

Linear Motor Active Damper (LMAD) for Vibration Reduction in Precision Manufacturing System

2016144066
Dept. of Mechanical Engineering
Inho Kee

Contents

1. Intro
 - Machining vibration issue
 - Passive strategies
 - Active strategies
 - This research?
2. Analytical modeling
 - System modeling, Identification
 - Required Force constant
 - Required Actuator mass
3. Single Frequency vibration reduction
 - Result
4. Multi-Frequency vibration reduction
 - Result
5. Conclusion
6. Future work
7. Acknowledgments

1. Intro – Machining Vibration issue



bmmagazine

- **Chatter vibration**

- Free vibration
 - Forced vibration
- } Widely developed

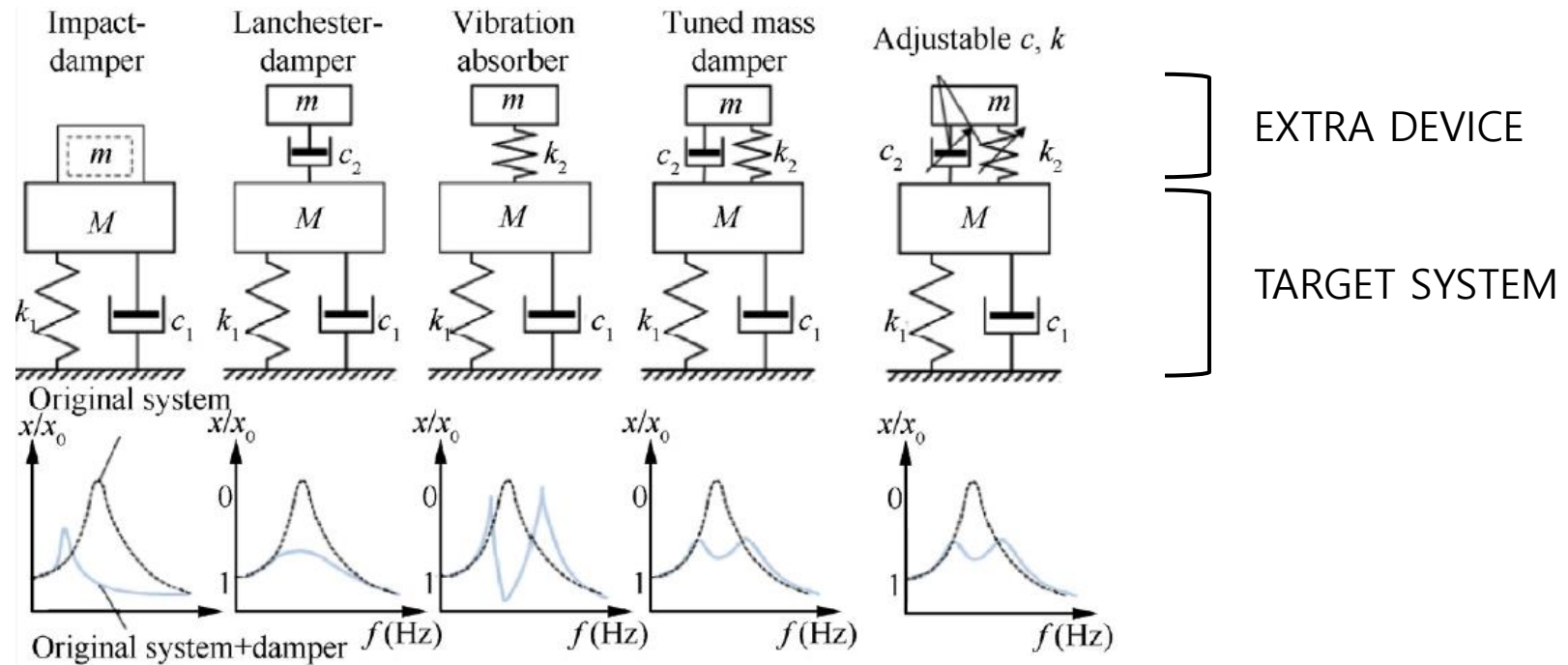
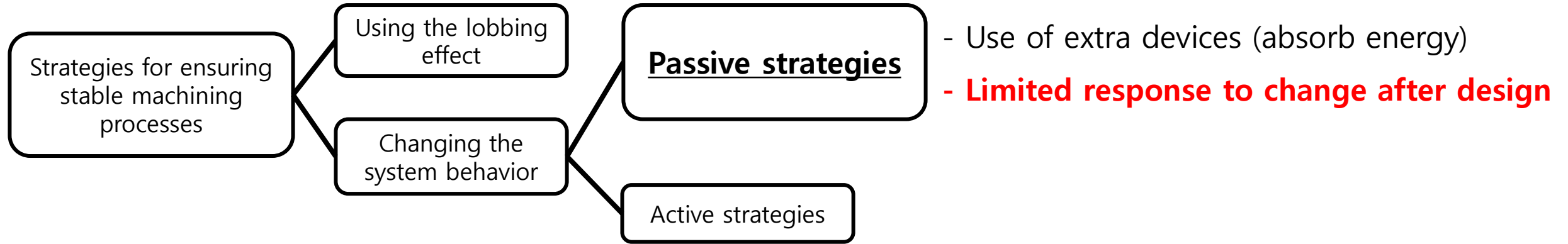
- **Self-excited vibration** **TARGET**

└─ Made by interaction between tool & workpiece

- **Negative Effect of Chatter**

- Poor surface quality
- Inaccuracy
- Noise
- Machine tool damage
- And so on....

1. Intro – Passive strategies



C. Yue, H. Gao, X. Liu, S.Y. Liang, L. Wang
A review of chatter vibration research in milling
Chin J Aeronaut, 32 (2) (2019), pp. 215-242

1. Intro – Active strategies

Strategies for ensuring stable machining processes

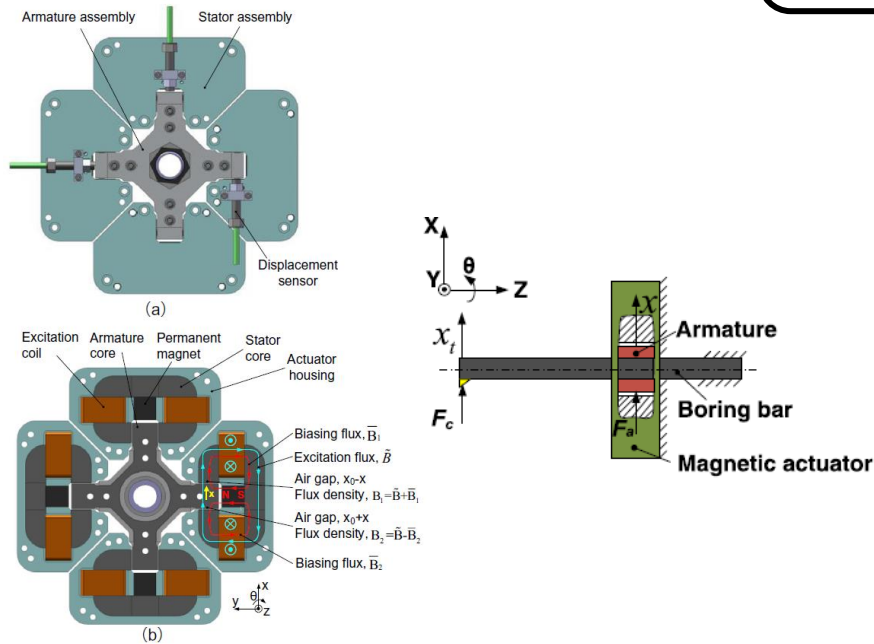
Using the lobbing effect

Passive strategies

Changing the system behavior

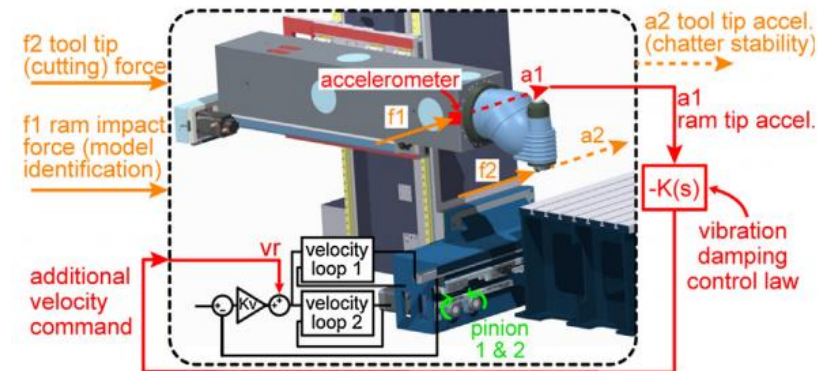
Active strategies

- Monitor dynamic behavior of tools
- Adjust with actuator
- **Active response to change**



Chen F, Liu G (2016) Active damping of machine tool vibrations and cutting force measurement with a magnetic actuator. Int J Adv Manuf Technol:1–10.

- Monitor : Displacement sensor
- Actuator : Magnetic actuator



Munoa J, Beudaert X, Erkorkmaz K, Lglesias A, Barrios A. Active suppression of structural chatter vibrations using machine drives and accelerometers. CIRP Ann- Manuf Technol 2015;64(1):385–8.

- Monitor : Accelerometer
- Actuator : tool's own drive

1. Intro – This research?

Active strategy

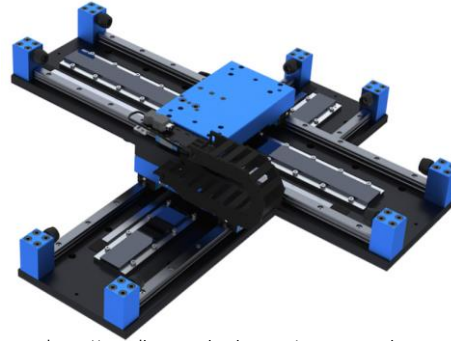
Accelerometer (Monitor)



Digiducer Model 333D01



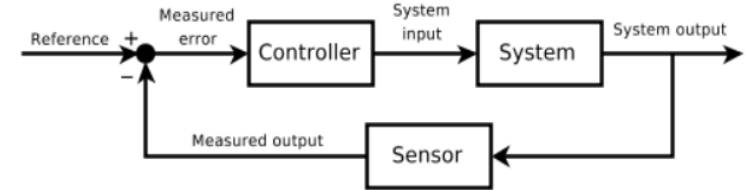
Linear Motor (Actuator)



<https://www.linearmotiontips.com/new-generation-of-linear-motor-stages-from-yaskawa/>



Direct Velocity Feedback (DVF)

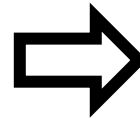


<https://electronics.stackexchange.com>

Method of
Vibration reduction

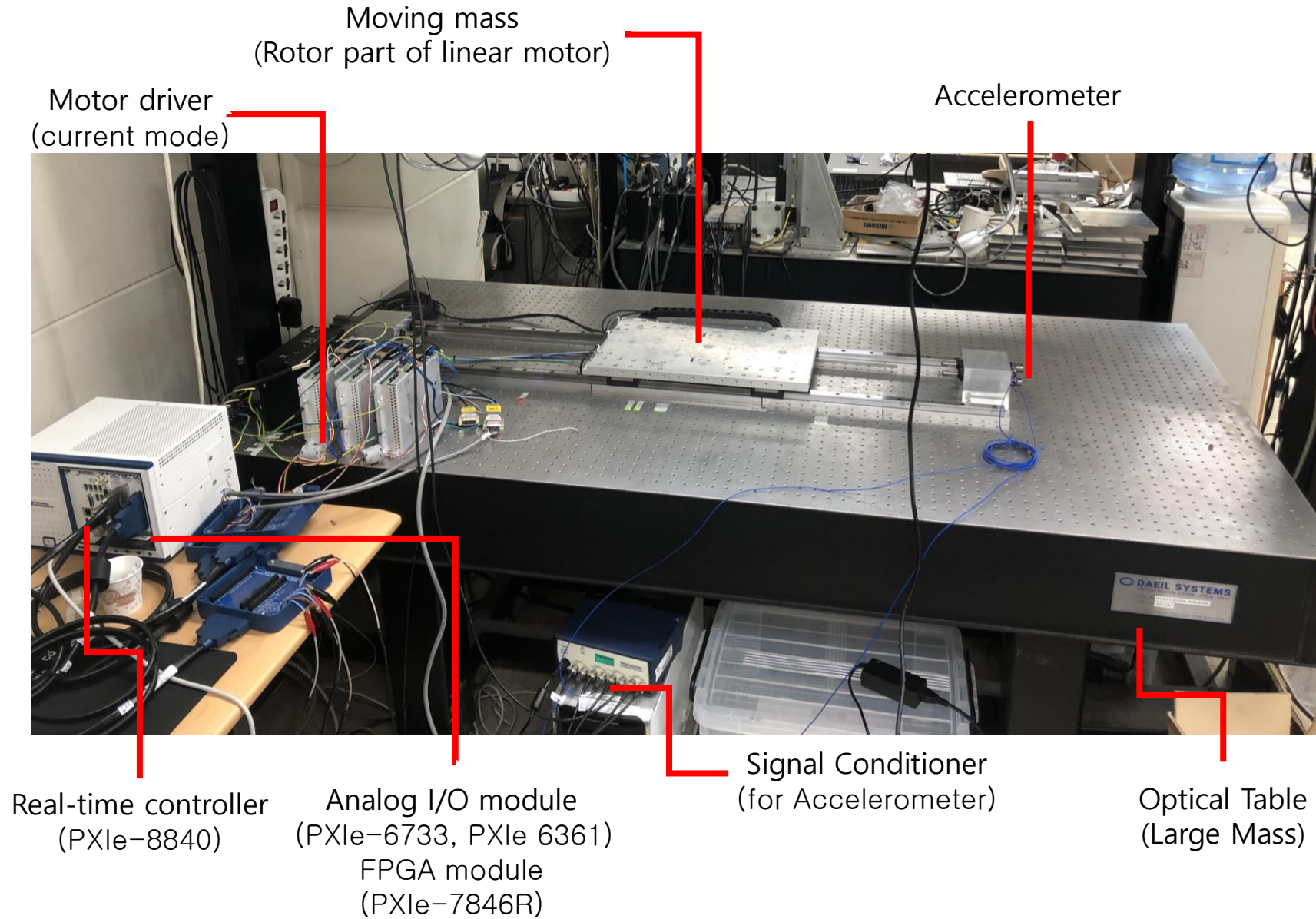
Single frequency

Multiple frequency

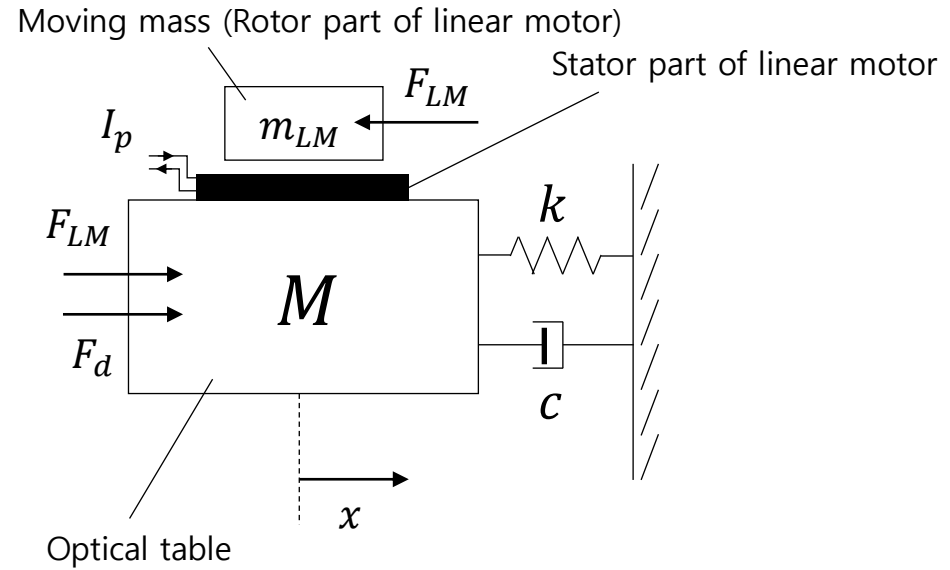
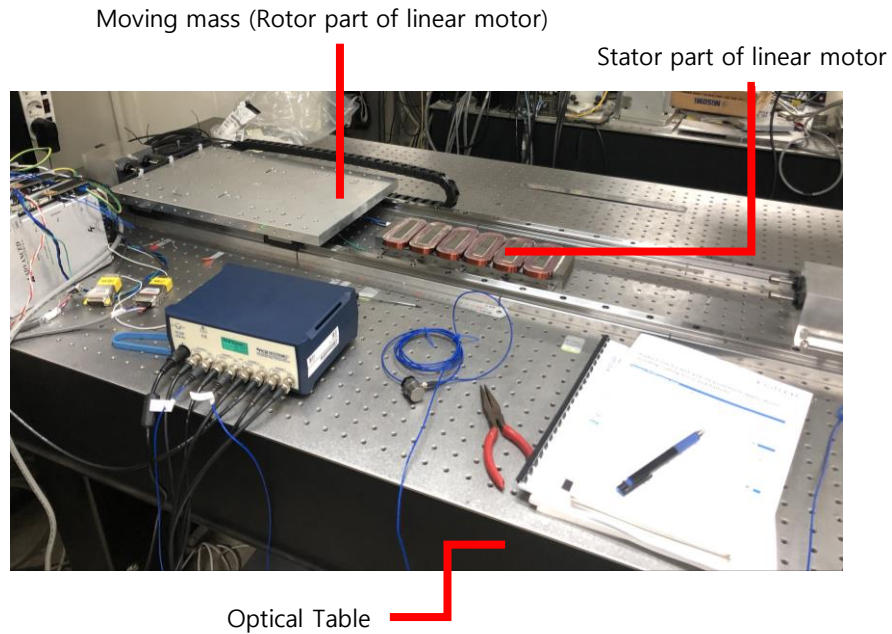


Find basis for dealing with the
Entire Frequency

2. Analytical Modeling – Setup



2. Analytical Modeling – System Modeling



I_p : Peak current of commutation law for the linear motor. Positive if $F_{LM} > 0$

F_d : Disturbance force

Standard Second-order system of Optical table

$$M\ddot{x} + c\dot{x} + kx = F_{LM} + F_{\text{disturbance}}$$

Mechanical governing equation of Linear Motor

$$m_{LM}\ddot{x}_{LM} = K_i I_p - \cancel{K_d x_{LM}} - \cancel{c_d \dot{x}_{LM}} \Rightarrow m_{LM}\ddot{x}_{LM} = F_{LM} = K_i I_p$$

SJ Moon, TY Chung, CW Lim, DH Kim, "A linear motor damper for vibration control of steel structures", Mechatronics, 14(10), 1157-1181, 2004

M_{LM} : moving mass

x_{LM} : Relative position of LM from the table

K_i : linear motor force constant

I_p : peak current of commutation law for the linear motor

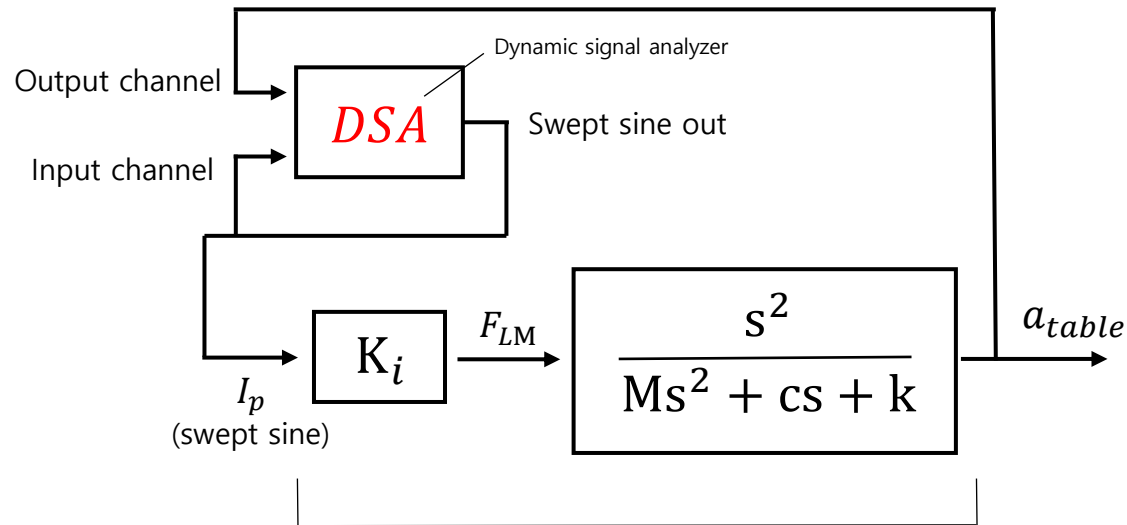
2. Analytical Modeling – System Modeling(Identification)

- **DSA Experiment**

- Frequency domain analysis for **Unknown** : c, k

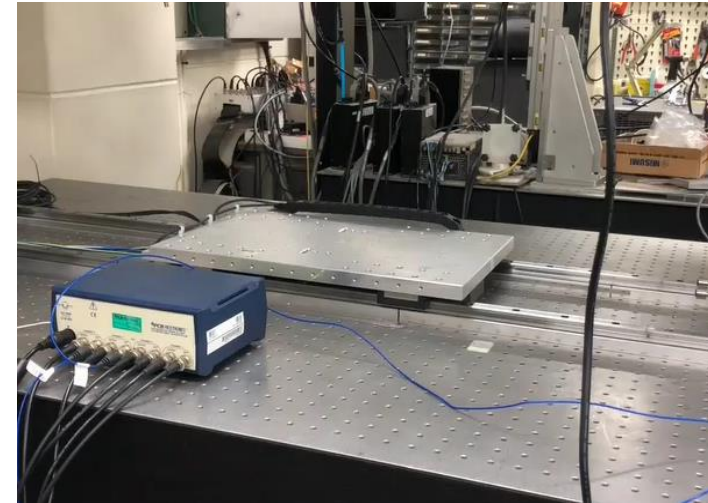
Open-loop Transfer Function

$$\frac{A(s)}{I_p(s)} = \frac{K_i s^2}{Ms^2 + cs + k}$$



Open loop plant $G(s) = \frac{A(s)}{I_p(s)}$

(Sampling rate of 10kHz / Excitation amplitude of 3.0A for all frequencies)



Frequency 별로 Magnitude, Phase 데이터 수집

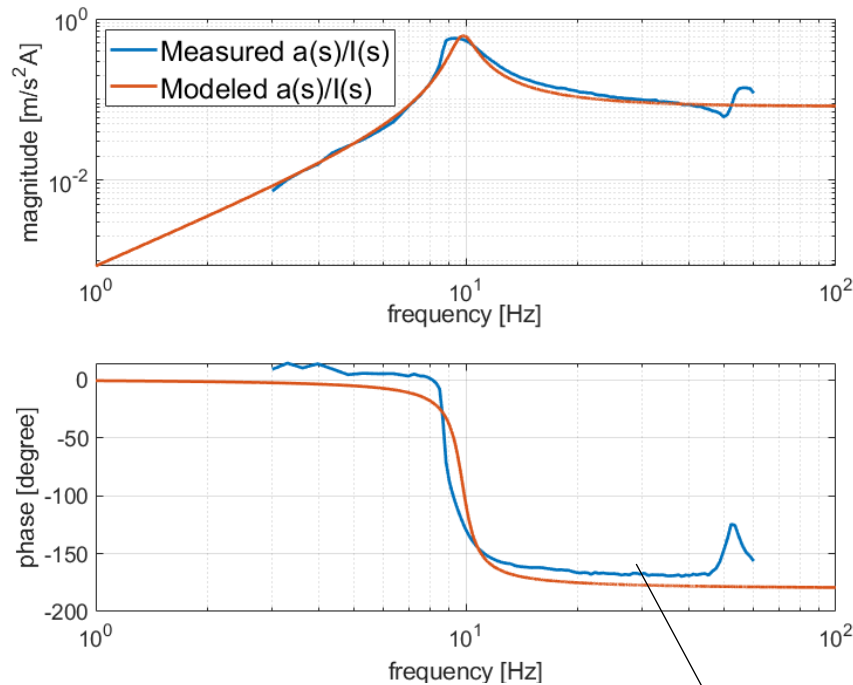
Natural frequency 근접 \Rightarrow Magnitude

2. Analytical Modeling – System Modeling(Identification)

- **Estimated parameters (DSA test)**

$$M = 280kg, \quad c = 2300 \text{ Ns/m}, \quad k = 1,018,700 \text{ N/m}$$

($k = M(2\omega_n\pi)^2$)



flipped phase : measurement of $-A(s)/I_p(s)$

Open-loop Transfer Function

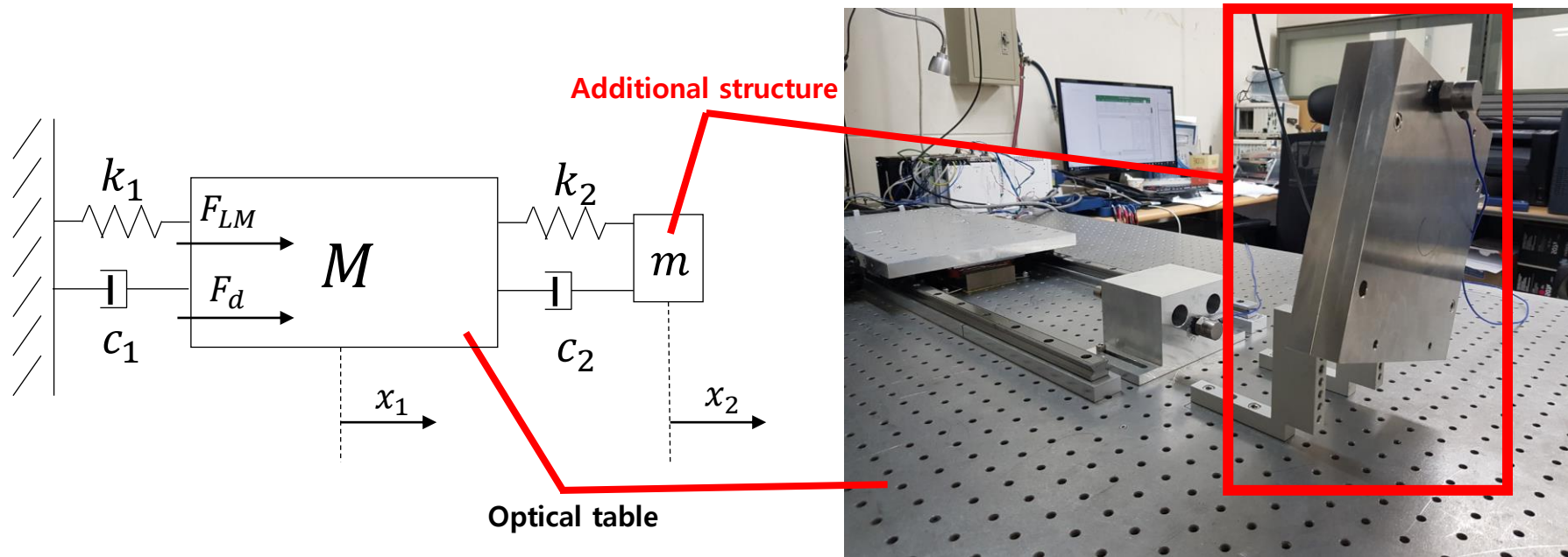
$$\frac{A(s)}{I_p(s)} = \frac{K_i s^2}{Ms^2 + cs + k}$$

Frequency domain analysis for **Unknown** : c, k

Modeled Open-loop Transfer Function

$$\frac{A(s)}{I_p(s)} = \frac{23s^2}{280s^2 + 2300s + 1061622}$$

2. Analytical Modeling – Multi-Frequency System Modeling



$$(1) M\ddot{x}_1 + c_1\dot{x}_1 + c_2(\dot{x}_1 - \dot{x}_2) + k_1x_1 + k_2(x_1 - x_2) = F_{LM} + F_d$$

$$(2) m\ddot{x}_2 + c_2(\dot{x}_2 - \dot{x}_1) + k_2(x_2 - x_1) = 0 \quad (F_{LM} = K_i i)$$

$$(3) i = -[g_1 \dot{x}_1 + g_2(\dot{x}_1 - \dot{x}_2)]$$

$$\Rightarrow M\ddot{x}_1 + (c_1 + K_i g_1)\dot{x}_1 + (c_2 + K_i g_2)(\dot{x}_1 - \dot{x}_2) + k_1x_1 + k_2(x_1 - x_2) = F_d$$

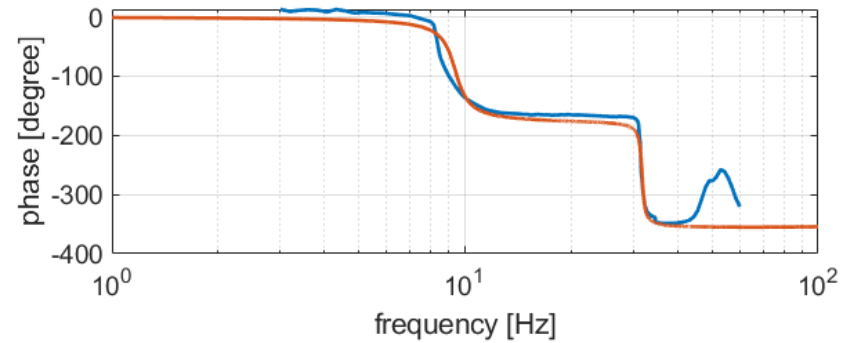
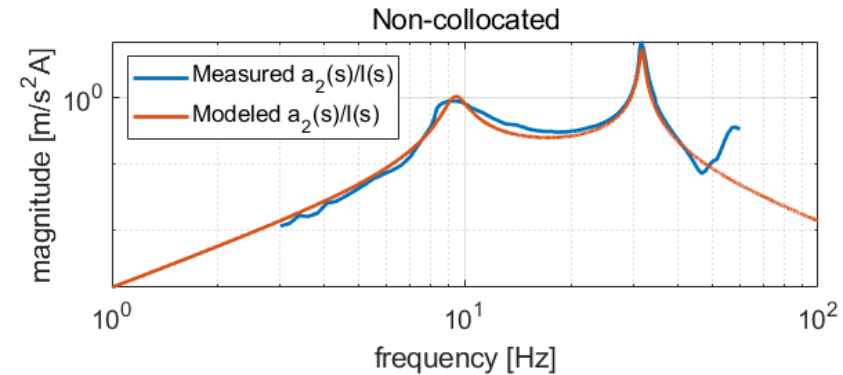
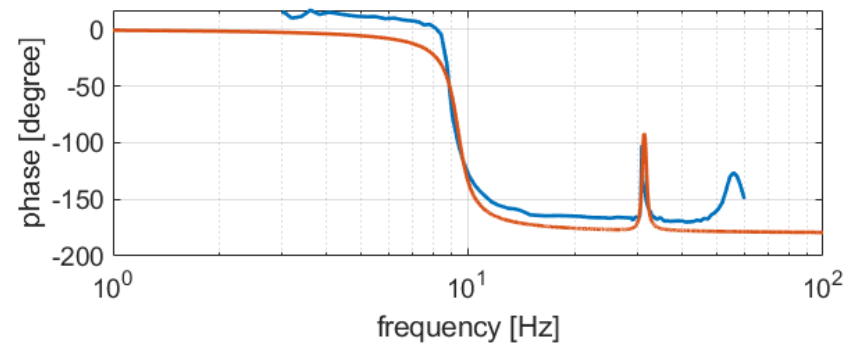
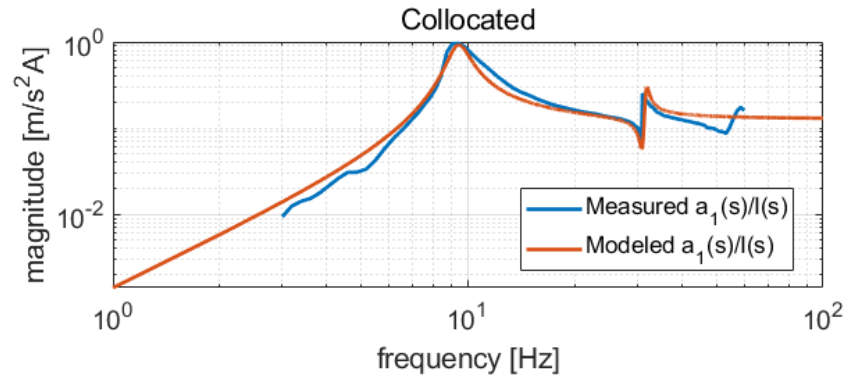
Additional damping coefficient to the collocated mass

2. Analytical Modeling – Multi-Frequency System Modeling(Identification)

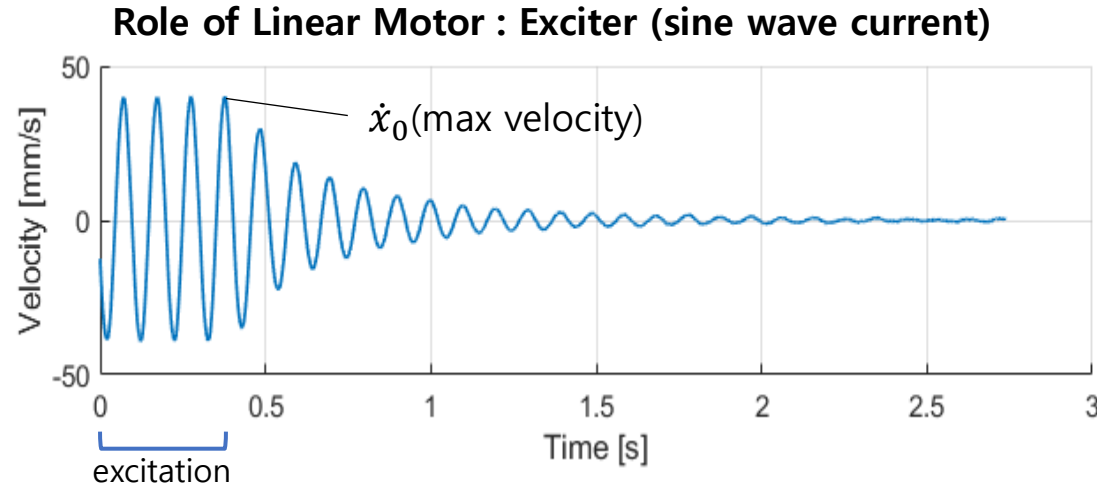
- Estimated parameters (DSA test)**

$$M = 280kg, \quad c_1 = 2300 \text{ Ns/m}, \quad k_1 = 1,018,700 \text{ N/m}$$

$$m = 30kg, \quad c_2 = 55 \text{ Ns/m}, \quad k_2 = 455,270 \text{ N/m} \quad K_i = 36 \text{ N/A}$$



2. Analytical Modeling – Required Force Constant(LMAD)



$$X(s) = \frac{M\dot{x}_0}{Ms^2 + (c + K_v K_i)s + k}$$

$$\left(\begin{array}{c} \text{w/o Active Damping} \\ X_{plant}(s) = \frac{M\dot{x}_0}{Ms^2 + cs + k} \end{array} \right)$$

Amplitude attenuation ratio(η) at target frequency (w_n)

$$\eta = \left| \frac{X(s)}{X_{plant}(s)} \right|_{s=jw_n} = \frac{c}{c + K_v K_i}$$

w_n : Natural frequency of optical table

K_i : Linear motor force constant

c : Damping coefficient of optical table

K_v : Velocity feedback controller gain

2. Analytical Modeling – Required Force Constant(LMAD)

- **Active Damper Design Specification**

- Required force constant(K_i) of the actuator

$$\eta = \frac{c}{c + K_i K_v} \xrightarrow{K_v = I_p / \dot{x}} K_i = \frac{(1 - \eta) V_{max} c}{\eta I_{max}}$$

(1) (2) (3) (4)

(1) η : Required amplitude attenuation ratio → 80% reduction target

(2) V_{max} : Maximum treatable velocity amplitude (0.040m/s by test)

(3) c : Obtained by experiment (Linear motor excitation, DSA test, ...)

(4) I_{max} : Maximum capacity of current driver ~ 21A

2. Analytical Modeling – Required Force Constant(LMAD)

- **Required force constant(K_i) of the actuator**

$$K_{i,required} = \frac{(1-\eta)V_{max}c}{\eta I_{max}} = 14.4734 \text{ N/A}$$

η : Required amplitude attenuation ratio $\rightarrow 0.20$ (**80% reduction**)

V_{max} : Maximum treatable velocity amplitude $\rightarrow 0.040 \text{ m/s}$

c : Damping coefficient of the optical table system $\rightarrow 2300 \text{ Ns/m}$

I_{max} : Maximum capacity of current driver $\rightarrow 21\text{A}$

For our system

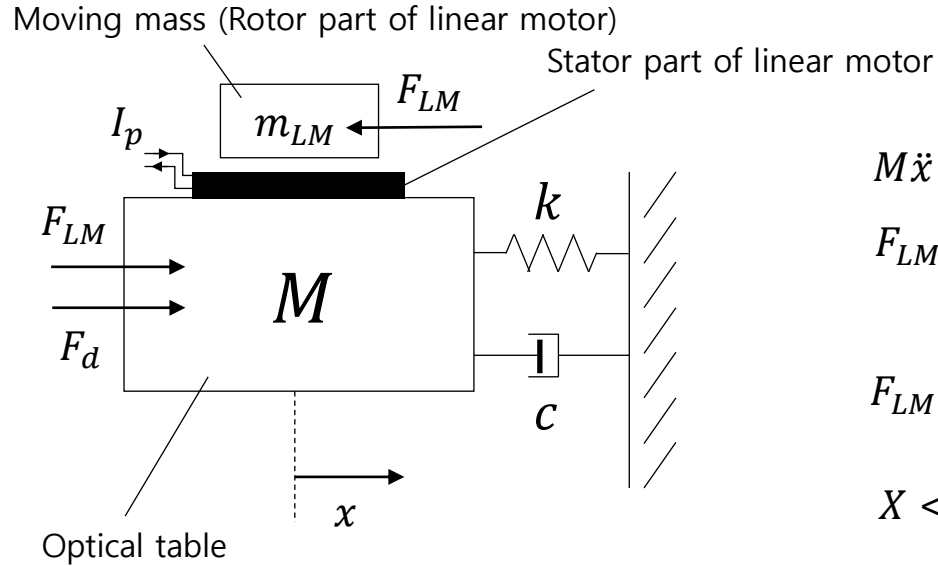


$$K_{i,LMAD} = 36\text{N/A} > K_{i,required} = 14.47\text{N/A}$$

$$\eta = \frac{c}{c+K_v K_i} \rightarrow K_v = 255.6 \text{ As/m}$$

2. Analytical Modeling – Required Actuator Mass

- Required actuator mass



$$M\ddot{x} + c\dot{x} + kx = F_{LM} + F_d \quad : \text{Table dynamics}$$

$$F_{LM} = K_i i \quad : \text{Linear Motor plant}$$

$$F_{LM} = m_{LM}a = m_{LM}\omega_L^2 X \sin(\omega_L t) = K_i I_{max} \sin(\omega_L t)$$

$$X < L_{max}/2$$

X : Actuator amplitude

m_{lim} : Maximum actuator mass (system limit)

ω_L : Minimum frequency of actuator excitation

L_{max} : Maximum Stroke of actuator

$$\frac{2K_i I_{max}}{L_{max}\omega_L^2} < m < m_{lim}$$

For our system

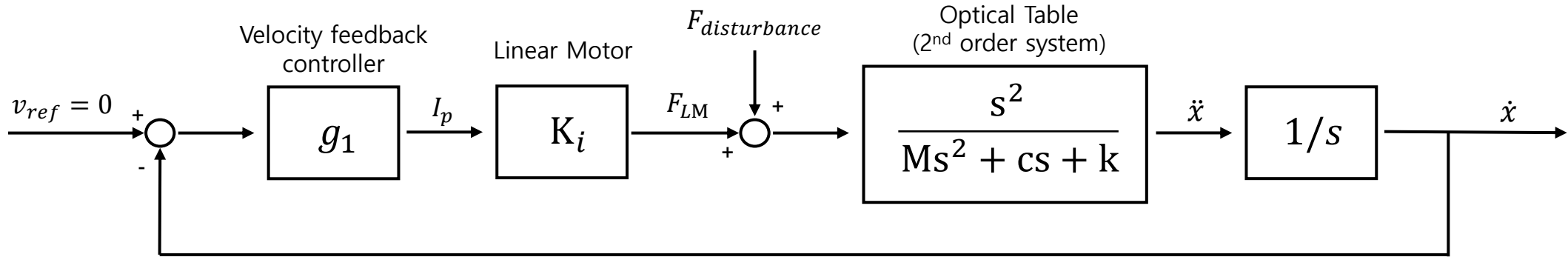
$$\Rightarrow \frac{2K_i I_{max}}{L_{max}\omega_L^2} = 3.36kg < m = 10.8kg$$

3. Single Frequency Vib. Reduction – Direct Velocity Feedback

Standard Second-order system of Optical table
 $M\ddot{x} + c\dot{x} + kx = F_{LM} + F_{\text{disturbance}}$

Mechanical governing equation of Linear Motor
 $m_{LM}\ddot{x}_{LM} = F_{LM} = K_i I_p$

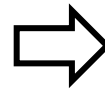
Direct Velocity feedback



$$M\ddot{x} + c\dot{x} + kx = F_{LM} + F_{\text{disturbance}}$$

$$F_{LM} = K_i I_p$$

$$I_p = -g_1 \dot{x} \quad (\text{Velocity feedback control})$$

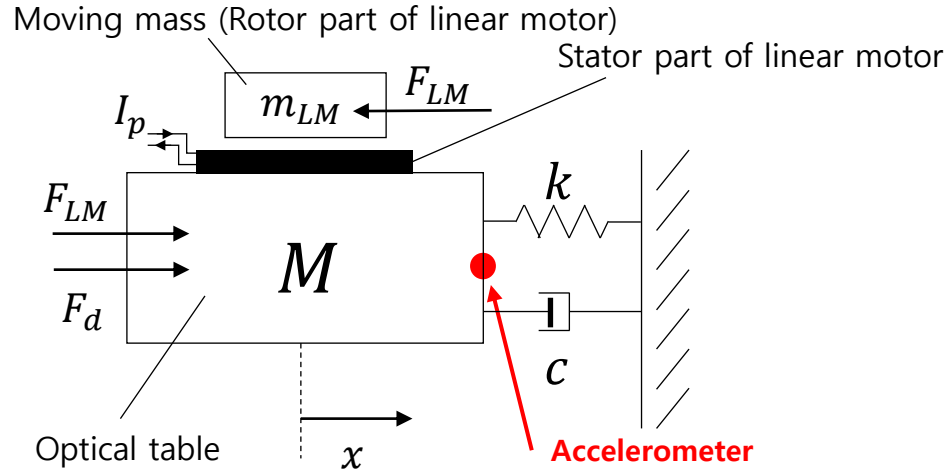


$$\eta = \frac{c}{c + g_1 K_i} \rightarrow g_1 = 255.6 \text{ As/m}$$

$$M\ddot{x} + (c + g_1 K_i)\dot{x} + kx = F_{\text{disturbance}}$$

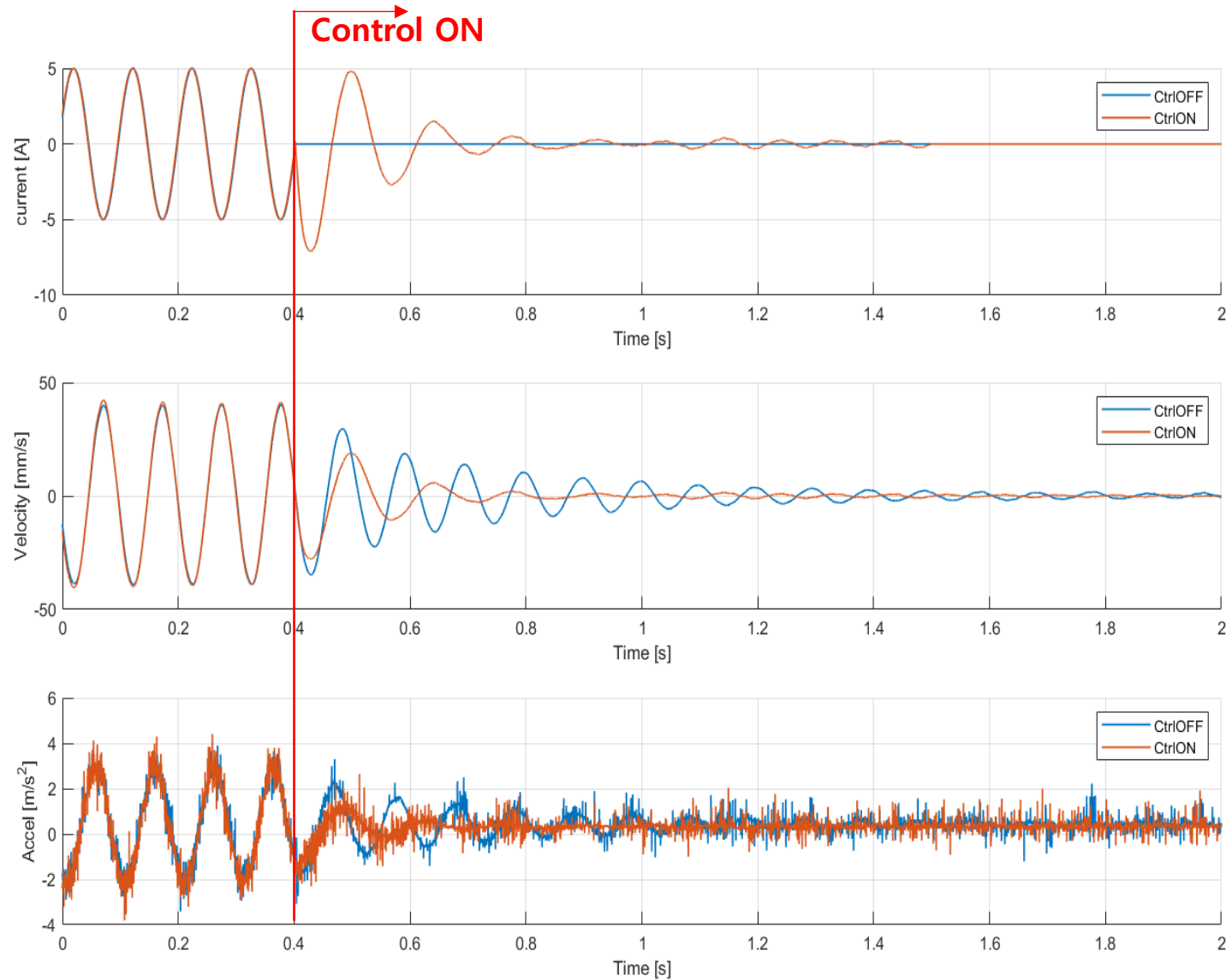
Adjustable Damping Term

3. Single Frequency Vib. Reduction – Direct Velocity Feedback



• Test Results

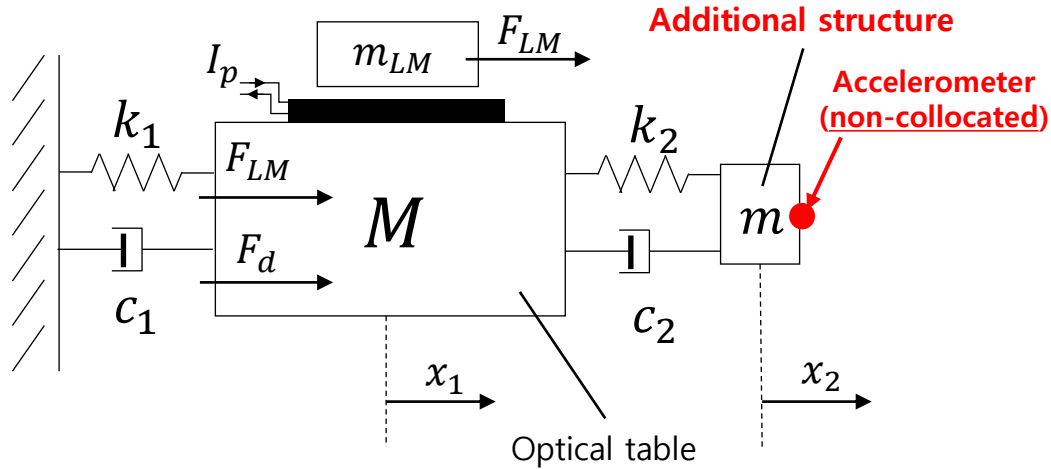
- **Role of Linear Motor** (Absence of exciter)
Control OFF : Exciter (sine wave current)
Control ON : Active Damper
- **Excitation**
9.8 Hz : 5.0A excitation (by LM)
- **Control gain**
 $g_1 = 255.6$



2% settling time 43.3% reduced

$$t_{s,natural} = 1.68 \ll t_{s,control} = 0.95$$

4. Multi-Frequency Vib. Reduction – Direct Velocity Feedback



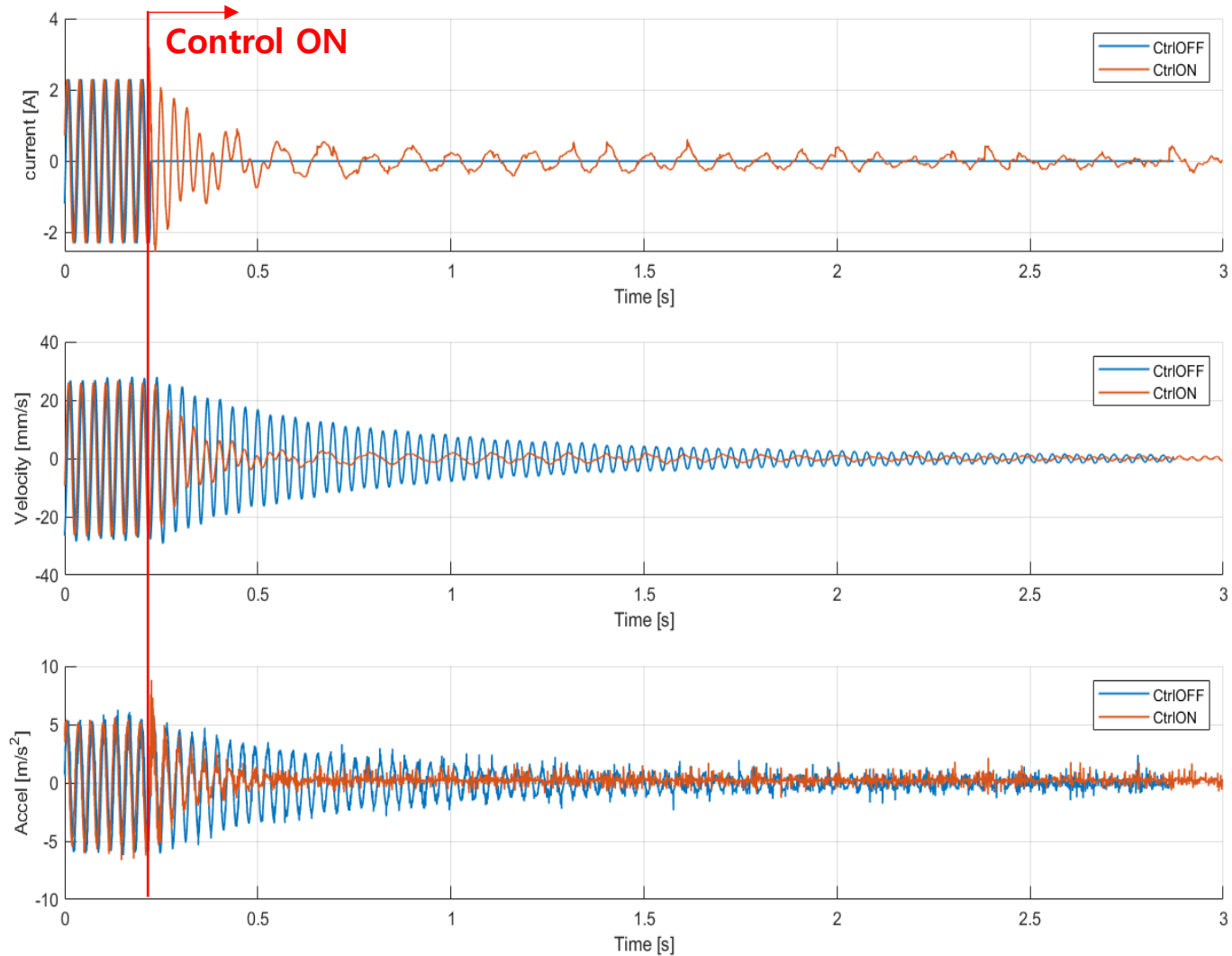
• Test Results

- **Role of Linear Motor** (Absence of exciter)
Control OFF : Exciter (sine wave current)
Control ON : Active Damper
- **Excitation**
9.8 Hz : no excitation
31.3 Hz : 2.3A excitation (by LM)
- **Control gain**
 $g_1 = 255.6$, $g_2 = 100$

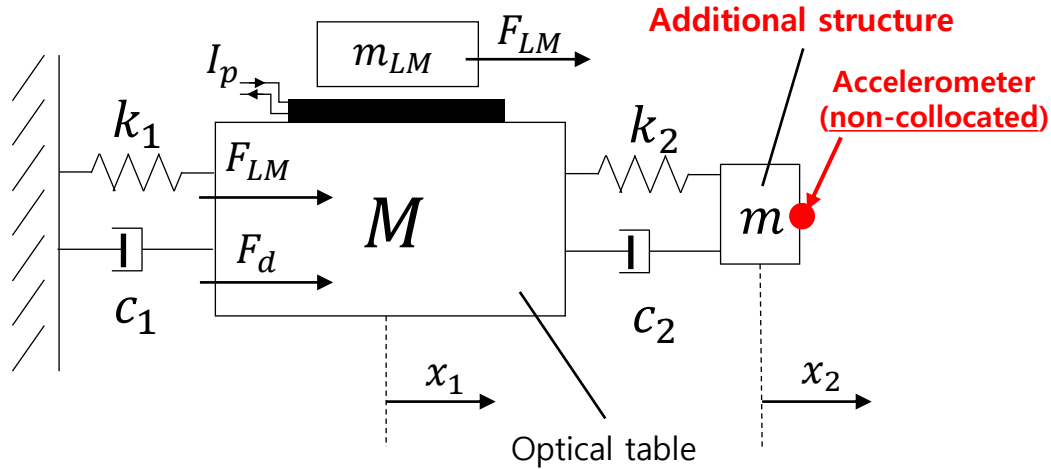


5% settling time 39.5% reduced

$$t_{s,natural} = 2.26 \ll t_{s,control} = 1.36$$



4. Multi-Frequency Vib. Reduction – Direct Velocity Feedback



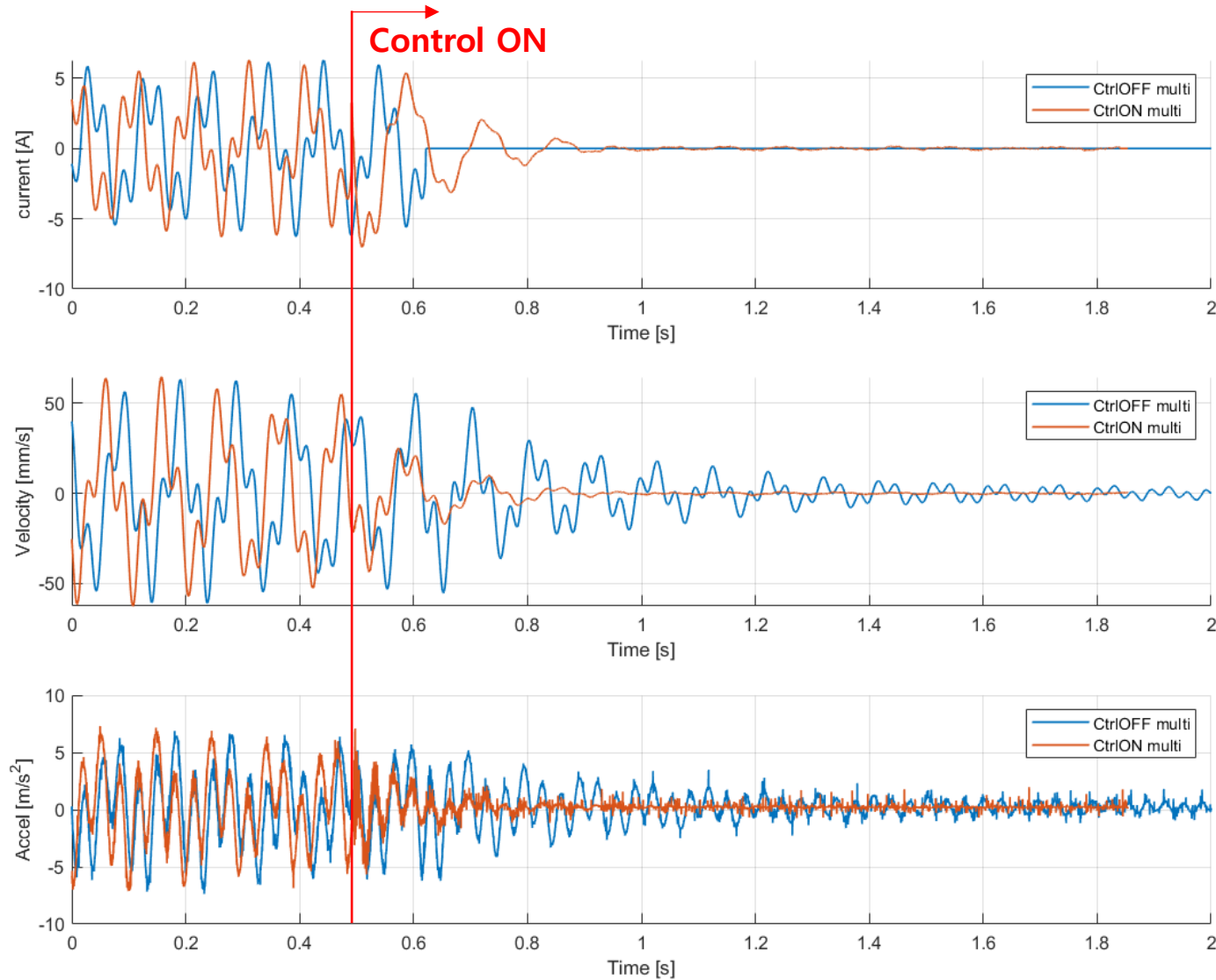
• Test Results

- **Role of Linear Motor** (Absence of exciter)
Control OFF : Exciter (sine wave current)
Control ON : Active Damper
- **Excitation**
9.8 Hz : 4.0A excitation
31.3 Hz : 2.3A excitation (by LM)
- **Control gain**
 $g_1 = 255.6$, $g_2 = 100$



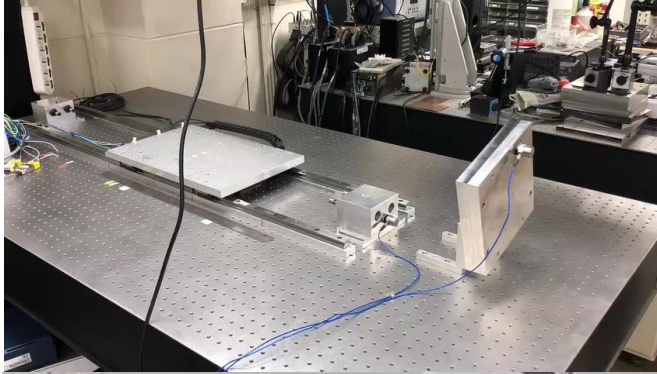
5% settling time 71.5% reduced

$$t_{s,natural} = 1.71 \ll t_{s,control} = 0.49$$



5. Conclusion

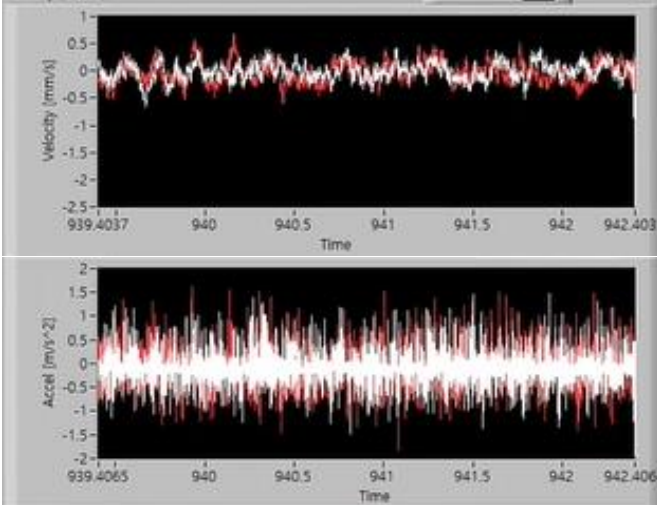
Natural dissipate



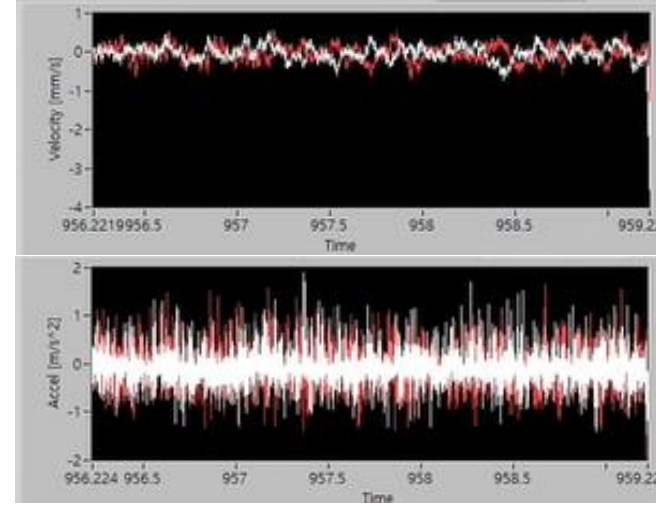
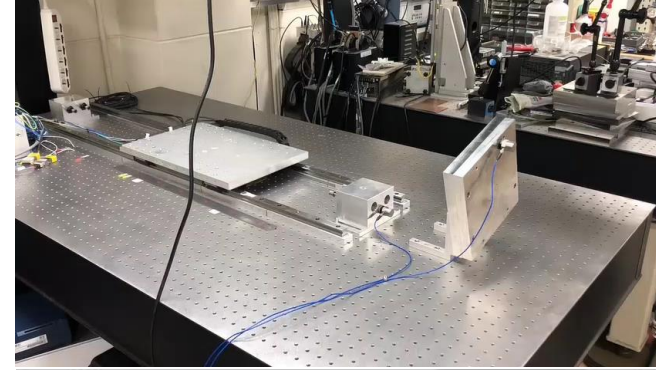
Speed X0.25

Excitation
9.8Hz, 31.3Hz

Red : non-collocated
White : collocated



Control



Found feasibility for dealing with the
Entire Frequency

6. Future work

- **During control, LMAD deviates from the center**
 - Apply parallel controller (Separate effect on performance)
 - LMAD position controller with low frequency bandwidth
- **Only 1DOF & 2DOF applications (modeling, controller)**
 - Generalize n-DOF applications
- **Used simple controller (DVF, P control)**
 - Apply specific stability conditions
 - Specification of control methods

7. Acknowledgements

Special thanks to



Professor Min



Professor Yoon



T.A. Kim