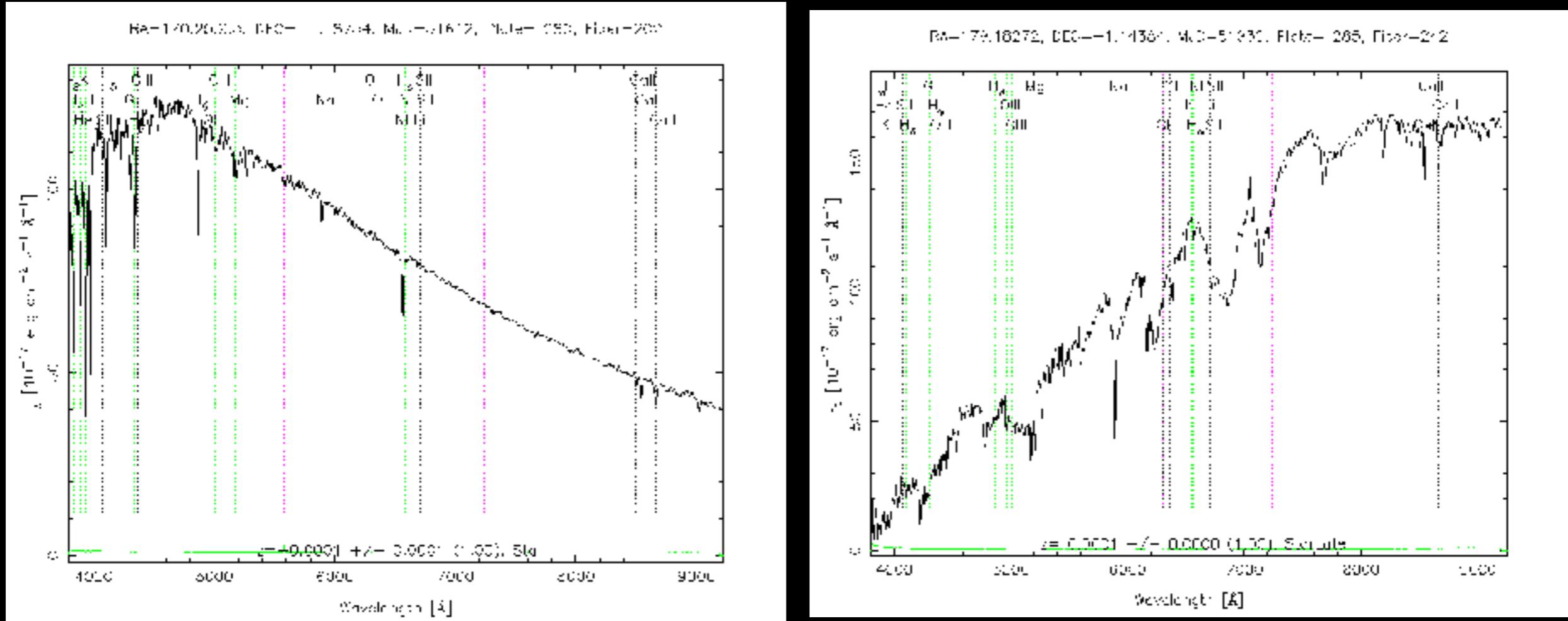


Abstracts

- Everyone present theirs...

Spectroscopy



Gratings

- If every point on a wavefront acts like a source, why don't we see radiation everywhere in space?
- off-axis, phases add up sometimes with positive phase, sometimes with negative phase
- What would happen if we blocked everywhere radiation added up out-of-phase?
- This is a diffraction grating

Reflection Grating/Blaze

- If we blocked half the light, that would make us sad
- Gratings in general have many sidelobes, called “orders”. Light in other orders also makes us sad
- Instead, can etch lines in a mirror, reflect off that
- More efficient, puts signal (mostly) in one order. Surface figure (the “blaze”) distributes how power goes into orders.

Spectral Resolution

- Say I use CCD to measure spectrum. What is the narrowest line I can see?
- Usually referred to as R, spectral resolution, $\lambda/\delta\lambda$
- How would you want spectrograph to behave if you had a 4k chip?

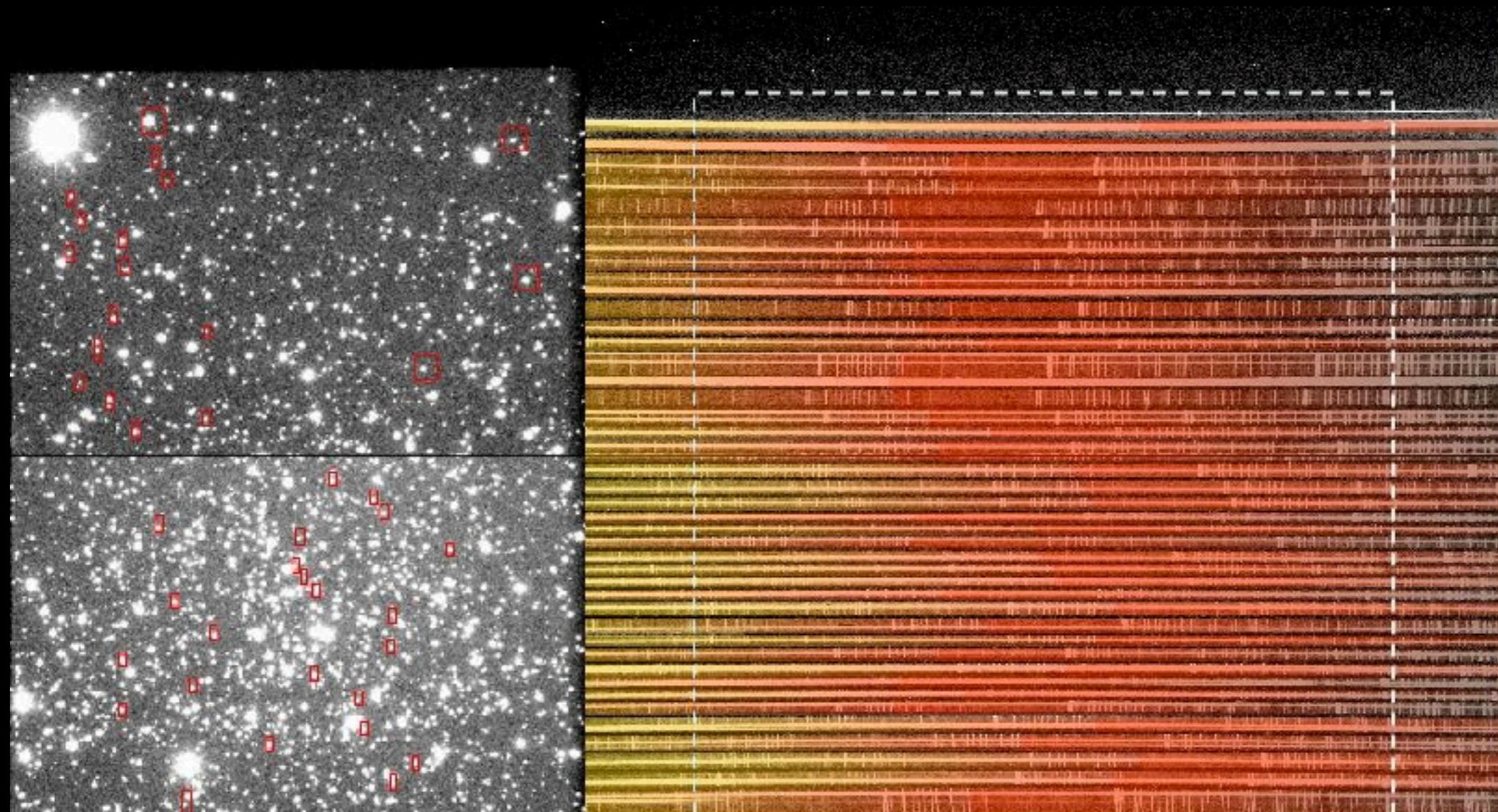
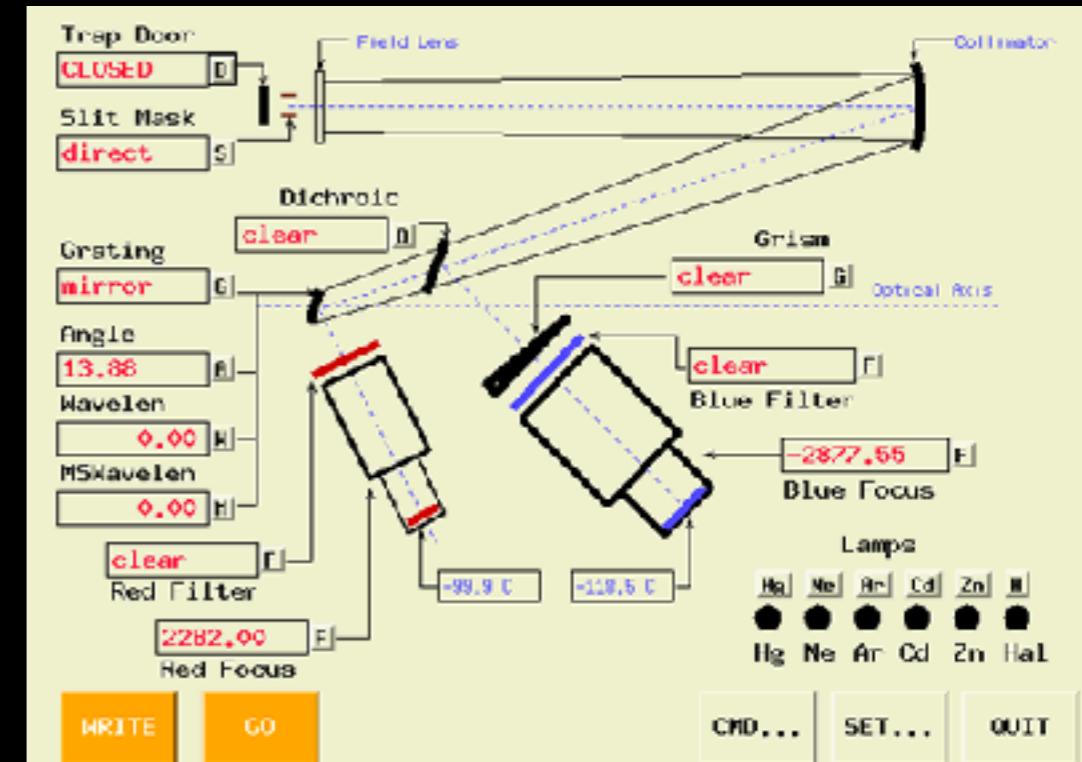
Spectral Resolution

- Say I use CCD to measure spectrum. What is the narrowest line I can see?
- Usually referred to as R, spectral resolution, $\lambda/\delta\lambda$
- How would you want spectrograph to behave if you had a 4k chip?
 - As usual, want to Nyquist sample. For fixed spectrograph, if seeing gets worse, star image will get fuzzier. Limit would be ~2k resolution elements.

Classical Slit Spectroscopy

- If you want one or a few objects, send light onto grating, take picture with CCD
- Often make a mask that covers focal plane with slits. Each slit can be put on object.

Keck LRIS



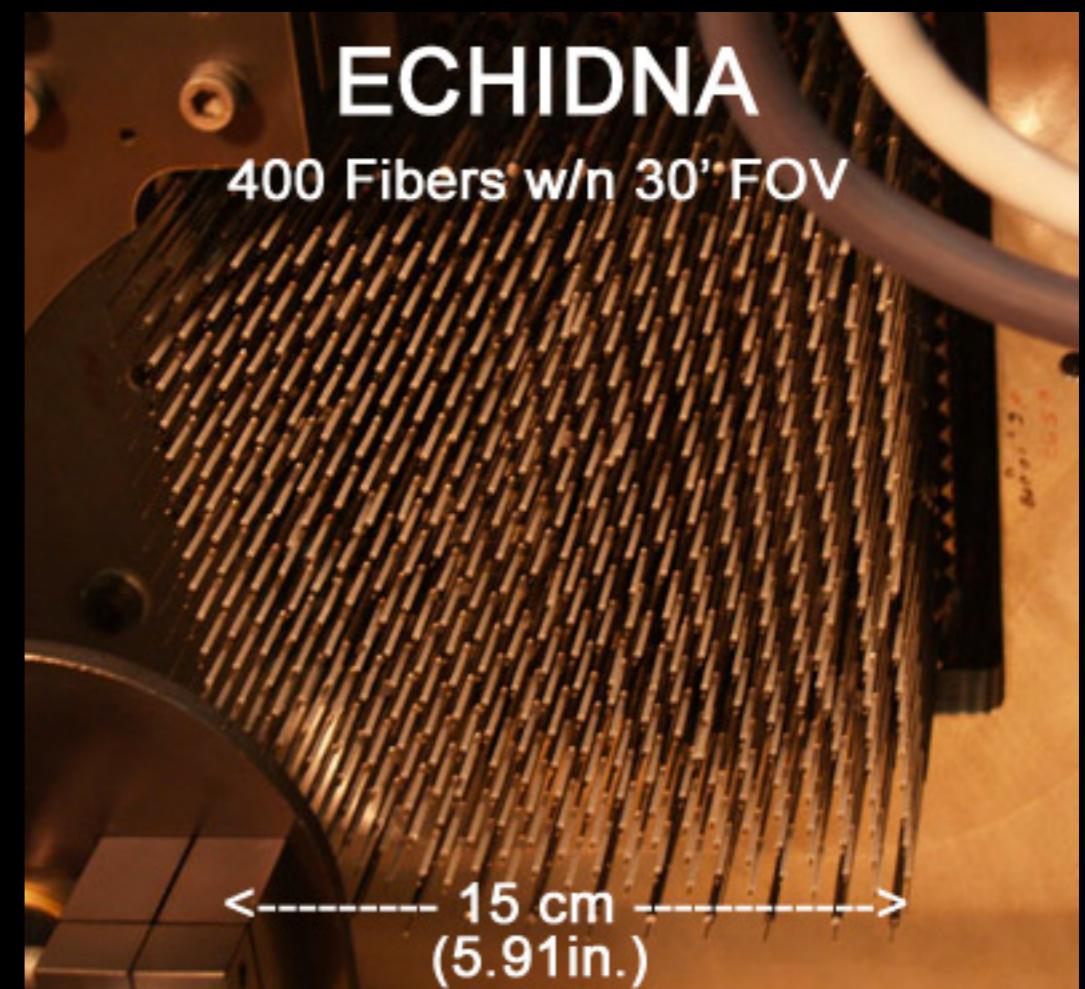
Sky Subtraction

- For faint sources, the sky will be brighter than the source.
- Sky has many lines that are spatially and temporally variable.
- Slit should be larger than source so you can fit night sky signal and subtract off.

Fiber Spectroscopy

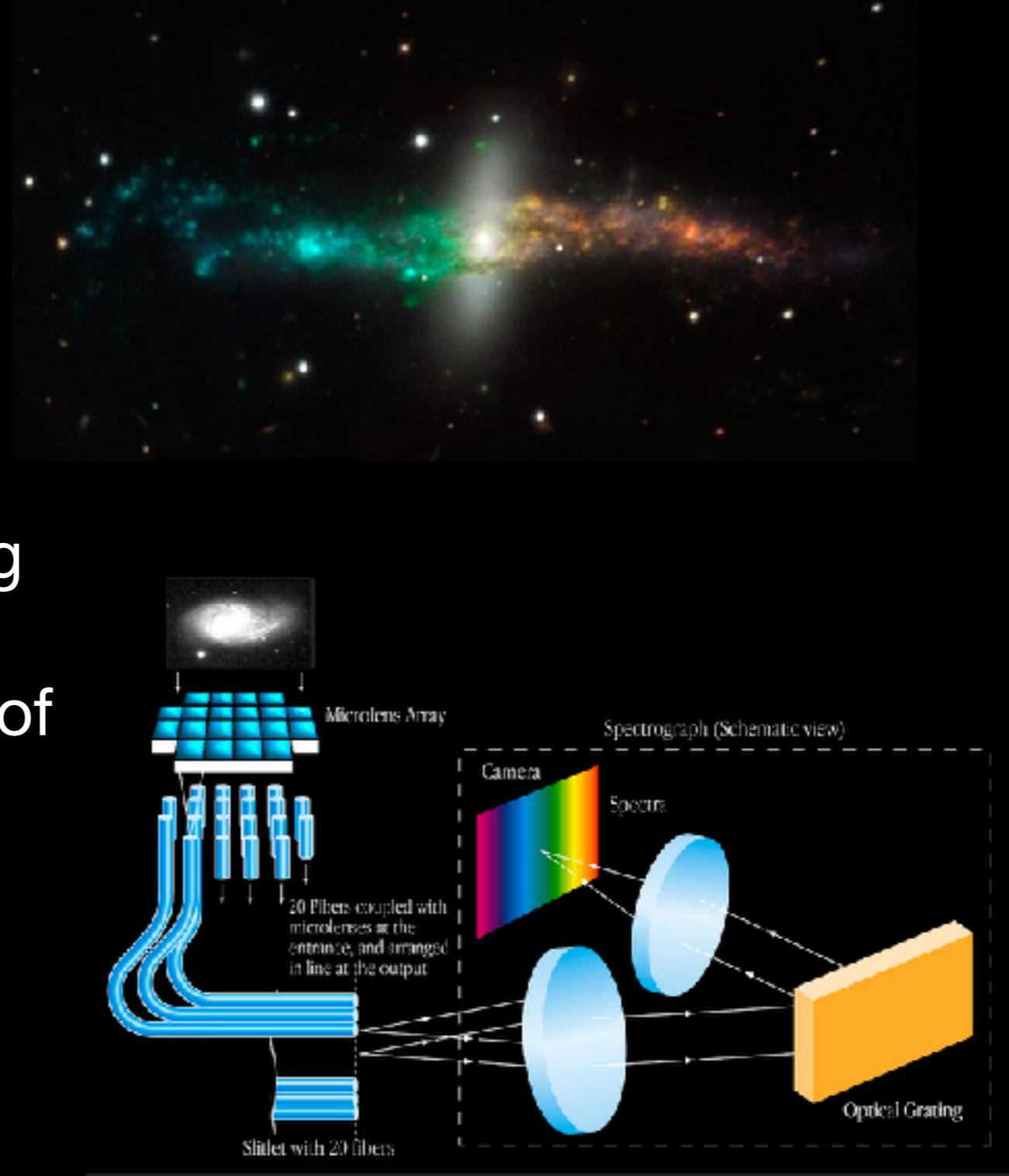
- Rather than making slits, can also use optical fibers
- Position fibers where desired sources will be.
- Can do this with plates, but robots are now usually used.

Top: fiber plug plate on SDSS
Bottom: Fiber robot for FMOS instrument on Subaru



IFU

- Integral field units a way of taking spectra over area - say for mapping out velocity dispersion of face-on galaxy.
- Variety of techniques, including lenslets into fibers.
- Top: MUSE (VLT) image, bottom: instrument schematic

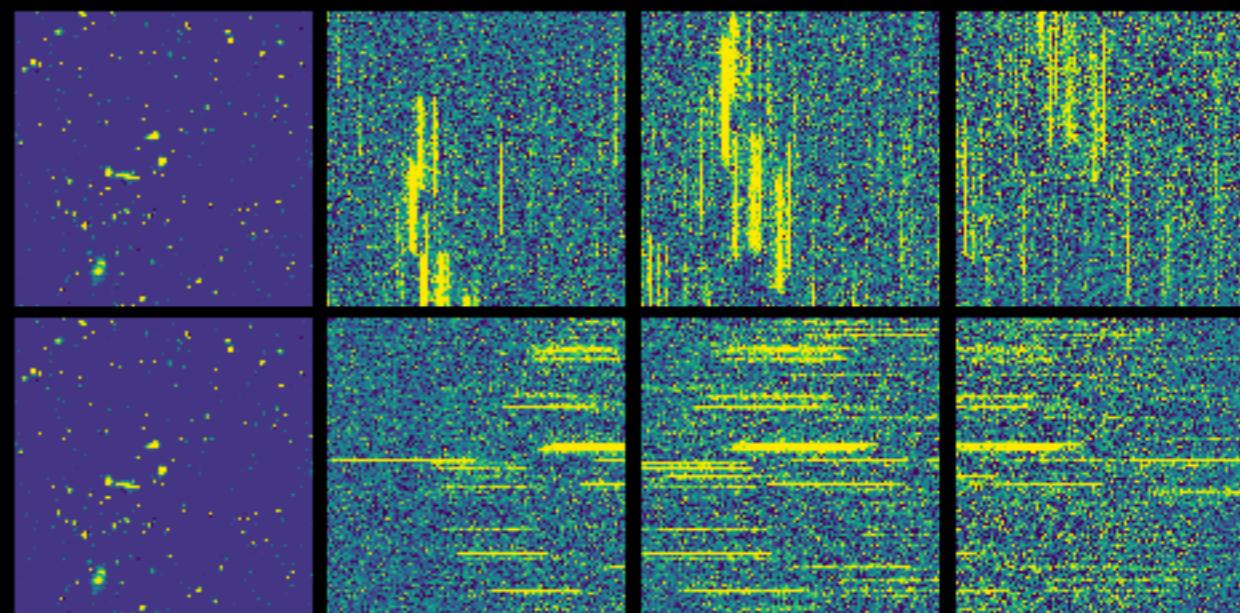
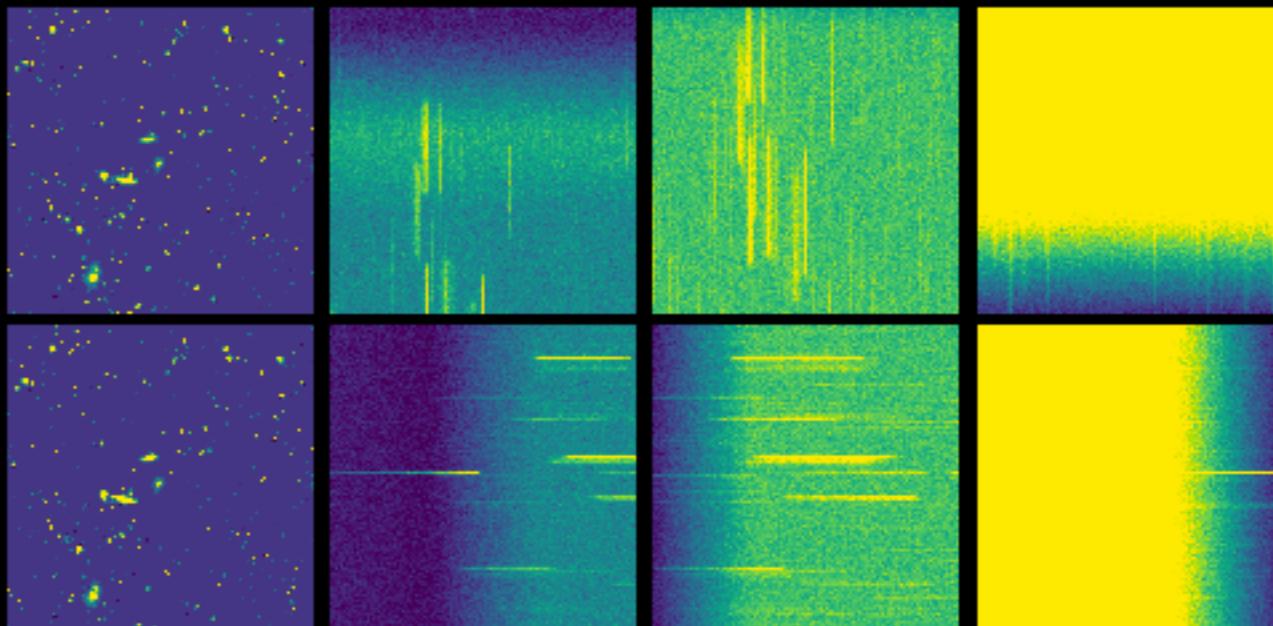


Grism

- Can do hundreds to thousands of spectra with fibers/IFUs.
- Alternatively, can put a grating+prism (“grism”) that spreads out light but leaves reference frequency unchanged.
- Can take spectra of every point in a large field. Downside
 - each pixel sees different frequencies from different points on sky.

NIRCam simulations

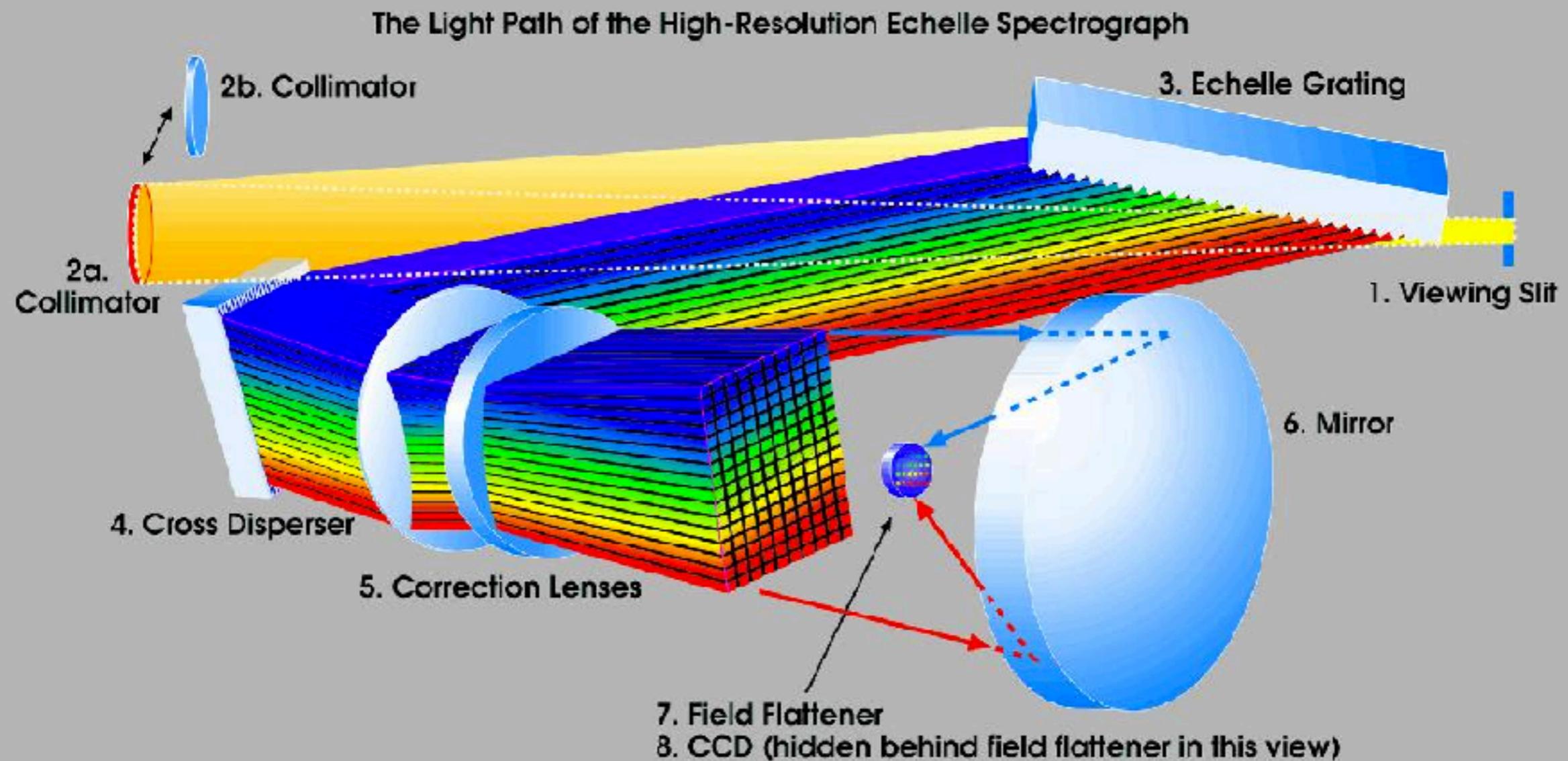
- What grism data can look like
- Can take multiple directions to try to break sky/frequency degeneracy.
- Could I get good spectrum at every map pixel this way?
 - No - two directions gives two bits of information per pixel. Could do more rotation angles



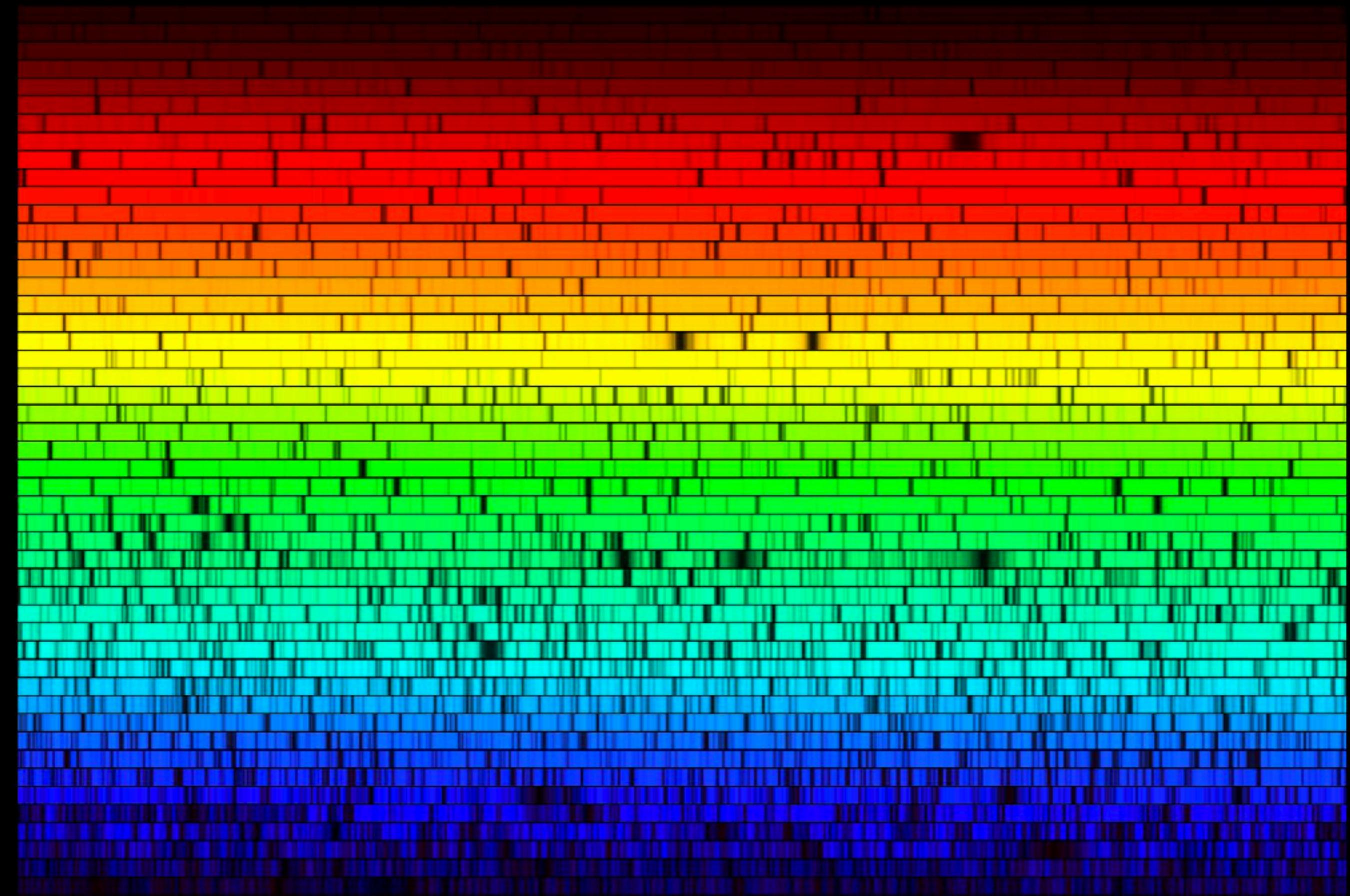
High Resolution

- If I want to measure radial velocity from a planet, what R would I need?
- Take hot jupiter - $M=1e-3$ solar masses, $R=0.4$ AU
- Typical scale 10s of m/s. Lower for habitable planet
- $c/10$ m/s=30,000,000. Need much higher resolution than simple grating will usually give us.
- Solution - echelle. Coarse grating in one direction that stacks up many orders on top of each other. Fine grating in other direction to spread them out.

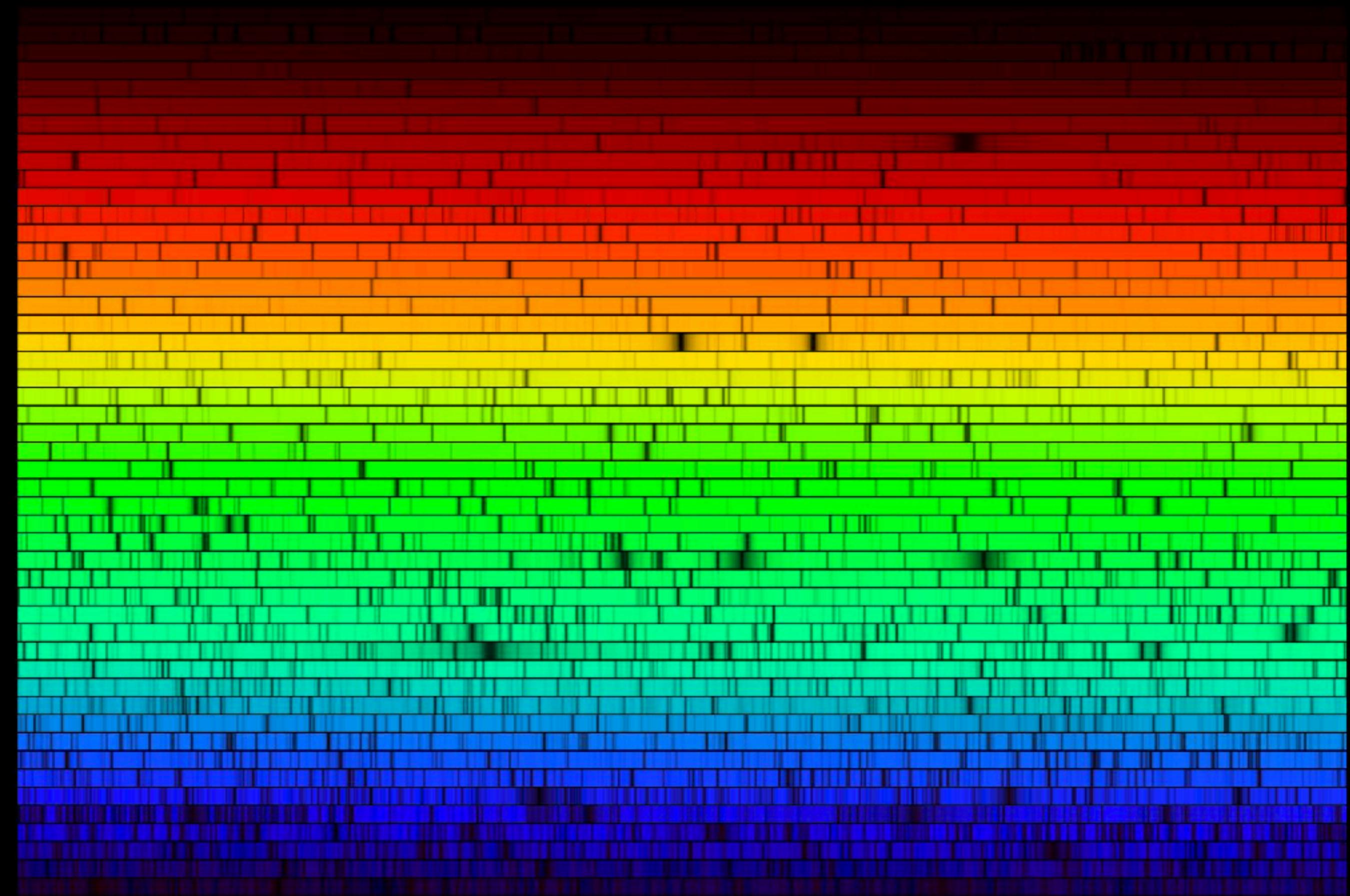
Keck HI-RES



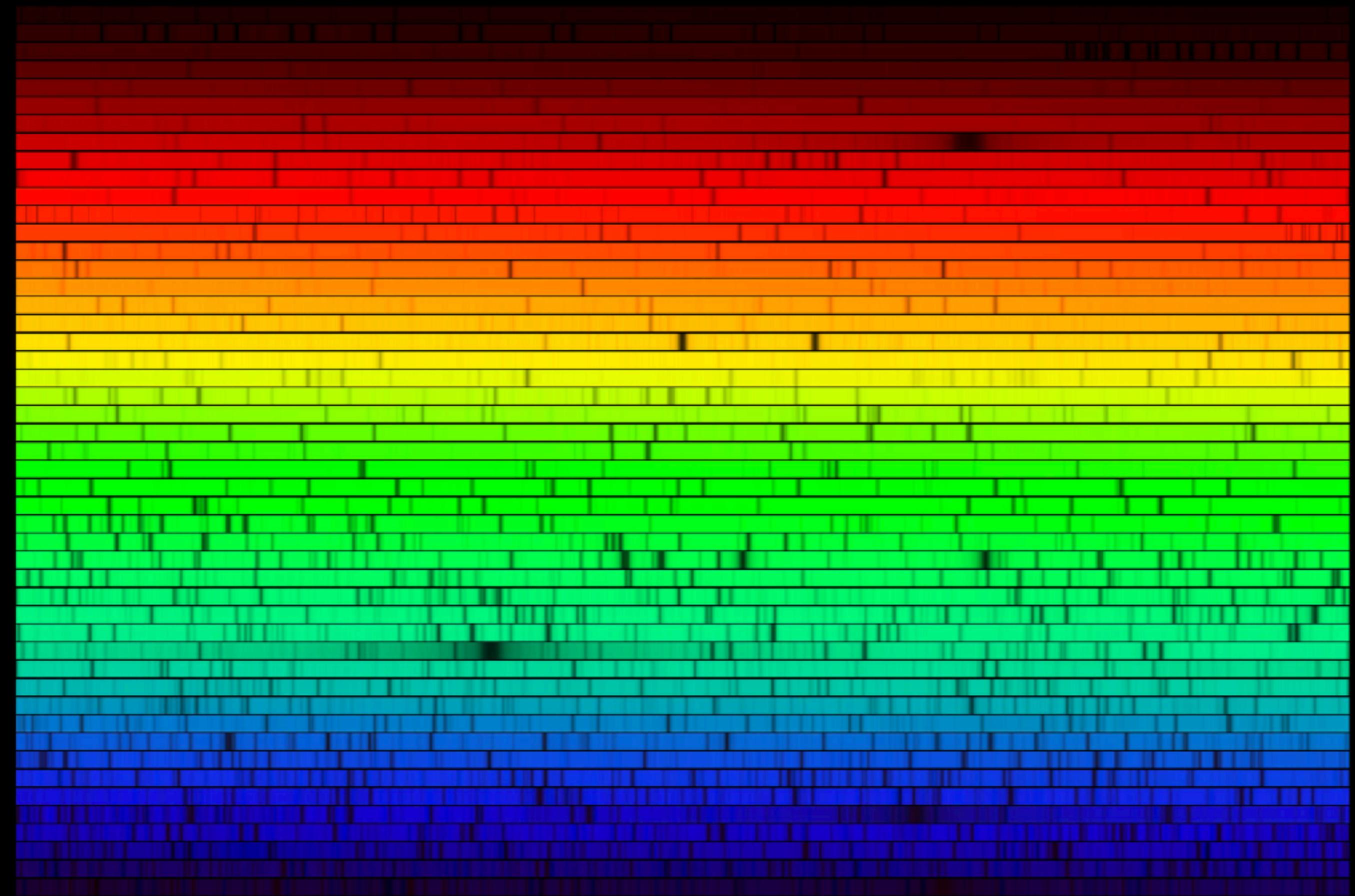
Arcturus



Sun

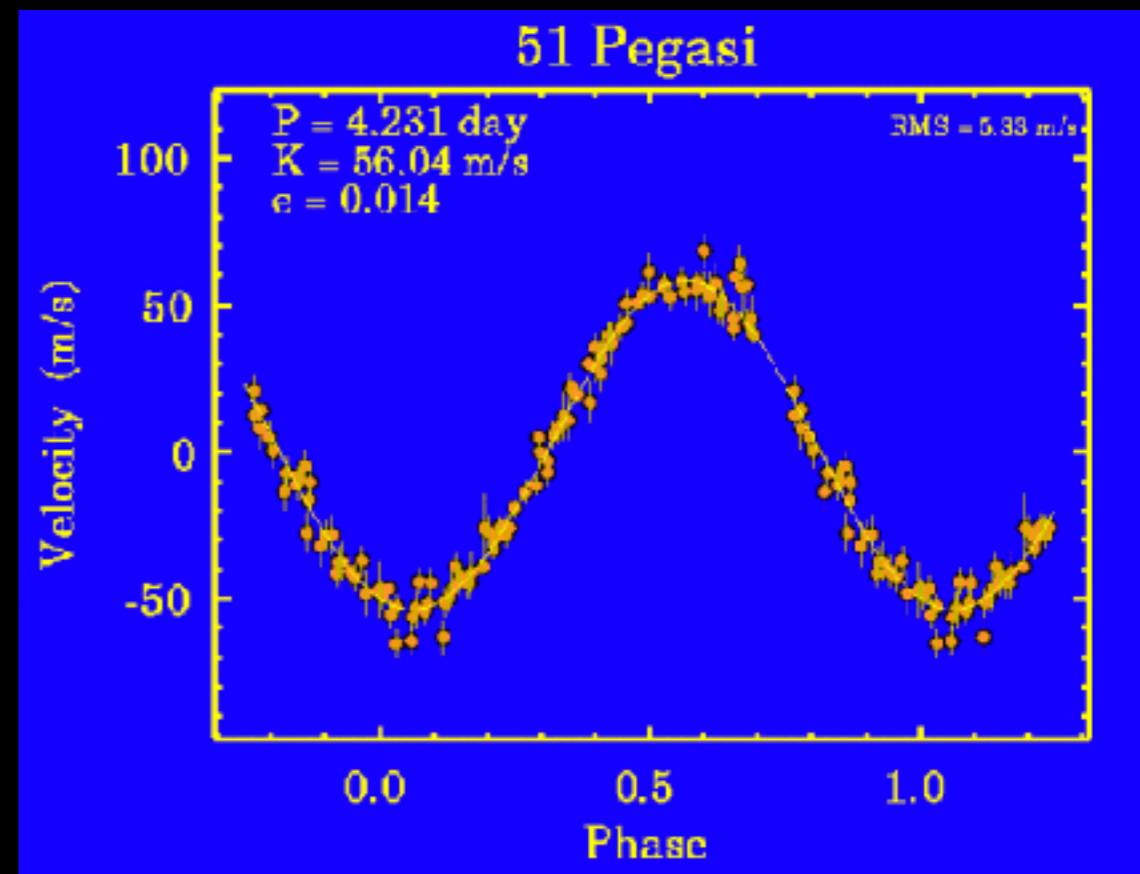


Procyon



How would you find a planet?

- Native spectral resolution of high resolution spectroscopy $\sim 1\text{e}5$. Need a factor of 300 more.
- If you have many lines at high SNR could centroid shifts to R^*SNR
- Reference important as well - e.g. use iodine lamps (which have lots of lines).



Why are Metals Shiny?

- Moving on...
- Because they conduct.
- So why can we see through sea water?
- Well, sometimes we can't. Radio doesn't make it through.

Plasma Frequency

- Say I have a block of plasma, and move all electrons by x . What is electric field?
- Surface charge is $en_e x$. From Gauss's law, $E = en_e x / 2\epsilon_0$, where factor of 2 is from 2-sided cylinder.
- Of course, have protons have charge, so total field is $en_e x / \epsilon_0$.
- $F = qE = -e^2 n_e x / \epsilon_0$. also $F = ma = mx''$, so $x'' = -(e^2 n_e / m_e \epsilon_0) x$
- Plasma will oscillate with angular frequency $\omega_p = \sqrt{(e^2 n_e / m_e \epsilon_0)}$.

Dispersion Relation

- If I send an EM wave into plasma, plasma can adjust if low frequency, not if high frequency.
- Dispersion relation is $\omega^2 = \omega_p^2 + k^2 c^2$.
- Phase velocity is $\omega/k = c(1 + \omega_p^2/k^2 c^2)^{1/2}$, $> c$
- Group velocity $d\omega/dk = kc^2/(\omega_p^2 + k^2 c^2)^{1/2}$, $< c$

Low Frequency

- Recall wave equation is $\exp(i(kx-\omega t))$. If $\omega < \omega_p$, $k = (\omega_p^2 - \omega^2)^{1/2}i/c$ and spatial part of wave equation is $\exp(-kx)$
- Wave decays exponentially with decay length $c/(\omega_p^2 - \omega^2)^{1/2}$
- Limit is c/ω_p , the plasma skin depth.
- What is skin depth of typical conductor?
- Other effects (like collisions) become important in real media, e.g. submarines can communicate underwater at very low (few kHz) frequencies.

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- Limit is c/ω_p , the plasma skin depth.
- What is skin depth of typical conductor?
 - copper atomic wt. is 63.5, density is 9. If 1 e⁻ per atom, then $\omega_p = 1.6e16$, and skin depth is ~200 Å.
 - NB - sea water has ions instead of electrons, and only ~2% vs. H₂O, so simple plasma model would put frequency at ~1e12, skin depth of 0.3mm.
- Other effects become important in real media, e.g. submarines can communicate underwater at very low (few kHz) frequencies.

High Frequency

- Group velocity $d\omega/dk = kc^2/(\omega_p^2 + k^2c^2)^{1/2}$
- For large ω , $kc \gg \omega_p$, and $v_g \sim kc^2/kc(1 + \omega_p^2/k^2c^2)^{1/2} = c(1 - \omega_p^2/2k^2c^2)$
- But, $kc \sim \omega$, so $v_g/c = 1 - \omega_p^2/2\omega^2$.
- If I had 1 e/cm³ for 1 pc, how long would a 1 MHz signal be delayed relative to high frequency?

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- But, $kc \sim \omega$, so $v_g/c = 1 - \omega_p^2/2\omega^2$.
- If I had 1 e/cm^3 for 1 pc, how long would a 1 MHz signal be delayed relative to high frequency?
 - $\omega_p \sim 56 \text{ kHz}$ / $\nu_p \sim 9 \text{ kHz}$. Fractional velocity change is $0.5 * (9 \text{ kHz}/1 \text{ MHz})^2 = 4e-5$. Light travel time is 3.26 years, so total delay is $4e-5 * 3.26 = 4150$ seconds.
 - Origin of pulsar delay law that $dt = 4150 * DM/v^2$ where v in MHz and DM defined to be column density of electrons relative to $1/\text{cm}^3$ for 1 pc.

Waves in Plasma/Why Metals Reflect

- If free space wave hits plasma, if frequency below plasma frequency wave can't propagate, gets reflected by plasma.
- If above v_p , wave can go through, with group velocity $< c$, phase velocity $> c$.
- Metals have $v_p \sim 2 \times 10^{15} \text{ Hz} \sim 10 \text{ eV}$. Optical photons reflect, but hard UV/x-rays will go through.
- If I want to build an X-ray telescope, I can't use traditional mirrors.

Refraction

- If I have a wave propagating at some angle going between two different media, what happens?
- Wave phase has to be continuous across boundary.
- Wave will bend so that phase velocity along boundary is same on both sides.
- Phase velocity vs. free space is inverse of index of refraction, n .
- Snell's law is phase continuity constraint: $\sin(\theta_1)n_1=\sin(\theta_2)n_2$.

Total Internal Reflection

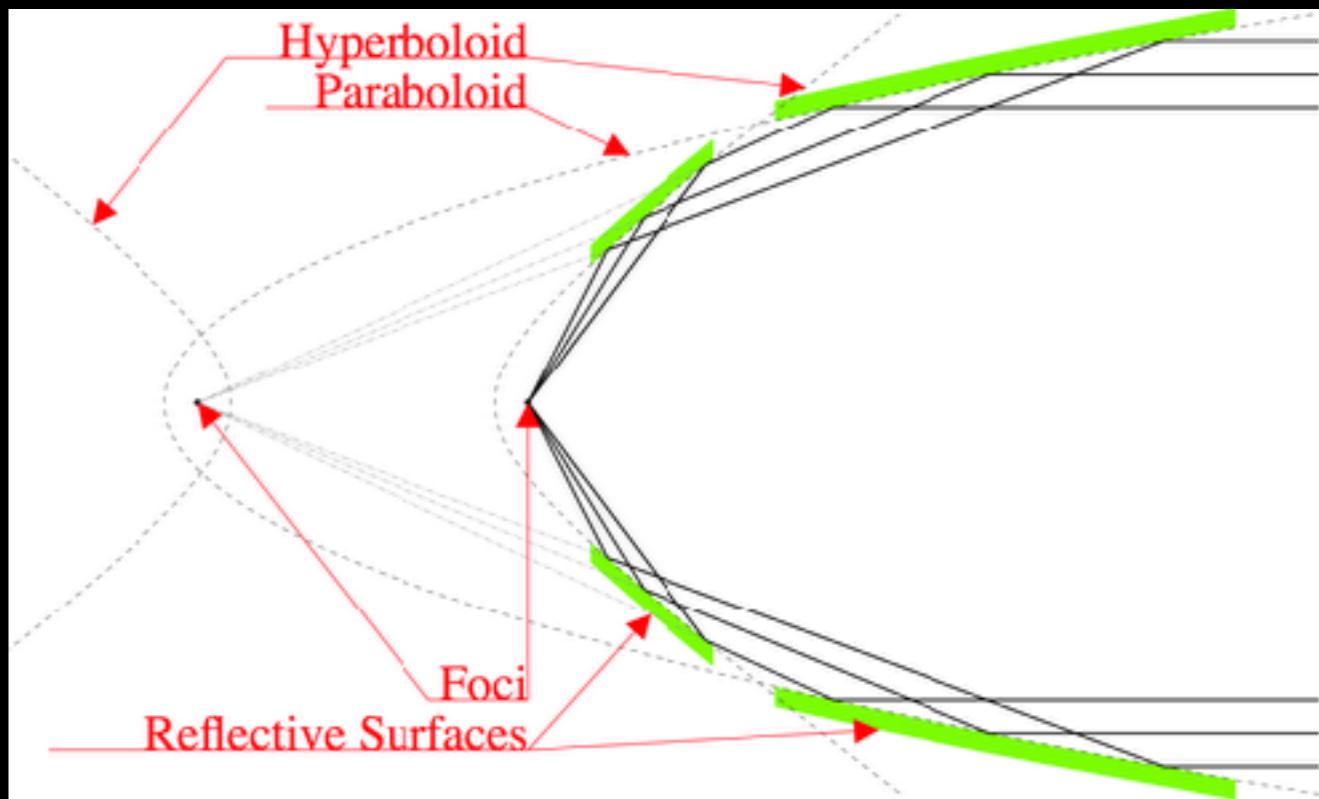
- $\sin(\theta_2)$ can't be larger than 1. So, $\sin(\theta_1) < n_2/n_1$.
- If $n_2 < n_1$, then there's a critical angle at which we can no longer go through. Instead, wave reflects.
- This is called total internal reflection.
- Only happens if we go from medium with low phase velocity to medium with high phase velocity.

Grazing Incidence

- What is index of refraction of metals at 1 keV?
- phase velocity= $c(1+\omega_p^2/k^2c^2)^{1/2}$, $\sim c(1+v_p^2/v^2)^{1/2}$, $v_p/c \sim 1 - 0.5(v_p/v)^2$.
- Index of refraction $\sim 1 - 0.5(v_p/v)^2$.
- At 1 kHz, $n \sim 1 - 0.5(10/1000)^2 = 1 - 5e-5$ Critical angle is $\arcsin(1-5e-5) \sim 89.5$ degrees.
- So, if X-ray comes in within half degree of parallel, it will reflect. This is *grazing incidence*.

X-ray Telescope Design

- Turns out FOV is tiny for single grazing incidence mirror.
 - Solution is to have multiple element to correct coma.
 - Few different designs possible (Wolter types 1-3)
 - To get collecting area, have to stack many elements.



Top: Wolter type 1 diagram
Bottom: Chandra primary mirror