

# CP2410 Practical 10

---

Sihan Chen, jcu ID: 14187662

## Question 1

The **merge-sort** will always take  $O(n \times \lg(n))$  time.

The **quick-sort** will expected (on average) to have time complexity of  $\Theta(n \times \lg(n))$ , while the worst case time complexity is  $O(n^2)$ .

## Question 2

Here is an implementation with time complexity of  $O(n)$ :

```
def get_non_duplicates(A: list) -> list:
    """ Return all non-duplicated elements. """
    result = []
    # In case of empty list
    if not A:
        return result
    # Insert the first element, start iteration from index of 1
    result.append(A[0])
    for i in range(1, len(A)):
        if A[i] != A[i - 1]:
            result.append(A[i])
    return result
```

Here is a screenshot from testing the code:



The screenshot shows a code editor with a dark theme. At the top, there's a code editor window with the following code:

```
14 A = [0, 1, 1, 2, 3, 5, 8]
1  print(get_non_duplicates(A))
```

Below the code editor, there's a terminal window with the following output:

```
pwsh ~\Dev\cp2410\Week10 > python .\q2.py
[0, 1, 2, 3, 5, 8]
```

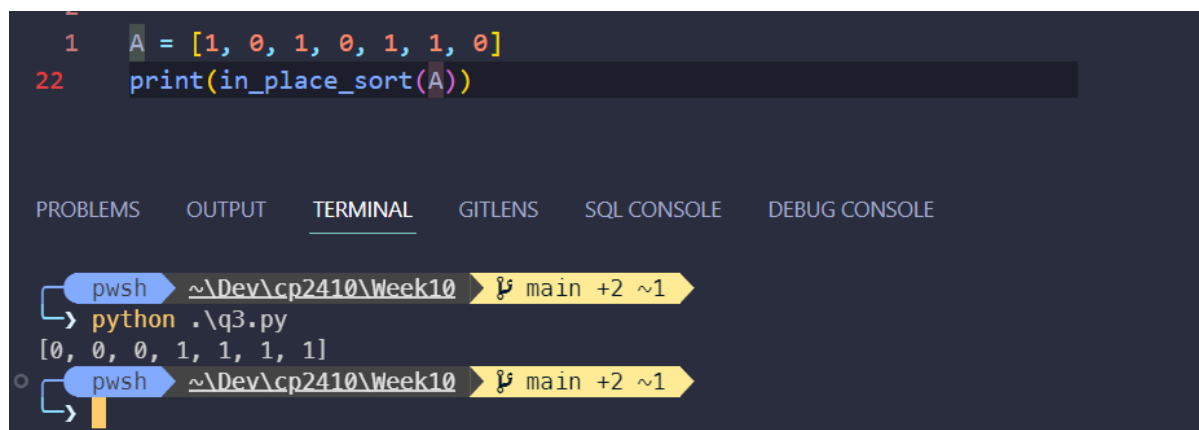
The terminal window also shows the command prompt and the file path.

## Question 3

Here is an in-place method of sorting all 0s before 1s.

```
def in_place_sort(A: list[int]) -> list:
    """ Sort all 0s before 1s in place. """
    i, j = 0, len(A) - 1
    # from left to right, find first 1 at index i
    for i in range(len(A)):
        if A[i] == 1:
            break
    # from right to left, find first 0 at index j
    for j in range(len(A)-1, -1, -1):
        if A[j] == 0:
            break
    # if i is bigger, the list is sorted
    if i > j:
        return A
    else:
        # otherwise 1 appears before 0, swap i and j
        A[i] = 0
        A[j] = 1
        return in_place_sort(A)
```

Here is a screenshot from testing the code:



The screenshot shows a code editor with a dark theme. At the top, there are two lines of code:

```
1 A = [1, 0, 1, 0, 1, 1, 0]
22 print(in_place_sort(A))
```

Below the code, there is a terminal window with the following tabs: PROBLEMS, OUTPUT, TERMINAL, GITLENS, SQL CONSOLE, and DEBUG CONSOLE. The TERMINAL tab is active, showing the execution of the code:

```
powershell ~\Dev\cp2410\Week10 > python .\q3.py
[0, 0, 0, 1, 1, 1, 1]
```

The terminal output shows the list [0, 0, 0, 1, 1, 1, 1] after the function is executed.

## Question 4

To achieve time complexity of  $O(n \times \log(n))$ , we can do a merge-sort on the sequence  $S$ . Then loop through the sorted array to find the most common element.

```
def find_winner(S:list[int]) -> int:
    """ Return the most frequent int, which represents a candidate. """
    # two edge cases
    if not S:
        return -1
    if len(S) == 1:
        return S[0]

    merge_sort(S)
    winner = S[0]
    prev_start = 0
    most_frequent = 0
    for i in range(1, len(S)):
        if S[i] != S[i-1]:
            count = i - prev_start
            if count > most_frequent:
                most_frequent = count
                winner = S[i-1]
            prev_start = i
    return winner

def merge_sort(arr):
    if len(arr) > 1:
        mid = len(arr) // 2
        L = arr[:mid]
        R = arr[mid:]
        merge_sort(L)
        merge_sort(R)
        i = j = k = 0
        while i < len(L) and j < len(R):
            if L[i] <= R[j]:
                arr[k] = L[i]
                i += 1
            else:
                arr[k] = R[j]
                j += 1
            k += 1
        while i < len(L):
            arr[k] = L[i]
            i += 1
            k += 1
        while j < len(R):
            arr[k] = R[j]
            j += 1
            k += 1
```

Here is a screenshot from testing the code:

```

1
51 S = [1, 2, 1, 2, 0, 5, 2, 3, 5, 1, 2]
1 print(find_winner(S))

```

PROBLEMS OUTPUT TERMINAL GITLENS SQL CONSOLE DEBUG CONSOLE

```

pwsh ~\Dev\cp2410\Week10 > python .\q4.py
[0, 1, 1, 1, 2, 2, 2, 2, 3, 5, 5]
(2, 4)

```

## Question 5

To achieve time complexity of  $O(n)$ , we can use dictionary (hash table) to track votes:

```

def find_election_winner(S: list[str]) -> str:
    """ Find the ecandidate with most votes. """
    d = {}
    for i in S:
        if i in d:
            d[i] = d[i] + 1
        else:
            d[i] = 0

    # return the key with highest value
    return max(d, key=d.get)

```

Here is a screenshot from testing the code:

```

1 S=['a', 'a', 'b', 'c', 'c', 'b', 'b']
14 print(find_election_winner(S))

```

PROBLEMS OUTPUT TERMINAL GITLENS SQL CONSOLE DEBUG CONSOLE

```

pwsh ~\Dev\cp2410\Week10 > python .\q5.py
b

```

## Question 6

Q 6.

merge-sort on [1000, 80, 10, 50, 70, 60, 90, 20]

1000	80	10	50	70	60	90	20
------	----	----	----	----	----	----	----

1000	80	10	50
------	----	----	----

70	60	90	20
----	----	----	----

1000	80
------	----

10	50
----	----

70	60
----	----

90	20
----	----

1000
------

80
----

10
----

50
----

70
----

60
----

90
----

20
----

80	1000
----	------

10	50
----	----

60	70
----	----

20	90
----	----

10	50	80	1000
----	----	----	------

20	60	70	90
----	----	----	----

10	20	50	60	70	80	90	1000
----	----	----	----	----	----	----	------