

Chapter 3 General Principles in Simulation

Banks, Carson, Nelson & Nicol
Discrete-Event System Simulation

Concepts In Discrete-Event Simulation



- **System**
 - A collection of entities (people and machines..) that interact together over time for one or more goals
- **Model**
 - An abstract representation of a system, usually containing structural, logical or mathematical relationship that describe a system in term of state, entities and their attributes , sets, processes,...
- **System state**
 - A collection of variables in any time that describe the system
- **Entity**
 - Any object or component in system that require explicit representation (server, customer,...)
- **Attributes**
 - The properties of a given customer
- **List**
 - A collection of associated entities , ordered in some logical fashion (FIFO, priority,...)

Concepts In Discrete-Event Simulation (cont.)

- Event
 - An instantaneous occurrence that changes the state of a system
- Event Notice
 - A record of a event to occur at the current or future time (type and time)
- Event List
 - FEL (future event list)
- Activity (unconditional wait)
 - A duration time of specified length (service time or interarrival time,...)
 - Deterministic, Statistical and functional
- Delay (conditional wait)
 - A duration of time of unspecified indefinite length, which is not known until it ends (customer delay in waiting line)
- Clock
 - A variable representing simulated time

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Able-Baker Call center

- System state
 - $LQ(t)$: the number of callers waiting to serve
 - $LA(t)$: 0 or 1 indicate Able is idle or busy
 - $LB(t)$: 0 or 1 indicate Baker is idle or busy
- Entities
 - Caller
- Events
 - Arrival event, service completion by Able or Baker
- Activities
 - Service time by Able/Baker and Inter-arrival time
- Delay
 - A caller wait in queue until Able or Baker becomes free

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Event scheduling

- How does each event affect system state, attributes?
- How activities are defined (deterministic, probabilistic,...)?
- Which events trigger the beginning of each delay?
- What is system state at time 0?

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Event scheduling (cont.)

Clock	System state	Attributes	Future Event List (FEL)	Cumulative statistics and counters
t	(x,y,z, ...)		(3,t1) (1,t2) ... (4,tn)	

$T_1 < t_2 < \dots < T_n$

FEL is ordered by event time

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Event scheduling/Time-advance algorithm

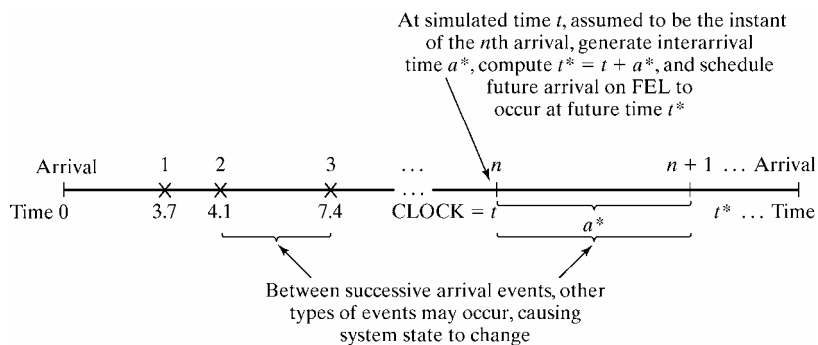
Clock	System state	...	Future Event List (FEL)
t_0	(5, 1, 6...)		(3, t_1) (1, t_2) (5, t_3) ... (4, t_n)

■ $t_2 < t^* < t_3$

Clock	System state	...	Future Event List (FEL)
t_1	(5, 1, 5...)		(1, t_2) (5, t_3) ... (4, t_n)

Clock	System state	...	Future Event List (FEL)
t_1	(5, 1, 5...)		(1, t_2) (4, t^*) (5, t_3) ... (4, t_n)

Generation Arrival Stream by Bootstrapping



The stop time of simulation

- AT time 0 the simulation stop time is specified, T_E
- Run length TE is determined by the simulation itself.
 - The time of occurrence of some specified events

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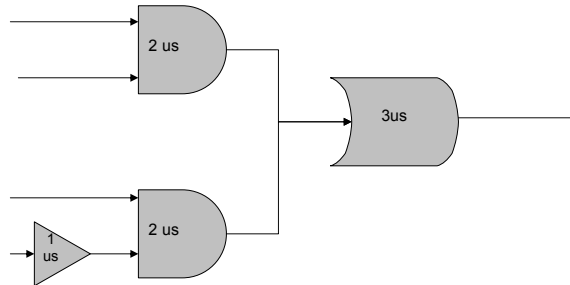
World views of Model for simulation (Three Types)

Polling And Interrupt

- Event-scheduling world view
 - We concentrate on events and their effects on system
- Process-interaction world view (like processes in OS)
 - We define the model in terms of entities or objects and their life cycle of an entity
 - It has intuitive appeal and allow to describe the process flow in terms of high level block or network constructs
 - Event scheduling is hidden
 - Both use a variable time advance (clock is advanced to next imminent event)
- Activity scanning world view
 - Use fixed time increment and rule based approach to decide which activity can begin
 - At each clock advance the conditions for each activity are checked and if they are true then corresponding activity begins
 - It is suitable for small system
 - It is very fast

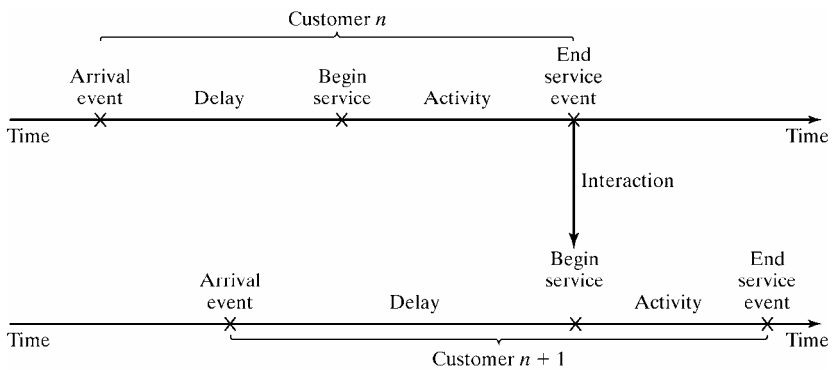
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Activity scanning example (Gate simulation)



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Two customer processes interaction in single server queue



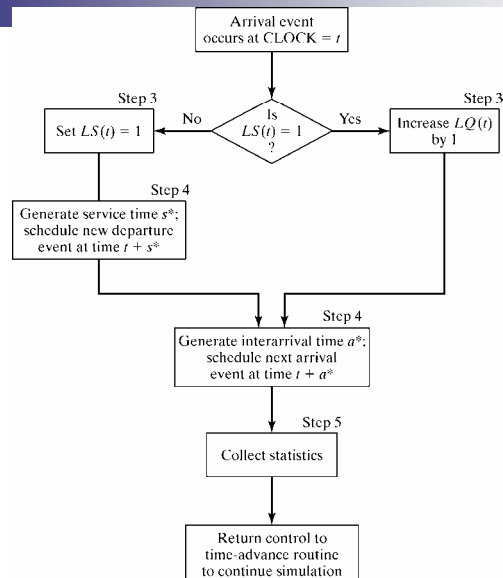
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Event Scheduling example (Grocery Center)

- System State
 - $LQ(t), LS(t)$
- Entities
 - The server and customer are not explicitly modeled
- Events
 - Arrival (A), Departure (D), Stopping event ($E=60$)
- Event notices
 - $(A,t), (D,t), (E,60)$
- Activities
 - Inter-arrival time, service time
- Delay
 - Customer time spent in waiting time

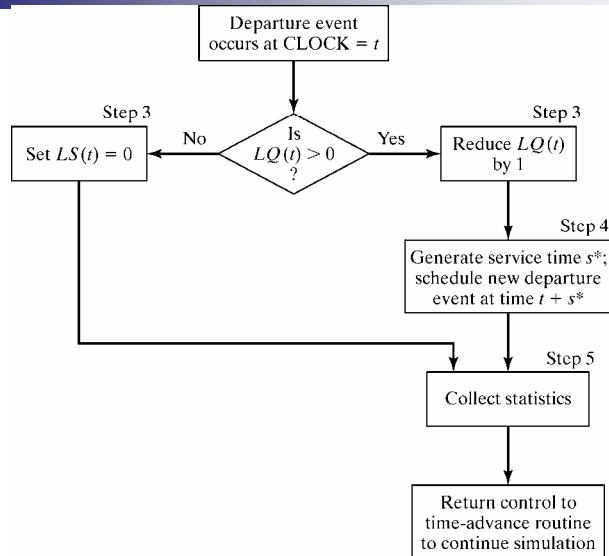
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Execution of the arrival event



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Execution of the departure event



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Simulation Table

clock	System state		Future Event List	Comment	Cumulative Statistics	
	LQ(t)	LS(t)			B	MQ
0	0	1	(A,1)(D,4)(E,60)	First A occurs (a*=1) schedule next A (s*=4) schedule first D	0	0
1	1	1	(A,2)(D,4)(E,60)	Second A occurs:(A,1) (a*=1) schedule next A (Customer delayed)	1	1
2	2	1	(D,4) (A,8)(E,60)	Third A occurs:(A,2) (a*=6) schedule next A (Two customer delayed)	2	2
4	1	1	(D,6) (A,8)(E,60)	First D occurs:(D,4) (s*=2) schedule next D (Customer delayed)	4	2
6	0	1	6	2

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Computing Mean Response Time (cont.)

- Entities
 - (C_i, t) , representing customer C_i who arrive at time t
- Event notices
 - (A, t, C_i) , the arrival of customer C_i at future time t
 - (D, t, C_j) , the departure of customer C_j at future time t
- Set
 - "CHECKOUT LINE" the set of all customers currently at the checkout counter, ordered by time of arrival
- Response time
 - CLOCK TIME-attribute "time of arrival"
- S : sum of customer response time
- N_D : all number of customers that currently are departure
- F : Total number of customers that spend more than 5 minutes in system

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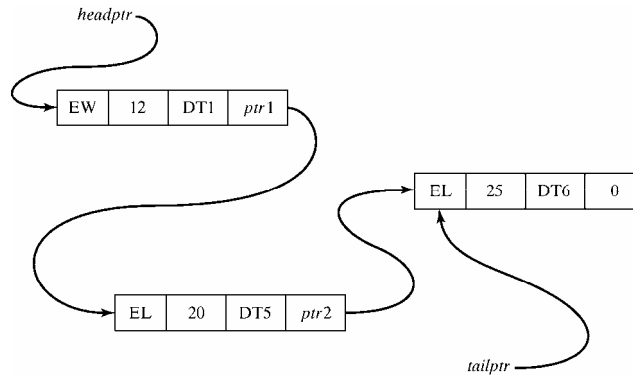
Simulation Table

clock	System state		CHECKOUT LINE	Future Event List	Cumulative Statistics		
	LQ(t)	LS(t)			S	N_D	F
0	0	1	(C1,0)	(A,1,C2)(D,4,C1)(E,60)	0	0	0
1	1	1	(C1,0)(C2,1)	(A,2,C3)(D,4,C1)(E,60)	0	0	0
2	2	1	(C1,0)(C2,1) (C3,2)	(D,4,C1) (A,8,C4)(E,60)	0	0	0
4	1	1	(C2,1) (C3,2)	(D,6,C2) (A,8,C4)(E,60)	4	1	0
6	0	1	9	2	1

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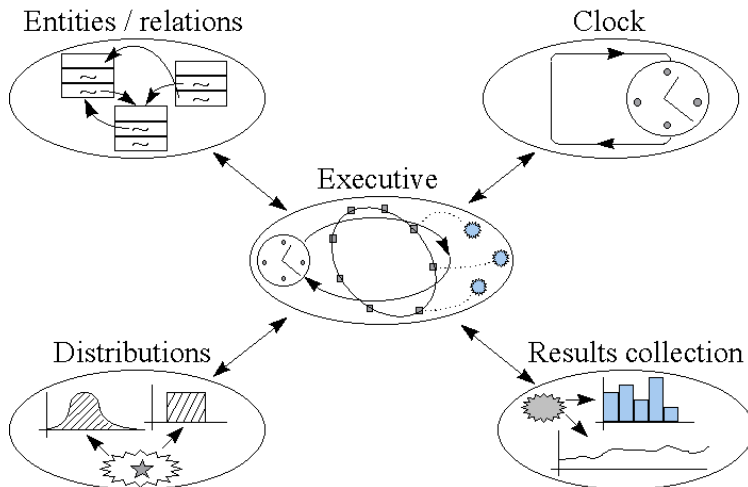
List Processing

- List processing is base of event management in event and process orientation systems.



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Structure of a simulation system



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Event Scheduling Example

