# How to type-set logic and natural deductions using GNU troff, pic and eqn

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#### Introduction

troff is a software system for type-setting using Unix<sup>TM</sup> and related operating systems (Ossanna and Kernighan, 1994). Brian W. Kernighan was one of the creators of Unix and the C programming language. pic (Kernighan, 1982) and eqn (Kernighan and Cherry, 1975) are systems for typesetting graphs and mathematics, also created by Brian Kernighan and his friends. This group created a full set of tools for the type-setting of scientific text, graphs and diagrams, mathematics, chemistry, reference management and complex tables. GROFF aka GNU troff is the implementation I am using (FSF, 1990). There are other competitors, in particular the slightly younger TeX and LaTeX, I am not able to give you advice on how to use those for logic or science. There are alternative implementations of troff, but the GNU one is the one I have used for 35 years.

These systems are old, but they are readily available for Linux and Apple iOS computers, because they are based on the Unix<sup>™</sup> operating system (guess that you can get them for Windows as well). troff were developed by software developers for software developers, scientists and mathematicians. It is not very difficult to use, just very different from what modern users expect. And you must write your document in a programmer's editor. troff works on shell command lines.

Fitch is a notation for natural deduction (Pelletier and Hazen, 2024). It has got its name after its inventor, Fredric Fitch. This notation seems to be a de facto standard: It is used in all the text books I have been able to find electronically, and seems to be taught at logics courses in mathematics as well as philosophy. I started to write this tutorial while learning Fitch while reading philosophy; my intention is to demonstrate how to write predicate and propositional logic, and deduction on this platform. I cannot teach you how to format scientific text in general (that is large job), neither can I give an introduction to logic and natural deduction (I am not qualified for that).

This document lives in an open project at github.

https://github.com/siglun/logic-and-groff

Feel free to use the snippets of code and examples.

## Writing text and equations

First, we need to be able to write our texts (there is a good tutorial by Kollar and Robinson (2023)) and then we can continue with formulas and sentences using eqn (Harding, 2011). At a first glance, all of them are are "equations", or anyone who are not familiar with mathematics and logic and the differences between the two will regard them as such. Logic is

Table 1. Unicode characters for logical signs and operators. On some operating systems you can type them by pressing ctrl-shift-u and then the four character code (following u+ in the table). The Groff name is usually better to use than the Unicode character, but takes a long time to type. The eqn macros are for easier typing and I have tried to adjust spacings for a nicer look.

Unicode	Character	Groff name	eqn macro	Comment
U+00AC	_	\[no]	not	
U+2227	٨	\[AN]	and	
U+2228	V	\[OR]	or	
U+2200	A	\[fa]	any	
U+2200	A	\[fa]	forall(x)	
U+2203	3	\[te]	some	
U+2203	3	\[te]	exists(x)	
U+2192	$\rightarrow$	\[->]	implies	
U+2194	$\leftrightarrow$	\[<>]	iff	
U+2194	$\leftrightarrow$	\[<>]	equiv	
U+21D4	⇔	\[hA]		
U+22A5	1	\[pp]	falsum	
U+22A2	F	\[/-]	vdash†	syntactic consequence, turnstile requires font support*
U+22A2	<b>-</b>	\[/-]	entails†	
U+22A8	F	\[/]	vDash†	semantic consequence, double turnstile requires font support*
U+22A8	F	\[/]	satisfies†	
U+2261	=	\[==]	identicalto	
U+25A1		\[sq]	nece	
U+25A1		\[sq]	necessarily	
U+25C7	$\Diamond$	\[lz]	possi	
U+25C7	$\Diamond$	\[lz]	possibly	
U+2234	:.	\[tf]	therefore	
U+2205	Ø	\[es]	empty	
U+2208	€	\[mo]	member	
U+2209	∉	\[nm]	notmember	
U+2286	⊆	\[ib]	subset	
U+2118	80	\[wp]	powerset	

<sup>\*)</sup> I use the math font from Scientific and Technical Information Exchange (STIX) font creation project https://www.stixfonts.org/

actually a special genre of its own when it comes to formulas or equations.

To write these formulas, you need to use either the unicode characters, their Groff names or macros I have defined in order to simplify typing. See Table 1.

 $<sup>\</sup>dagger$ ) These operators are names used in eqn only. vdash and vDash are used in TeX/LaTeX for  $\vdash$  and  $\vDash$  respectively. I have also added the operators entails and satisfies because I feel that I can remember them and their functions.

Here is a set of predicate logic sentences, first in eqn source,

```
.EQ (1)
  pile {
    forall(x) SameSize(x)
    above
    forall(x) Cube(x) implies Cube(b)
    above
    (Cube(b) and b=c) implies Small(c)
    above
    (Small(b) and SameSize(b,c) implies Small(c)
  }
.EN
```

and then formatted, in Equation (1).

$$\forall x \ SameSize(x)$$

$$\forall x \ Cube(x) \rightarrow Cube(b)$$

$$(Cube(b) \land b = c) \rightarrow Small(c)$$

$$(Small(b) \land SameSize(b, c)) \rightarrow Small(c)$$

$$(1)$$

## Using logics in tables and graphs

See Table 2 and Figure 1. These things are here just for demonstrating how typographic elements can be combined.

Table 2. Some useful equivalents if you are doing logic. They are presented here as an example how you can embed formulas in a table.

Assertion of Universality	$\forall x Ax \leftrightarrow \neg \exists x \neg Ax$	If everything is, there exists nothing that is not.
Denial of Universality	$\neg \forall x Ax \leftrightarrow \exists x \neg Ax$	If not everything is, there exists something that is not.
Denial of Existence	$\forall x \neg Ax \leftrightarrow \neg \exists x Ax$	If everything is not, there exists nothing that is.
Assertion of Existence	$\neg \forall x \neg Ax \leftrightarrow \exists x Ax$	If not everything is not, there exists something that is.

## Writing Fitch arguments

Authoring natural deduction is similar to embedding formulas in a graph, as demonstrated in Figure 1.

Any proof is initialized by calling this macro, which informs all scripts on the number of steps in the proof and its maxiumum depth, i.e., how deep the hierarchy of proofs is. That is, how many inside proofs, whitin proofs ... do we have. You better add one or the references at the right will come to close to the logical statements.

```
set_steps_and_depths(8,3)
```

Any proof (the root proof or any sub-proof) starts with the start\_proof() macro, which also names that proof. After we have started the proof, we add its premises, and end it with premis\_end().

```
start_proof(START);
```

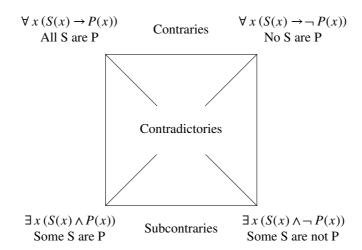


Figure 1. The traditional aristotelian syllogisms, the figure shows how one can embed formulas into a graph.

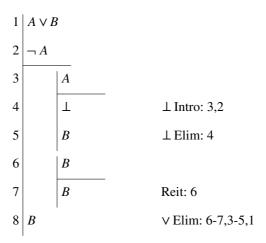


Figure 2. Proof that  $A \vee B$ ,  $\neg A \therefore B$ . The line numbering is in the left-most margin. Then there is a vertical line, as long as the proof. The step 1-2 in the proof is where the premises lives. The horisontal line after step 2 is usually referred to as the *fitch line*. The two groups, 3–5 and 3–6 are subproofs, with their own premises, vertical lines and fitch lines

```
add_premis(START, "$A or B$");
add_premis(START, "$not A$");
premis_end(START);
```

After ending the premiws section, we enter the body of our proofs. In this case we start the sub-proofs

```
start_proof(SUB1);
add_premis(SUB1, "$A$");
premis_end(SUB1);
```

In the body of a proof, we use the add\_step() macro, which has three argument: (i) the name of the current proof, (ii) the result of the step, and finally (iii) the references to earlier steps needed for the step.

```
add_step(SUB1,"$falsum$","\( \text{Intro: 3,2"});
add_step(SUB1,"$B$","\( \text{Elim: 4"});
end_proof(SUB1);
```

We end a proof (be it a sub\_proof or a proof) with the end\_proof() macro, which needs the name of the current proof as an argument. Now we start another subproof.

```
start_proof(SUB2);
add_premis(SUB2,"$B$");
premis_end(SUB2);
add_step(SUB2,"$B$","Reit: 6");
end_proof(SUB2);
```

After we have completed the two sub-proofs, return to the main proof and completes it with a nice  $\vee$  elimination.

```
add_step(START, "$B$", "V Elim: 6-7, 3-5, 1");
end_proof(START)
```

Note that the macros do not check your references. Sanity checks and proof reading is your job. There are two more examples below, in Figure 3–4.

### References

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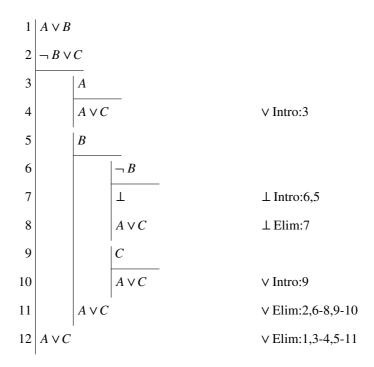


Figure 3. A slightly longer example: Prove that  $A \lor B$ ,  $\neg B \lor C : A \lor C$ .

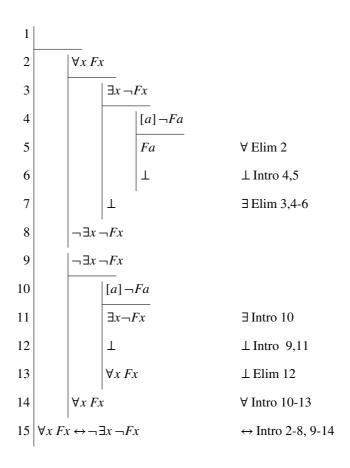


Figure 4. A proof using predicate logic. It proves without premisses one of the de Morgan formulas:  $\forall x \, Fx \leftrightarrow \neg \exists x \, \neg Fx$ , All x are F if and only if there is no x which is not F.

## Github project

Scan QR to get project at https://github.com/siglun/logic-and-groff

