

Modsim cheat sheet

Simple Rotations

$$R_x(\theta) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos(\theta) & -\sin(\theta) \\ 0 & \sin(\theta) & \cos(\theta) \end{bmatrix}$$

$$R_y(\theta) = \begin{bmatrix} \cos(\theta) & 0 & \sin(\theta) \\ 0 & 1 & 0 \\ -\sin(\theta) & 0 & \cos(\theta) \end{bmatrix}$$

$$R_z(\theta) = \begin{bmatrix} \cos(\theta) & -\sin(\theta) & 0 \\ \sin(\theta) & \cos(\theta) & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Positive Real

$H(s)$ positive real iff

1. No poles with real part > 0
2. $H(s)$ real for all positive and real s
3. $\text{Re}[H(s)] \geq 0$ for all $\text{Re}[s] > 0$.

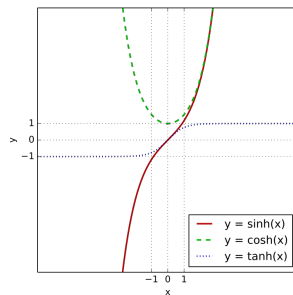
Euler's Formula

$$e^{ix} = \cos(x) + i \sin(x)$$

Hyperbolic Trig

$$\sinh(\sigma + j\omega) = \sinh \sigma \cos \omega + j \cosh \sigma \sin \omega$$

$$\cosh(\sigma + j\omega) = \cosh \sigma \cos \omega + j \sinh \sigma \sin \omega$$

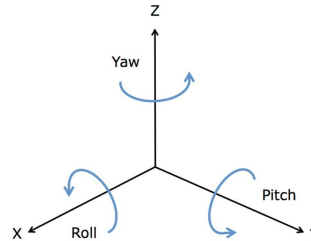


Skew Symmetric Matrix

$$\mathbf{a} = \begin{bmatrix} a_1 \\ a_2 \\ a_3 \end{bmatrix} \iff \mathbf{a}^\times = \begin{bmatrix} 0 & -a_3 & a_2 \\ a_3 & 0 & -a_1 \\ -a_2 & a_1 & 0 \end{bmatrix}$$

- $u \times v$ corresponds to $\mathbf{u}^\times \mathbf{v}$
- $(\mathbf{a}^\times)^\top = -(\mathbf{a}^\times)$

Roll Pitch Yaw



Dot Product

- $\vec{v} \cdot \vec{u} = |\vec{v}| |\vec{u}| \cos \theta$
- $\mathbf{v} \cdot \mathbf{u} = \mathbf{u}^\top \mathbf{v}$

Transpose

1. $(\mathbf{A} + \mathbf{B})^\top = \mathbf{A}^\top + \mathbf{B}^\top$
2. $(\mathbf{AB})^\top = \mathbf{B}^\top \mathbf{A}^\top$
3. $(c\mathbf{A})^\top = c\mathbf{A}^\top$
4. $\det(\mathbf{A}^\top) = \det(\mathbf{A})$
5. $(\mathbf{A}^\top)^{-1} = (\mathbf{A}^{-1})^\top$

Stability Function

- Explicit methods
 $R(h\lambda) = \det [\mathbf{I} - \lambda h(\mathbf{A} - \mathbf{1b}^\top)]$
- Other methods
 $R(h\lambda) = [1 + \lambda h \mathbf{b}^\top (\mathbf{I} - h\lambda \mathbf{A})^{-1}]$
 $R(h\lambda) = \frac{\det[\mathbf{I} - \lambda h(\mathbf{A} - \mathbf{1b}^\top)]}{\det[\mathbf{I} - \lambda h \mathbf{A}]}$

Matrix Inverse

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix}^{-1} = \frac{1}{ab - cd} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$$