

$$b) \mathcal{L}[\ddot{x} + 2\dot{x} + 5x = 10] = s^2 x + 2sx + 5x = \frac{10}{s}$$

$$x(s^2 + 2s + 5) = \frac{10}{s}$$

$$x = \frac{10/s}{s^2 + 2s + 5} = \frac{2}{s} - \frac{2s + 4}{s^2 + 2s + 5}$$

$$\mathcal{L}^{-1}[X(s)] = 2 - e^{-t} \left( (\cos(2t) + \frac{\sin(2t)}{2}) \cdot 2 \right)$$

$$c) \mathcal{L}[\ddot{y} + 3\dot{y} + 5y = 1] = s^2 Y(s) + s^2 \cdot 3Y(s) + s \cdot 5Y(s) + 1$$

$$\mathcal{L}[\ddot{x} + 4\dot{x} + 6x = 8] = s^2 X(s) + s^2 \cdot 4X(s) + s \cdot 6X(s) + 8$$

$$\frac{Y(s)}{X(s)} = \frac{s^3 Y(s) + s^2 \cdot 3Y(s) + s \cdot 5Y(s) + 1}{s^3 X(s) + s^2 \cdot 4X(s) + s \cdot 6X(s) + 8}$$

$$= \underline{\underline{1 + \frac{1}{-s^2 - s - 7}}}$$