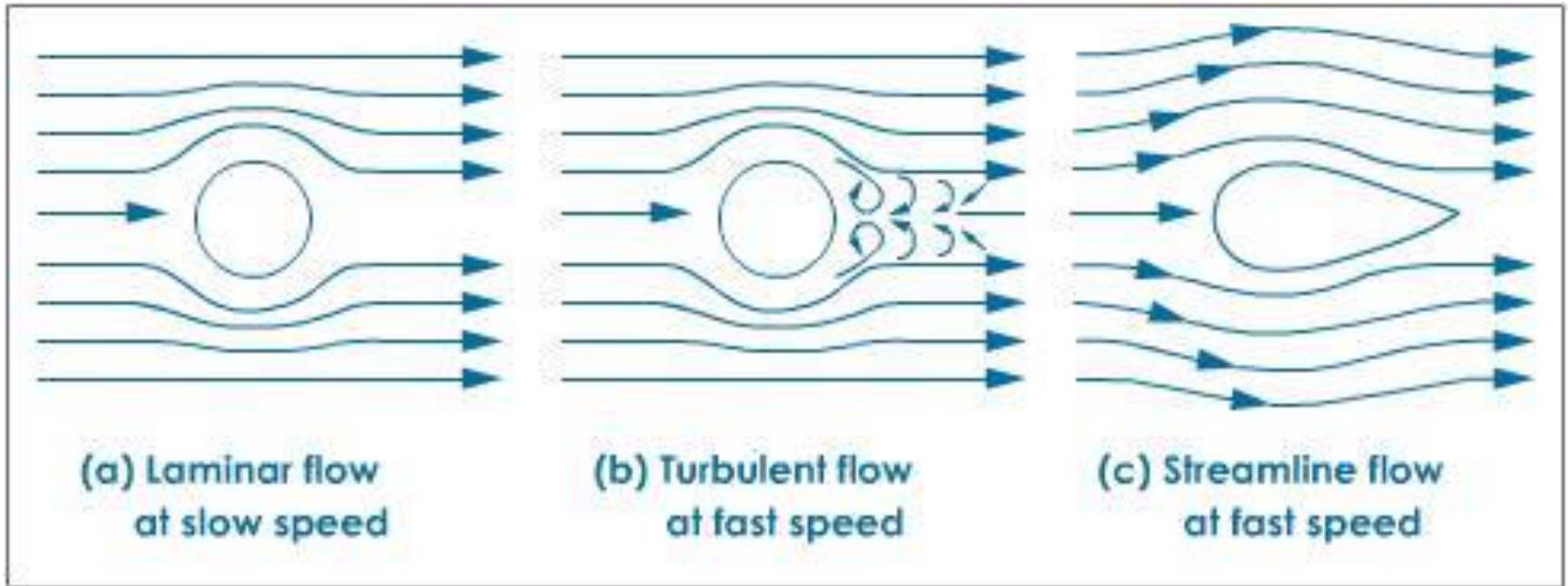


# Viscosity and Compressibility

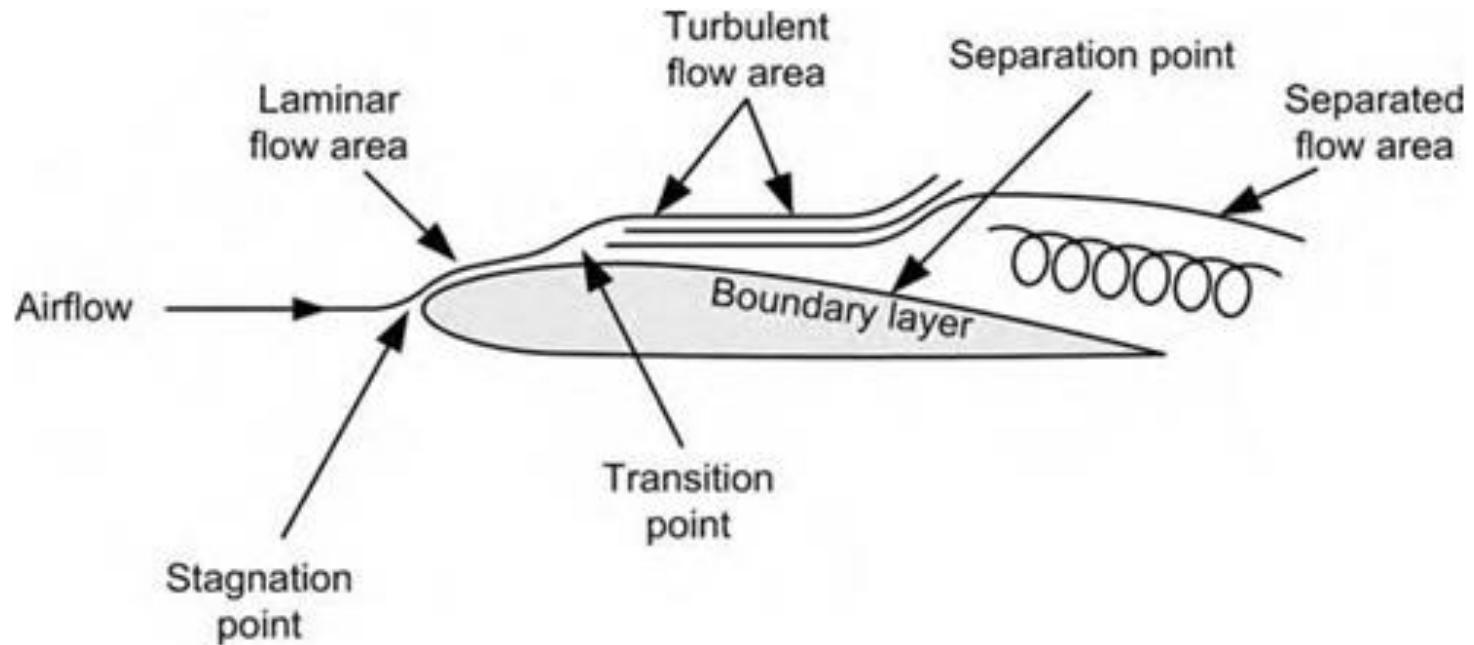
Innova Lee(이상훈)  
gcccompil3r@gmail.com

# Ideal Flow & Viscous Flow



<http://dvapphysics.wikispaces.com/Fluids+in+motion?showComments=1>

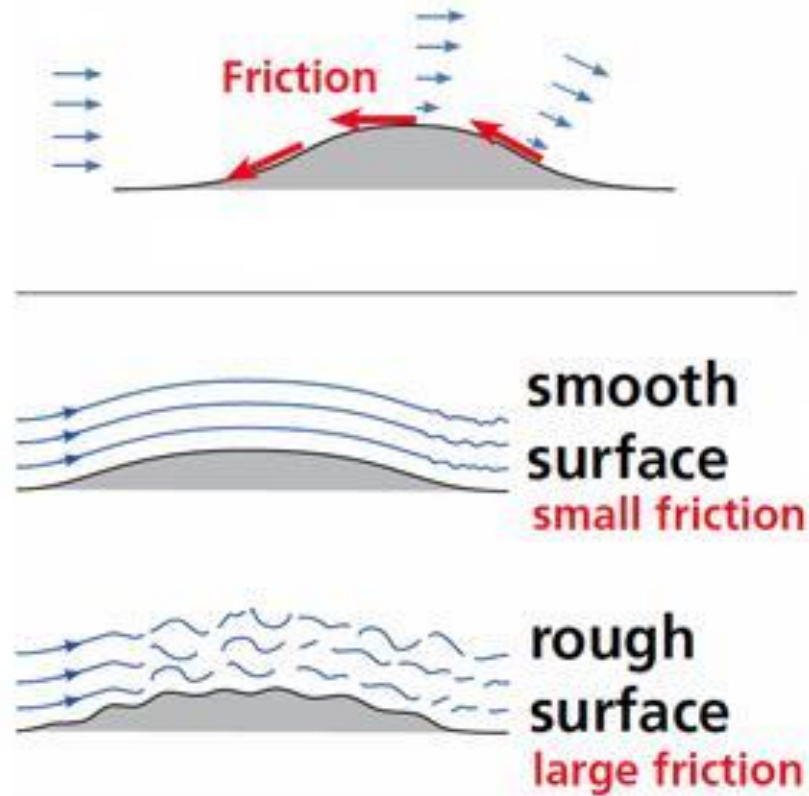
# Boundary Layer

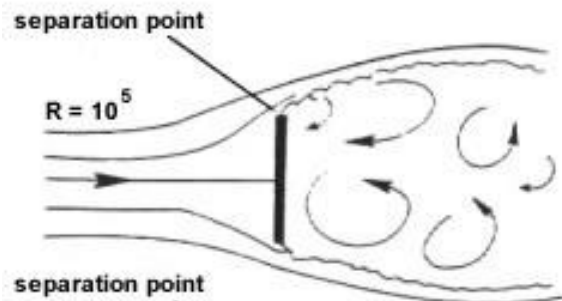


<http://www.zoombd24.com/boundary-layer-control-airfoil-boundary-layer-separation-control-devices-details/>

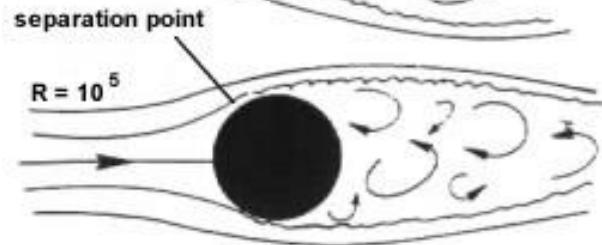
# Reason of Boundary Layer Separation

## Frictional drag





flat plate  
(broadside length) =  $d$   $C_D = 2.0$



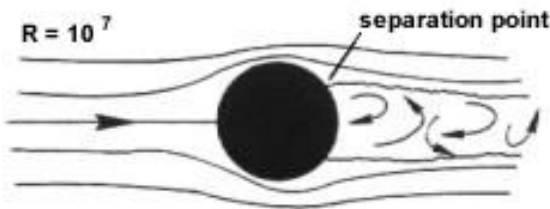
cylinder diameter =  $d$   $C_D = 1.2$



streamline body  
thickness =  $d$   $C_D = 0.12$



cylinder  
diameter =  $\frac{1}{10} d$   $C_D = 1.2$



cylinder  
diameter =  $d$   $C_D = 0.6$

## **Newtonian Fluid Reynolds** **Number (Re) Formula**

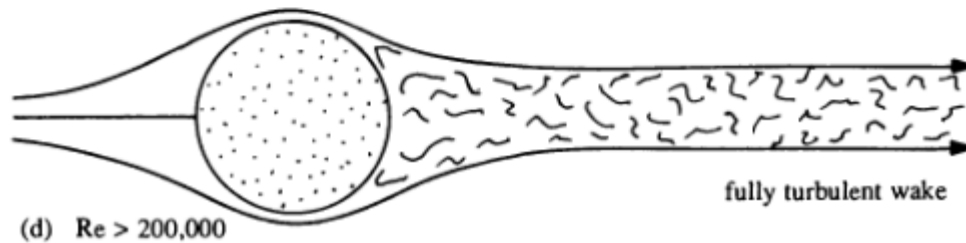
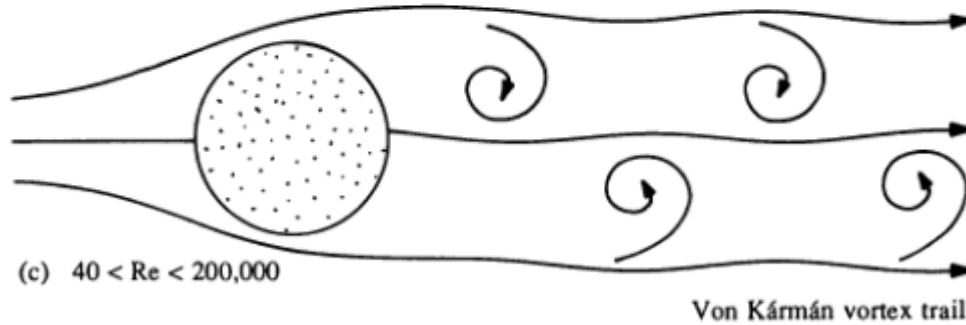
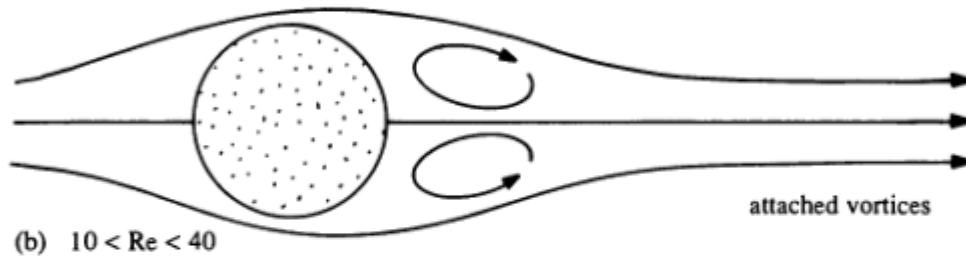
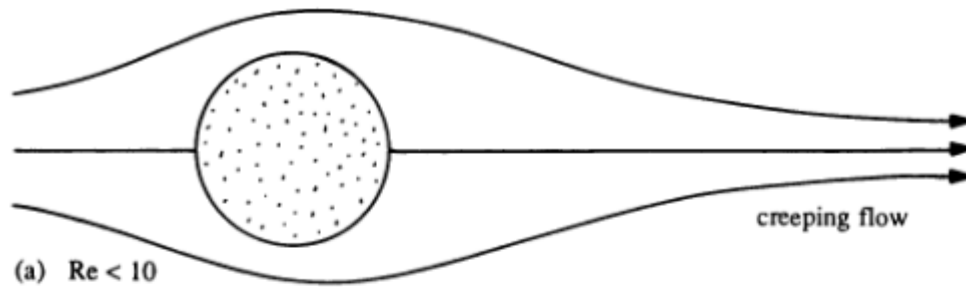
$$Re = \frac{\rho V D}{\mu}$$

$\mu$  – fluid dynamic viscosity in  $kg/(m.s)$

$\rho$  – fluid density in  $kg/m^3$

$V$  – fluid velocity in  $m/s$

$D$  – pipe diameter in  $m$



# Vortex Generator

**Before VGs**



Smooth airflow



Boundary layer  
begins to separate



Wing stalls

**After VGs**



Vortex airflow



Boundary layer  
energized by vortices

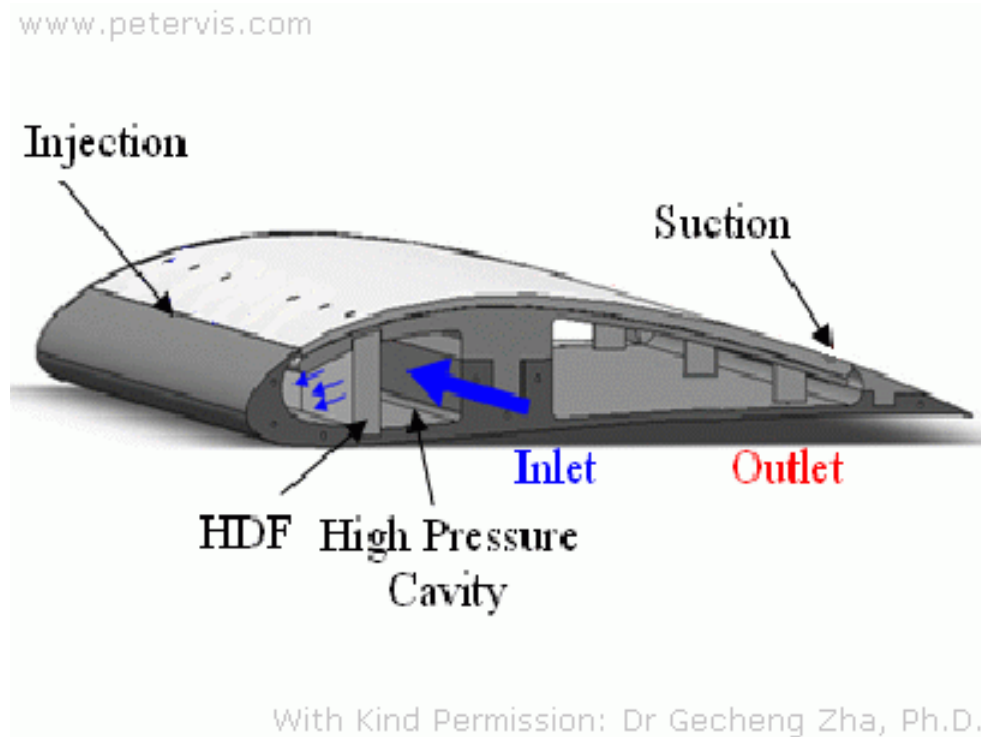


Boundary layer  
remains attached

<https://aviation.stackexchange.com/questions/13876/what-is-a-vortex-generator>



# Airfoil Suction



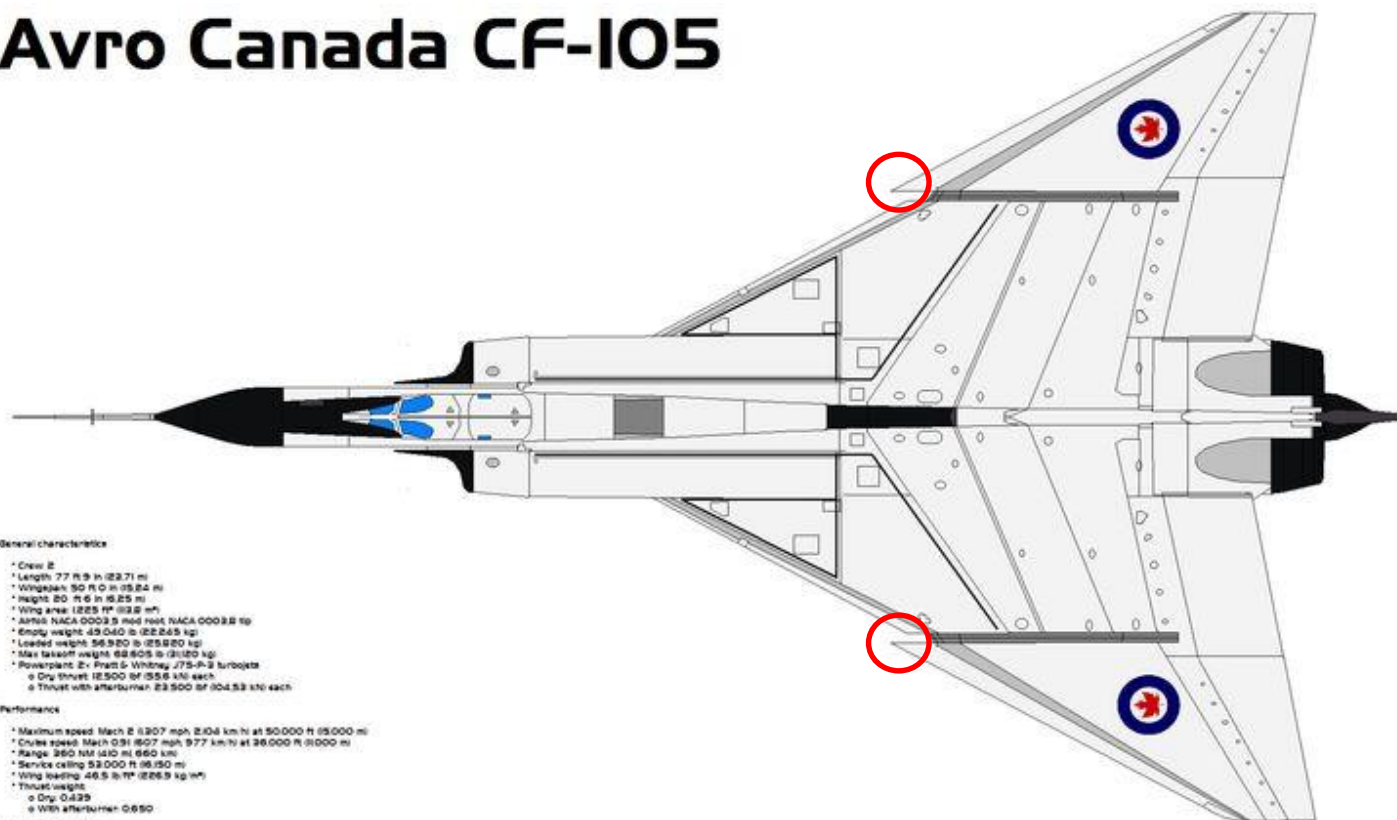
[https://www.petervis.com/interests/published/Supersonic Bi-directional flying wing SBiDir Sideways Flying Plane/ZNMF CFJ Airfoil.html](https://www.petervis.com/interests/published/Supersonic%20Bi-directional%20flying%20wing%20SBiDir%20Sideways%20Flying%20Plane/ZNMF%20CFJ%20Airfoil.html)

# Applying Saw-Tooth



[https://www.reddit.com/r/aviation/comments/6dn56x/mcdonnell\\_douglas\\_f4\\_phantom\\_ii/](https://www.reddit.com/r/aviation/comments/6dn56x/mcdonnell_douglas_f4_phantom_ii/)

# Avro Canada CF-105



## General characteristics

- \* Crew: 2
- \* Length: 77 ft 9 in (23.71 m)
- \* Wingspan: 50 ft 0 in (15.24 m)
- \* Height: 20 ft 6 in (6.25 m)
- \* Wing area: 1,225 ft² (113.8 m²)
- \* empty NACA 0003.5 mid root NACA 0009.8 tip
- \* Empty weight: 43,040 lb (22,245 kg)
- \* Loaded weight: 56,920 lb (25,820 kg)
- \* Max takeoff weight: 68,605 lb (31,180 kg)
- \* Powerplant: 2x Pratt & Whitney J75-P-3 turbojets
  - o Dry thrust: 12,500 lb (5,56 kN) each
  - o Thrust with afterburner: 23,500 lb (104.53 kN) each

## Performance

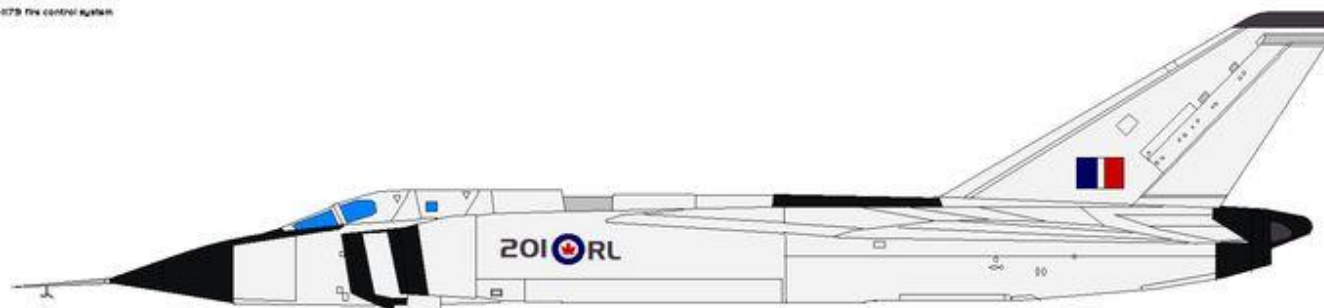
- \* Maximum speed: Mach 2 (2,007 mph, 3,234 km/h) at 50,000 ft (15,000 m)
- \* Cruise speed: Mach 0.91 (607 mph, 977 km/h) at 26,000 ft (8,000 m)
- \* Range: 360 NM (410 mi, 660 km)
- \* Service ceiling: 53,000 ft (16,150 m)
- \* Wing loading: 46.5 lb/ft² (226.9 kg/m²)
- \* Thrust weight:
  - o Dry: 0.439
  - o With afterburner: 0.690

## Armament (projected)

- \* Rockets: 4x AIM-26 denig unguided nuclear rockets
- \* Missiles: 2x AIM-4 Falcon Canada's Veint Dove cancelled (1956); 2 AIM-7 Sparrow II 2D active guidance missiles cancelled

## Avionics

- \* Hughes MX-579 fire control system



[This Link](#)



# ***Mach Number***

## ***Role in Compressible Flows***

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**V = velocity**

**$\rho$  = density**

**p = pressure**

**M = Mach**

**T = temperature**

**R = gas constant**

**a = speed of sound**

**$\gamma$  = specific heat ratio**

**Conservation of Momentum:**

$$\rho V dV = - dp$$

**Isentropic Flow:**

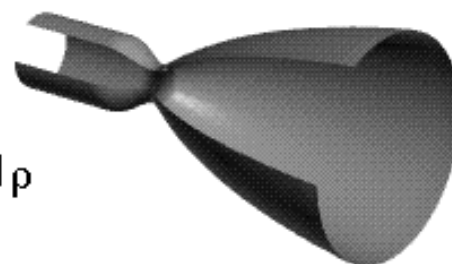
$$\frac{dp}{\rho} = \gamma \frac{d\rho}{\rho}$$

$$dp = \gamma \frac{p}{\rho} d\rho = \gamma R T d\rho$$

$$dp = a^2 d\rho$$

**Combine with Momentum:**

$$\rho V dV = - a^2 d\rho$$



$$-M^2 \frac{dV}{V} = \frac{d\rho}{\rho}$$

For subsonic flow ( $M < 1$ ), density is relatively constant

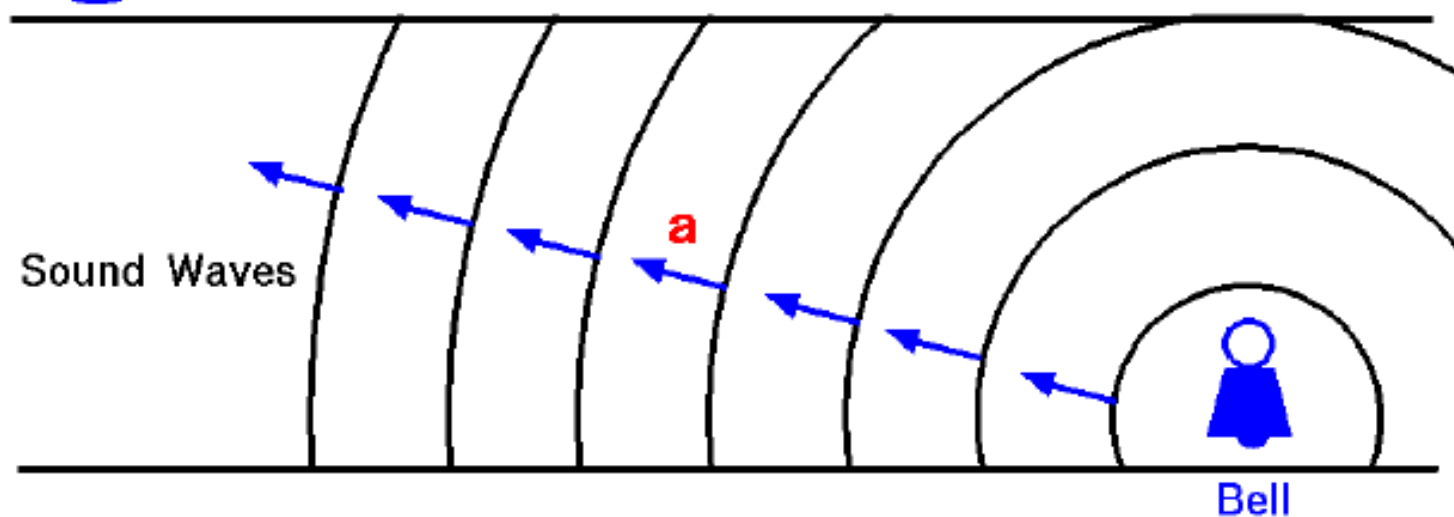
For transonic flow ( $M \sim 1$ ), density change is nearly equal to velocity change

For supersonic flow ( $M > 1$ ), density changes faster than the velocity  
by a factor of  $M^2$



## Speed of Sound

Glenn  
Research  
Center



Speed of sound (**a**) depends on the type of medium and the temperature of the medium.

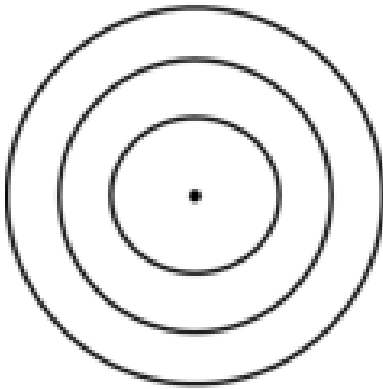
$$a = \text{sqrt}(\gamma R T)$$

$\gamma$  = ratio of specific heats (1.4 for air at STP)

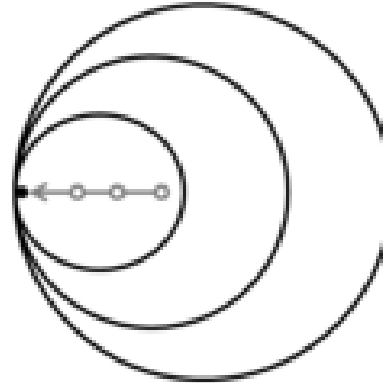
$R$  = gas constant ( $286 \text{ m}^2/\text{s}^2/\text{K}^0$  for air)

$T$  = absolute temperature ( $273.15 + ^\circ\text{C}$ )

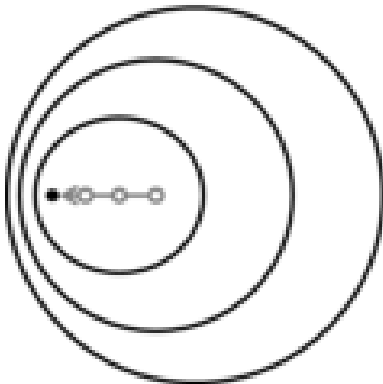
**Stationary  $M=0$**



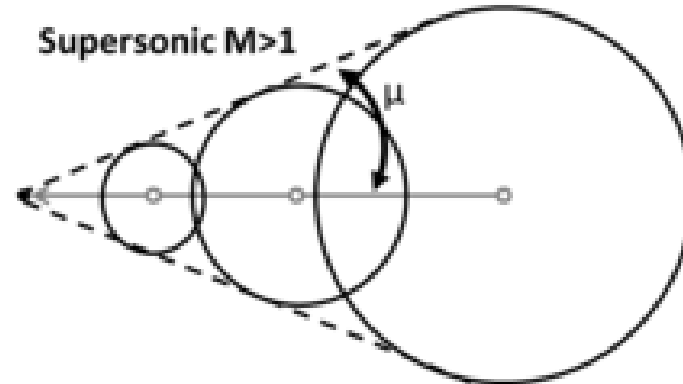
**Sonic  $M=1$**



**Subsonic  $0 < M < 1.0$**

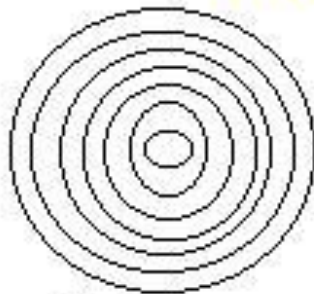


**Supersonic  $M > 1$**

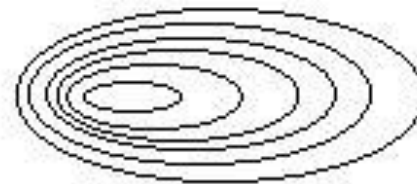


[https://en.wikipedia.org/wiki/Compressible\\_flow](https://en.wikipedia.org/wiki/Compressible_flow)

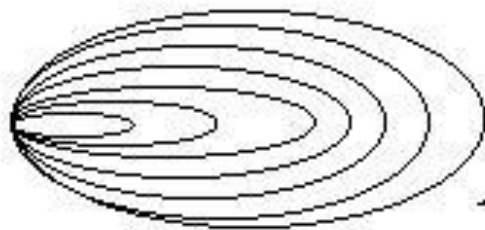
## Sound Waves At Various Velocities



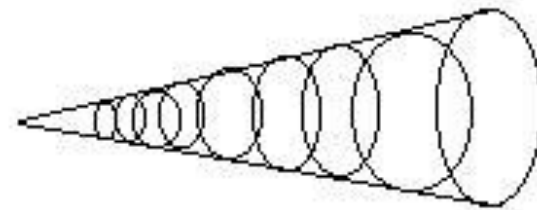
Stationary



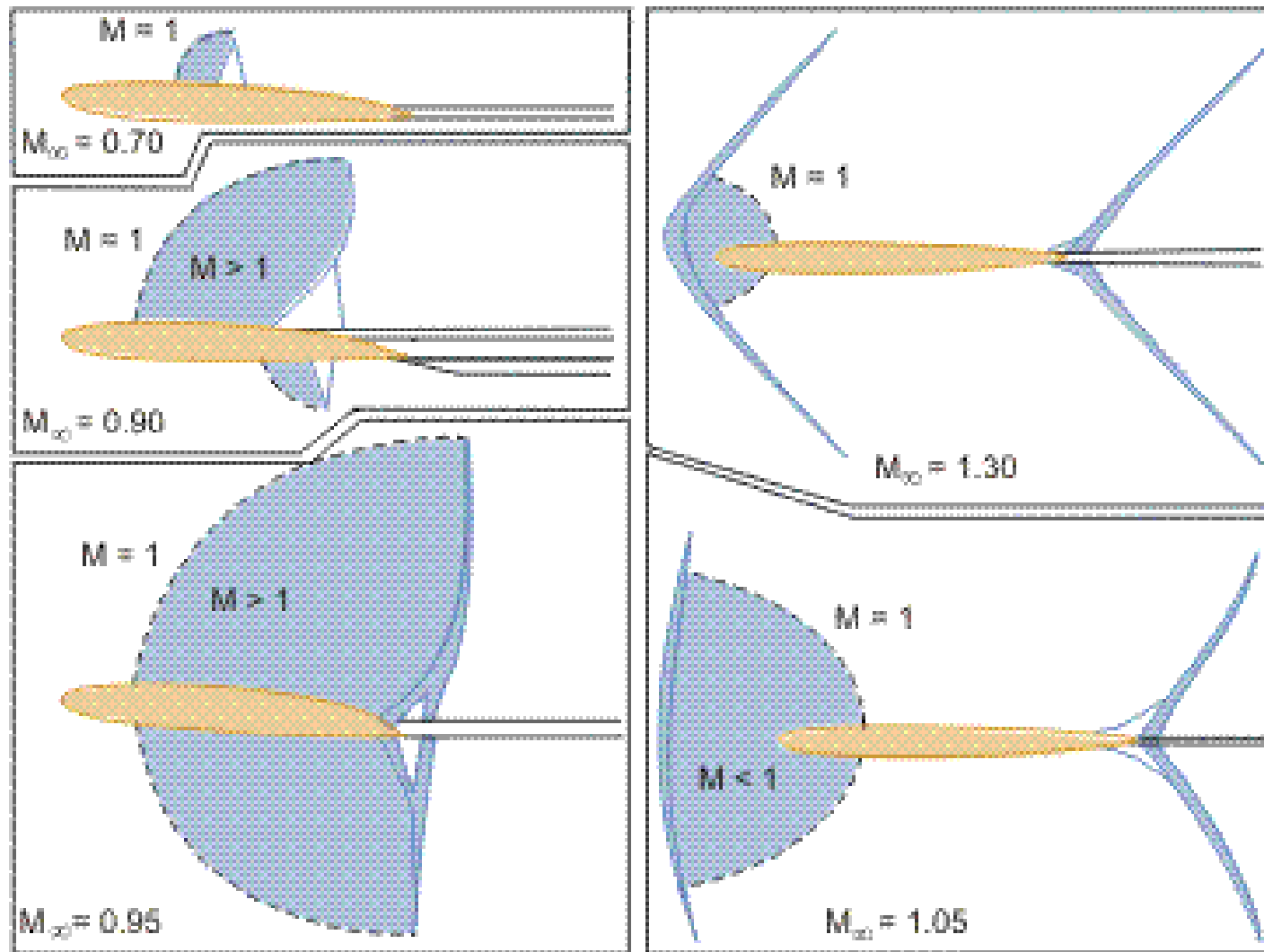
Moving Slower Than the Speed of Sound



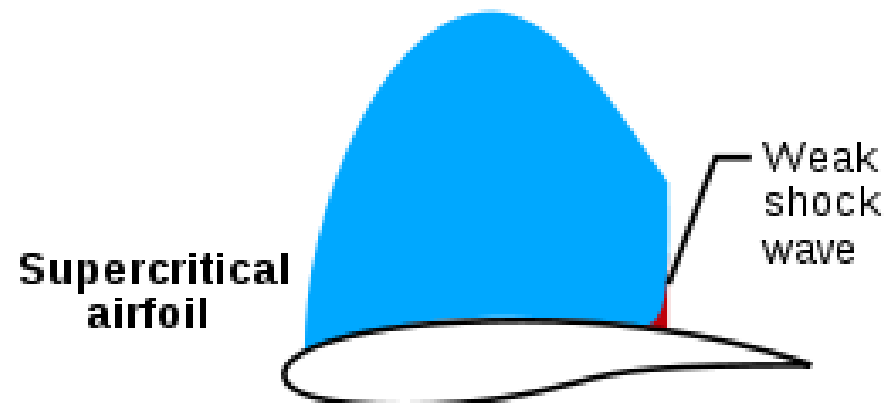
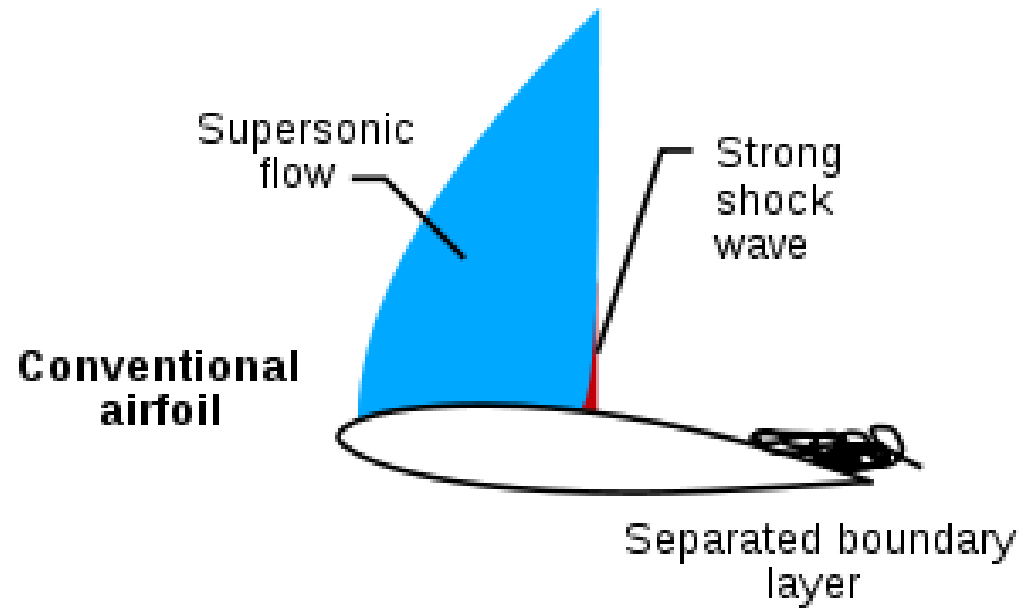
Moving at the Speed of Sound

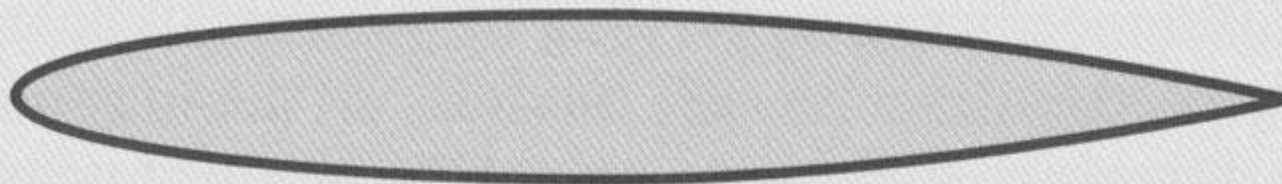


Moving Faster Than the Speed of Sound









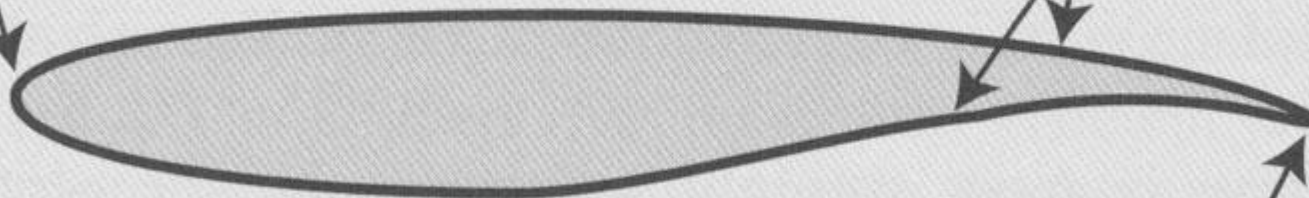
Conventional Aerofoil

Increased Nose  
Radius



Flat Upper  
Surface

Cambered  
Rear



Modern Supercritical  
Aerofoil

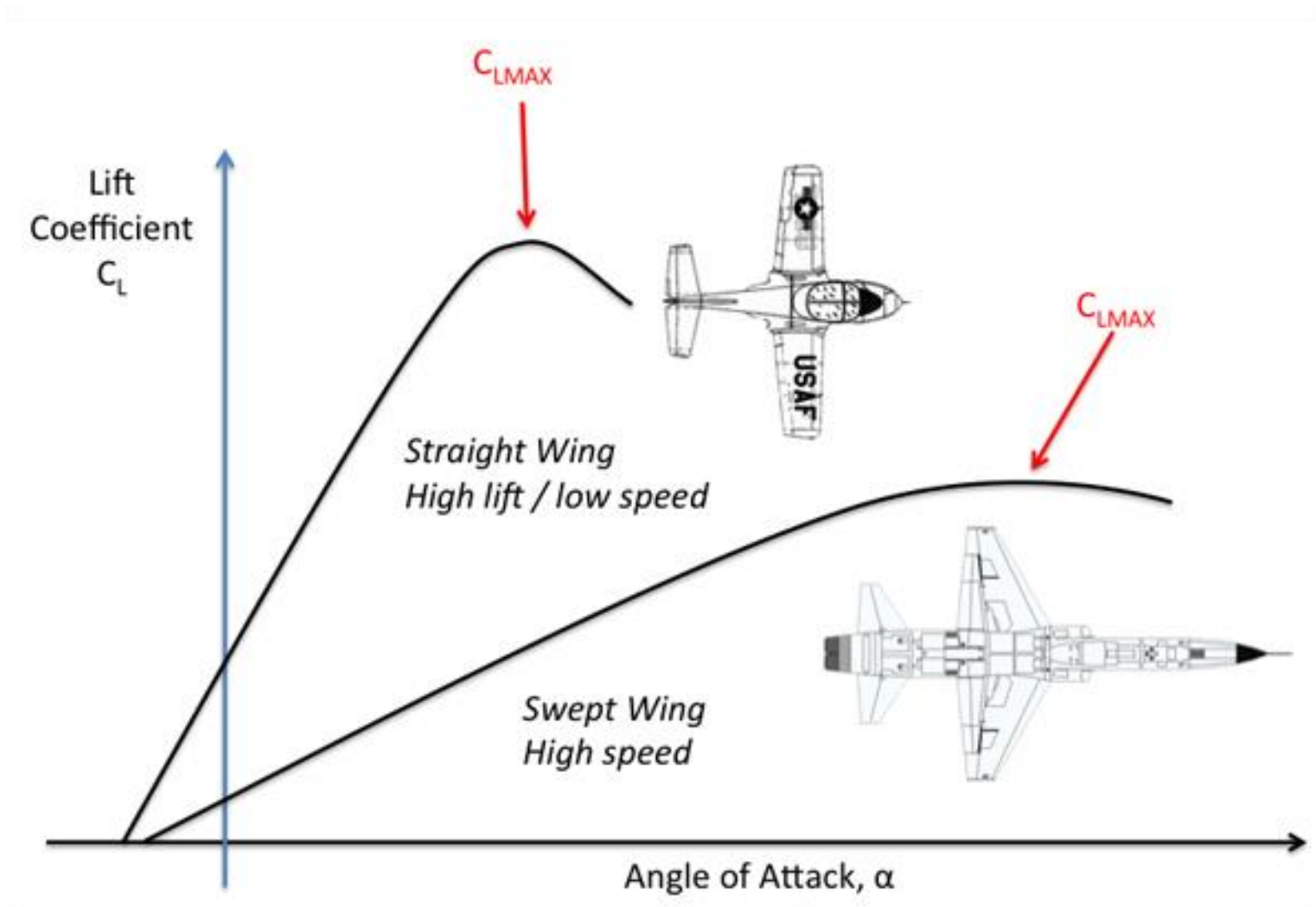
Blunt trailing  
Edge



Image copyright R. Whitford <http://www.VC10.net>



<https://www.flickr.com/photos/multiplyleadership/5299637305>







[https://en.wikipedia.org/wiki/Swept\\_wing](https://en.wikipedia.org/wiki/Swept_wing)



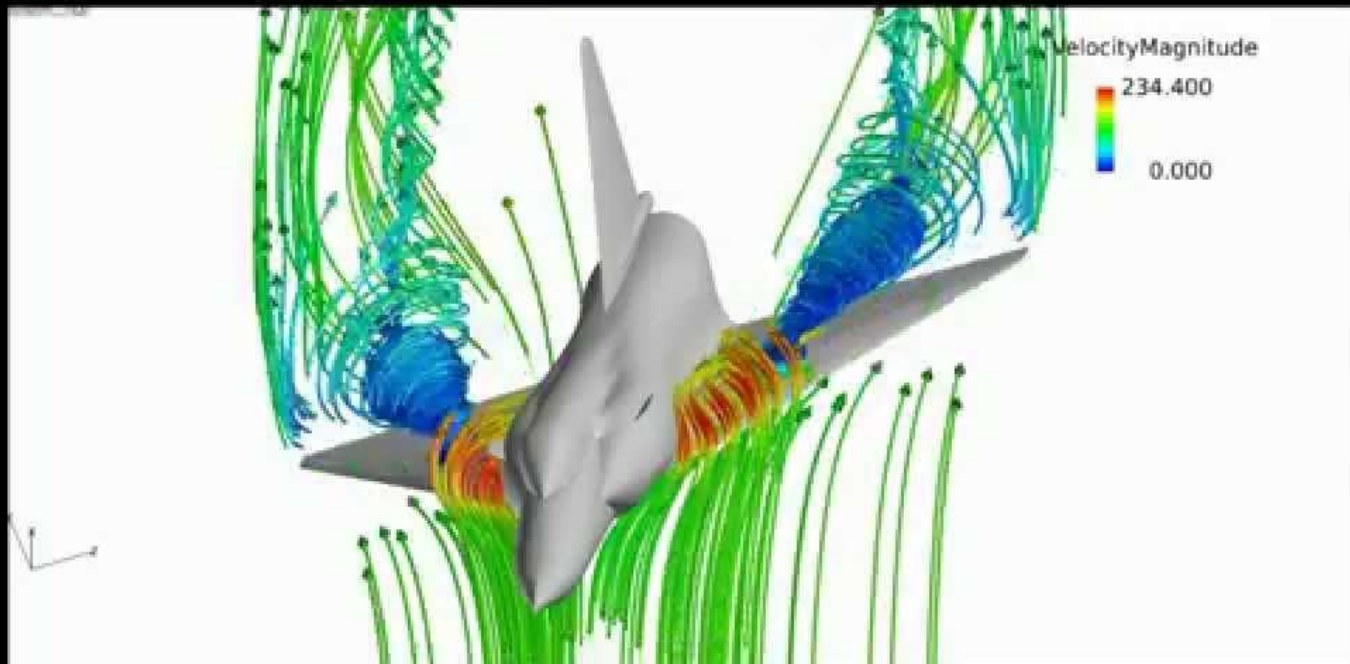
<http://aermech.com/variable-geometry-wing-design/>

# Delta Wing



<http://www.ausairpower.net/Analysis-Typhoon.html>





<https://www.youtube.com/watch?v=S7V0awkweZc>



# Ogee Wing



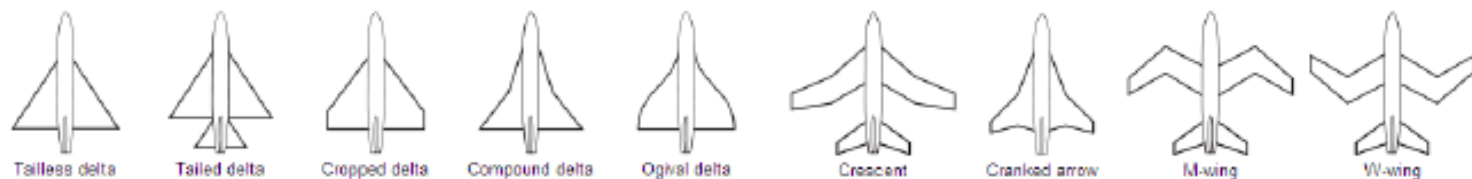
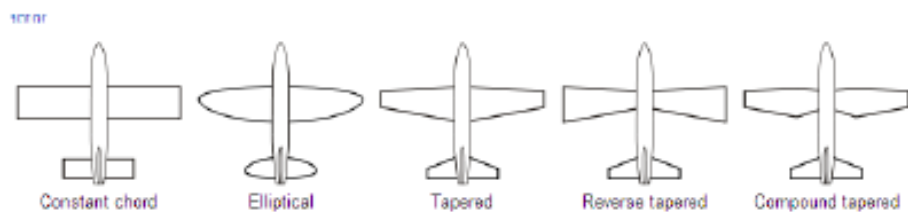
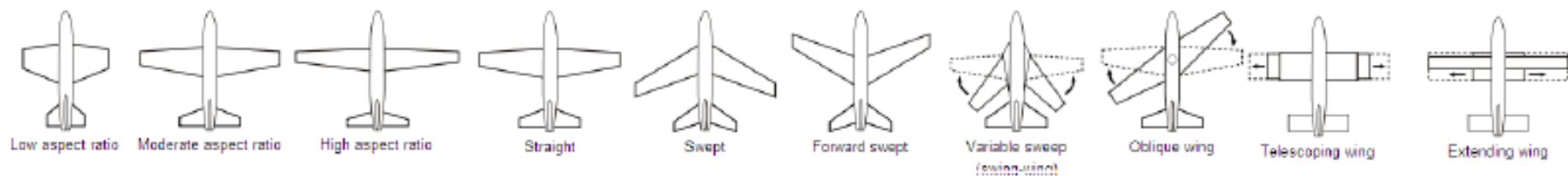
[https://en.wikipedia.org/wiki/Supersonic\\_transport](https://en.wikipedia.org/wiki/Supersonic_transport)

# Trapezoidal Wing

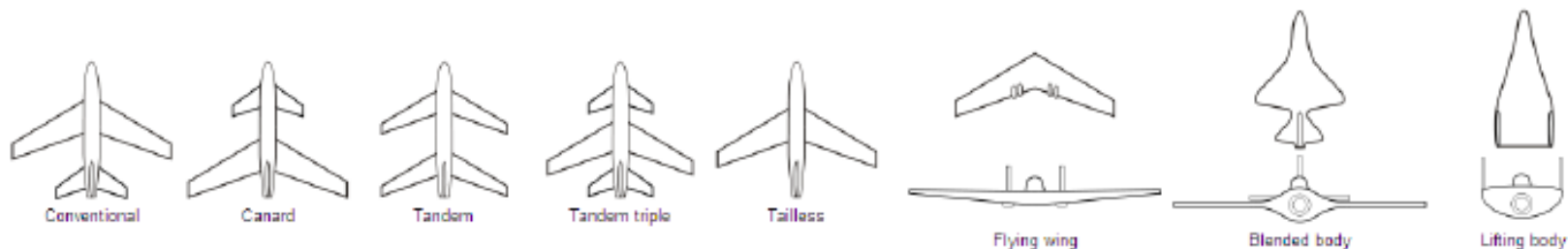


최신형 미군기에서 발견되는 특징이며 효율적인 초음속 비행을 수행할 수 있도록 구성되어 있다.  
또한 날개 형상이 스텔스 기능에 매우 적합하다.  
날개 하중이 높아 기동성이 떨어진다는 단점이 존재한다.  
특히 선회력이 떨어지는데 과거와 같이 근접전을 벌일 필요가 없기에 가히 현존 최강의 전투기라 할 수 있다  
(스텔스 기능에 고성능 레이더로 인해 미사일 트럭에서 좌표만 찍어주면 장거리에서 미사일이 날아가 내리 쏜다)

[https://en.wikipedia.org/wiki/Lockheed\\_Martin\\_F-35\\_Lightning\\_II](https://en.wikipedia.org/wiki/Lockheed_Martin_F-35_Lightning_II)  
[https://en.wikipedia.org/wiki/Lockheed\\_Martin\\_F-22\\_Raptor](https://en.wikipedia.org/wiki/Lockheed_Martin_F-22_Raptor)



**antibody**

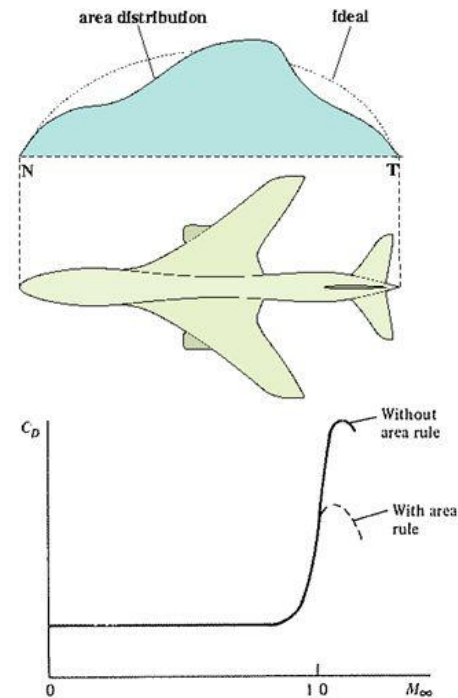
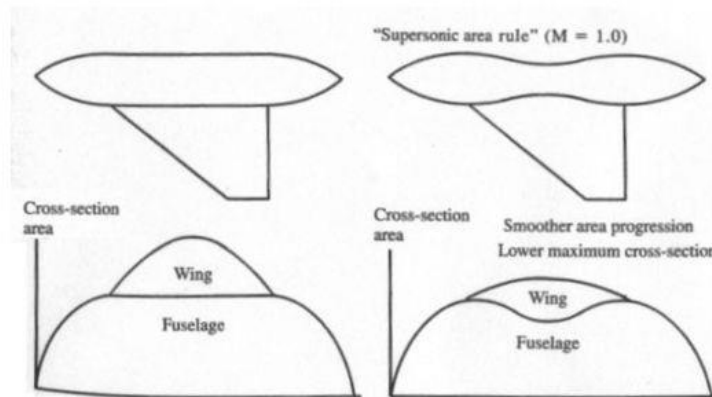


<https://defence.pk/pdf/threads/design-characteristics-of-canard-non-canard-fighters.178592/page-2>

# Area Rule

## TRANSONIC AREA RULE

- Drag created related to change in cross-sectional area of vehicle from nose to tail
- Shape itself is not as critical in creation of drag, but rate of change in shape
  - Wave drag related to 2<sup>nd</sup> derivative of volume distribution of vehicle

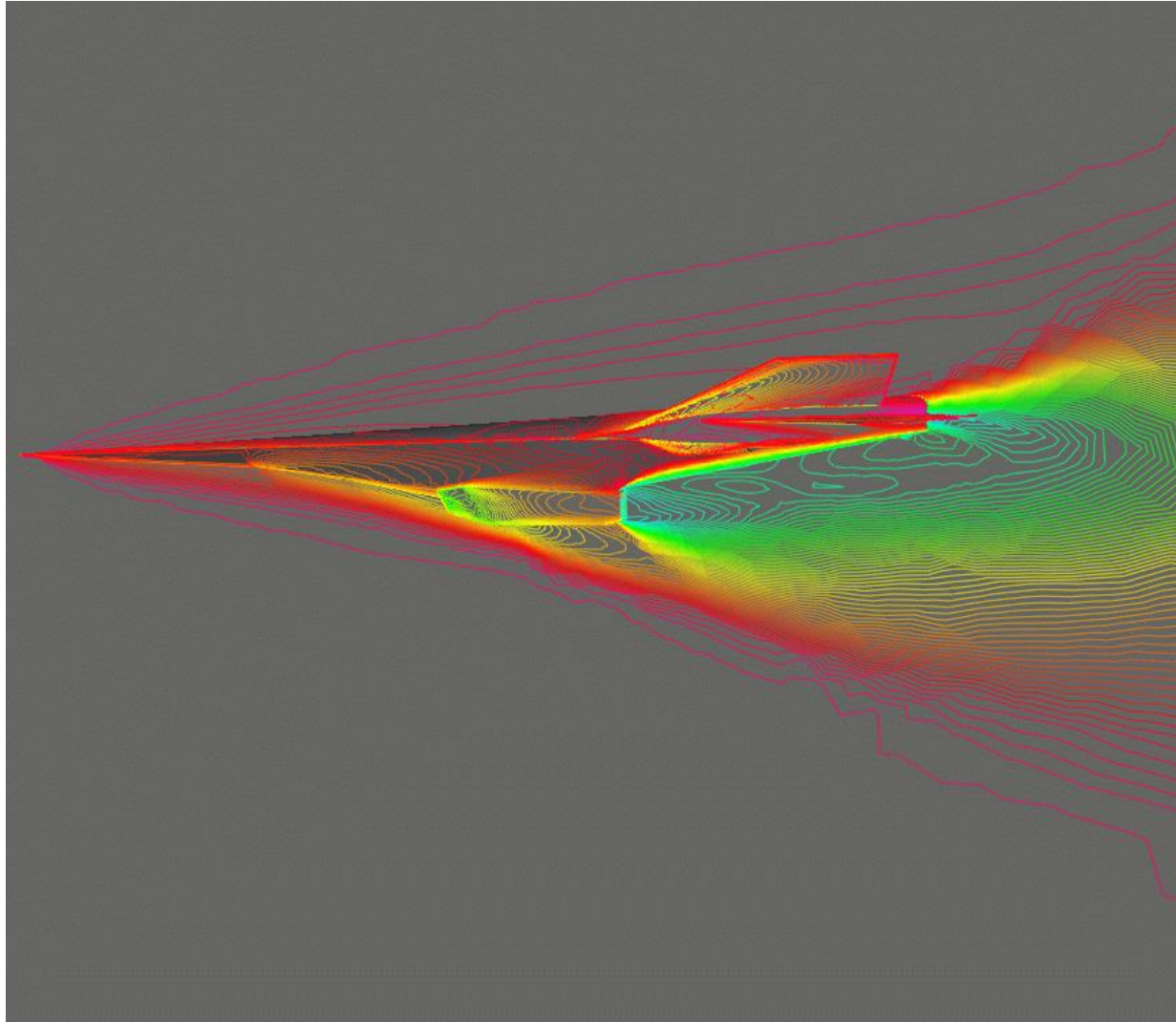






<http://www.boldmethod.com/learn-to-fly/aerodynamics/area-rule/>

# Aerodynamic Heating on Hypersonic



<https://cfp.gmu.edu/~rlohner/pages/pics/optimization.html>