

# TTK4215 Adaptive Control

## Assignment 8

**6.1** Consider the first order plant

$$y = \frac{b}{s-1}u$$

where  $b > 0$  is the only unknown parameter. Design and analyze a direct MRAC scheme that can stabilize the plant and force  $y$  to follow the output  $y_m$  of the reference model

$$y_m = \frac{2}{s+2}r$$

for any bounded and continuous reference signal  $r$ .

**6.2** The dynamics of a throttle to speed subsystem of a vehicle may be represented by the first-order system

$$V = \frac{b}{s+a}\theta + d$$

where  $V$  is the vehicle speed,  $\theta$  is the throttle angle and  $d$  is a constant load disturbance. The parameters  $b > 0, a$  are unknown constants whose values depend on the operating state of the vehicle that is defined by the gear state, steady-state velocity, drag, etc. We would like to design a cruise control system by choosing the throttle angle  $\theta$  so that  $V$  follows a desired velocity  $V_m$  generated by the reference model

$$V_m = \frac{0.5}{s+0.5}V_s$$

where  $V_s$  is the desired velocity set by the driver.

- (a) Assume that  $a, b$ , and  $d$  are known exactly. Design an MRC law that meets the control objective.
- (b) Design and analyze a direct MRAC scheme to be used in the case of  $a, b$ , and  $d$  (with  $b > 0$ ) being unknown.
- (c) Simulate your scheme in (b) by assuming  $V_s = 35$  and using the following values for  $a, b$ , and  $d$ : (i)  $a = 0.02, b = 1.3, d = 10$ ; (ii)  $a = 0.02(2 + \sin 0.01t), b = 1.3, d = 10 \sin 0.02t$ .