Chapter 6 Semantic Analysis

2022 Spring&Summer

Outline

- Attributes and attribute grammars
- Algorithms for attribute computation
- The symbol table
- Data types and type checking
- •A semantic analyzer for the TINY language

- Attributes: any property of a programming language construct such as
 - The data type of a variable
 - The value of an expression
 - The location of a variable in memory
 - The object code of a procedure
 - The number of significant digits in a number
- Attributes may be fixed prior to the compilation process.
- Attributes may be only determinable during program execution.

- Binding of the attribute: the process of computing an attribute and associating its computed value with the language construct in question.
- Binding time: the time during the compilation/ execution process when the binding of an attribute occurs.

- Binding times of different attributes vary, and even the same attributes that can have quite different binding times from language to language.
- Static attributes/Dynamic attributes: Based on the difference of the binding time be bound prior to execution be bound during execution

- A type checker: is an important part of semantic analysis (in a language like C or Pascal)
- A type checker is an analyzer
 - Computes the data type attribute of all language entities for which data types are defined
 - Verifies that these types conform to the type rules of the language.

• Type checking = set of rules that ensure the type consistency of different constructs in the program

• Examples:

- The type of a variable must match the type from its declaration
- The operands of arithmetic expressions (+, *, -, /) must have integer types; the result has integer type
- ➤ The operands of comparison expressions (==, !=) must have integer or string types; the result has boolean type

More examples:

- For each assignment statement, the type of the updated variable must match the type of the expression being assigned
- For each call statement foo(v1, ..., vn), the type of each actual argument vi must match the type of the corresponding formal argument fi from the declaration of function foo
- The type of the return value must match the return type from the declaration of the function

- X.a: the value of a associated to X
 X is a grammar symbol and a is an attribute associated to X.
- Syntax-directed semantics: attributes are associated directly with the grammar symbols of the language.
- Given attributes $a_1, a_2, ..., a_k$, for each grammar rule $X_0 \rightarrow X_1 X_2 ... X_n$ (X_0 is a nonterminal), the values of the attributes $X_i a_j$ of each grammar symbol X_i are related to the values of the attributes of the other symbols in the rule.

• An attribute grammar for attributes a_1, a_2, \ldots, a_k is the collection of all attribute equations or semantic rules of the following form, for all the grammar rules of the language.

$$X_{i.}a_{j}=f_{ij}(X_{0}.a_{1},...,X_{0}.a_{k},X_{1}.a_{l},...,X_{1}.a_{k}...X_{n}.a_{1},...X_{n}.a_{k})$$

 f_{ij} is a mathematical function of its arguments

• Attribute grammars are written in tabular form as follows:

Grammar Rule	Semantic Rules
Rule 1	Associated attribute equations
• • • •	• • • • • • • •
• • • • • • • •	• • • • • • • • • •

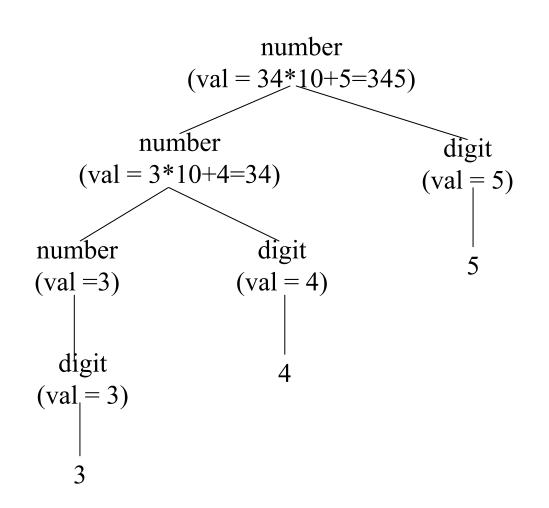
Rule n Associated attribute equations

Example 6.1:

number \rightarrow number digit | digit digit \rightarrow 0|1|2|3|4|5|6|7|8|9

Grammar Rule	Semantic Rules
number1 → number2 digit	number1.val = number2.val*10+digit.val
$number \rightarrow digit$	number.val = digit.val
$digit \rightarrow 0$	digit.val = 0
$digit \rightarrow 1$	digit.val = 1
$digit \rightarrow 2$	digit.val = 2
$digit \rightarrow 3$	digit.val = 3
$digit \rightarrow 4$	digit.val = 4
$digit \rightarrow 5$	digit.val = 5
$digit \rightarrow 6$	digit.val = 6
$digit \rightarrow 7$	digit.val = 7
$digit \rightarrow 8$	digit.val = 8
$digit \rightarrow 9$	digit.val = 9

The parse tree showing attribute computations for the number 345 is given as follows



Example 6.2:

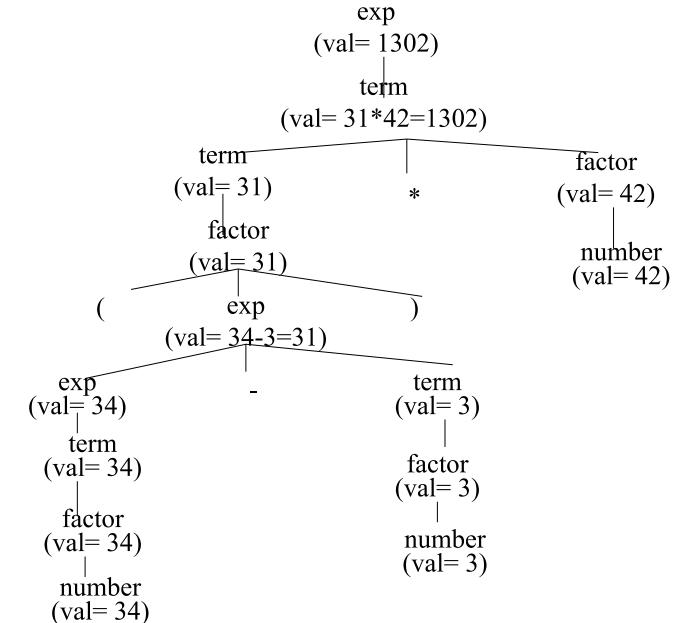
```
exp \rightarrow exp + term \mid exp-term \mid term

term \rightarrow term * factor \mid factor

factor \rightarrow (exp) \mid number
```

grammar Rule	semantic Rules
$exp1 \rightarrow exp2 + term$	exp1.val = exp2.val + term.val
$exp1 \rightarrow exp2$ - term	exp1.val = exp2.val - term.val
$exp1 \rightarrow term$	exp1.val = term.val
term1 → term2*factor	term1.val = term2.val*factor.val
term→factor	term.val = factor.val
$factor \rightarrow (exp)$	factor.val = exp.val
factor→number	factor.val = number.val

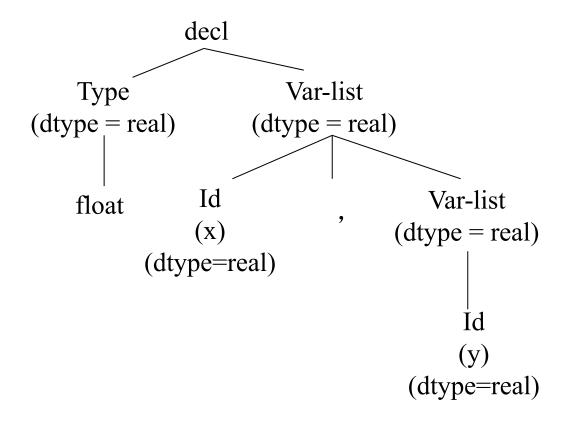
The computations implied by this attribute grammar by attaching equations to nodes in a parse tree is as follows. (Given the expression (34-3)*42)



Example 6.3: $decl \rightarrow type \ var-list$ $type \rightarrow int \mid float$ $var-list \rightarrow id, var-list \mid id$

grammar Rule	semantic Rules
$decl \rightarrow type \ var-list$	var-list.dtype = type.dtype
$type \rightarrow int$	type.dtype = integer
type →float	type.dtype = real
var-list1 → id, var-list2	id.dtype = var-list1.dtype var-list2.dtype = var-list1.dtype
var -list $\rightarrow id$	id.dtype = var-list.dtype

Parse tree for the string *float x,y* showing the *dtype* attribute as specified by the attribute grammar above is as follows



Example 6.4

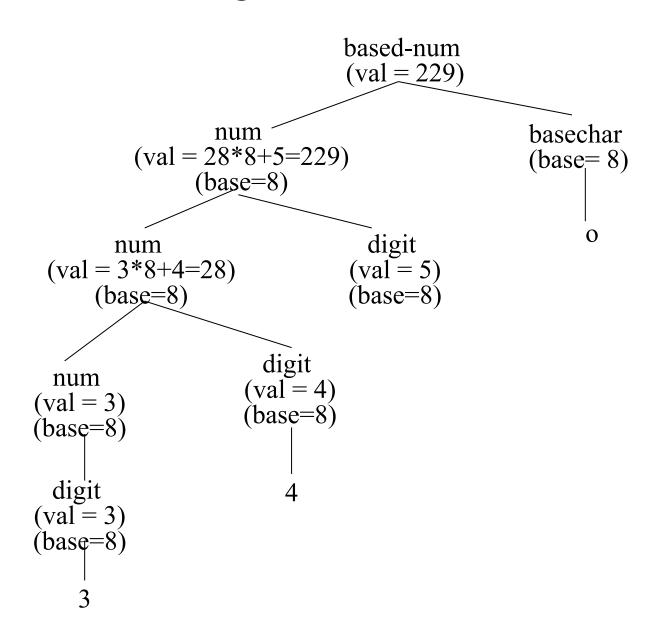
based-num \rightarrow num basechar

basechar \rightarrow o | d

num \rightarrow num digit | digit

digit \rightarrow 0|1|2|3|4|5|6|7|8|9

grommar Dula	somentie Pules
grammar Rule	semantic Rules
$ based$ -num \rightarrow num	based-num.val = num.val
basechar	num.base = basechar.base
$basechar \rightarrow o$	basechar.base = 8
$basechar \rightarrow d$	basechar.base = 10
$num1 \rightarrow num2 \ digit$	num1.val =
	If digit.val = error or num2.val = error
	Then error
	Else_num2.val*num1.base+digit.val
	num2.base = num1.base
	digit.base = num1.base
$num \rightarrow digit$	num.val = digit.val
	digit.base = num.base
digit →0	digit.val = 0
digit →1	digit.val = 1
	••••
digit →7	digit.val = 7
digit →8	digit.val = if digit.base = 8 then error rlse 8
digit →9	digit.val = if digit.base = 8 then error rlse 9



- *Metalanguage* for the attribute grammar: the collection of expressions allowable in an attribute equation.
 - Here limited to *arithmetic*, *logical* and a few other kinds of *expressions*.
 - > an *if-then-els*e expression and occasionally a case or switch expression.
- *Functions* can be added to the *metalanguage* whose definitions may be given elsewhere.

```
digit \rightarrow D (D is understood to be one of the digits) digit.val = numval(D)
```

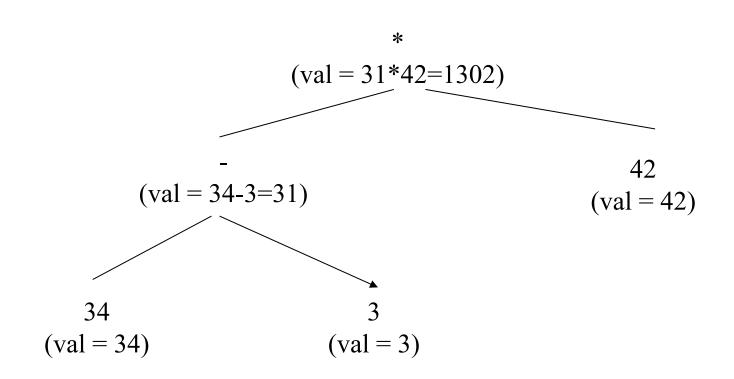
Simplifications:

1. Using ambiguous grammar: (all ambiguity will have been dealt with at the parser stage)

$$exp \rightarrow exp + exp \mid exp - exp \mid exp * exp \mid (exp) \mid number$$

grammar Rule	semantic Rules
$exp1 \rightarrow exp2 + exp3$	exp1.val = exp2.val + exp3.val
$exp1 \rightarrow exp2 - exp3$	exp1.val = exp2.val - exp3.val
$exp1 \rightarrow exp2 * exp3$	exp1.val = exp2.val * exp3.val
$exp1 \rightarrow (exp2)$	exp1.val = exp2.val
$exp \rightarrow number$	exp.val = number.val

2. Using abstract syntax tree instead of parse tree



Example 6.5 define an *abstract syntax tree* for simple integer arithmetic expressions by the attribute grammar as follows:

grammar Rule	semantic Rules
$exp1 \rightarrow exp2 + term$	exp1.tree = mkOpNode(+,exp2.tree, term.tree)
$exp1 \rightarrow exp2$ - term	exp1.tree = mkOpNode(-,exp2.tree, term.tree)
$exp1 \rightarrow term$	exp1.tree = term.tree
term1 → term2*factor	term1.tree= mkOpNode(*,term2.tree , factor.tree)
term→factor	term.tree = factor.tree
$factor \rightarrow (exp)$	factor.tree = exp.tree
factor→number	factor.tree = mkNumNode(number.lexval)

6.2 Algorithms for attribute computation

Purpose:

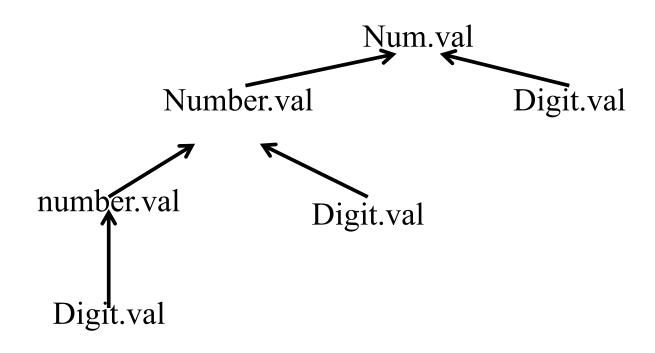
- Study the ways an attribute grammar can be used as basis for a compiler to compute and use the attributes defined by the equations of the attribute grammar.
- $X_{i.}a_{j} = f_{ij}(X_{0}.a_{1},...,X_{0}.a_{k}, X_{1}.a_{l},...,X_{1}.a_{k},...,X_{n}.a_{1},...X_{n}.a_{k})$ is viewed as an assignment of the value of the functional expression on the right- hand side to the attribute $X_{i.}a_{j}$.

• Each grammar rule choice has an *associated* dependency graph.

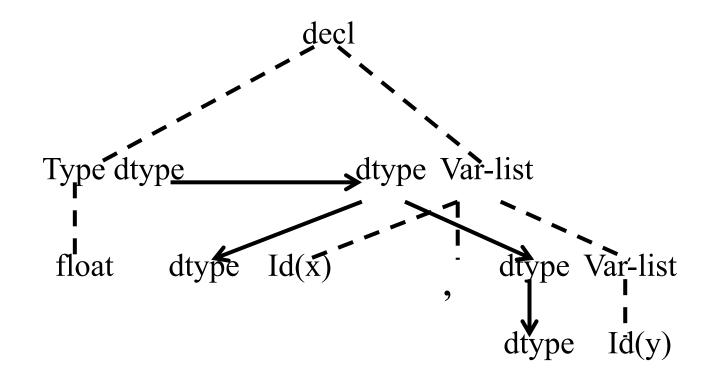
This graph has a node labeled by each attribute $X_i.a_j$ of each symbol in the grammar rule.

- Dependency graph of the string (sentence) is the union of the dependency graphs of the grammar rule choices representing each node(nonleaf) of the parse tree of the string.
- $X_{i}.a_{j} = f_{ij}(..., X_{m}.a_{k}...)$ An edge from each node $X_{m}.a_{k}$ to $X_{i}.a_{j}$ the node expressing the dependency of $X_{i}.a_{j}$ on $X_{m}.a_{k}$

The string 345 has the following dependency graph.



```
decl → type var-list
type → int | float
var-list → id, var-list | id
```

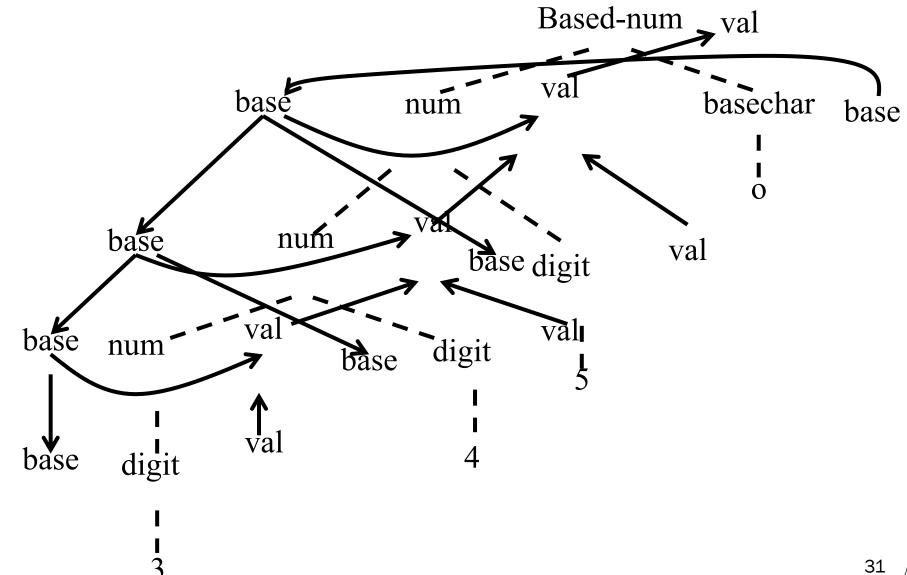


```
based-num → num basechar

num → num digit

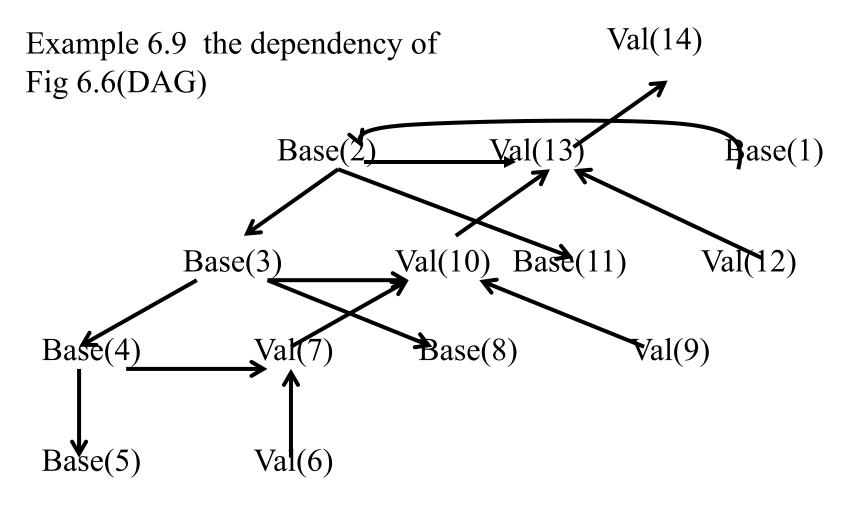
num → digit

digit → 9
.....
```



Directed acyclic graphs(DAG)

- Algorithm must compute the attribute at each node in the dependency graph before it attempts to compute any successor attributes.
- A traversal order of the dependency graph that obeys this restriction is called a *topological sort*.
- The graph must be *acyclic*



Another topological sort is given by the order 12 6 9 1 2 11 3 8 4 5 7 10 13 14

How attribute values are found at the roots of the graph

- Parse tree method: construction of the dependency graph is based on the specific parse tree at compile time., add complexity, and need circularity detective.
- Rule based method: fix an order for attribute evaluation at compiler construction time. It depends on an analysis of the attribute equations, or semantic rules.

6.2.2 Synthesized and inherited attributes

Classification of the attributes:

- 1. Synthesized attributes
- 2. Inherited attributes

6.2.2 Synthesized and inherited attributes

Synthesized attributes

- An attribute is *synthesized*
 - if all its dependencies point from child to parent in the parse tree.
 - Given a grammar rule $A \rightarrow X_1 X_2 ... X_n$, the only associated attribute equation with an a on the left-hand side is of the form:
 - \rightarrow $A.a = f(X_1.a_1,...X_1.a_k,...X_n.a_1,...X_n.a_k)$
- S-attributed grammar:

An attribute grammar in which all the attributes are synthesized.

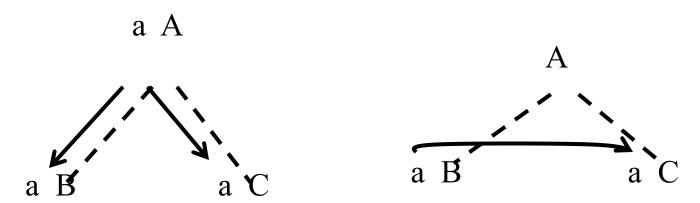
Synthesized attributes

• The attribute values of an *S-attributed* grammar can be computed by a single bottom-up, or post-order, traversal of the parse or syntax tree.

```
procedure postEval (T: treenode);
begin
  for each child C of T do
    postEval(C);
  compute all synthesized attributes of T;
end
```

Inherited attributes

- •An attribute that is not synthesized is called an *inherited* attribute.
- •Such as *dtype* in example 6.3 and *base* in example 6.4.



(a) Inheritance from parent to siblings (b) inheritance from sibling to sibling

Inherited attributes

• Inherited attributes: computed by a preorder traversal, or combined preorder/inorder traversal of the parse or syntax tree, represented by the following pseudocode:

```
procedure preEval(T: treenode);
begin
  for each child C of T do
      compute all inherited attributes of C;
  preEval(C);
end;
```

Inherited attributes

- The order in which the *inherited* attributes of the children are computed is important.
- It must adhere to any requirements of the dependencies.

Example 6.12

• The grammar with the inherited attribute *dtype* and whose dependency graphs are given in example 6.7.

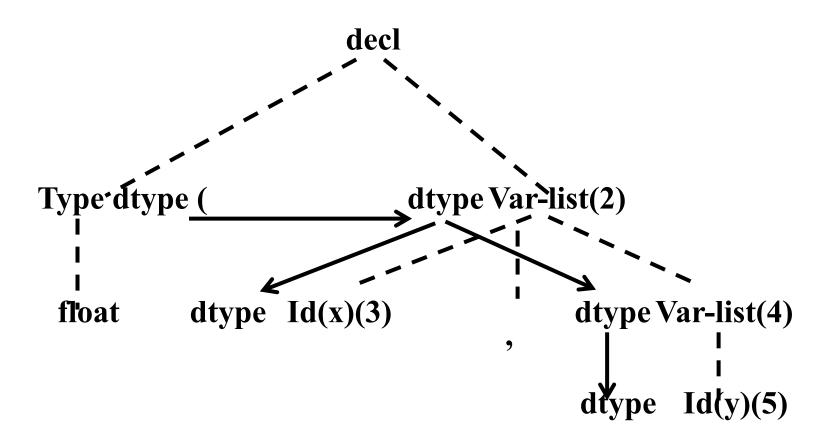
```
decl \rightarrow type \ var-list
type \rightarrow int \mid float
var-list \rightarrow id, var-list \mid id
```

Example 6.12

end EvalType;

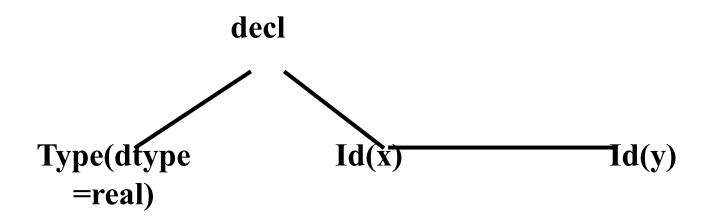
```
procedure evalType(T: treenode);
begin
    case nodekind of T of
    decl:
             evalType(type child of T);
             assign dtype of type child of T to var-list child of T;
             evalType(var-list child of T);
     type:
             if child of T = int then T.dtype := integer
             else T.dtype :=real;
     var-list:
             assign T.dtype to first child of T;
             if third child of T is not nil then
                      assign T.dtype to third child;
               evalType(third child of T);
     end case;
```

- Preorder and inorder operations are mixed.
- Inorder: decl node
- Preorder: *var-list* node



Example 6.12

• If use the actual C code, assume that a syntax tree has been constructed, in which *var-list* is represented by a sibling list of *id* nodes as follows.



```
typedef enum {decl, type,id} nodekind;
typedef enum {integer, real} typekind;
typedef struct treenode
   {nodekind kind;
    struct treenode *lchild, *rchild, *sibling;
    typekind dtype;
    char *name:
   } *Syntaxtree;
```

```
void evaltype (syntaxtree t)
{ switch (t->kind)
   {case decl:
       t->rchild->dtype = t->lchild->dtype
       evaltype(t->rchild);
       break;
    case id:
       if(t->sibling != NULL)
             t->sibling->dtype = t->dtype;
              evaltype(t->sibling);
       break:
```

```
void evaltype (syntaxtree t)
\{if(t->kind==decl)\}
      syntaxtree\ p = t->rchild;
      p->dtype = t->lchlild->dtype;
      while (p->sibling !=NULL)
      {p->sibling->dtype = p->dtype};
         p = p->sibling;
```

- The simple version of an expression grammar:
 - $exp \rightarrow exp / exp | num | num.num$
- Operations may be interpreted differently depending on whether they are *floating-point* or strictly *integer* operations.
- For instance:

$$5/2/2.0 = 1.25$$

 $5/2/2 = 1$

Example 6.14

• The attributes needed to express the corresponding semantic:

isFloat: boolean, indicates if any part of an expression has a floating-point value (*synthesized*)

etype: gives the type of each subexpression and depends on *isFloat* (*inherited*), here is int or float

val: gives the numeric value of each subexpression, depends on *etype*.

Grammar Rule	Semantic Rules	
S→exp	exp.etype = if exp.isFloat then float else int	
	S.val = exp.val	
$\exp 1 \rightarrow \exp 2/\exp 3$	exp1.isFloat = exp2.isFloat or $exp3.isFloat$	
	exp2.etype = exp1.etype	
	exp3.etype = exp1.etype	
	exp1.val =	
	if $exp1.etype = int then exp2.val div exp3.val$	
	else exp2.val/exp3.val	
exp → num	exp.isFloat = false	
	exp.val =	
	if $exp.etype = int$ then num.val	
	else <i>Float</i> (num. <i>val</i>)	
exp→num.num	exp.isFloat = true	
-	exp.val = num.num.val	
	4	50

- Many attributes are the same or are only used temporarily to compute other attribute values, needn't be stored as fields in a syntax tree record structure.
- Inherited attributes be computed in preorder, often be treated as parameters of the call.
- Synthesized attributes be computed in postorder, often be treated as returned values of the call.

- The recursive procedure *evalWithBase* of example 6.13
- turn base into a parameter and val into a returned value.

```
based-num \rightarrow num basechar
basechar \rightarrow o|d
num \rightarrow num digit | digit
```

Example 6.15

• To start the computation, one would have to make a call such as *EvalWithBase(rootnode, 0)*.

```
function EvalWithBase(T: treenode; base:integer): integer;
var temp, temp2 : integer;
begin
    case nodekind of T of
    based-num:
           temp := EvalWithBase(right child of T, base);
           return EvalWithBase(left child of T, temp);
    num:
           temp:= EvalWithBase(left child of T, base);
           if right child of T is not nil then
              temp2 := EvalWithBase(right child of T, base);
```

```
if temp != error and temp2 !=error then
                        return base*temp + temp2
          else return error;
        else return temp;
basechar:
        if child of T = o then return 8
        else return 10;
digit:
        if base = 8 and child of T = 8 or 9 then return error
        else return numval(child of T);
    end case:
end EvalWithBase;
```

```
function EvalBasedNum(T: treenode): integer;
(/*only called on root node */)
begin
    return EvalNum(left child of T, EvalBase(right child of
    T)):
end;
function EvalBase(T: treenode): integer;
(/*only called on basechar node*/)
begin
    if child of T = o then return 8
    else return 10;
end
```

```
function EvalNum(T:treenode; base: integer): integer;
var temp, temp2: integer;
begin
  case nodekond of T of
    num:
      temp:= EvalWithBase(left child of T, base);
      if right child of T is not nil then
        temp2 := EvalWithBase(right child of T, base);
        if temp != error and temp2 !=error then
                return base*temp + temp2
           else return error:
      else return temp;
    digit:
      if base = 8 and child of T = 8 or 9 then return error
        else return numval(child of T);
    end case;
end.
```

6.2.4 The use of external data structures to store attributes values.

Applicability:

- Not suitable to the method of *parameters* and *returned* values
- Particularly when the attribute values have significant structure and may be needed at arbitrary points during translation.
- Not reasonable to be stored in the syntax tree nodes.

6.2.4 The use of external data structures to store attributes values.

Ways:

- External data structures: table, graphs and other data structures. one of the prime examples is the symbol table.
- Replace attribute equations by calls to procedures representing operations on the appropriate data structure used to maintain the attribute values.

- Attributes that computed successfully at the same time as the parsing stage depends on the power and properties of the parsing method employed.
- All the major parsing methods process the input program from left to right (LL, or LR).
- Require the attribute be capable of evaluation by a left-toright traversal of the parse tree (*synthesized* attributes will always be OK).

L-attributed Definition:

• An attribute grammar for attribute $a_1, ..., a_k$ is *L-attributed* if, for each inherited attribute a_j and each grammar rule:

$$X_0 \rightarrow X_1 X_2 ... X_n$$

The associated equations for a_i are all of the form:

$$X_{i}.a_{j} = f_{ij}(X_{0}.a_{1}, X_{0}.a_{k}, X_{1}.a_{l}, ..., X_{1}.a_{k}, X_{i-1}.a_{1}, ... X_{i-1}.a_{k})$$

• S-attributed grammar is L-attributed grammar.

L-attributed

Given an *L-attributed* grammar in which the *inherited* attributes do not depend on the *synthesized* attributes:

- 1. Top-down parser: a recursive-descent parser can evaluate all the attributes by turning the *inherited* attributes into *parameters* and *synthesized* attributes into *returned* values.
- 2. Bottom-up parser: LR parsers are suited to handling primarily *synthesized* attributes, but are difficult for *inherited* attributes.

Computing synthesized attributes during LR parsing.

Value stack: store *synthesized* attributes, be manipulated in parallel with the parsing stack.

6.2.5 The computation of attributes during parsing. Computing synthesized attributes during LR parsing

\$	3*4+5\$	Shift	\$	
\$n	*4+5\$	Reduce E→n	\$n	E.val = n.val
\$E	*4+5\$	Shift	\$3	
\$E*	4+5\$	Shift	\$3*	
\$E*n	+5\$	Reduce E→n	\$3*n	E.val =n.val
\$E*E	+5\$	Reduce E→E*E	\$3*4	E1.val=E2.val*E3.
\$E	+5\$	Shift	\$12	
\$E+	5\$	Shift	\$12+	
\$E+n	\$	Reduce E→n	\$12+n	E.val = n.val
\$E+E	\$	Reduce E→E+E	\$12+5	E1.val=E2.val +E3.val
\$E	\$		\$17	

Inheriting a previously computed synthesized attributes during LR parsing

An action associated to a nonterminal in the right-hand side of a rule can make use of *synthesized* attributes of the symbols to the left of it in the rule.

• For instance:

$$A \rightarrow B C$$

C.i = f(B.s) s is a synthesized attribute.

• The question can be settled through a ε–production as follows

Grammar Rule	Semantic Rules	
A →BDC		
$B \rightarrow \dots$	{computer B.s}	
$D \rightarrow \varepsilon$	<pre>saved_i= f(valstack[top])</pre>	
$C \rightarrow \dots$	{now saved_i is available}	

• In Yacc this process is made easier. The action of storing the computed attribute is simply written at the place in the rule where it is to be scheduled:

```
A: B { saved_i=f($1);} C;
```

The following attribute grammar satisfy the above request.

Grammar Rule	Semantic Rules
decl → type var-list	var-list. $dtype = type.dtype$
type) int	type.dtype = integer
type > float	type.dtype = real
var-list1 →var-list2,id	insert(id.name, var-list1.dtype)
	var-list2. $dtype = var$ -list1. $dtype$
var-list → id	insert(id.name, var-list.dtype)

Problems

1. Require the programmer to directly access the value stack during a parse

This may be risky in automatically generated parsers.

2. Only works if the position of the previously computed attribute is predictable from the grammar.

The best technique for dealing with inherited attributes in LR parsing:

Use external data structures, to hold *inherited* attribute values and to add ε _production or embedded actions as in Yacc (may add parsing conflicts).

• Modifications to the grammar that do not change the legal strings of the language

Make the computation of attributes simpler or more complex.

• The properties of attributes depend heavily on the structure of the grammar.

Theorem

Given an attribute grammar, <u>all inherited attributes</u> can be changed into synthesized attributes by suitable modification of the grammar, without changing the language of the grammar.

(From Knuth [1968]).

Example 6.18

- An inherited attribute can be turned into a synthesized attribute by modification of the grammar.
- Consider the grammar as follows:

```
decl → type var-list
type →int|float
var-list →id,var-list|id
```

• The *dtype* attribute is inherited. Rewrite the grammar as follows

```
decl → var-list id
var-list → var-list id, | type
type → int | float
```

• Turned the inherit attribute into synthesized attribute as follows:

Grammar Rule	Semantic Rules
decl → var-list id	id.dtype = var-list.dtype
var-list1 →var-list2 id	varlist1.dtype = varlist2.dtype
	id.dtype = varlist2.dtype
var-list → type	var-list. $dtype = type.dtype$
type > int	type.dtype = integer
type → float	type.dtype = real