Miscellaneous Problems in R

Here are some miscellaneous problems in R.

Lists

After all that work with subsetting, let's do something a bit more enjoyable.

 Write a function nesting_depth(L) that takes as input a list L and returns the nesting depth of L. (For example, nesting_depth(list(1, list(2, 3), list(4, 5))) would return 2.)

Let's call an n-domino a list of length 2, where both entries are integers from 0 to n inclusive.

Write a function to return a list of every unique n-domino, given n. (Treat list(a, b) as being equivalent to list(b, a).)

A valid circle of n-dominoes is given by a list of n-dominoes, with the following properties:

- Given two consecutive dominoes list(n, m) and list(p, q), where the latter domino is located immediately after the former domino in the circle of n-dominoes, we require that m == p.
- The 1st entry of the 1st *n*-domino is equal to the last entry of the last *n*-domino.

For example, list(list(1, 2), list(2, 3), list(3, 1)) is a valid circle of n-dominoes.

 Write a function is_circle(L) that returns a logical value corresponding to whether or not L is a valid circle of n-dominoes.

Data frames

Take a look at the built-in variable letters.

- Write a function that uses grep() to count the number of times each letter appears in the column names of an input dataframe. It should return a numeric vector with appropriate names and of length 26 where the *i*th entry is the determined frequency of letter *i*.
- Write a function that uses gsub() to modify the column names of an input dataframe, (1) changing every space (" ") into a dot (".") and (2) appending "_mod" to the end of each name.

- Write a function that *removes* the last 4 characters of every column name of an input dataframe. (If the name is 4 or fewer characters long, turn it into an empty string.) You may find substr() and nchar() helpful.
- Write a function that prints all of the row names of an input data frame
 joined together by an underscore ("_") between each name. You may find
 paste() useful.
- Given a data frame of purely numeric data, write a function that returns the entries of the data frame ordered in a "spiral" fashion starting at the top left and proceeding counterclockwise and inward.
 - For example, the function appplied to data.frame(matrix(1:9, nrow=3)) would return c(1, 2, 3, 6, 9, 8, 7, 4, 5).
 - Add a "clockwise" parameter to your function, defaulting to FALSE, which if set to TRUE returns the entries corresponding to a clockwise traversal of the spiral.
- Think back to the exercise yesterday about the divisibility properties of Fibonacci numbers. Let F_i denote the *i*th Fibonacci number, starting with $F_1 = F_2 = 1$.
 - Make a data frame where the nth column is a logical vector with TRUE in position m if F_m divides F_n and FALSE otherwise. (The data frame can be as large as you want.)
 - Make another data frame in the same way, except look at whether or not m divides n (instead of F_m and F_n).
 - Explain yesterday's computational results using the patterns that you notice today.

Miscellaneous

- Write a function that prints out the longest "run" (sequence of consecutive identical values) in an input vector. (If there's more than one, print out the one that occurs first.)
 - Rewrite your function, incorporating the usage of rle().
- Find a counterexample to the following statement: By changing at most a single digit of any positive integer, we can obtain a prime number. (Memoization may be useful to speed up computation.)

The following continuation to the study of n-dominoes is **challenging** and purely optional.

Suppose that you have a single copy of every unique n-domino for some value of n.

- Write a function make_circle(n) that tries to construct a valid circle of *n*-dominoes from a *single copy* of every unique *n*-domino.
 - In the process of doing so, keep track of your various approaches.
 - Are there values of n for which no approach seems to work?
 - If so, can you make an argument about why you can't make a valid circle of n-dominoes for those values of n (using a single copy of every n-domino)? It may be instructive to look at the intermediate steps of your algorithm and how it fails.
 - Give a proof of your heuristic results.