

Hands on 2

② Argue correctness of selection sort.

SELECTION-SORT(A, n)

for $i = 0$ to $n-2$:

$\text{min} = i$

 for $j = i+1$ to $n-1$:

 if $A[j] < A[\text{min}]$:

$\text{min} = j$

$\text{swap}(A[i], A[\text{min}])$

At the start of each iteration, the first i elements of the array are the smallest i elements in sorted order.

Base case ($i=0$), initially the sorted portion is empty. The algorithm finds the smallest element in the array and places it at index 0.

Assuming that after i iterations, the first i elements are correctly sorted.

At the $(i+1)$ th iteration, the algorithm finds the smallest element in the unsorted portion element placed at $A[i]$ ($A[i]$ to $A[n-1]$)

this holds for all i ,
means the selection sort correctly sorts
the array.

After the $n-2$ iterations, the outer loop
terminates, the array is fully sorted,
and the algorithm terminates.

Hence, Selection sort is correct.