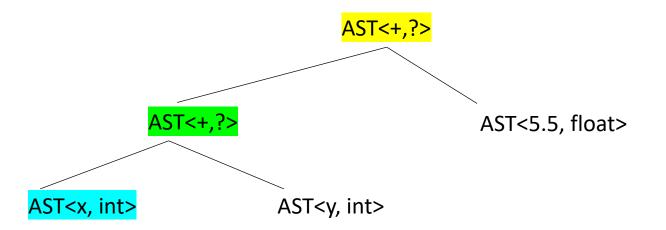
#### def type\_inference(n):

```
case split on type of n:

if n is a leaf node:
   return n.get_type()

if n is a bin op node:
   do type inference on children
   t = lookup type from table
   set n type to t
   return t
```

```
int x;
int y;
float w;
w = x + y + 5.5
```

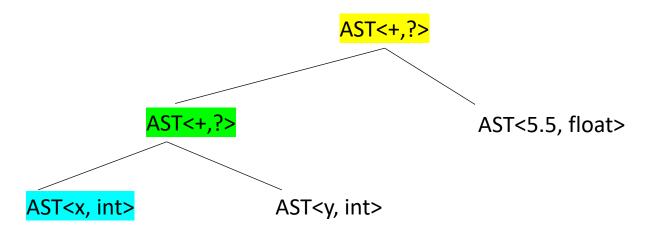


#### def type\_inference(n):

```
if n is a leaf node:
   return n.get_type()

if n is a bin op node:
   do type inference on children
   t = lookup type from table
   set n type to t
   return t
```

```
int x;
int y;
float w;
w = x + y + 5.5
```



#### def type\_inference(n):

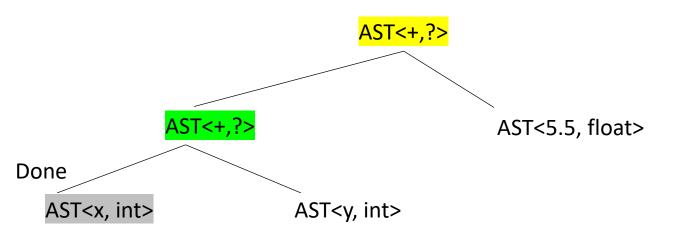
case split on type of n:

#### if n is a leaf node:

return n.get type()

if n is a bin op node:
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 t = lookup type from table
 set n type to t
 return t

```
int x;
int y;
float w;
w = x + y + 5.5
```



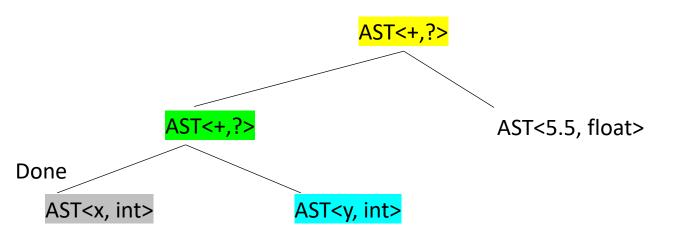
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```
case split on type of n:

if n is a leaf node:
   return n.get_type()

if n is a bin op node:
   do type inference on children
   t = lookup type from table
   set n type to t
   return t
```

```
int x;
int y;
float w;
w = x + y + 5.5
```



### def type\_inference(n):

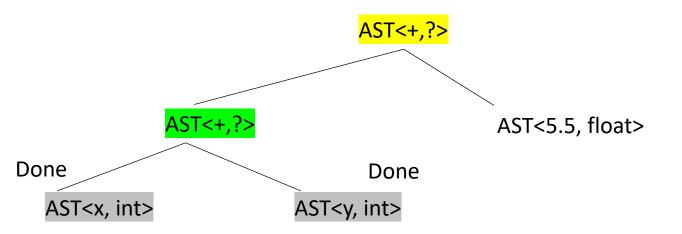
case split on type of n:

#### if n is a leaf node:

return n.get\_type()

if n is a bin op node:
 do type inference on children
 t = lookup type from table
 set n type to t
 return t

```
int x;
int y;
float w;
w = x + y + 5.5
```



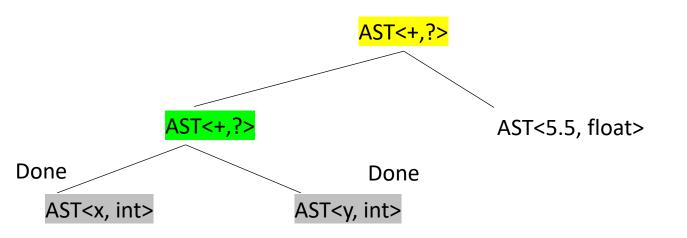
#### def type\_inference(n):

```
case split on type of n:

if n is a leaf node:
   return n.get_type()

if n is a bin op node:
   do type inference on children
   t = lookup type from table
   set n type to t
   return t
```

```
int x;
int y;
float w;
w = x + y + 5.5
```



#### def type\_inference(n):

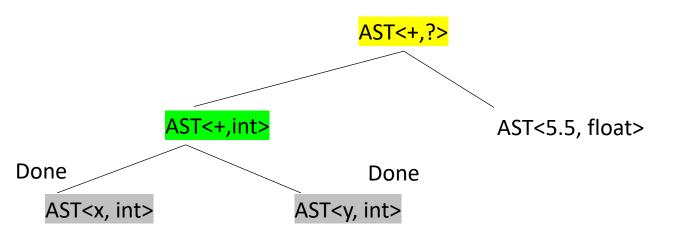
case split on type of n:

if n is a leaf node:
 return n.get\_type()

if n is a bin op node:
 do type inference on children
 t = lookup type from table
 set n type to t
 return t

left child	right child	result
int	int	int
int	float	float
float	int	float
float	float	float

```
int x;
int y;
float w;
w = x + y + 5.5
```



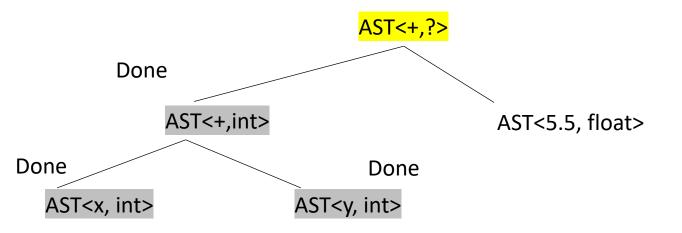
#### def type\_inference(n):

if n is a leaf node:
 return n.get\_type()

if n is a bin op node:
 do type inference on children
 t = lookup type from table
 set n type to t
 return t

left child	right child	result
int	<mark>int</mark>	<mark>int</mark>
int	float	float
float	int	float
float	float	float

```
int x;
int y;
float w;
w = x + y + 5.5
```



#### def type\_inference(n):

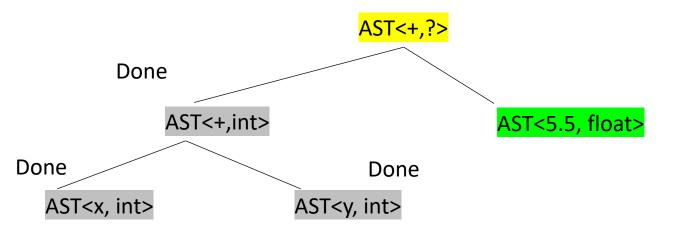
case split on type of n:

if n is a leaf node:
 return n.get\_type()

if n is a bin op node:
 do type inference on children
 t = lookup type from table
 set n type to t
 return t

left child	right child	result
int	int	int
int	float	float
float	int	float
float	float	float

```
int x;
int y;
float w;
w = x + y + 5.5
```



#### def type\_inference(n):

case split on type of n:

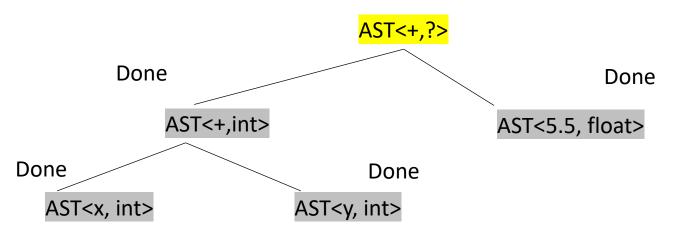
### if n is a leaf node:

return n.get\_type()

if n is a bin op node:
 do type inference on children
 t = lookup type from table
 set n type to t
 return t

left child	right child	result
int	int	int
int	float	float
float	int	float
float	float	float

```
int x;
int y;
float w;
w = x + y + 5.5
```



#### def type\_inference(n):

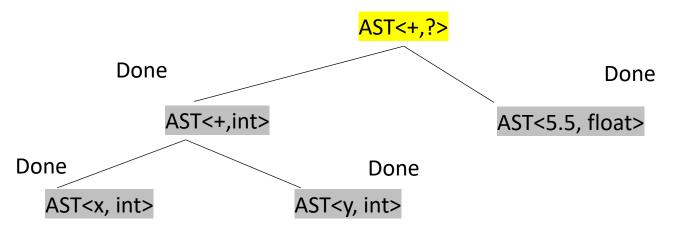
```
case split on type of n:

if n is a leaf node:
   return n.get_type()

if n is a bin op node:
   do type inference on children
   t = lookup type from table
   set n type to t
   return t
```

left child	right child	result
int	int	int
int	float	float
float	int	float
float	float	float

```
int x;
int y;
float w;
w = x + y + 5.5
```



#### def type\_inference(n):

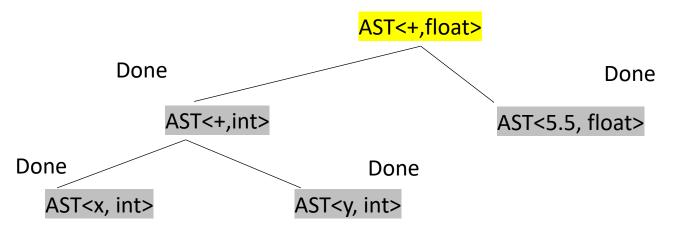
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case split on type of n:

if n is a leaf node:
   return n.get_type()

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   do type inference on children
   t = lookup type from table
   set n type to t
   return t
```

left child	right child	result
int	int	int
int	float	float
float	int	float
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```
int x;
int y;
float w;
w = x + y + 5.5
```



#### def type\_inference(n):

```
case split on type of n:

if n is a leaf node:
   return n.get_type()

if n is a bin op node:
   do type inference on children
   t = lookup type from table
   set n type to t
   return t
```

left child	right child	result
int	int	int
<mark>int</mark>	float	float
float	int	float
float	float	float

```
int x;
int y;
float w;
w = x + y + 5.5
```

```
Done

AST<+,float>

Done

AST<+,int>

Done

AST<5.5, float>

AST<y, int>
```

#### def type\_inference(n):

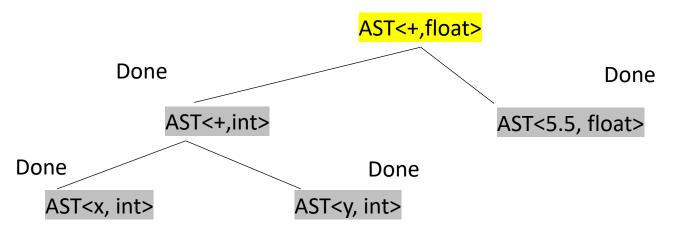
```
case split on type of n:

if n is a leaf node:
   return n.get_type()

if n is a bin op node:
   do type inference on children
   t = lookup type from table
   set n type to t
   return t
```

Are we done?

```
int x;
int y;
float w;
w = x + y + 5.5
```



### def type\_inference(n):

```
if n is a leaf node:
   return n.get_type()

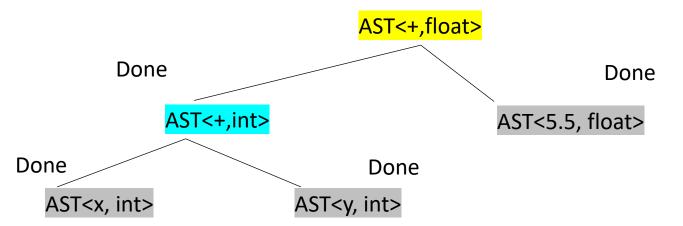
if n is a bin op node:
   do type inference on children
   t = lookup type from table
   set n type to t
   do any required type conversions
   return t
```

#### Are we done?

### def type\_conversion(n):

this will need to be done for both children

if n.left child type is NOT the same as n type:
 conv = get conversion AST node
 conv.child = left child
 set n.left\_child to = conv



```
class ASTUnOpNode(ASTNode):
  def __init__(self, child):
    self.child = child
class ASTIntToFloatNode(ASTUnOpNode):
  def __init__(self, child):
    super().__init__(child)
class ASTFloatToIntNode(ASTUnOpNode):
  def __init__(self, child):
    super().__init__(child)
```

```
from enum import Enum

class Types(Enum):
    INT = 1
    FLOAT = 2
```

what types are these nodes?

```
class ASTUnOpNode(ASTNode):
  def __init__(self, child):
    self.child = child
class ASTIntToFloatNode(ASTUnOpNode):
  def __init__(self, child):
    super().__init__(child)
class ASTFloatToIntNode(ASTUnOpNode):
  def __init__(self, child):
    super().__init__(child)
```

```
from enum import Enum

class Types(Enum):

INT = 1

FLOAT = 2
```

what types are these nodes?

```
class ASTUnOpNode(ASTNode):
  def __init__(self, child):
    self.child = child
class ASTIntToFloatNode(ASTBinUnNode):
  def __init__(self, child):
    self.set_type(Types.FLOAT)
    super().__init__(child)
class ASTFloatToIntNode(ASTBinUnNode):
  def __init__(self, child):
    self.set_type(Types.INT)
    super().__init__(child)
```

```
from enum import Enum

class Types(Enum):

INT = 1

FLOAT = 2
```

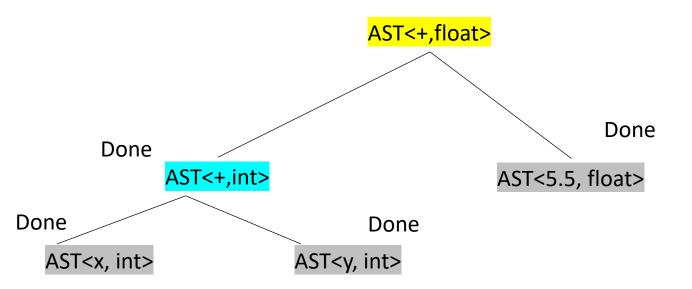
what types are these nodes?

We can go further than just checking to ensure our children are the right type

```
class ASTUnOpNode(ASTNode):
  def __init__(self, child):
    self.child = child
class ASTIntToFloatNode(ASTBinUnNode):
  def init (self, child):
    self.set_type(Types.FLOAT)
    assert(child.get_type() == Types.INT)
    super().__init__(child)
class ASTFloatToIntNode(ASTBinUnNode):
  def __init__(self, child):
    self.set_type(Types.INT)
    assert(child.get_type() == Types.FLOAT)
    super().__init__(child)
```

### def type\_conversion(n):

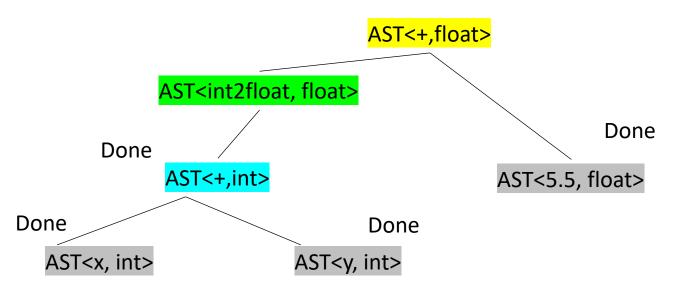
```
if n.left child type is NOT the same as n type:
    conv = get conversion AST node
    conv.child = left child
    set n.left_child to = conv
```



AST<int2float, float>

### def type\_conversion(n):

```
if n.left child type is NOT the same as n type:
    conv = get conversion AST node
    conv.child = left child
    set n.left_child to = conv
```



```
int x;
      int y;
      float w;
      w = x + y + 5.5
                                           Done
                                AST<+,float>
   Done implicitly
             AST<int2float, float>
                                                      Done
       Done
             AST<+,int>
                                            AST<5.5, float>
Done
                                Done
  AST<x, int>
                          AST<y, int>
```

#### def type\_inference(n):

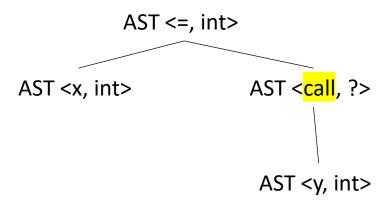
```
if n is a leaf node:
    return n.get_type()

if n is a bin op node:
    do type inference on children
    t = lookup type from table
    set n type to t
    do any required type conversions
    return t
```

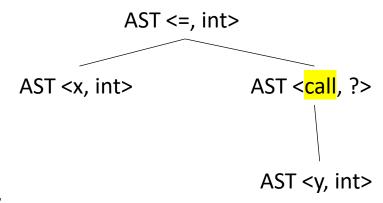
Done

# Topic: Functions

```
int x;
int y;
x = sqrt(y)
```



```
int x;
int y;
x = sqrt(y)
```



requires a function specification, using in the .h file:

float sqrt(float x);

using in the .h file:

float sqrt(float x);

```
int x;
int y;
x = sqrt(y)

AST <=, int>

AST <call, float>

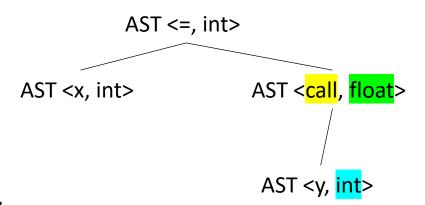
requires a function specification,

type of the AST node
becomes the return type
of the function

AST <<, int>

AST <</pre>
AST <</pre>
AST <y, int>
```

```
int x;
int y;
x = sqrt(y)
```

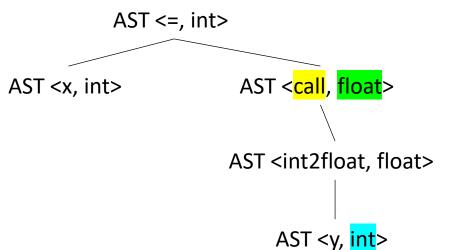


type inference must make sure arguments match types

requires a function specification, using in the .h file:

```
float sqrt(float x);
```

```
int x;
int y;
x = sqrt(y)
```

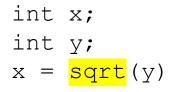


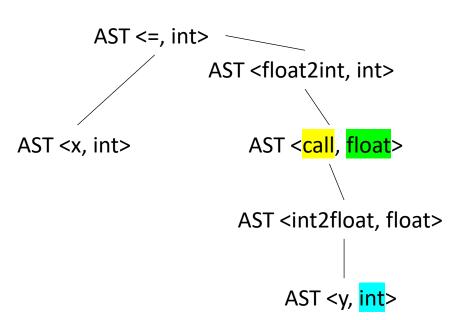
type inference must make sure arguments match types

requires a function specification, using in the .h file:

float sqrt(float x);

```
int x;
   int y;
   x = \frac{\text{sqrt}}{\text{y}}
                                                                        How would type inference finish this?
                                               AST <=, int>
                                                             AST < call, float >
                                    AST <x, int>
                                                            AST <int2float, float>
requires a function specification,
using in the .h file:
                                                                 AST <y, int>
float sqrt(float x);
```





How would type inference finish this? remember that assignment converts to the lhs type

Binding to the dummy parameter is a type of assignment.

requires a function specification, using in the .h file:

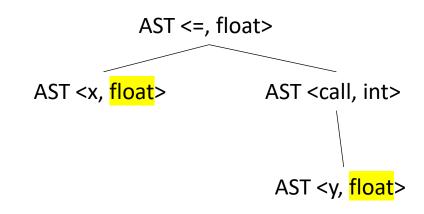
```
float sqrt(float x);
```

# Topic: More on Types

# What about floats to ints?

```
int int_sqrt(int input);
float x;
float y;
x = int_sqrt(y)
```

Does this compile?



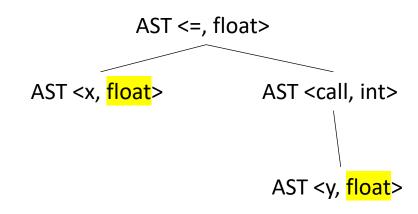
# What about floats to ints?

```
int int_sqrt(int input);

float x;
float y;
x = int_sqrt(y)

Does this compile? Yes!
```

In this case the compiler will convert floats to an int. Is that the right choice? ...

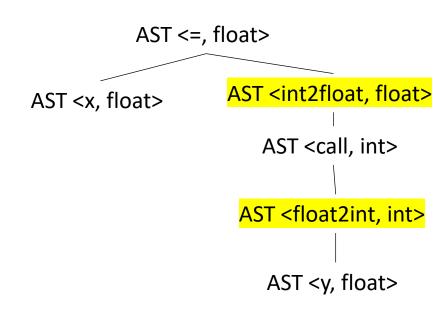


# What about floats to ints?

```
int int_sqrt(int input);
float x;
float y;
x = int_sqrt(y)
```

Does this compile? Yes!

In this case the compiler will convert floats to an int. Is that the right choice? ...



### Discussion

 Many languages (and styles) state that the programmer extends the type system through functions

- Other languages allow operator overloading
  - Controversial design pattern
  - But it can be really nice (e.g. it is used extensively in LLVM internals)

```
class Complex {
    private:
        float real;
        float imag;
    public:
        // Constructor to initialize real and imag to 0
        Complex() : real(0), imag(0) {}

        // Overload the + operator
        Complex operator + (const Complex obj) {
            Complex temp;
            temp.real = real + obj.real;
            temp.imag = imag + obj.imag;
            return temp;
        }
}
```

#### Table for *plus* binary ops

left child	right child	result
int	int	int
int	float	float
float	int	float
float	float	float
Complex	Complex	Complex

```
class Complex {
 private:
  float real;
  float imag;
 public:
  // Constructor to initialize real and imag to 0
  Complex() : real(0), imag(0) {}
  // Overload the + operator
  Complex operator + (const Complex & obj) {
   Complex temp;
   temp.real = real + obj.real;
   temp.imag = imag + obj.imag;
   return temp;
     Complex operator + (const float& i) {
       Complex temp;
       temp.real = real + i;
       temp.imag = imag;
       return temp;
```

#### Table for *plus* binary ops

left child	right child	result
int	int	int
int	float	float
float	int	float
float	float	float
Complex	Complex	Complex

```
class Complex {
 private:
  float real;
  float imag;
 public:
  // Constructor to initialize real and imag to 0
  Complex() : real(0), imag(0) {}
  // Overload the + operator
  Complex operator + (const Complex & obj) {
   Complex temp;
   temp.real = real + obj.real;
   temp.imag = imag + obj.imag;
   return temp;
     Complex operator + (const float& i) {
       Complex temp;
       temp.real = real + i;
       temp.imag = imag;
       return temp;
```

#### Table for *plus* binary ops

left child	right child	result
int	int	int
int	float	float
float	int	float
float	float	float
Complex	Complex	Complex
Complex	float	<pre>Complex</pre>

We can add extra rows

# Type systems finished

- Defined what a type system is and discussed various different design decisions
  - static vs. dynamic, choice of primitive types, size of primitive types
- Implemented type inference parameterized by type conversion tables on an AST.
  - identified common conversions (int to float) and when the opposite can happen
- Discussed how programmers can extend the type system
  - function calls
  - operator overloading