

$$1) a) f(s) = \frac{s+3}{(s+1)(s+2)} = \frac{a_1}{s+1} + \frac{a_2}{s+2}$$

$$s+3 = a_1(s+2) + a_2(s+1)$$

$$\text{Set } s = -1$$

$$-1+3 = a_1(-1+2) + a_2(-1+1)$$

$$\underline{a_1 = 2}$$

$$\text{Set } s = -2$$

$$-2+3 = a_1(-2+2) + a_2(-2+1)$$

$$\underline{a_2 = -1}$$

$$\mathcal{L}^{-1}(f(s)) = 2 \cdot \mathcal{L}^{-1}\left(\frac{1}{s+1}\right) + \mathcal{L}^{-1}\left(\frac{-1}{s+2}\right)$$

$$= \underline{\underline{2 \cdot e^{-t} - e^{-2t}}}$$