

Miscellaneous Problems in R

Here are some miscellaneous problems in R.

Lists

After all that work with subsetting, let's do something a bit more enjoyable.

- Write a function `nesting_depth(L)` that takes as input a list `L` and returns the nesting depth of `L`. (For example, `nesting_depth(list(1, list(2, 3), list(4, 5)))` would return 2.)

Let's call an n -domino a list with two integers, where both entries are integers from 0 to n inclusive. For example, `list(4,5)` is an n -domino (for any $n \geq 4$).

- Write a function to return a list of every unique n -domino, given n . (Treat `list(a, b)` as being equivalent to `list(b, a)`.)

A valid *circle* of n -dominoes is given by a list of n -dominoes, with the following properties:

- Given two consecutive dominoes `list(n, m)` and `list(p, q)`, where the latter domino is located immediately after the former domino in the circle of n -dominoes, we require that `m == p`.
- The 1st entry of the 1st n -domino is equal to the last entry of the last n -domino.

For example, `list(list(1, 2), list(2, 3), list(3, 1))` is a valid circle of n -dominoes.

- Write a function `is_circle(L)` that returns a logical value corresponding to whether or not `L` is a valid circle of n -dominoes.

Data frames

Take a look at the built-in variable `letters`.

- Write a function that uses `grep()` to count the number of times each letter appears in the column names of an input dataframe. It should return a numeric vector with appropriate names and of length 26 where the i th entry is the determined frequency of letter i .
- Write a function that uses `gsub()` to modify the column names of an input dataframe, (1) changing every space (" ") into a dot (".") and (2) appending "_mod" to the end of each name.

- Write a function that *removes* the last 4 characters of every column name of an input dataframe. (If the name is 4 or fewer characters long, turn it into an empty string.) You may find `substr()` and `nchar()` helpful.
- Write a function that prints all of the row names of an input data frame joined together by an underscore ("_") between each name. You may find `paste()` useful.
- Given a data frame of purely numeric data, write a function that returns the entries of the data frame ordered in a “spiral” fashion starting at the top left and proceeding counterclockwise and inward.
 - For example, the function applied to `data.frame(matrix(1:9, nrow=3))` would return `c(1, 2, 3, 6, 9, 8, 7, 4, 5)`.
 - Add a `"clockwise"` parameter to your function, defaulting to `FALSE`, which if set to `TRUE` returns the entries corresponding to a clockwise traversal of the spiral.
- Think back to the exercise yesterday about the divisibility properties of Fibonacci numbers. Let F_i denote the i th Fibonacci number, starting with $F_1 = F_2 = 1$.
 - Make a data frame where the n th column is a logical vector with `TRUE` in position m if F_m divides F_n and `FALSE` otherwise. (The data frame can be as large as you want.)
 - Make another data frame in the same way, except look at whether or not m divides n (instead of F_m and F_n).
 - Explain yesterday’s computational results using the patterns that you notice today.

Miscellaneous

- Write a function that prints out the longest “run” (sequence of consecutive identical values) in an input vector. (If there’s more than one, print out the one that occurs first.)
 - Rewrite your function, incorporating the usage of `rle()`.
- Find a counterexample to the following statement: By changing at most a single digit of any positive integer, we can obtain a prime number. (Memoization may be useful to speed up computation.)

The following continuation to the study of n -dominoes is **challenging** and purely optional.

Suppose that you have a single copy of every unique n -domino for some value of n .

- Write a function `make_circle(n)` that tries to construct a valid circle of n -dominoes from a *single copy* of every unique n -domino.
 - In the process of doing so, keep track of your various approaches.
 - Are there values of n for which no approach seems to work?
 - If so, can you make an argument about why you can't make a valid circle of n -dominoes for those values of n (using a single copy of every n -domino)? It may be instructive to look at the intermediate steps of your algorithm and how it fails.
 - Give a proof of your heuristic results.