CSE110A: Compilers

Topics: Algorithms for Parsing

- Syntactic Analysis continued
 - Top down parsing
 - Oracle parser
 - Rewriting to avoid left recursion

```
int main() {
  printf("");
  return 0;
}
```

New topic: Algorithms for parsing

One goal:

• Given a string s and a CFG G, determine if G can derive s

• We will do that by implicitly attempting to derive a parse tree for S

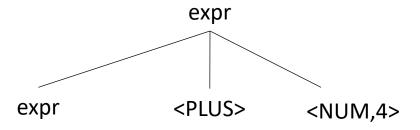
- Two different approaches, each with different trade-offs:
 - Top down
 - Bottom up

input: 2+3+4

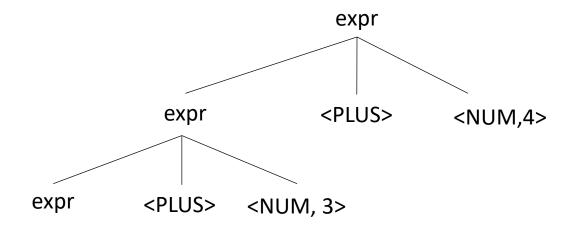
expr

Operator	Name	Productions
+	expr	: expr PLUS NUM

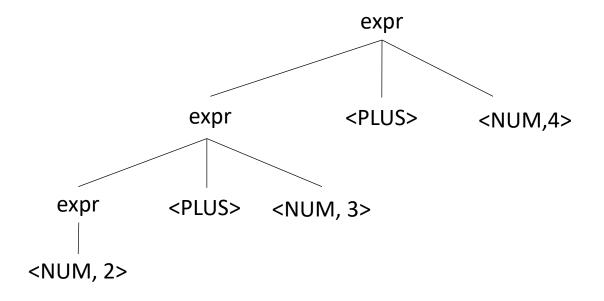
Operator	Name	Productions
+	expr	: expr PLUS NUM



Operator	Name	Productions
+	expr	: expr PLUS NUM



Operator	Name	Productions
+	expr	: expr PLUS NUM



Pros:

- Algorithm is simpler
- Faster than bottom-up
- Easier recovery

Cons:

- Not efficient on arbitrary grammars
- Many grammars need to be re-written

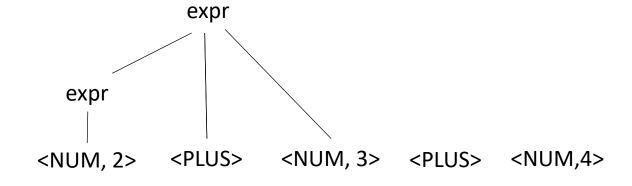
input: 2+3+4

Operator	Name	Productions
+	expr	: expr PLUS NUM

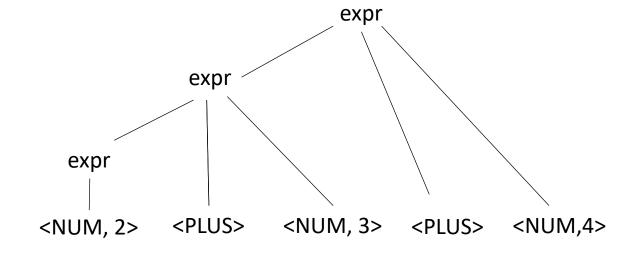
<NUM, 2> <PLUS> <NUM, 3> <PLUS> <NUM,4>

Operator	Name	Productions
+	expr	: expr PLUS NUM

Operator	Name	Productions
+	expr	: expr PLUS NUM



Operator	Name	Productions
+	expr	: expr PLUS NUM



Bottom up

Pros:

- can handle grammars expressed more naturally
- can encode precedence and associativity even if grammar is ambiguous

Cons:

- algorithm is complicated
- in many cases slower than top down

Let's start with top down

```
root = start symbol; # Expr
focus = root;
push (None);
to match = s.token(); # Read first token
while (true):
  if (focus is a nonterminal)
    pick next rule (A ::= B1, B2, B3...BN);
   push (BN... B3, B2);
    focus = B1  # First symbol in rule
  else if (focus == to match):
    to match = s.token()
    focus = pop()
  else if (to match == None and focus == None)
    Accept
```

Variable	Value
focus	
to_match	
s.istring	
stack	

Expanded Rule	Sentential Form
start	Expr

```
root = start symbol;
focus = root;
push (None);
                                    Currently we assume this
to match = s.token();
                                    is magic and picks
                                    the right rule every time
while (true):
  if (focus is a nonterminal)
    pick next rule (A ::= B1, B2, B3...BN);
    push (BN... B3, B2);
    focus = B1
  else if (focus == to match)
    to match = s.token()
    focus = pop()
  else if (to match == None and focus == None)
    Accept
    Variable
                          Value
     focus
     to_match
```

s.istring

stack

Can we derive the string (a+b) *c

Expanded Rule	Sentential Form
start	Expr

```
root = start symbol;
focus = root;
push (None);
                                    Currently we assume this
to match = s.token();
                                    is magic and picks
                                    the right rule every time
while (true):
  if (focus is a nonterminal)
    pick next rule (A ::= B1, B2, B3...BN);
    push (BN... B3, B2);
    focus = B1
  else if (focus == to match)
    to match = s.token()
    focus = pop()
  else if (to match == None and focus == None)
    Accept
```

Variable	Value
focus	Ор
to_match	' +'
s.istring	b) *c
stack	Unit ')' Op, Expr, None

Expanded Rule #	Sentential Form
start	Expr
1	Expr Op Unit
2	Unit Op Unit
3	'(' Expr ')' Op Unit
1	'(' Expr Op Unit ')' Op Unit
2	'(' Unit Op Unit ')' Op Unit
4	'(' ID Op Unit ')' Op Unit

And so on...

```
root = start symbol;
focus = root;
push (None);
                                   What can go wrong if
to match = s.token();
                                   we don't have a magic
                                   choice
while (true):
  if (focus is a nonterminal)
    pick next rule (A ::= B1, B2, B3...BN);
    push (BN... B3, B2);
    focus = B1
  else if (focus == to match)
    to match = s.token()
    focus = pop()
  else if (to match == None and focus == None)
    Accept
```

Variable	Value
focus	
to_match	
s.istring	
stack	

Expanded Rule	Sentential Form
start	Expr

```
root = start symbol;
focus = root;
push (None);
                                   What can go wrong
to match = s.token();
while (true):
  if (focus is a nonterminal)
    pick next rule (A ::= B1, B2, B3...BN);
    push (BN... B3, B2);
    focus = B1
  else if (focus == to match)
    to match = s.token()
    focus = pop()
  else if (to match == None and focus == None)
    Accept
```

Variable	Value
focus	
to_match	
s.istring	
stack	

Expanded Rule	Sentential Form
start	Expr
2	Expr Op Unit
2	Expr Op Unit Op Unit
2	Expr Op Unit Op Unit Op Unit
2	Expr Op Unit

Infinite recursion!

Top down parsing does not handle left recursion

direct left recursion

indirect left recursion

Top down parsing cannot handle either of these

Top down parsing does not handle left recursion

- In general, any CFG can be re-written without left recursion
 - However, the transformation may affect associativity
 - or increase the number of rules
 - but it is always possible

```
Fee ::= Fee "a"
```

What does this grammar describe?

The grammar can be rewritten as

```
Fee ::= Fee "a"
| "b"
```

In general, A and B can be any sequence of non-terminals and terminals

```
Fee ::= Fee A

| B

Fee ::= B Fee2

| Fee2 ::= A Fee2

| ""
```

Lets do this one as an example:

```
Fee ::= B Fee2

| Fee ::= B Fee2
| Fee2 ::= A Fee2
| ""
```

```
A = ?
B = ?
```

Lets do this one as an example:

```
A = Op Unit
B = Unit
```

Lets do this one as an example:

```
root = start symbol;
focus = root;
push (None);
to match = s.token();
while (true):
  if (focus is a nonterminal)
    pick next rule (A ::= B1,B2,B3...BN);
    push (BN... B3, B2);
    focus = B1
  else if (focus == to match)
    to match = s.token()
    focus = pop()
  else if (to_match == None and focus == None)
   Accept
 Variable
                      Value
```

focus	
to_match	
s.istring	
stack	

1:	Expr	::= Unit Expr2
2:	Expr2	::= Op Unit Expr2
3:		""
4:	Unit	::= '(' Expr ')'
5:		ID
6:	Ор	::= \+'
7:	_	*/

Sentential Form
Expr

```
root = start symbol;
focus = root;
                                               How to handle
push (None);
                                               this case?
to match = s.token();
while (true):
  if (focus is a nonterminal)
    pick next rule (A ::= B1,B2,B3...BN);
    push (BN... B3, B2);
    focus = B1
  else if (focus == to match)
    to_match = s.token()
    focus = pop()
  else if (to match == None and focus == None)
    Accept
  Variable
                       Value
  focus
  to_match
  s.istring
  stack
```

1:	Expr	::=	Unit	Expi	2
2:	Expr2	::=	J qO	Jnit E	Expr2
3:		""			
4:	Unit	::=	`(`	Expr	`)'
5:			ID		
6 :	Ор	::=	\+'		
7:		1	\ * /		

Expanded Rule	Sentential Form
start	Expr

```
root = start symbol;
focus = root;
                                              How to handle
push (None);
                                              this case?
to match = s.token();
while (true):
  if (focus is a nonterminal)
    pick next rule (A ::= B1,B2,B3...BN);
    if A == "": focus=pop(); continue; # ignore it
    push (BN... B3, B2);
    focus = B1
  else if (focus == to match)
    to match = s.token()
    focus = pop()
  else if (to match == None and focus == None)
    Accept
 Variable
                      Value
 focus
 to_match
 s.istring
```

stack

1:	Expr	::=	Unit Expr2
2:	Expr2	::=	Op Unit Expr2
3:		""	Í
4:	Unit	::=	'(' Expr ')'
5:			ID
6 :	Ор	::=	\ + '
7:			\ * /

Expanded Rule	Sentential Form
start	Expr

direct left recursion

indirect left recursion

Top down parsing cannot handle either

Identify indirect left left recursion

$$Expr_base \rightarrow_{lhs} Expr_op \rightarrow_{lhs} Expr_base$$

Identify indirect left left recursion

$$Expr_base \rightarrow_{lhs} Expr_op \rightarrow_{lhs} Expr_base$$

Substitute indirect non-terminal closer to initial non-terminal

```
1: Expr base ::= Unit
                              1: Expr base ::= Unit
 | Expr op
                                 3: Expr_op ::= Expr_base Op Unit
                              3: Expr op ::= Expr base Op Unit
4: Unit ::= '(' Expr_base ')'
                              4: Unit ::= '(' Expr base ')'
5:
  | ID
                              5:
                                           ΙD
6: Op ::= '+'
                               6: Op ::= '+'
            1 * /
7:
                               7:
                                           1 * /
```

Identify indirect left left recursion

What to do with production rule 3?

$$Expr_base \rightarrow_{lhs} Expr_op \rightarrow_{lhs} Expr_base$$

Substitute indirect non-terminal closer to initial non-terminal

```
1: Expr base ::= Unit
                                  1: Expr base ::= Unit
              Expr_op
                                      3: Expr_op ::= Expr_base Op Unit
                                  3: Expr op ::= Expr base Op Unit
4: Unit ::= '(' Expr_base ')'
                                  4: Unit ::= '(' Expr base ')'
5:
              ΙD
                                  5:
                                                ΙD
6: Op ::= '+'
                                  6: Op ::= '+'
              1 * /
7:
                                  7:
                                                 1 * /
```

Identify indirect left left recursion

What to do with production rule 3? It may need to stay if another production rule references it!

$$Expr_base \rightarrow_{lhs} Expr_op \rightarrow_{lhs} Expr_base$$

Substitute indirect non-terminal closer to initial non-terminal

Next time: algorithms for syntactic analysis

- Continue with our top down parser.
 - Backtracking
 - Lookahead sets