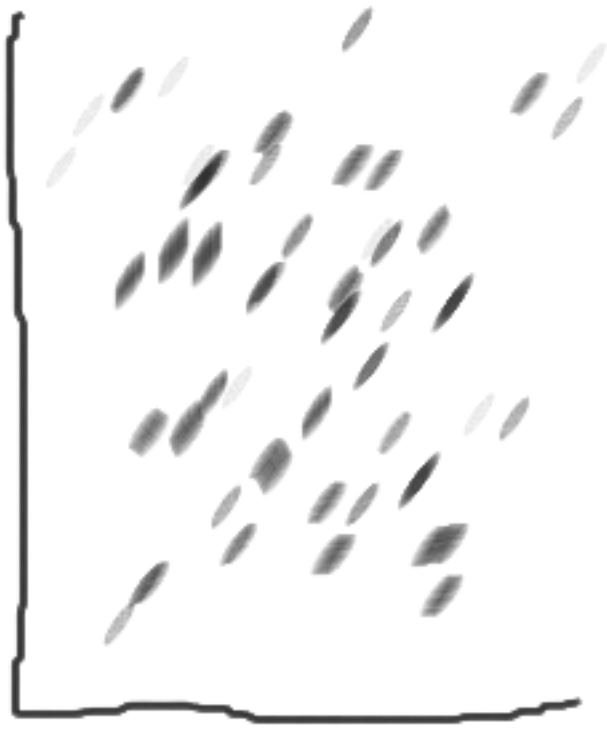
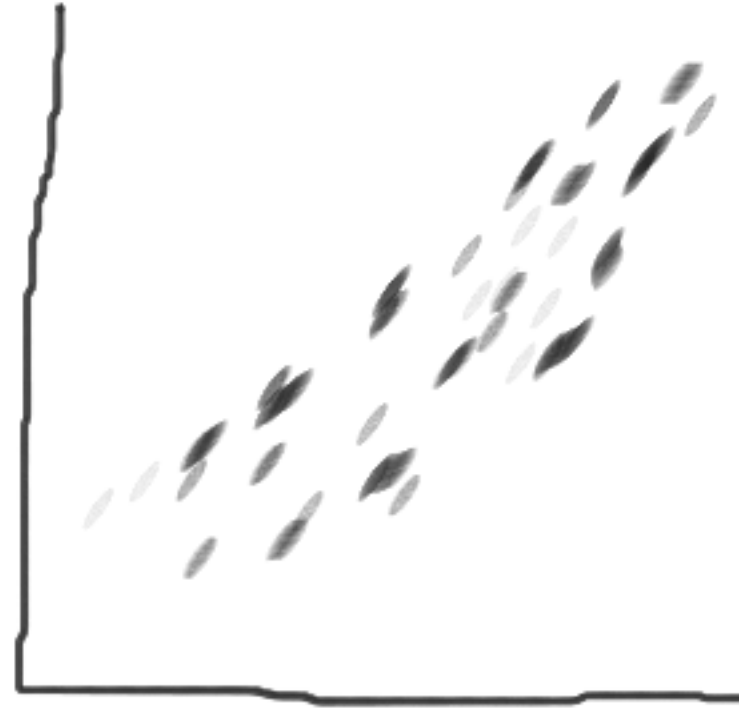


## Correlation



$R$  near 0



+ve  
 $R$  near 1



-ve  
 $R$  near -1

# Variance

$$V = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n} = \frac{200}{10} = 20$$

when sample size 1455

$$\frac{\quad}{n-1}$$

$$= \frac{20}{5-1} = \frac{20}{4} = 4+1=5$$

$$x_i =$$

$$\bar{x} =$$

$$n =$$



$$+ 2 - 2 - 3$$

$$+ 5$$

$$= 1$$

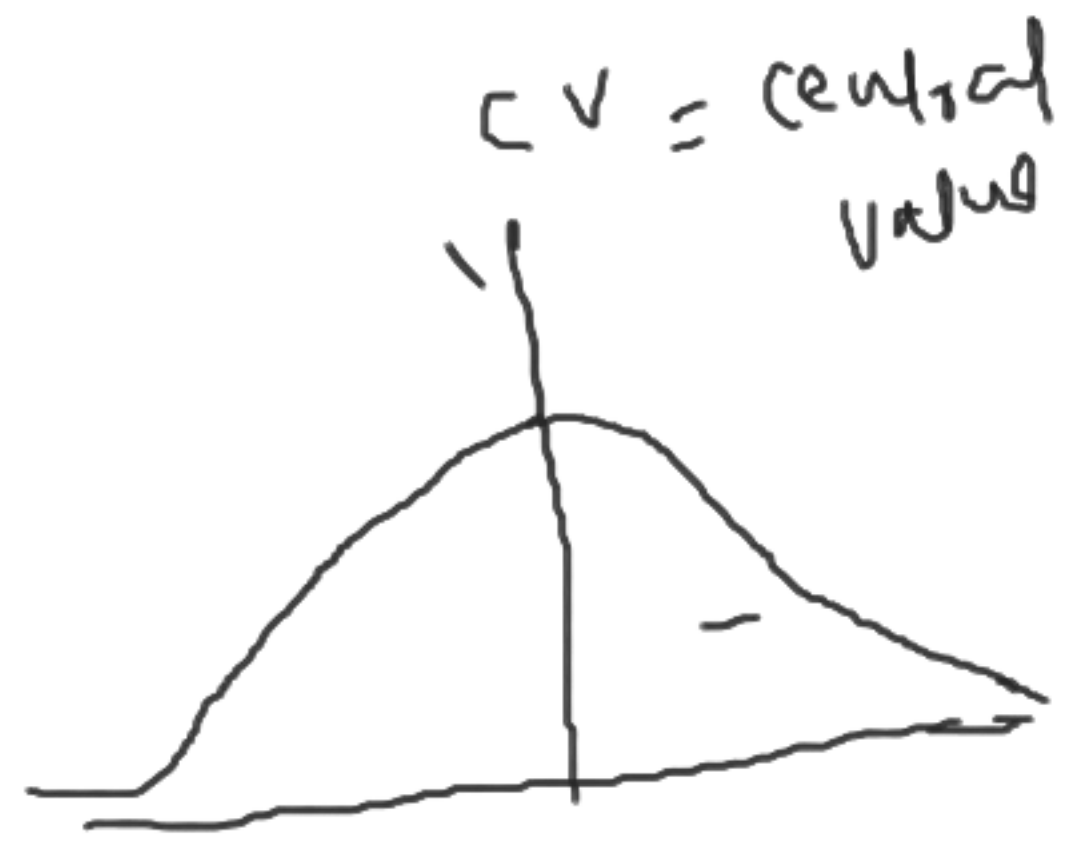
$$2^2 - 2^2 - 3^2$$

$$4^2$$

$$= 20$$

when 1 var is there

$$(x_i - \bar{x})^2$$

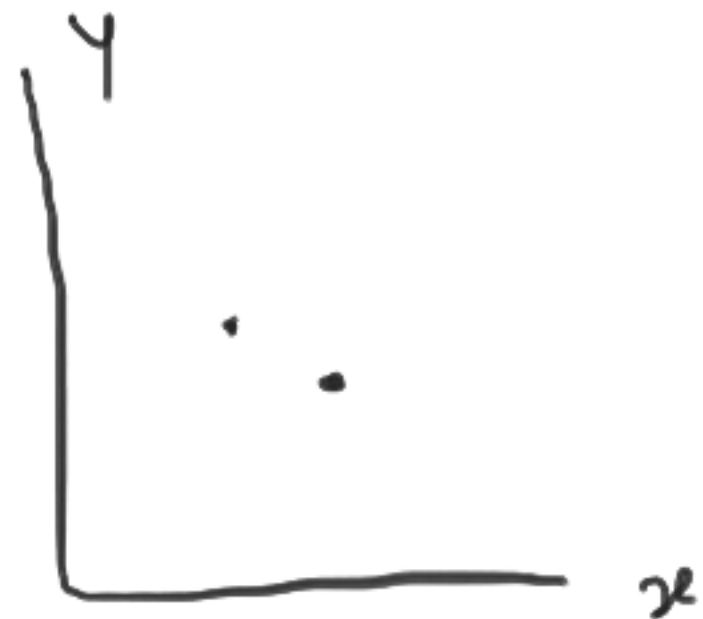


x dev / var

158  
178  
172

## Covariance

$$\text{Covariance} = \frac{(x_i - \bar{x}) \times (y_i - \bar{y})}{n}$$



$$\text{COV} = 0$$

$$\text{corr} = 0$$

✓ 1  
✓ 2

$$\text{Var} = E \frac{(x_i - \bar{x})^2}{n}$$

$$(\sigma) \text{ std} = \sqrt{\frac{E(x_i - \bar{x})^2}{n}}$$

- 1 var

Pearson's  
Correlation  
Coefficient

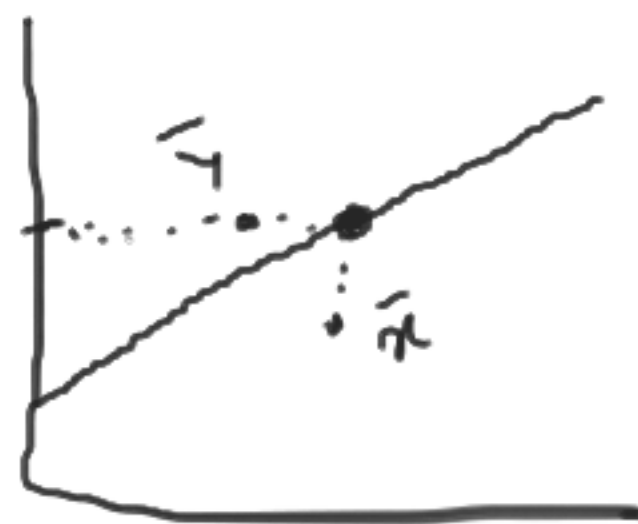
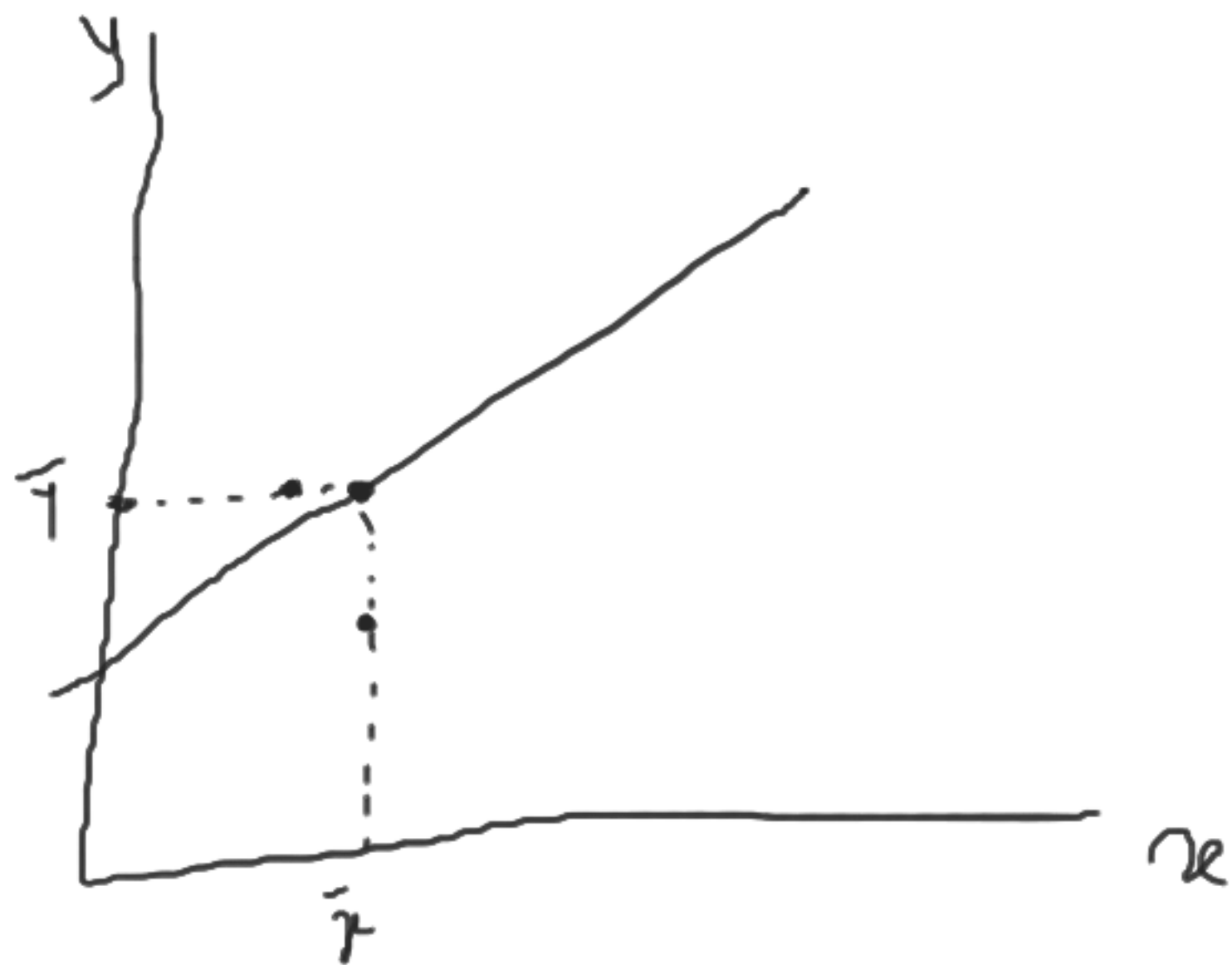
$$R_{(x,y)} = \frac{\sum (x_i - \bar{x}) \cdot (y_i - \bar{y})}{\sqrt{\sum (x_i - \bar{x})^2} \times \sqrt{\sum (y_i - \bar{y})^2}}$$

$r_{(x,y)}$

$$\rightarrow \frac{\frac{1}{\sum x}}{\frac{1}{\sum y}} \quad \frac{k/y}{\frac{1}{\sum y}} \quad \frac{1}{\sum y}$$

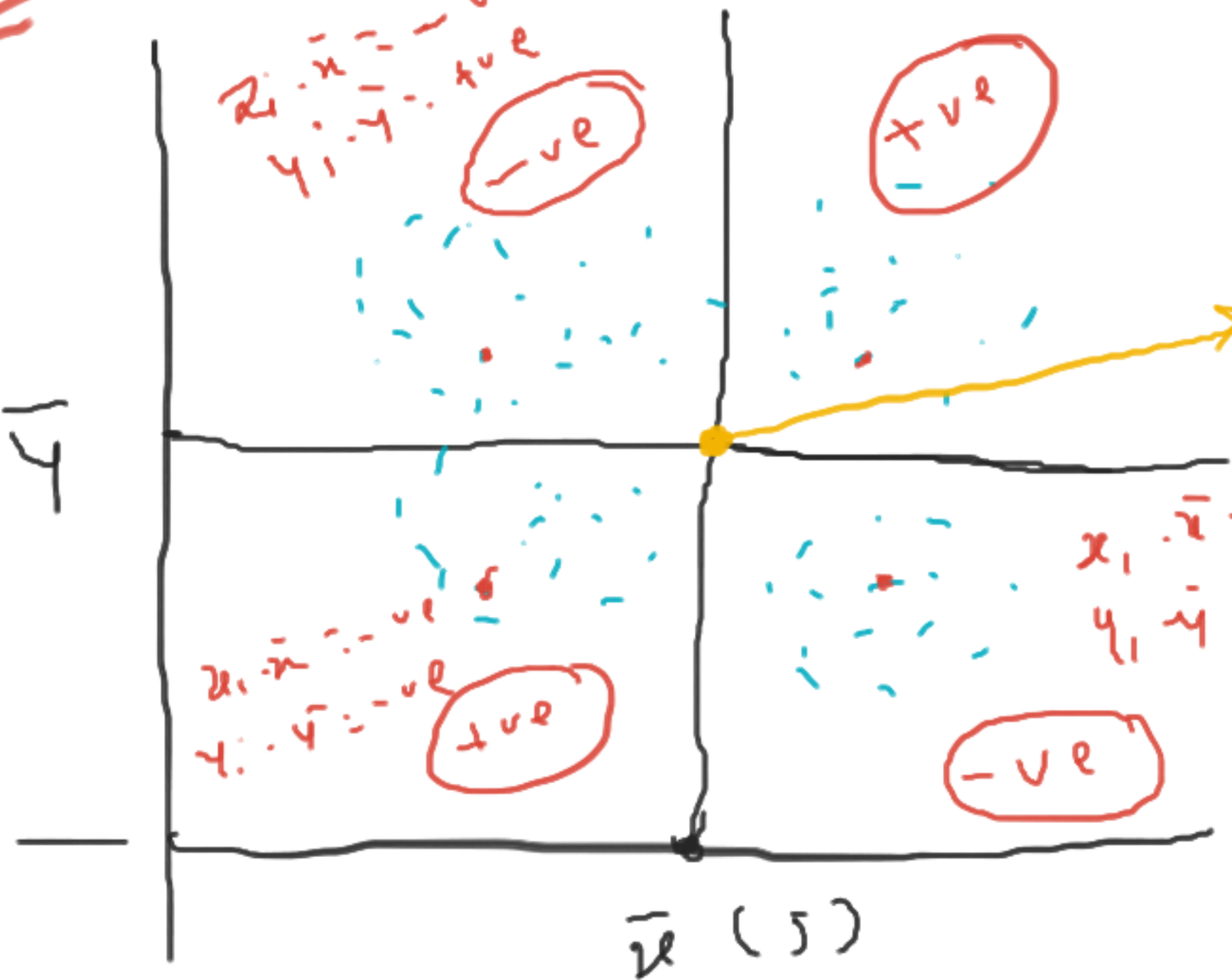
covariance  
-  $\text{std}(x), \text{std}(y)$

$$r_{(x,y)} = \frac{\text{covariance}}{s_x s_y}$$



Linear 0

(6) 4



$$x_i - \bar{x} = 8 - 5 = +3$$

$$y_i - \bar{y} = 8 - 6 = +2$$

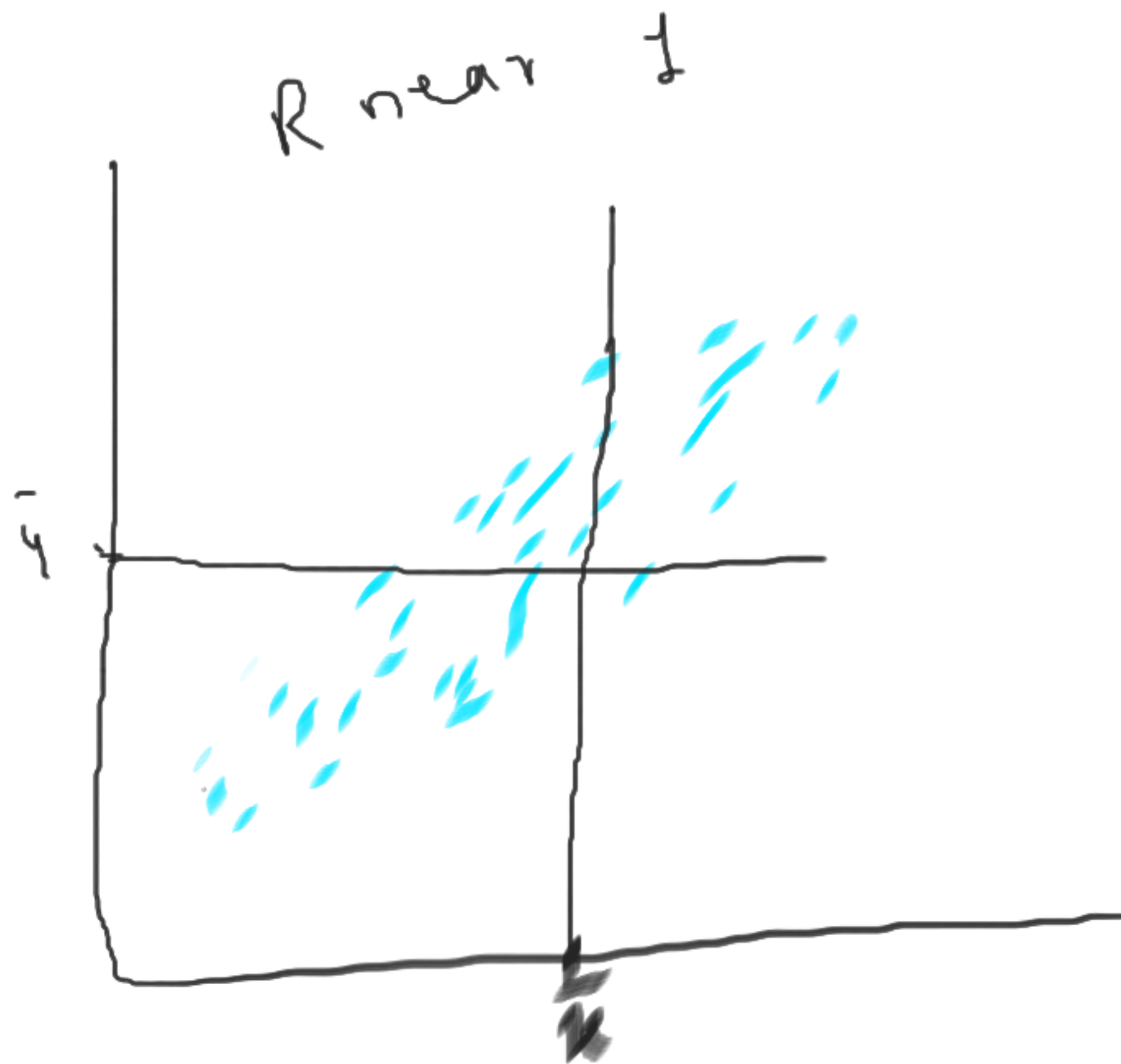
$$\begin{pmatrix} 5, 6 \\ (\bar{x}, \bar{y}) \end{pmatrix}$$

$$x_i - \bar{x} = +ve$$

$$y_i - \bar{y} = -ve$$

$$\begin{matrix} \bar{x} \\ \bar{y} \\ -2\bar{x} \\ -2\bar{y} \end{matrix}$$





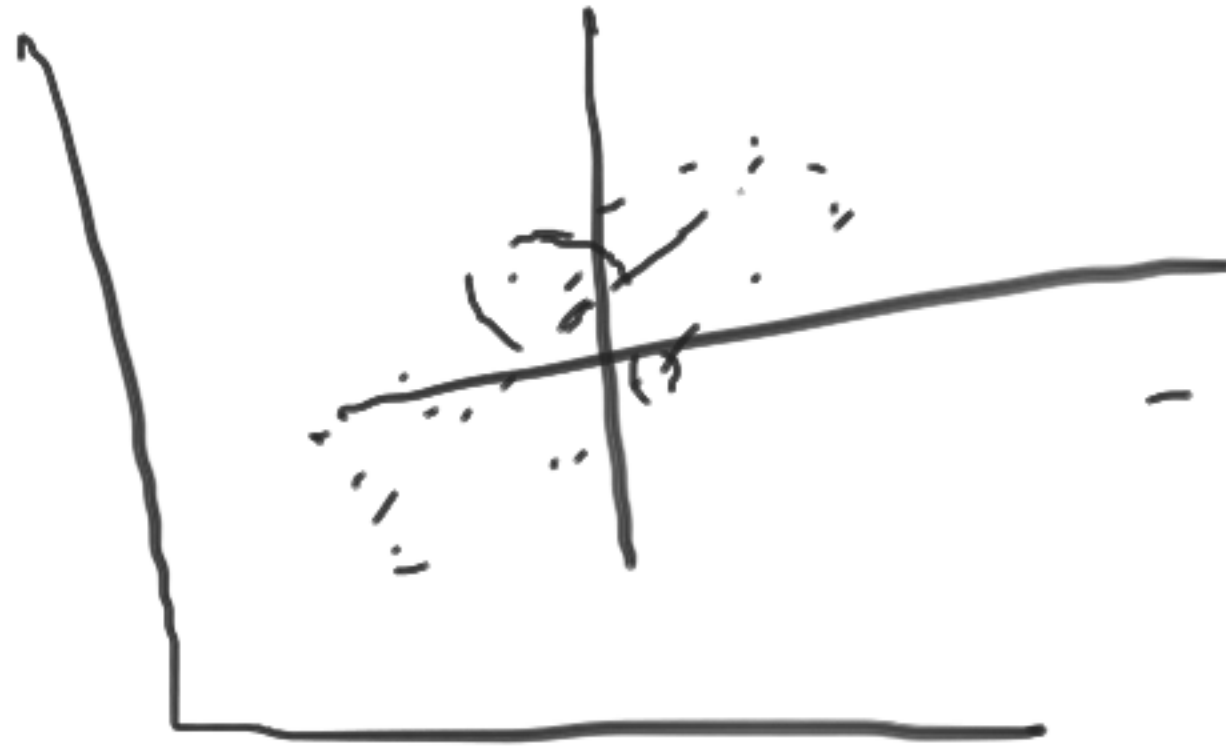
$$\begin{array}{r}
 20 \\
 24 \\
 - 66 \\
 \hline
 37 \\
 \hline
 37 \\
 51 \\
 \hline
 \textcircled{-0.7}
 \end{array}$$



$R_{pear} = -1$

$$\begin{array}{r}
 + 5 \\
 + 10 \\
 - 68 \\
 \hline
 69 \\
 \hline
 117 \\
 \hline
 132 \\
 \hline
 - 0.9
 \end{array}$$

Beacuse of  
Random  
sampling  
while  
computing  
correlation  
there could  
be  
statistical  
fluke.



0.5 - 10<sup>-7</sup>  
0.3

Statistical Fluke

or 0.09