Multiple logistic regression

INTERMEDIATE REGRESSION IN R



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Bank churn dataset

has_churned	time_since_first_purchase	time_since_last_purchase
0	0.3993247	-0.5158691
1	-0.4297957	0.6780654
0	3.7383122	0.4082544
0	0.6032289	-0.6990435
•••	•••	•••
response	length of relationship	recency of activity

¹ https://www.rdocumentation.org/packages/bayesQR/topics/Churn



glm()

```
glm(response ~ explanatory, data = dataset, family = binomial)

glm(response ~ explanatory1 + explanatory2, data = dataset, family = binomial)

glm(response ~ explanatory1 * explanatory2, data = dataset, family = binomial)
```



Prediction flow

```
explanatory_data <- expand_grid(
  explanatory1 = some_values,
  explanatory2 = some_values
)
prediction_data <- explanatory_data %>%
  mutate(
    has_churned = predict(mdl, explanatory_data, type = "response")
)
```

The four outcomes

	actual false	actual true
predicted false	correct	false negative
predicted true	false positive	correct

¹ https://campus.datacamp.com/courses/introduction-to-regression-in-r/simple-logistic-regression?ex=10



Confusion matrix

```
actual_response <- dataset$response</pre>
predicted_response <- round(fitted(mdl))</pre>
outcomes <- table(predicted_response, actual_response)</pre>
confusion <- conf_mat(outcomes)</pre>
autoplot(confusion)
summary(confusion, event_level = "second")
```



Visualization

- Use faceting for categorical variables.
- For 2 numeric explanatory variables, use color for response.
- Give responses below 0.5 one color; responses above 0.5 another color.

```
scale_color_gradient2(midpoint = 0.5)
```

Let's practice!

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The logistic distribution

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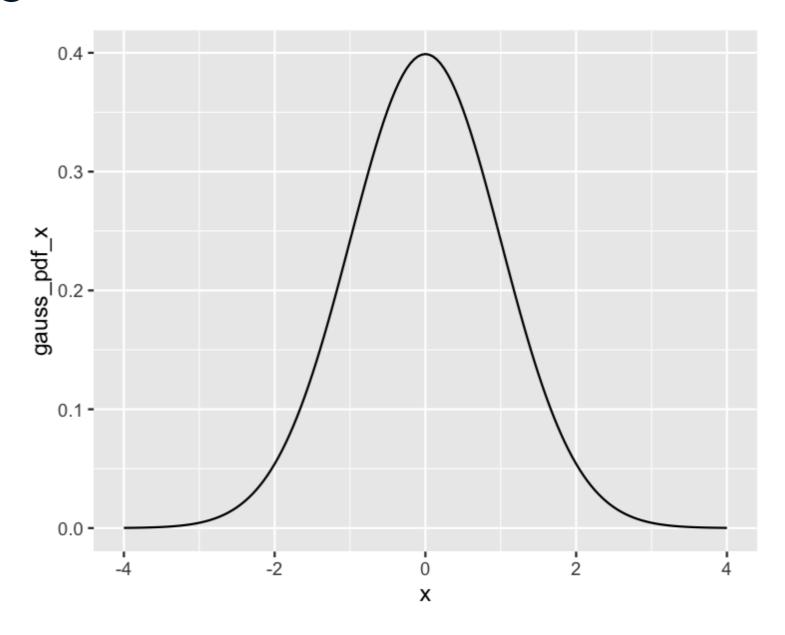
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Gaussian probability density function (PDF)

```
gaussian_distn <- tibble(
  x = seq(-4, 4, 0.05),
  gauss_pdf_x = dnorm(x)
)</pre>
```

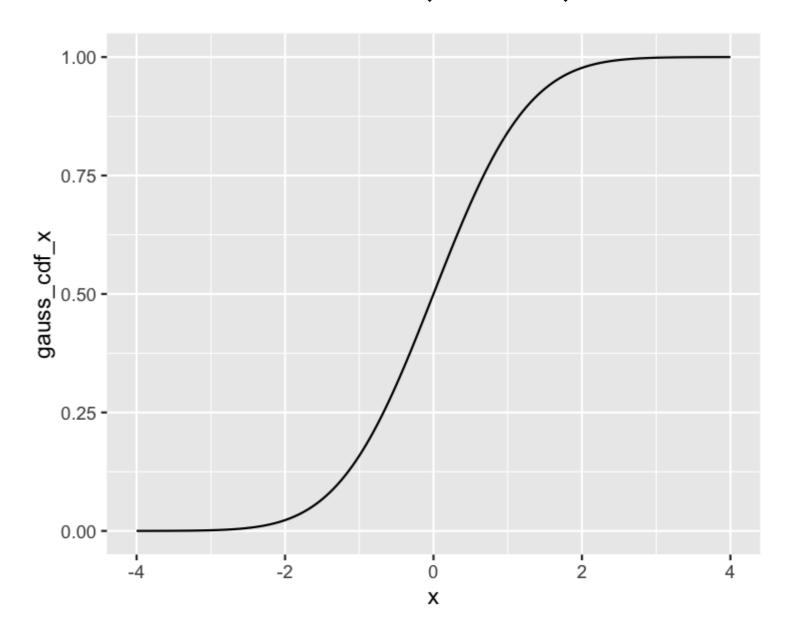
```
ggplot(gaussian_distn, aes(x, gauss_pdf_x)) +
  geom_line()
```



Gaussian cumulative distribution function (CDF)

```
gaussian_distn <- tibble(
  x = seq(-4, 4, 0.05),
  gauss_pdf_x = dnorm(x),
  gauss_cdf_x = pnorm(x)
)</pre>
```

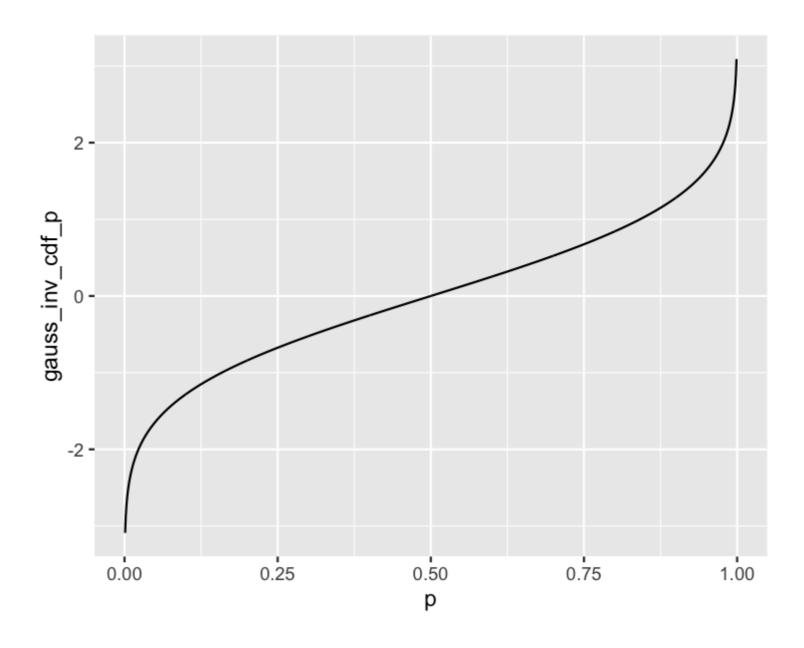
```
ggplot(gaussian_distn, aes(x, gauss_cdf_x)) +
  geom_line()
```



Gaussian inverse CDF

```
gaussian_distn_inv <- tibble(
    p = seq(0.001, 0.999, 0.001),
    gauss_inv_cdf_p = qnorm(p)
)</pre>
```

```
ggplot(gaussian_distn_inv, aes(p, gauss_inv_cdf_p)) +
  geom_line()
```



Distribution function names

curve	prefix	normal	logistic	nmemonic
PDF	d	dnorm()	dlogis()	"d" for differentiate - you differentiate the CDF to get the PDF
CDF	p	pnorm()	plogis()	"p" is backwards "q" so it's the inverse of the inverse CDF
Inv. CDF	q	qnorm()	qlogis()	"q" for quantile

glm()'s family argument

```
lm(response ~ explanatory, data = dataset)
glm(response ~ explanatory, data = dataset, family = gaussian)
glm(response ~ explanatory, data = dataset, family = binomial)
```

¹ https://campus.datacamp.com/courses/introduction-to-regression-in-r/simple-logistic-regression?ex=1



gaussian()

str(gaussian())

```
List of 11
$ family
           : chr "gaussian"
$ link : chr "identity"
 $ linkfun :function (mu)
$ linkinv :function (eta)
 $ variance :function (mu)
 $ dev.resids:function (y, mu, wt)
 $ aic :function (y, n, mu, wt, dev)
 $ mu.eta :function (eta)
 $ initialize: expression({ n <- rep.int(1, nobs) if (is.null(etastart) && is.null(start) &&</pre>
    is.null(mustart) && ((family$lin| __truncated__
 $ validmu :function (mu)
 $ valideta :function (eta)
- attr(*, "class")= chr "family"
```



linkfun and linkinv

Link function is a transformation of the response variable

```
gaussian()$linkfun
```

```
function (mu)
mu
```

gaussian()\$linkinv

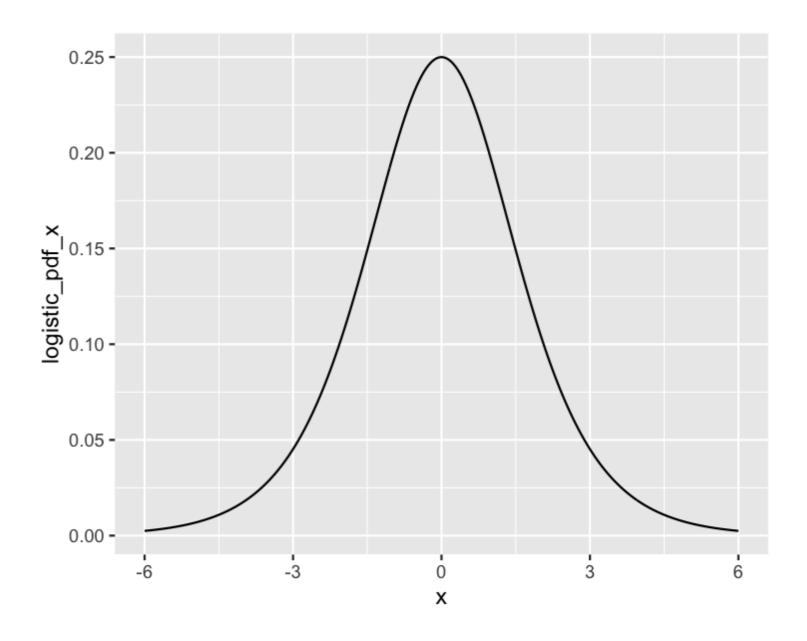
```
function (eta)
eta
```



Logistic PDF

```
logistic_distn <- tibble(
  x = seq(-6, 6, 0.05),
  logistic_pdf_x = dlogis(x)
)</pre>
```

```
ggplot(logistic_distn, aes(x, logistic_pdf_x)) +
  geom_line()
```



Logistic distribution

- Logistic distribution CDF is also called the logistic function.
- $\operatorname{cdf}(x) = \frac{1}{(1 + exp(-x))}$
- Logistic distribution inverse CDF is also called the *logit function*.
- inverse_cdf $(p) = log(\frac{1}{(1-p)})$

Let's practice!

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How logistic regression works

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Sum of squares doesn't work

```
sum((y_pred - y_actual) ^ 2)

y_actual is always 0 or 1.

y_pred is between 0 and 1.
```

There is a better metric than sum of squares.

Likelihood

y_pred * y_actual



Likelihood

```
y_pred * y_actual + (1 - y_pred) * (1 - y_actual)
```

Likelihood

```
sum(y_pred * y_actual + (1 - y_pred) * (1 - y_actual))
```

When $y_actual = 1$

$$y_{pred} * 1 + (1 - y_{pred}) * (1 - 1) = y_{pred}$$

When $y_actual = 0$

$$y_{pred} * 0 + (1 - y_{pred}) * (1 - 0) = 1 - y_{pred}$$

Log-likelihood

- Computing likelihood involves adding many very small numbers, leading to numerical error.
- Log-likelihood is easier to compute.

```
log(y_pred) * y_actual + log(1 - y_pred) * (1 - y_actual)
```

Both equations give the same answer.

Negative log-likelihood

Maximizing log-likelihood is the same as minimizing negative log-likelihood.

-sum(log_likelihoods)

Logistic regression algorithm

```
calc_neg_log_likelihood <- function(coeffs) {
  intercept <- coeffs[1]
  slope <- coeffs[2]
  # More calculation!
}</pre>
```

```
optim(
  par = ???,
  fn = ???
)
```

Let's practice!

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Congratulations

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You learned things

Chapter 1

Fit/visualize/predict/assess parallel slopes

Chapter 2

- Interactions between explanatory variables
- Simpson's Paradox

Chapter 3

- Extend to many explanatory variables
- Implement linear regression algorithm

Chapter 4

- Logistic regression with multiple explanatory variables
- Logistic distribution
- Implement logistic regression algorithm

There is more to learn

- Training and testing sets
- Cross validation
- P-values and significance

Advanced regression

- Modeling with Data in the Tidyverse
- Generalized Linear Models in R
- Machine Learning with caret in R
- Bayesian Regression Modeling with rstanarm

Let's practice!

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