## practical\_exercise\_2, Methods 3, 2021, autumn semester

[FILL IN YOUR NAME]

[FILL IN THE DATE]

# Assignment 1: Using mixed effects modelling to model hierarchical data

In this assignment we will be investigating the *politeness* dataset of Winter and Grawunder (2012) and apply basic methods of multilevel modelling.

```
pacman::p_load(rstanarm, tidyverse, lmerTest, lme4)
pacman::p_load(MuMIn, effects)
```

#### **Dataset**

The dataset has been shared on GitHub, so make sure that the csv-file is on your current path. Otherwise you can supply the full path.

```
politeness <- read.csv('politeness.csv') ## read in data</pre>
```

## Exercises and objectives

The objectives of the exercises of this assignment are:

- 1) Learning to recognize hierarchical structures within datasets and describing them 2) Creating simple multilevel models and assessing their fitness
- 3) Write up a report about the findings of the study

REMEMBER: In your report, make sure to include code that can reproduce the answers requested in the exercises below

REMEMBER: This assignment will be part of your final portfolio

## Exercise 1 - describing the dataset and making some initial plots

- 1) Describe the dataset, such that someone who happened upon this dataset could understand the variables and what they contain
  - i. Also consider whether any of the variables in *politeness* should be encoded as factors or have the factor encoding removed. Hint: ?factor

#### summary(politeness)

```
##
      subject
                          gender
                                              scenario
                                                         attitude
   Length: 224
##
                       Length: 224
                                                       Length: 224
                                          Min.
                                                  :1
   Class : character
                       Class :character
                                           1st Qu.:2
                                                       Class : character
##
   Mode :character
                       Mode :character
                                          Median:4
                                                       Mode :character
##
                                           Mean
##
                                           3rd Qu.:6
##
                                          Max.
                                                  :7
##
##
  total_duration
                           fOmn
                                        hiss_count
##
  Min.
          : 0.988
                      Min.
                             : 80.8
                                      Min.
                                             :0.0000
   1st Qu.: 6.140
                      1st Qu.:134.5
                                      1st Qu.:0.0000
## Median : 12.640
                      Median :211.6
                                      Median :0.0000
## Mean
          : 24.176
                      Mean
                             :197.9
                                      Mean
                                              :0.4509
## 3rd Qu.: 39.373
                      3rd Qu.:247.1
                                      3rd Qu.:1.0000
           :101.375
                             :415.8
                                              :5.0000
## Max.
                      Max.
                                      Max.
##
                      NA's
                             :12
```

```
#Change variables to appropiate factors
politeness <- politeness %>%
  mutate(scenario = as.factor(scenario)) %>%
  mutate(gender = as.factor(gender)) %>%
  mutate(attitude = as.factor(attitude))
head(politeness)
```

```
subject gender scenario attitude total_duration f0mn hiss_count
##
## 1
          F1
                   F
                                    pol
                                                 18.392 214.6
                             1
                   F
## 2
          F1
                                    inf
                                                 13.551 210.9
                                                                         0
                             1
## 3
          F1
                   F
                             2
                                    pol
                                                  5.217 284.7
                                                                         0
## 4
          F1
                   F
                             2
                                                  4.247 265.6
                                                                         0
                                    inf
## 5
          F1
                   F
                                    pol
                                                                         0
                             3
                                                  6.791 210.6
## 6
          F1
                   F
                             3
                                                  4.126 285.6
                                                                         0
                                    inf
```

2) Create a new data frame that just contains the subject F1 and run two linear models; one that expresses f0mn as dependent on scenario as an integer; and one that expresses f0mn as dependent on scenario encoded as a factor.

```
politeness_F1 <- politeness %>%
  filter(subject == "F1")
m1 <- lm(f0mn ~ scenario, data = politeness_F1)
m2 <- lm(f0mn ~ as.integer(scenario), data = politeness_F1)</pre>
```

i. Include the model matrices, \$X\$ from the General Linear Model, for these two models in your report a

### Scenario Encoded as Factor

# #Design Matrix model.matrix(m1)

```
##
       (Intercept) scenario2 scenario3 scenario4 scenario5 scenario6 scenario7
## 1
                             0
                                        0
                                                   0
                                                              0
                                                                          0
## 2
                             0
                                        0
                                                   0
                                                              0
                                                                          0
                                                                                     0
                 1
## 3
                 1
                             1
                                        0
                                                   0
                                                              0
                                                                          0
                                                                                     0
                                        0
                                                   0
                                                                                     0
## 4
                 1
                             1
                                                              0
                                                                          0
## 5
                 1
                             0
                                        1
                                                   0
                                                              0
                                                                          0
                                                                                     0
                             0
                                        1
                                                   0
                                                              0
                                                                          0
                                                                                     0
## 6
                 1
## 7
                             0
                                        0
                                                   1
                                                              0
                                                                          0
                                                                                     0
                 1
                             0
                                        0
                                                              0
                                                                                     0
## 8
                 1
                                                   1
                                                                          0
## 9
                 1
                             0
                                        0
                                                   0
                                                              1
                                                                         0
                                                                                     0
## 10
                 1
                             0
                                        0
                                                   0
                                                              1
                                                                          0
                                                                                     0
## 11
                 1
                            0
                                        0
                                                   0
                                                              0
                                                                         1
                                                                                     0
                                                              0
## 12
                 1
                             0
                                        0
                                                   0
                                                                          1
                                                                                     0
## 13
                             0
                                        0
                                                   0
                                                              0
                                                                          0
                                                                                     1
                 1
                             0
                                        0
                                                   0
                                                                          0
                                                                                     1
## attr(,"assign")
## [1] 0 1 1 1 1 1 1
## attr(,"contrasts")
## attr(,"contrasts")$scenario
## [1] "contr.treatment"
```

#### summary(m1)

```
##
## Call:
## lm(formula = f0mn ~ scenario, data = politeness_F1)
## Residuals:
##
     Min
              1Q Median
                            3Q
## -37.50 -13.86
                   0.00 13.86
                                37.50
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
                             20.35
                 212.75
                                  10.453 1.6e-05 ***
## (Intercept)
## scenario2
                  62.40
                             28.78
                                     2.168
                                             0.0668
                  35.35
                                     1.228
## scenario3
                             28.78
                                             0.2591
## scenario4
                  53.75
                             28.78
                                     1.867
                                             0.1041
                  27.30
                             28.78
                                     0.948
                                             0.3745
## scenario5
## scenario6
                 -7.55
                             28.78
                                    -0.262
                                             0.8006
## scenario7
                 -14.95
                             28.78
                                   -0.519
                                             0.6195
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 28.78 on 7 degrees of freedom
## Multiple R-squared: 0.6576, Adjusted R-squared:
## F-statistic: 2.24 on 6 and 7 DF, p-value: 0.1576
```

The design matrix is a [14x7] matrix, so we will get the following  $\beta_{0-6}$ . This is also shown by the summary of a our linear regression model. A simple regression f0mn ~ scenario was conducted. Scenario seemed to

account for 36.4% of the variance in f0mn following adjusted R^2. F(1,6) = 2.24, p > 0.5) all beta values were insignificant. We only have 14 observations spread out over 7 different levels. So the high p-value is most likely due to sample-size. A further power-analysis could show the required sample size required.

## Scenario Encoded as Int

```
#Design Matrix
model.matrix(m2)
### (Intercept) as.integer(scenario)
```

```
(Intercept) as.integer(scenario)
## 1
                                           1
                  1
## 2
                  1
                                           1
                                           2
## 3
                  1
## 4
                  1
                                           2
## 5
                  1
                                           3
## 6
                  1
                                           3
                                           4
## 7
                  1
## 8
                                           4
## 9
                                           5
                  1
                                           5
## 10
                  1
## 11
                  1
                                           6
## 12
                  1
                                           6
                                           7
## 13
                  1
## 14
                                           7
                  1
## attr(,"assign")
## [1] 0 1
```

### summary(m2)

```
##
## Call:
## lm(formula = f0mn ~ as.integer(scenario), data = politeness_F1)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
  -44.836 -36.807
                     6.686
                           20.918
                                   46.421
##
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         262.621
                                     20.616 12.738 2.48e-08 ***
                          -6.886
                                      4.610 -1.494
                                                       0.161
## as.integer(scenario)
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 34.5 on 12 degrees of freedom
## Multiple R-squared: 0.1568, Adjusted R-squared: 0.0865
## F-statistic: 2.231 on 1 and 12 DF, p-value: 0.1611
```

Now that scenario is encoded as an integer the design matrix will be a [14x2] matrix. Our model will therefore only give us  $\beta_{0-1}$  and not a  $\beta$  for each level of scenario as done in the previous model. This model assumes

that there is a constant increment of f0mn following a "increase" in scenario (if you can even talk about a unit increase of scenario). This would only make sense if scenarios were ordered as getting harder and harder. The model is again f0mn ~ scenario F(1,12) = 2.231, p>0.5) with an adjusted  $R^2 = 0.0865$  showing an explained variance of 8.65% ( $\beta_1 = -6.886$ , SE = 4.6, t = -1.5, p>0.16.) Again such a small sample size might be tricky to work with.

#### ii. Which coding of \_scenario\_, as a factor or not, is more fitting?

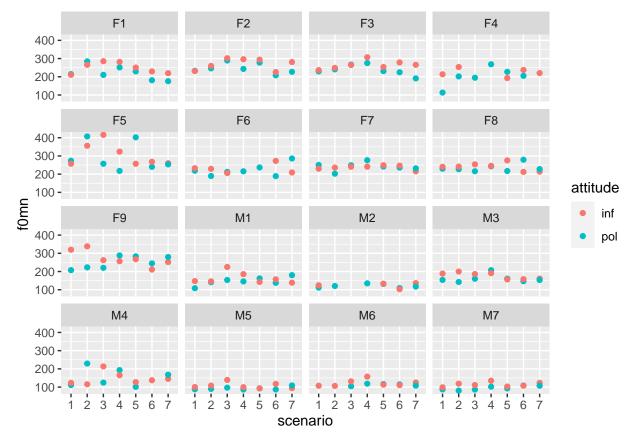
I would argue that scenario treated as a factor makes more sense. As mentioned a linear relationship between scenario number and f0mn does not make sense.

Scenario's effect on f0mn in such a scenario as, Scenario[1] < Scenario[2] > Scenario[3]. Would not be possible to model having scenario as an integer.

- 3) Make a plot that includes a subplot for each subject that has *scenario* on the x-axis and f0mn on the y-axis and where points are colour coded according to attitude
  - i. Describe the differences between subjects

```
ggplot(politeness, aes(x = scenario, y = f0mn, colour = attitude)) + geom_point()+
facet_wrap(~subject)
```

## Warning: Removed 12 rows containing missing values (geom\_point).



There seem to be a lower baseline/intercept given that you're a male. Attitude doesn't seem to have an large effect on f0mn. So an idea could be to add Gender as a fixed effect and subject as a random intercept as there is also individual variance within the gender category.

## Exercise 2 - comparison of models

For this part, make sure to have lme4 installed. You can install it using install.packages("lme4") and load it using library(lme4) lmer is used for multilevel modelling

```
mixed.model <- lmer(f0mn ~ scenario + gender + (1|subject), data=politeness)</pre>
```

- 1) Build four models and do some comparisons
  - i. a single level model that models f0mn as dependent on gender

```
m3.1 <- lm(f0mn ~ gender, data = politeness)
```

ii. a two-level model that adds a second level on top of i. where unique intercepts are modelled for ea

```
m3.2 <- lmer(f0mn ~ gender + (1|scenario), data = politeness, REML = F)
```

iii. a two-level model that only has \_subject\_ as an intercept

```
m3.3 <- lmer(f0mn ~ gender + (1|subject), data = politeness, REML = F)
summary(m3.3)</pre>
```

```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
    method [lmerModLmerTest]
## Formula: f0mn ~ gender + (1 | subject)
##
     Data: politeness
##
##
                      logLik deviance df.resid
        AIC
                BIC
##
     2112.0
             2125.5 -1052.0
                               2104.0
##
## Scaled residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -3.2405 -0.5471 -0.1431 0.4360 3.8443
##
## Random effects:
  Groups
           Name
                        Variance Std.Dev.
## subject (Intercept) 511.2
                                 22.61
## Residual
                        1026.7
                                 32.04
## Number of obs: 212, groups: subject, 16
##
## Fixed effects:
##
              Estimate Std. Error
                                        df t value Pr(>|t|)
## (Intercept) 246.547
                          8.083
                                    15.984 30.501 1.36e-15 ***
## genderM
              -115.193
                           12.239
                                    16.076 -9.412 6.08e-08 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Correlation of Fixed Effects:
##
           (Intr)
## genderM -0.660
```

```
iv. a two-level model that models intercepts for both _scenario_ and _subject_
m3.4 <- lmer(f0mn ~ gender + (1|scenario) + (1|subject), data = politeness, REML = F)
summary(m3.4)
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
     method [lmerModLmerTest]
## Formula: f0mn ~ gender + (1 | scenario) + (1 | subject)
     Data: politeness
##
##
        AIC
                BIC
                      logLik deviance df.resid
##
     2105.2
             2122.0 -1047.6
                               2095.2
                                            207
##
## Scaled residuals:
               1Q Median
      Min
##
                               3Q
## -3.0357 -0.5384 -0.1177 0.4346 3.7808
##
## Random effects:
## Groups
            Name
                        Variance Std.Dev.
## subject (Intercept) 516.19
                                 22.720
                                  9.453
## scenario (Intercept) 89.36
## Residual
                        940.25
                                 30.664
## Number of obs: 212, groups: subject, 16; scenario, 7
## Fixed effects:
              Estimate Std. Error
                                        df t value Pr(>|t|)
                                     19.248 27.952 < 2e-16 ***
## (Intercept) 246.778
                          8.829
## genderM
              -115.186
                           12.223
                                    16.011 -9.424 6.19e-08 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Correlation of Fixed Effects:
           (Intr)
## genderM -0.604
v. which of the models has the lowest residual standard deviation, also compare the Akaike Information
#Calculate Residual Standard Deivation
c(S_res1 = sqrt(sum(resid(m3.1)^2)/(nrow(politeness)-2)),
S_res2 = sqrt(sum(resid(m3.2)^2)/(nrow(politeness)-2)),
S_res3 = sqrt(sum(resid(m3.3)^2)/(nrow(politeness)-2)),
S_res4 = sqrt(sum(resid(m3.4)^2)/(nrow(politeness)-2)))
     S_res1
             S_res2
                      S_res3
                               S_res4
## 38.38130 37.10991 30.27006 28.62566
#Compare AIC
AIC(m3.1,m3.2,m3.3,m3.4)
       df
               ATC
## m3.1 3 2163.971
## m3.2 4 2162.257
## m3.3 4 2112.048
```

## m3.4 5 2105.176

m3.4 is the model with the lowest residual standard deviation and also performs the best following the AIC.

vi. which of the second-level effects explains the most variance?

```
#Anova cannot compare multi-level and single-level models. :(
anova(m3.2, m3.3, m3.4)
## Data: politeness
## Models:
## m3.2: f0mn ~ gender + (1 | scenario)
## m3.3: f0mn ~ gender + (1 | subject)
## m3.4: f0mn ~ gender + (1 | scenario) + (1 | subject)
                        BIC logLik deviance
##
                 AIC
                                                 Chisq Df Pr(>Chisq)
        npar
           4 2162.3 2175.7 -1077.1
## m3.2
                                       2154.3
## m3.3
           4 2112.1 2125.5 -1052.0
                                       2104.1 50.2095 0
## m3.4
           5 2105.2 2122.0 -1047.6
                                       2095.2 8.8725 1
                                                             0.002895 **
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
#Look for varaince explained
MuMIn::r.squaredGLMM(m3.2)
## Warning: 'r.squaredGLMM' now calculates a revised statistic. See the help page.
              R<sub>2</sub>m
                         R2c
## [1,] 0.6817304 0.6965456
MuMIn::r.squaredGLMM(m3.3)
               R2m
                         R<sub>2</sub>c
## [1,] 0.6798832 0.7862932
MuMIn::r.squaredGLMM(m3.4)
##
              R<sub>2</sub>m
                         R<sub>2</sub>c
## [1,] 0.6787423 0.8045921
```

M3.2 (f0mn  $\sim$  gender + (1|scenario)) showed the best variance explained purely by fixed effects. But m3.4 (f0mn  $\sim$  gender + (1|scenario) + (1|subject)) showed most explained variance with 80% of the variance being accounted for from both fixed and random effects.

We can also conclude that adding subject as random intercept rather than scenario explains more of the variance but also has more shared variance with our fixed effect gender.

- 2) Why is our single-level model bad?
  - i. create a new data frame that has three variables, subject, gender and f0mn, where f0mn is the average of all responses of each subject, i.e. averaging across attitude and scenario\_

```
politeness_sel <- politeness %>%
  filter(!is.na(f0mn)) %>%
  group_by(subject) %>%
  summarise(f0mn = mean(f0mn))

politeness_sel <- politeness_sel %>%
  mutate(gender = if_else(grepl("F", politeness_sel$subject, ignore.case = T), "F", "M")) %>%
  mutate(gender = as.factor(gender))
```

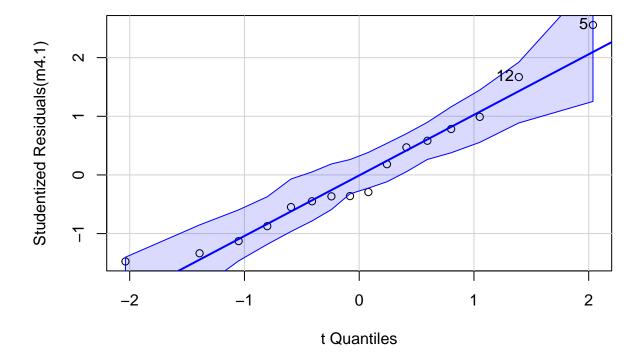
ii. build a single-level model that models \_fOmn\_ as dependent on \_gender\_ using this new dataset

```
m4.1 <- lm(f0mn ~ gender, data = politeness_sel)
```

iii. make Quantile-Quantile plots, comparing theoretical quantiles to the sample quantiles) using 'qqno

```
#qqPlot
car::qqPlot(m4.1, main = "QQplot for the mean model")
```

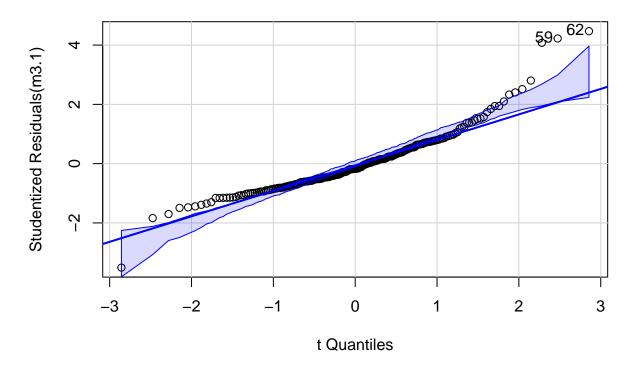
## **QQplot for the mean model**



```
## [1] 5 12
```

```
car::qqPlot(m3.1, main = "QQplot for the normal model")
```

# **QQplot for the normal model**



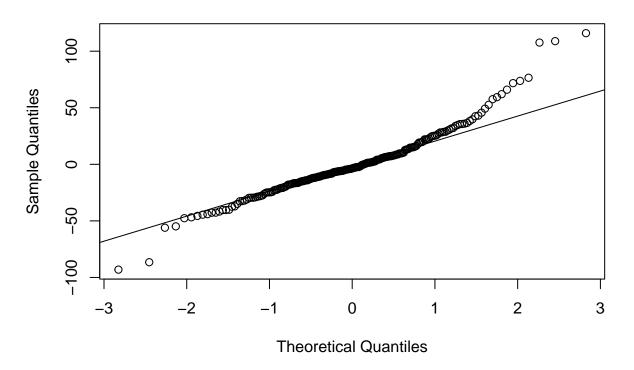
## [1] 59 62

Both models residual distribution seems to be slighly heavy tailed. This could be solved with a simple yuen trim of outliers. The first model 4.1 holds the assumptions for the GLM better than the new model where f0mn is averaged.

iv. Also make a quantile-quantile plot for the residuals of the multilevel model with two intercepts.

```
#car::qqPlot doesn't like mixed effect models so we do it like this.
qqnorm(resid(m3.4))
qqline(resid(m3.4))
```

## Normal Q-Q Plot



- 3) Plotting the two-intercepts model
  - i. Create a plot for each subject, (similar to part 3 in Exercise 1), this time also indicating the fitted value for each of the subjects for each for the scenarios (hint use fixef to get the "grand effects" for each gender and ranef to get the subject- and scenario-specific effects)

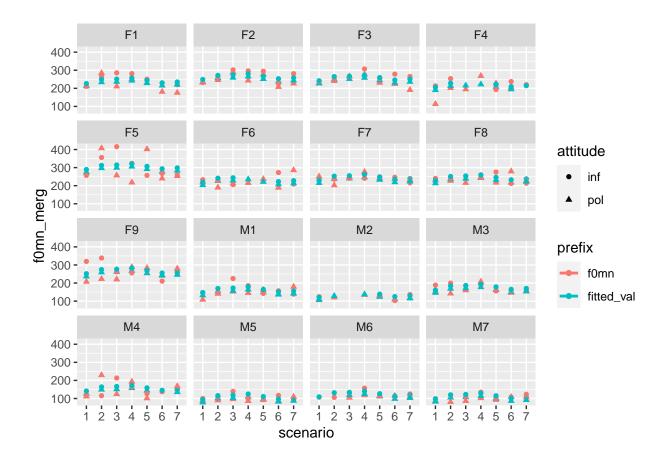
```
politeness_fil <- politeness %>% #Remove NA's
    filter(!is.na(f0mn))

m3.5<- lmer(f0mn ~ scenario + attitude + (1|subject), data = politeness_fil) #new fit

politeness_fit <- politeness_fil %>% #Create data frame with fitted and actual values.
    mutate(fitted_val = fitted.values(m3.5)) %>%
    pivot_longer(cols = c(f0mn,fitted_val) , names_to = "prefix", values_to = "f0mn_merg")

ggplot(politeness_fit, aes(x = scenario, y = f0mn_merg, colour = prefix, shape = attitude)) + geom_poin
```

## 'geom\_smooth()' using formula 'y ~ x'



### Exercise 3 - now with attitude

- 1) Carry on with the model with the two unique intercepts fitted (scenario and subject).
  - i. now build a model that has attitude as a main effect besides gender

```
m5.1 \leftarrow lmer(f0mn \sim attitude + gender + (1|subject) + (1|scenario), data = politeness, REML = F)
```

ii. make a separate model that besides the main effects of \_attitude\_ and \_gender\_ also include their is

 $m5.2 \leftarrow lmer(f0mn \sim attitude*gender + (1|subject)+ (1|scenario), data = politeness, REML = F)$ 

iii. describe what the interaction term in the model says about Korean men's pitch when they are polite

```
summary(m5.2)
```

```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
## method [lmerModLmerTest]
## Formula: f0mn ~ attitude * gender + (1 | subject) + (1 | scenario)

## Data: politeness
##
## AIC BIC logLik deviance df.resid
## 2096.0 2119.5 -1041.0 2082.0 205
```

```
##
## Scaled residuals:
##
       Min
                 1Q Median
                                         Max
   -2.8460 -0.5893 -0.0685
                             0.3946
                                      3.9518
##
##
##
  Random effects:
##
    Groups
             Name
                          Variance Std.Dev.
##
    subject
             (Intercept) 514.09
                                    22.674
##
    scenario (Intercept)
                           99.08
                                     9.954
##
    Residual
                          876.46
                                    29.605
##
   Number of obs: 212, groups:
                                  subject, 16; scenario, 7
##
##
  Fixed effects:
                        Estimate Std. Error
##
                                                    df t value Pr(>|t|)
                                                        27.521
                                                                 < 2e-16 ***
## (Intercept)
                         255.632
                                       9.289
                                                23.556
## attitudepol
                         -17.198
                                       5.395
                                               190.331
                                                        -3.188
                                                                 0.00168 **
                        -118.251
                                      12.841
                                                        -9.209 1.28e-08 ***
##
  genderM
                                                19.922
## attitudepol:genderM
                           5.563
                                       8.241
                                               190.388
                                                         0.675
                                                                0.50049
##
                   0 '*** 0.001 '** 0.01 '* 0.05 '. ' 0.1 ' 1
## Signif. codes:
##
## Correlation of Fixed Effects:
##
                (Intr) atttdp gendrM
## attitudepol -0.299
## genderM
                -0.605
                       0.216
## atttdpl:gnM 0.195 -0.654 -0.323
MuMIn::r.squaredGLMM(m5.2)
               R<sub>2</sub>m
                         R<sub>2</sub>c
## [1,] 0.6904904 0.8178935
levels(politeness$gender)
## [1] "F" "M"
levels(politeness$attitude)
```

```
## [1] "inf" "pol"
```

The model f0mn ~ attitude:gender + (1|subject)+ (1|scenario)has an  $R^2c$  0.81 both attitude and gender showed a significant effect on f0mn ( $\beta_1$ (attitude\_pol) = -17.2, SE = 5.4, p>0.05) and ( $\beta_2$ (genderM) = -119, SE = 12.8, p>0.05). Being polite and male lowers your frequency. Being both Male and Polite has an interaction effect of ( $\beta_3$  = 5.5, SE = 8.24, p<0.05). Hereby concluding that there is a small positive insignificant interaction effect of being male and polite. The SE being proportional large compared to the effect size makes it very difficult to say anything meaningfull.

2) Compare the three models (1. gender as a main effect; 2. gender and attitude as main effects; 3. gender and attitude as main effects and the interaction between them. For all three models model unique intercepts for *subject* and *scenario*) using residual variance, residual standard deviation and AIC.

```
#reidual variance
c(RS_5.2 = sum(residuals(m5.2)^2),
RS 5.1 = sum(residuals(m5.1)^2),
RS 3.4 = sum(residuals(m3.4)^2)
    RS_5.2
              RS_5.1
                       RS_3.4
## 169305.6 169681.1 181913.0
#residual standard deviation
c(S_{res5.2} = sqrt(sum(resid(m5.2)^2)/(nrow(politeness)-2)),
S_res5.1 = sqrt(sum(resid(m5.2)^2)/(nrow(politeness)-2)),
S_{res3.4} = sqrt(sum(resid(m3.4)^2)/(nrow(politeness)-2)))
## S_res5.2 S_res5.1 S_res3.4
## 27.61590 27.61590 28.62566
anova(m3.4, m5.1, m5.2)
## Data: politeness
## Models:
## m3.4: f0mn ~ gender + (1 | scenario) + (1 | subject)
## m5.1: f0mn ~ attitude + gender + (1 | subject) + (1 | scenario)
## m5.2: f0mn \sim attitude * gender + (1 | subject) + (1 | scenario)
                AIC
                       BIC logLik deviance
                                              Chisq Df Pr(>Chisq)
##
        npar
## m3.4
           5 2105.2 2122.0 -1047.6
                                     2095.2
## m5.1
           6 2094.5 2114.6 -1041.2
                                     2082.5 12.6868 1
                                                        0.0003683 ***
           7 2096.0 2119.5 -1041.0
## m5.2
                                     2082.0 0.4551 1 0.4998998
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

- 3) Choose the model that you think describe the data the best and write a short report on the main findings based on this model. At least include the following:
- i. describe what the dataset consists of
- ii. what can you conclude about the effect of gender and attitude on pitch (if anything)?
- iii. motivate why you would include separate intercepts for subjects and scenarios (if you think they should be included)
- iv. describe the variance components of the second level (if any)
- v. include a Quantile-Quantile plot of your chosen model

## My answer to all of the above

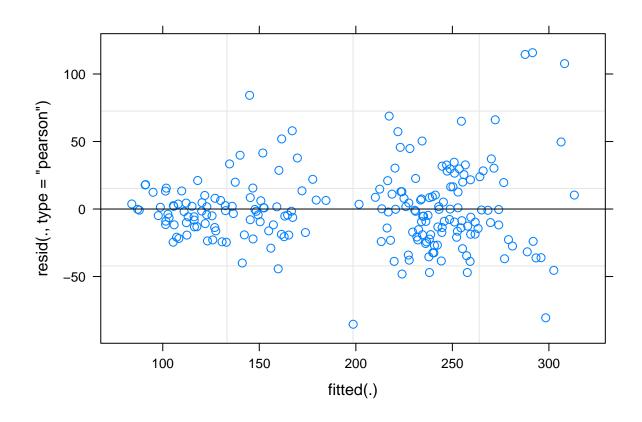
I have selected the model 5.1 (f0mn  $\sim$  gender + attitude + (1|subject) + (1|scenario)) My decision is based primary based on AIC R\_res and RS. But theoretically it also makes sense to include both random intercepts due to the study being repeated measure and some variance being random/unsystematic. attitude furthermore seems like an important addition to the model as specific attitudes are correlated with pitch frequency

(See imaginary study). However the interaction between gender:attitude doesn't add any explaining to the model.

```
summary(m5.1)
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
    method [lmerModLmerTest]
##
## Formula: f0mn ~ attitude + gender + (1 | subject) + (1 | scenario)
     Data: politeness
##
##
##
        AIC
                 BIC
                       logLik deviance df.resid
              2114.6 -1041.2
##
     2094.5
                                2082.5
                                            206
##
## Scaled residuals:
##
               1Q Median
                                3Q
      Min
                                       Max
## -2.8791 -0.5968 -0.0569 0.4260 3.9068
##
## Random effects:
## Groups
            Name
                         Variance Std.Dev.
## subject (Intercept) 514.92
                                  22.692
## scenario (Intercept) 99.22
                                   9.961
                         878.39
                                  29.638
## Residual
## Number of obs: 212, groups: subject, 16; scenario, 7
##
## Fixed effects:
##
              Estimate Std. Error
                                         df t value Pr(>|t|)
## (Intercept) 254.408
                             9.117
                                     21.800 27.904 < 2e-16 ***
## attitudepol -14.817
                             4.086 190.559 -3.626 0.000369 ***
                                    16.000 -9.494 5.63e-08 ***
## genderM
              -115.447
                            12.161
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Correlation of Fixed Effects:
##
               (Intr) atttdp
## attitudepol -0.231
## genderM
              -0.583 0.006
MuMIn::r.squaredGLMM(m5.1)
              R<sub>2</sub>m
                        R2c
```

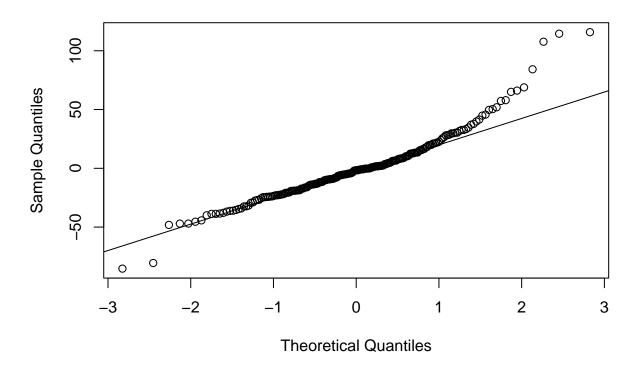
```
#check assumptions
plot(m5.1)
```

## [1,] 0.6899193 0.8175096



```
qqnorm(resid(m5.1))
qqline(resid(m5.1))
```

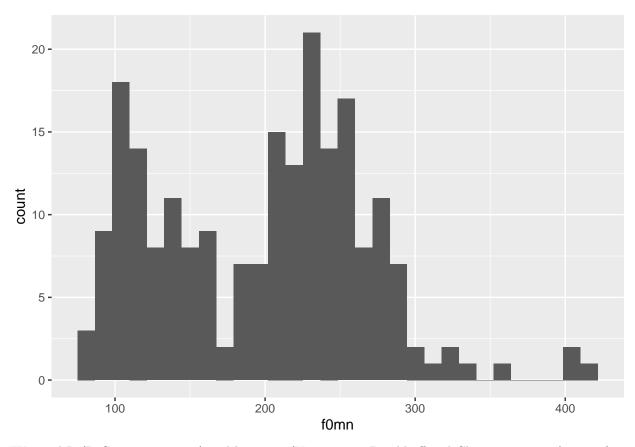
# Normal Q-Q Plot



```
ggplot(politeness, aes(x= f0mn)) + geom_histogram()
```

## 'stat\_bin()' using 'bins = 30'. Pick better value with 'binwidth'.

## Warning: Removed 12 rows containing non-finite values (stat\_bin).



"We used R (R Core Team, 2019) and lmerTest (Kuznetsova, Brockhoff and Christensen, 2017) to perform a linear mixed effects analysis of the relationship between f0mn, gender and attitude. As random effects, we had intercepts for subjects, and scenario.

Both fixed and random effects accounted for roughly 82% of the variance in the f0mn variable with random effects proportion being 12.7%. Visual inspection shows that both the qqplot and histogram violates the assumption of a mixed effect linear model. The more robust generalized mixed effect model with a link function would be preferred. But as did was not the task such model was not constructed.

f0mn was found to be significantly modulated by gender.  $\beta_2=-115, SE=12.16, p<0.05$  Attitude also showed a significant modulating of f0mn  $\beta_1=-14.8, SE=4, p<0.05$