

# Project for KIV/UPA

# Task 02 - Program in MIPS

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# 1 Assignment description

The program will print out a step by step solution for the problem of Hanoi Towers where the number of disks on the first rod is between 1 and 9.

## 2 Analysis

## 2.1 Problem description

A detailed description of this problem can be found at https://en.wikipedia.org/wiki/Tower\_of\_Hanoi.

Tower of Hanoi is a mathematical problem where disks of different diameters are being moved among three rods. In the initial configuration, all the disks are stacked on the first rod such that the largest disk is placed at the bottom and the smallest one on the top. The goal is to efficiently move all the disks from the first rod to the last one using the middle rod. In other words, all the disks from the first rode must be put onto the last one in the same order with as minimal moves as possible. Additionally, there are some rules that must be followed (2.2).

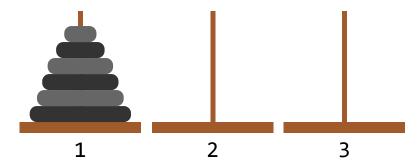


Figure 2.1: Visualization of the problem

#### 2.2 Rules

- (1) Only one disk can me moved at a time.
- (2) One move means taking a disk from the top of a rod a placing it on the top of another.
- (3) It is not allowed to place a disk of a larger diameter onto a disk of a smaller diameter.

## 3 Algorithm

The input of the procedure solving this problem would be N, R1, R2, and R3, where N is the number of disks and R1, R2, and R3 are the numbers of rods. We want to move N disks from rod R1 to rod R2.

The solution is trivial for N=1. We simply move the disk from rod R1 to rod R2 and we are all done. In case N>1, we need to break the whole algorithm down into smaller steps. It is clear that we need to first move N-1 disks from rod R1 to rod R3, as a temporary step, so we can move the largest disk from rod R1 right onto rod R2. Once the largest disk is at its final position, all we need to do is put all the N-1 disks from rod R3 onto rod R2 and the problem is solved.

Now we are facing another problem - how to move N-1 disks from rod R1 to rod R3. We can simply use the same idea and think of rod R3 as rod R2 instead. We can break this down further and further until we are left with moving only one disk.

#### 3.1 Pseudo code

#### **Algorithm 1** Hanoi Towers

```
1: procedure HANOI(N, R1, R2, R3)
      if N == 1 then
2:
          print R1 \rightarrow R2
3:
4:
          return
      hanoi(N-1, R1, R3, R2)
                                          \triangleright move N-1 disks from R1 to R3
5:
6:
      hanoi(1, R1, R2, R3)
                                       ▶ move the largest disk from R1 to R2
      hanoi(N-1, R3, R2, R1)
                                          \triangleright move N-1 disks from R3 to R2
7:
```

### 3.2 Time complexity

The algorithm is recursive and works with a time complexity of  $O(2^n)$ , where n is the number of disks on the first rod. An example of how many moves it takes for a specific number of disks is shown in the table below.

Table 3.1: Example of particular number of disks

Number of disks	Total number of moves
1	1
2	3
3	7
4	15
10	1023
20	1048575
25	33554431
60	$1,1529.10^{18}$
100	$1,2677.10^{30}$
N	$2^{N-1}$

## 4 Implementation

### 4.1 Description

First, the program encourages the user to enter a number of disks, for which they want to print all the moves solving the problem of Hanoi Towers. If the user entered an invalid number that is not between 1 and 9. The program will print out an error message and terminate. Otherwise, it will print out all the moves for the particular number of disks the user entered.

## 4.2 Example of I/O

#### 4.2.1 Example A

Enter the number of disks: 1 -> 3 1 -> 3 3 -> 23 -> 2 2 -> 1 2 -> 1 1 -> 3 1 -> 3 3 -> 23 -> 2 2 -> 1 2 -> 1 1 -> 3 1 -> 3 3 -> 2

#### 4.2.2 Example B

Enter the number of disks: -5
The number is supposed to be between 1 and 9!

## 5 Conclusion

The algorithm was implemented using the Assembly language MISP and tested in Mars simulator - http://courses.missouristate.edu/kenvollmar/mars/. Everything works as required, and furthermore, an input validation was implemented within the program as well.