

$$\begin{aligned}
 6. \quad & \textcircled{1} U = X^{\frac{1}{2}} Y^{\frac{1}{2}} \\
 & \text{st: } 12000 = 400X + 600Y \\
 & \begin{cases} 12000 = 400X + 600Y \\ \frac{1}{2}X^{-\frac{1}{2}}Y^{\frac{1}{2}} \\ \frac{1}{2}X^{\frac{1}{2}}Y^{-\frac{1}{2}} \cdot = \frac{400}{600} \end{cases} \\
 & Y = \frac{2}{3}X
 \end{aligned}$$

$$\begin{aligned}
 X &= 15 \\
 Y &= 10
 \end{aligned}$$

$$\begin{aligned}
 ②. \quad & \text{Max } U = X^{\frac{1}{2}} Y^{\frac{1}{2}} \\
 & \text{st } 12000 = 400X + 600Y \\
 & X + Y = 23 \\
 & \begin{cases} X + Y = 23 \\ \text{求最大值 (时间)} \\ \text{实际效用} \end{cases} \\
 & \frac{MU_X}{P_X} = \frac{MU_Y}{P_Y} \\
 & Y = \frac{2}{3}X
 \end{aligned}$$

$$\begin{aligned}
 & \begin{cases} X + Y = 23 \\ Y = \frac{2}{3}X \end{cases} \\
 & X = 13.8 \\
 & Y = 9.2
 \end{aligned}$$