Vitamins

1. Draw the memory image of the linked list object as the following code executes:

```
from DoublyLinkedList import DoublyLinkedList


dll = DoublyLinkedList()
dll.add_first(1)
dll.add_last(3)
dll.add_last(5)
dll.add_after(dll.header.next, 2)
dll.add_before(dll.trailer.prev, 4)
dll.delete_node(dll.trailer.prev)
dll.add_first(0)

print(dll)
```

What is the output of the code?

2. During lecture you learned about the different methods of a doubly linked list.

   Provide the following worst-case runtime for those methods:

   a. `def __len__(self):`

   b. `def is_empty(self):`

   c. `def add_after(self, node, data):`

   d. `def add_first(self, data):`

   e. `def add_last(self, data):`

   f. `def add_before(self, node, data):`

   g. `def delete_node(self, node):`

   h. `def delete_first(self):`

   i. `def delete_last(self):`

3. Trace the following function. What is the output of the following code? Give mystery an appropriate name.

```
#dll = Doubly Linked List
def mystery(dll):

     if len(dll) >= 2:
          node = dll.trailer.prev.prev
          node.prev.next = node.next
          node.next.prev = node.prev

          node.next = None
          node.prev = None
          return node

     else:
          raise Exception("dll must have length of 2 of
          greater")

print(mystery(dll))
```

Coding

In this section, it is strongly recommended that you solve the problem on paper before writing code.

Download the **DoublyLinkedList.py** file attached under content on Brightspace

1. In class, we defined the `stack ADT` using a dynamic array as the underlying data structure. Because of the resizing, the ArrayStack run-time for its operations is not exactly in Θ(1). Instead, the cost is Θ(1) amortized.
   Define the stack ADT that guarantees each method to always run in Θ(1) **worst case**.
   ad

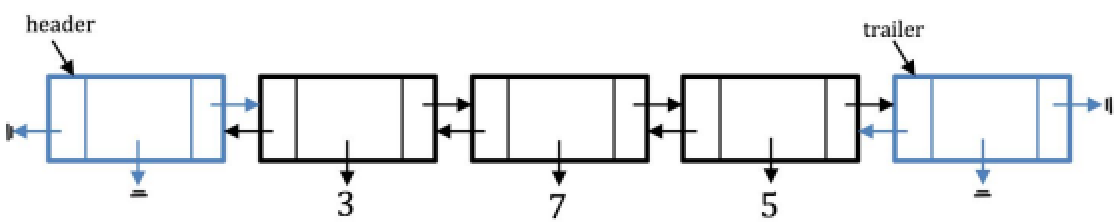
```
class LinkedStack:

    def __ init__(self):
        …

    def __len__(self):
    ''' Returns the number of elements in the stack. '''


    def is_empty(self):
    ''' Returns true if the stack is empty,false otherwise.
    '''


    def push(self, e):
    ''' Adds an element, e, to the top of the stack. '''


    def top(self):
    ''' Returns the element at the top of the stack.
        An exception is raised if the stack is empty. '''


    def pop(self):
    ''' Removes and returns the element at the top of the
    stack.
        An exception is raised if the stack is empty. '''
```

2. Implement the following method for the `DoublyLinkedList` class. The get item operator takes in an index, i, and returns the value at the ith node of the Doubly Linked List.

   You only need to support non-negative indices. Your solution should try to optimize the get item method. This means that you should decide whether to iterate from either the header or trailer based on whichever is closer to i. Index should start at 0.

```
def __getitem__(self, i):
    '''Return the value at the ith node. If i is out of range,
    an IndexError is raised'''
```

   For example, if your Doubly Linked List looks like this:




```
print(dll[0]) # 3 (should iterate from the header)

print(dll[1]) # 7 (either way works)

print(dll[2]) # 5 (should iterate from the trailer)

print(dll[3]) # IndexError
```

   What is the worst-case run-time of the get item operator? Can we do better?

3. In homework 5, you were asked to implement a `MidStack` ADT using an ArrayStack and an ArrayDeque. This time, you will create the MidStack using a **Doubly Linked List** with Θ(1) extra space. All methods of this MidStack should have a Θ(1) run-time.

   The middle is defined as the $(n + 1)//2\ th$ element, where n is the number of elements in the stack.

   Hint: To access the middle of the stack in constant time, you may want to define an additional data member to reference the middle of the Doubly Linked List.

```
class MidStack:

      def __ init__(self):
           self.data = DoublyLinkedList( )
           …

      def __len__(self):
      ''' Returns the number of elements in the stack. '''


      def is_empty(self):
      ''' Returns true if stack is empty and false otherwise.
      '''


      def push(self, e):
      ''' Adds an element, e, to the top of the stack. '''


      def top(self):
      ''' Returns the element at the top of the stack.
          An exception is raised if the stack is empty. '''


      def pop(self):
      ''' Removes and returns the element at the top of the
      stack.
          An exception is raised if the stack is empty. '''


      def mid_push(self, e):
      ''' Adds an element, e, to the middle of the stack.
          An exception is raised if the stack is empty. '''
```

4. Implement the `SinglyLinkedList`. A traditional SinglyLinkedList differs from the DoublyLinkedList in that there is only a header and no trailer. For this implementation of SinglyLinkedList however, we will include a header that is not pointing to a sentinel node and instead pointing to the first node of the SinglyLinkedList. We will also include a tail that is pointing to the last node of the SinglyLinkedList. Another difference between the SinglyLinkedList and the DoublyLinkedList is that each node only references the node after it. The last node in the linked list will reference its next Node as `None` (this would've been self.trailer for a DoublyLinkedList).

   You may add additional data members that are O(1) extra space. Analyze the run-time of each method after completing the implementation. Is it possible to make add_last and or delete_last work in O(1) constant run-time?

```
class SinglyLinkedList:
    class Node:
        def __init__(self, data=None, next=None):
            self.data = data
            self.next = next

        def disconnect(self):
            self.data = None
            self.next = None


    def __init__(self):
        self.header = None
        self.tail = None
        self.size = 0

    def __len__(self):
        return self.size

    def is_empty(self):
        return (len(self) == 0)

    def add_after(self, node, val):
      ''' Creates a new node containing val as its data and adds
      it after an existing node in the SinglyLinkedList'''

    def add_first(self, val):
      ''' Creates a new node containing val as its data and adds
      it to the front of the SinglyLinkedList'''
```

```
    def add_last(self, val):
     ''' Creates a new node containing val as its data and adds
     it to the back of the SinglyLinkedList'''


    def delete_first(self):
     ''' Removes an existing node from the front of the
     SinglyLinkedList and returns its value'''

    def delete_last(self):
     ''' Removes an existing node from the back of the
     SinglyLinkedList and returns its value'''

    def reverse(self):
     '''Reverses the list using node pointers and returns the
     new head. Solution must use constant space-complexity'''

    def __iter__(self):
        cursor = self.header
        while(cursor is not None):
            yield cursor.data
            cursor = cursor.next

    def __repr__(self):
        return "[" + " -> ".join([str(elem) for elem in self]) +
"]"
```