

## Transformation

Q. A cube defined by 8 vertices A(0,0,0), B(2,0,0), C(2,2,0), D(0,2,0), E(0,0,2), F(2,0,2), G(2,2,2), H(0,2,2). Find the final co-ordinates after it is rotated by 45 degree around a line joining the points (2,0,0) and (0,2,2).

Q. Calculate the position of a triangle P[2,4,1], Q[4,6,1], and R[2,6,1] after the reflection about a line  $x-2y=-4$ .

Q. A mirror is placed such that it passes through (2,0) and (0,2). Find the reflected view of a triangle with vertices (3,4), (5,5) and (4,7) in this mirror.

Q. A mirror is placed vertically such that it passes through the points(10,0) and (0,10). Find the reflected view of triangle ABC with co-ordinates A(5,50), B(20,40), C(10,70).

## Huffman Coding

What do you understand by compression techniques? Let  $A=\{a_1, \dots, a_6\}$  and frequency( $a_i$ )={45,13,12,16,9,5}, calculate the codeword length and entropy for the set using Huffman coding compression technique

## Illumination

Q.1. The position vectors for the vertices of a triangular surface are given by  $P_1 = (1,1,1)$ ,  $P_2 = (0,2,1)$ , and  $P_3 = (0,0,1)$ . Assume viewer position = (1,2,5),  $k_a = 0.7$ ,  $k_{diff} = 0.9$ ,  $k_{spec} = 0.6$ ,  $n = 10$ . White ambient intensity = 0.1, white point light position = (1,1,5) with intensity of 0.5. Illuminate a triangle using the Phong model where the intensity at the centroid of the triangle is  $P = (0.333, 1, 1)$ .

The following assumes a white object  $(r,g,b) = (1,1,1)$

Because the light is white, the intensity will be the same for each colour channel  $(r,g,b)$

Ambient

$$I_a k_a = 0.1(0.7) = 0.07$$

Diffuse

$$N = (P_1 - P_3) \times (P_2 - P_3)$$

$$= (1,1,0)^T \times (0,2,0)^T$$

$$= (0,0,1)^T$$

$$L = (1,1,5)^T - (0.333, 1, 1)^T$$

$$= (0.164, 0, 0.986)^T \text{ (normalized)}$$

$$I_{diff} (N \cdot L) = 0.5(0.9)(0.986) = 0.444$$

Specular

$$R = 2N(N \cdot L) - L$$

$$= 2(0,0,1)^T [0.986] - (0.164, 0, 0.986)^T$$

$$\begin{aligned}
&= (-0.164, 0, 0.986) \\
V &= (1, 2, 5)^T - (0.333, 1, 1)^T \\
&= (0.160, 0.239, 0.958)^T \quad (\text{normalized}) \\
R \cdot V &= 0.971 \\
I_{\text{spec}}(R \cdot V)^n &= 0.5(0.6)(0.971)^{10} \\
&= 0.5(0.6)(0.745)
\end{aligned}$$

$$= 0.224$$

Total  $I = 0.07 + 0.444 + 0.224$   
 $= 0.738$

Q.2. Calculate the pixel color value at the centroid P of the triangle whose vertices are A(0,3,5), B(6,10,23) and C(8,2,15). The color values at A,B and C are 0,12,63 respectively. Use the Gouraud technique for interpolation.

Q.3. Three points on a shiny metallic surface is given X(3,0,5), Y(16,0,7) and Z(10,0,10). The light vector is  $L=-i+2j-k$  and the viewing vector is given by  $V=i+1.5j+0.5k$ . Assuming that there is only one object and that is illuminated by a single light source, calculate the resultant intensity. Take  $k_d=0.5$ ,  $k_a=0.3$  and the same for specular reflection  $W(\theta)$  is 0.85. The value of n for specular reflection is 5. Assume  $I_a=1$ ,  $I_l=10$ , and neglect any intensity attenuation.

Q.3. The position vectors for the vertices of a triangular surface are given by P1(20,0,0), P2(0,20,0) and P3(0,0,20). A point light source is at P(0,0,40). Find the intensities at the vertices of the quadrilateral, if the ambient light intensity is 1 and the directional light intensity is 20. Assume  $k_a= k_d=0.3$ . Neglect any intensity attenuation and specular effect. Calculate the intensity at the centroid of the triangle using the Phong model.