

COMP 3271 Tutorial

# Programming Assignment II

Tutorial on 3D Modeling

# Submission

- Deadline:

**11:59pm, Nov. 9, 2018HKT**

- Submission:

**rayView.cpp**

If you want to change any other files or implement the program without the template, please email me(wenhua00@hku.hk) before submission.

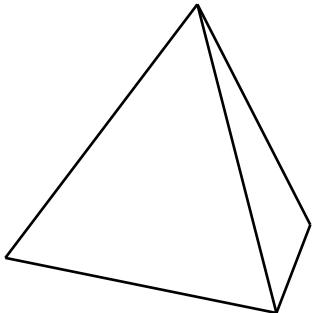
# Outline

- 3D Modeling & 3D Rendering in OpenGL
- 3D Modeling & Interface Design – Programming Assignment II
  - About the Template
  - About the Task
    - Mouse controlled model editing
    - 3D solid handles

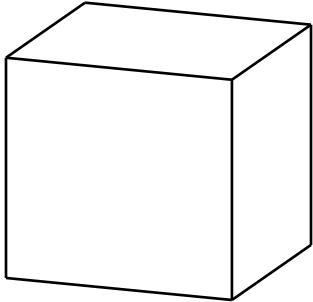
# Outline

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  - About the Template
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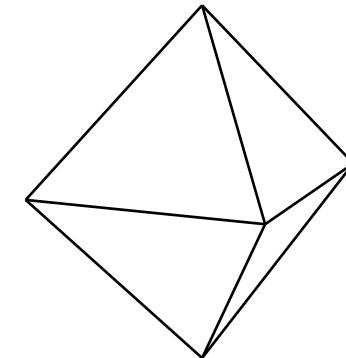
# Some 3D Primitives



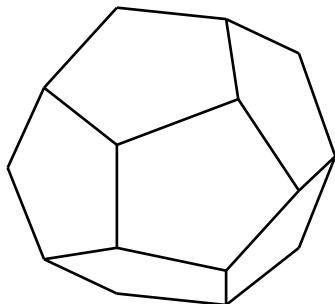
Tetrahedron



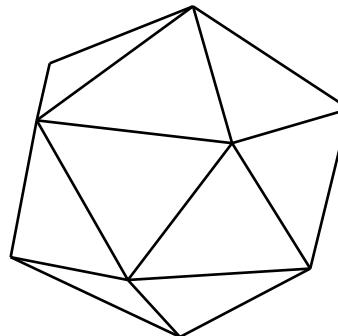
Cube



Octahedron



Dodecahedron (12 faces)



Icosahedron (20 faces)

# Draw Geometric Objects – 3D

```
void glVertex3{b,s,i,f,ub,us,ui}(TYPE x, TYPEy, TYPEz);
```

```
void glVertex3{b,s,i,f,ub,us,ui}v(const TYPE*v);
```

- Example1: draw a triangle in 3D space

```
glBegin(GL_TRIANGLES); //Specify object type
```

```
glVertex3f(-0.5, 0.5, 0.5); // Object's coordinates
```

```
glVertex3f(0.5, 0.5, 0.6);
```

```
glVertex3f(0.5, -0.5, 1.0);
```

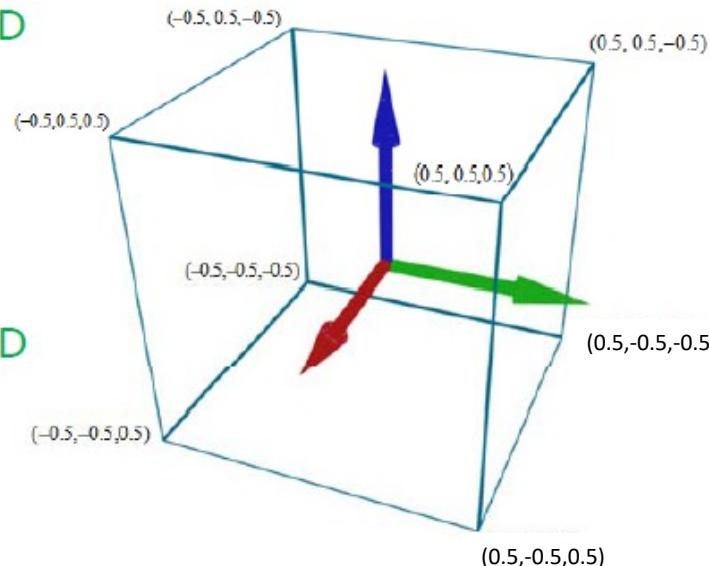
```
glEnd();
```

# Draw Geometric Objects – 3D

- Example2: draw a cube

Solution 1: Use GL\_QUADS to draw a box.

```
glBegin(GL_QUADS);
glVertex3f(-0.5f, -0.5f, -0.5f); //First QUAD
glVertex3f(-0.5f, 0.5f, -0.5f);
glVertex3f(0.5f, 0.5f, -0.5f);
glVertex3f(0.5f, -0.5f, -0.5f);
...
glVertex3f(-0.5f, -0.5f, 0.5f); //Sixth QUAD
glVertex3f(-0.5f, 0.5f, 0.5f);
glVertex3f(0.5f, 0.5f, 0.5f);
glVertex3f(0.5f, -0.5f, 0.5f);
glEnd();
```

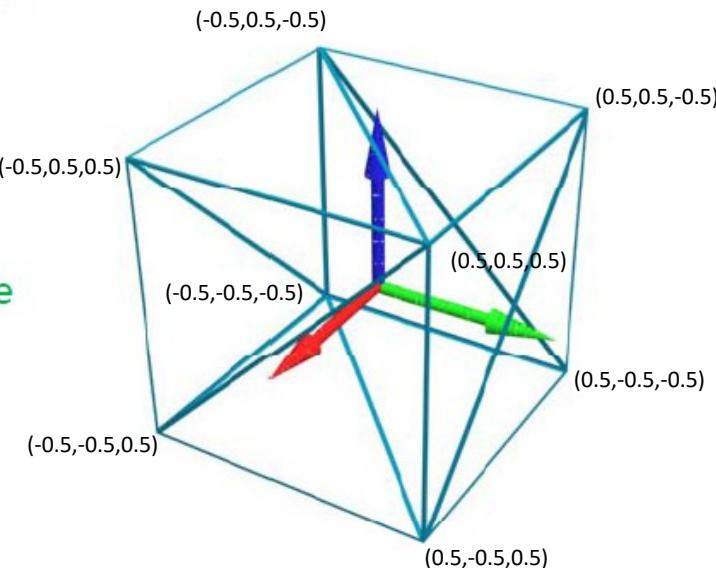


# Draw Geometric Objects – 3D

- Example2: draw a cube

Solution 2: Use GL\_TRIANGLES to draw a box.

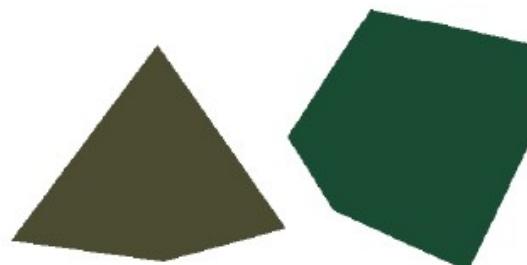
```
glBegin(GL_TRIANGLES);
glVertex3f(-0.5f, -0.5f, -0.5f); //1st triangle
glVertex3f(-0.5f, 0.5f, -0.5f);
glVertex3f(0.5f, 0.5f, -0.5f);
...
glVertex3f(-0.5f, 0.5f, 0.5f); //12th triangle
glVertex3f(0.5f, 0.5f, 0.5f);
glVertex3f(0.5f, -0.5f, 0.5f);
glEnd();
```



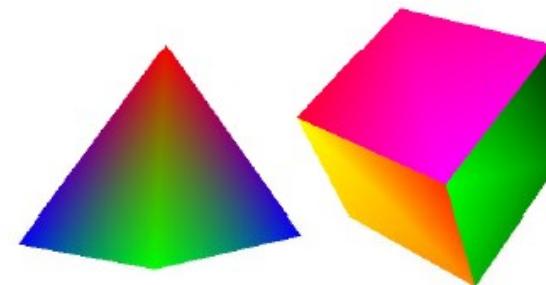
# Draw Geometric Objects – 3D

Sample: use color to show 3D effect.

```
glBegin(GL_TRIANGLES);
glColor3f(1.0f, 0.0f, 0.0f); //First triangle
glVertex3f(-0.5f, -0.5f, -0.5f);
glColor3f(0.0f, 1.0f, 0.0f);
glVertex3f(-0.5f, 0.5f, -0.5f);
glColor3f(0.0f, 0.0f, 1.0f);
glVertex3f(0.5f, 0.5f, -0.5f);
...
glEnd();
```



Vertices with the same color



Vertices with different colors

# GLU Quadrics

- **Function Introduction**

```
void gluSphere(GLUquadric* quadric,  
               GLdouble radius,  
               GLint slices,  
               GLint stacks)
```

**Purpose :** Draw a sphere symmetric around the origin.

**quadric :** Object pointer to a created quadric object.

**radius:** The radius of sphere .

**slices:** The number of segments in the vertical direction.

**stacks:** The number of segments in the horizon direction.

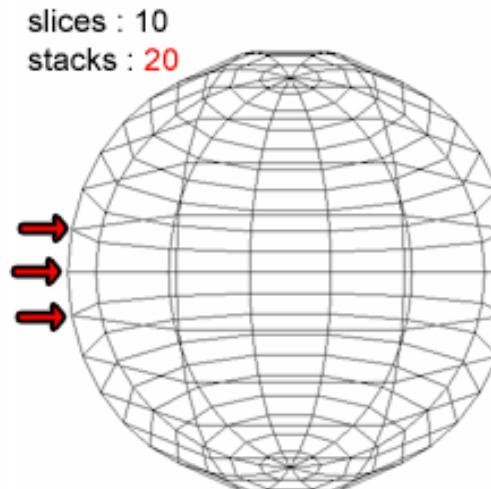
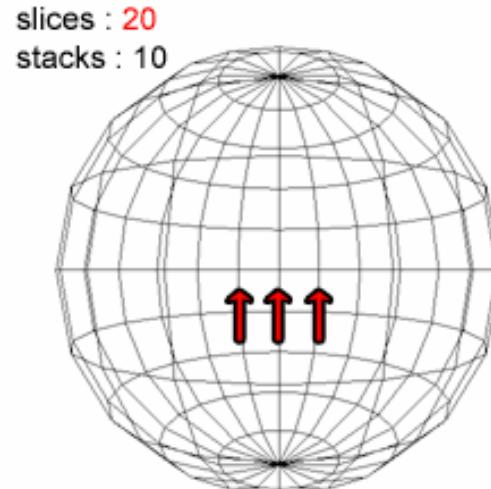
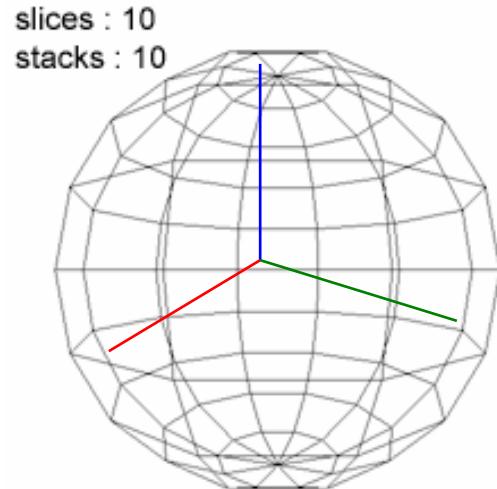
# GLU Quadrics

- Sample Code

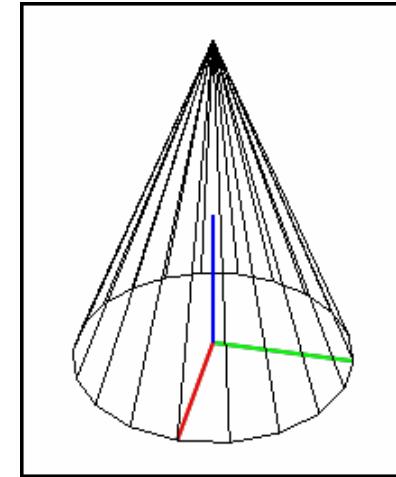
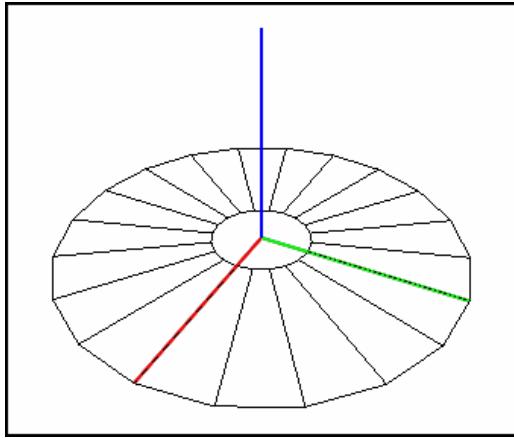
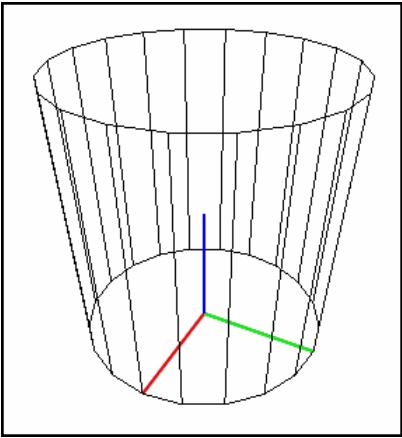
...

```
GLUquadricObj *qu;  
qu=gluNewQuadric();  
gluSphere(qu, 2.0f, 10, 10);  
gluDeleteQuadric(qu);
```

...



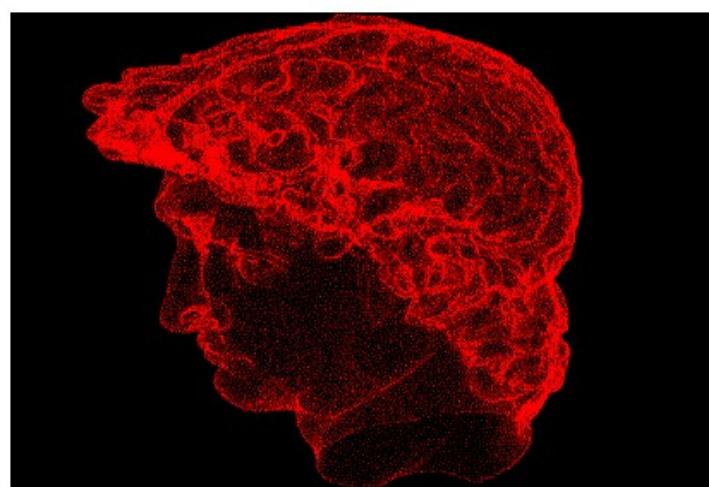
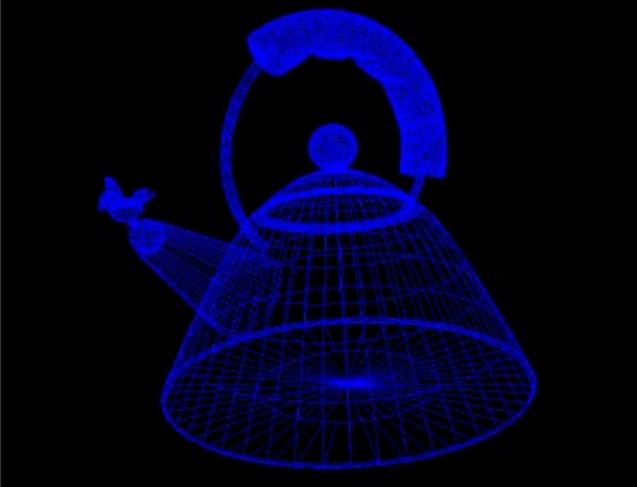
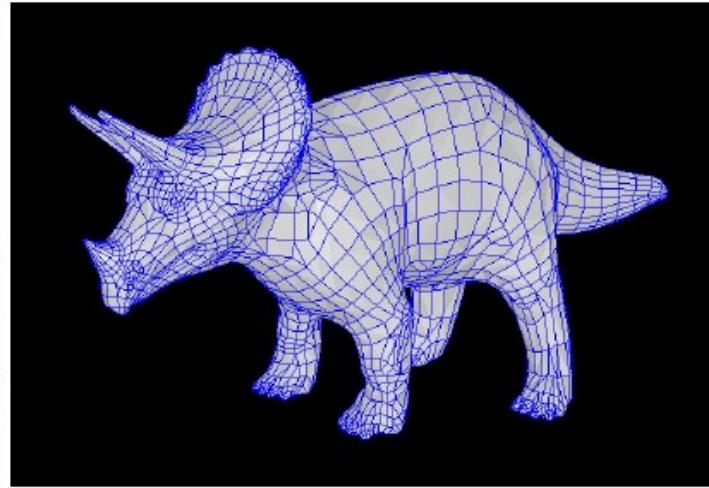
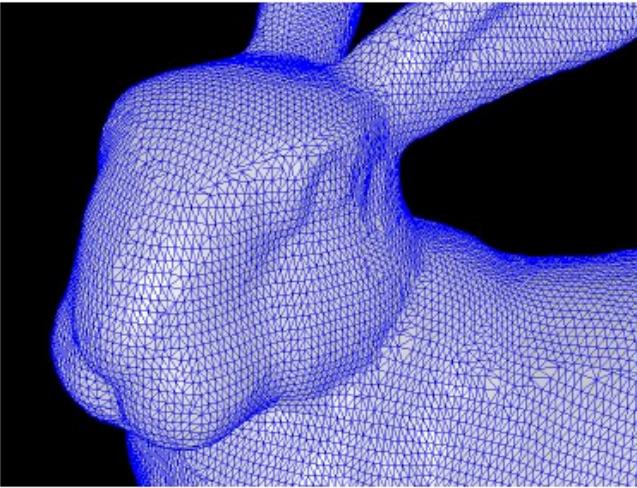
# Draw a cone



- **Cylinder** `gluCylinder(quadric, baseRadius, topRadius, height, slices, stacks)`
- (a **cone** is a cylinder with one radius = 0)
- **Disk** `gluDisk(quadric, innerRadius, outerRadius, slices, rings)`

```
/* draw a cone */  
GLUquadricObj *qu;  
qu=gluNewQuadric();  
gluCylinder(qu, 1.0f, .0f,  
2.0f,30,20);  
gluDisk(qu,.0f,1.0f,30,5);  
gluDeleteQuadric(qu);
```

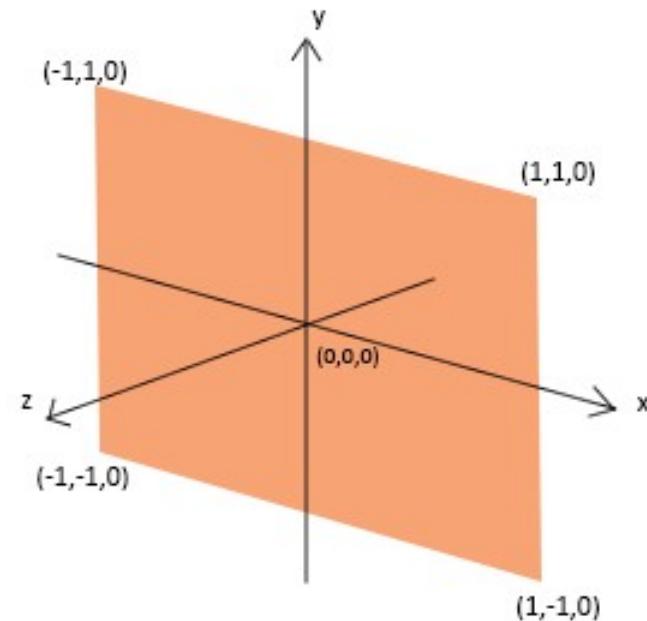
# Draw Geometric Objects – 3D



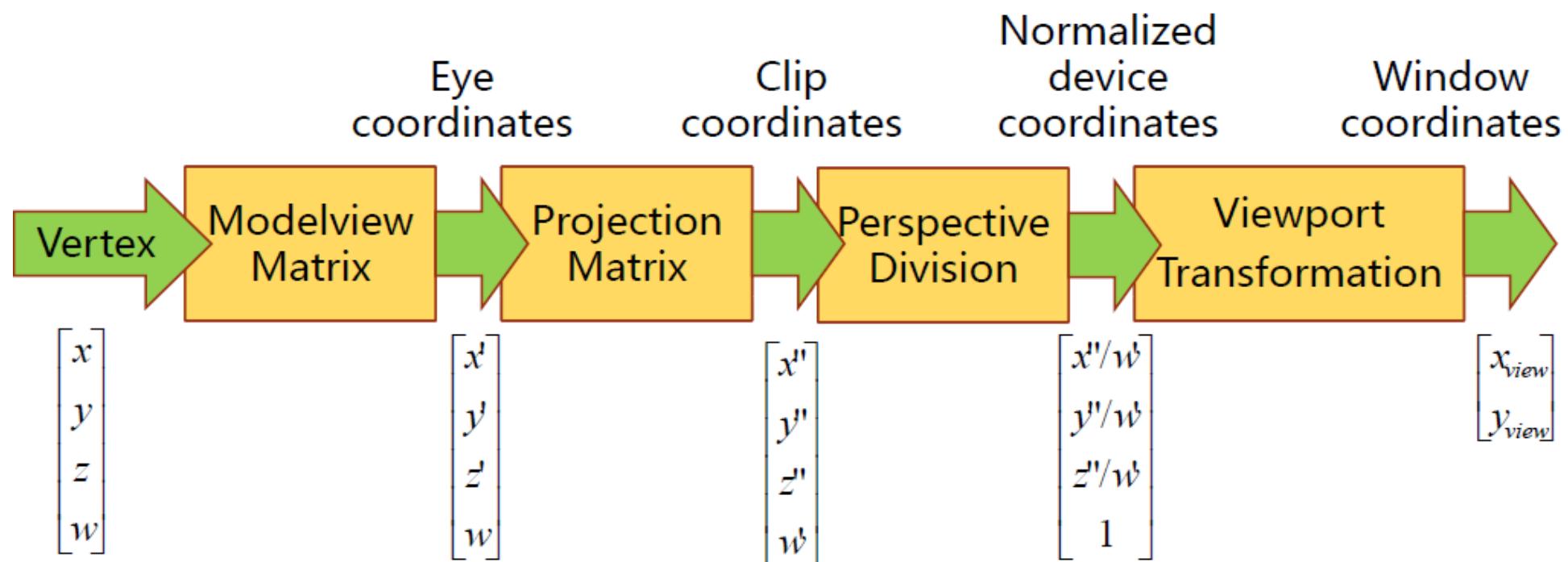
# 3D Rendering

- Coordinate system

1. Object or model coordinates
  2. World coordinates
  3. Eye (or Camera) coordinates
  4. Clip coordinates
  5. Normalized device coordinates
  6. Window (or screen) coordinates
- Initial state



# 3D Rendering



# 3D Rendering

- Choose the current matrix

## Projection matrix

Define the canvas in 2D case and the viewing volume in 3D case.

`gluOrtho2D, glOrtho, gluPerspective, glFrustum`

## Modelview matrix

Define the transformation of the camera and objects.

`gluLookAt, glTranslate, glRotate, glScale`

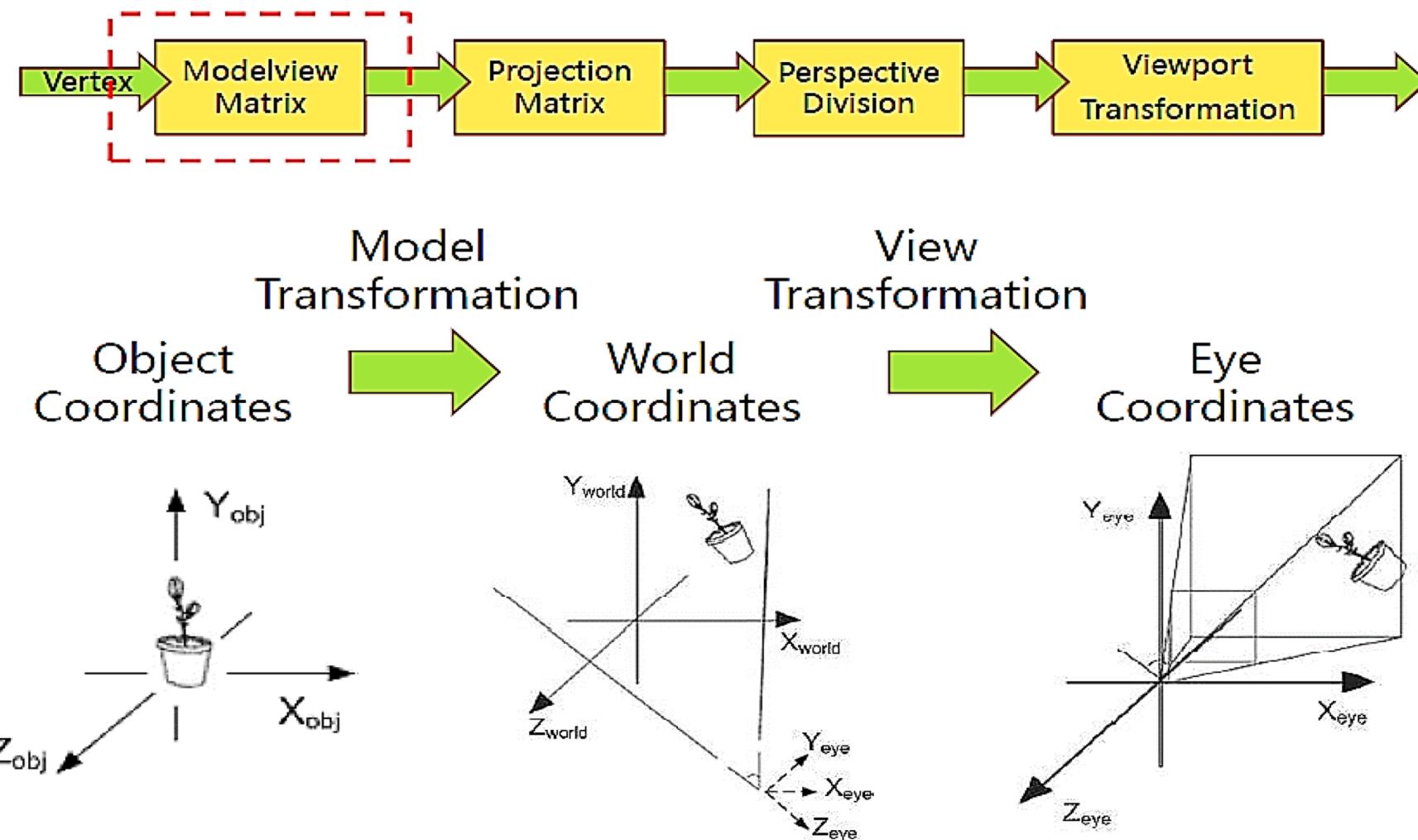
Choose the matrix to operate with:

`void glMatrixMode(MatrixType);`

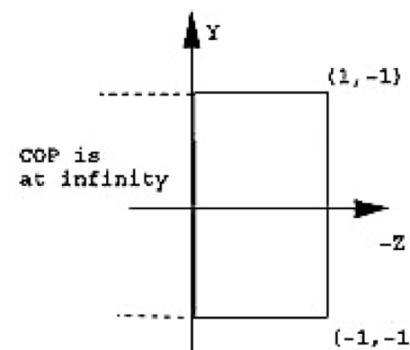
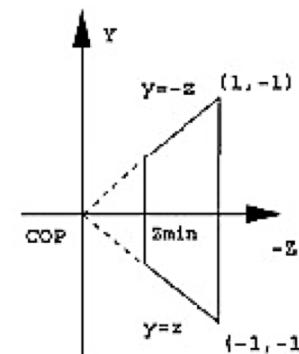
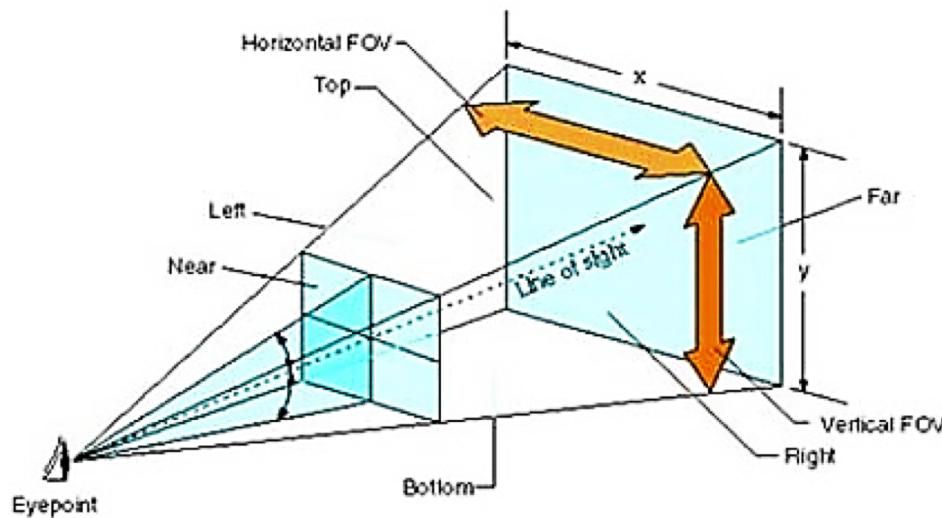
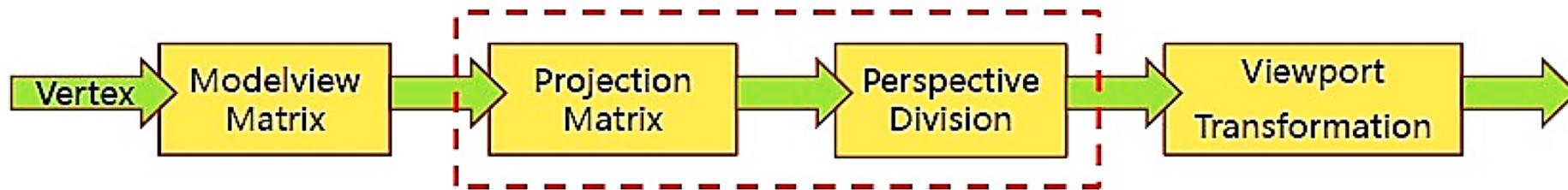
`GL_PROJECTION`: Choose projection matrix

`GL_MODELVIEW`: Choose model view matrix

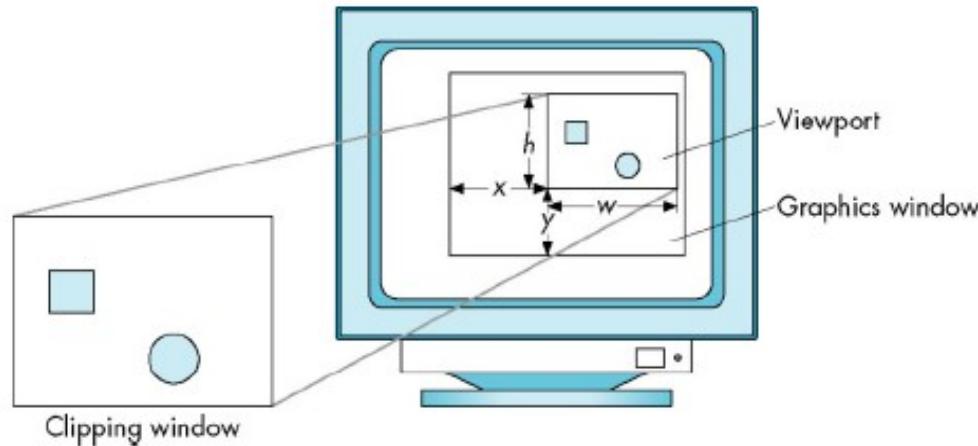
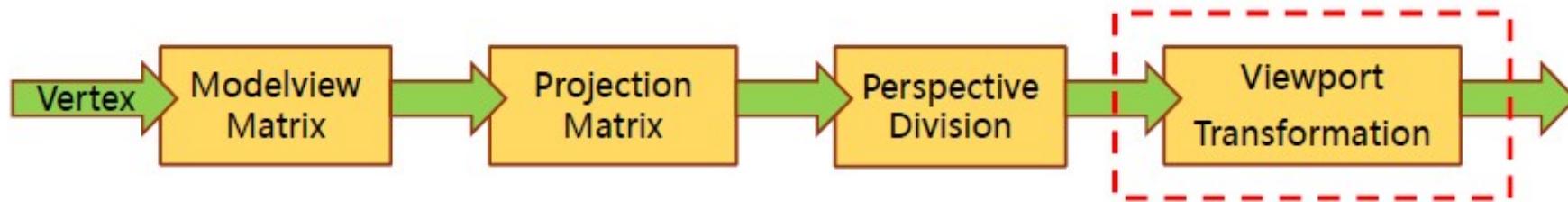
# 3D Rendering



# 3D Rendering



# 3D Rendering



# 3D Rendering

**As a programmer, you need to do the following things:**

- Specify the location/parameters of camera.
- Specify the geometry of the objects.
- Specify the lights (optional).

**OpenGL will compute the result 2D image!**

# 3D Rendering

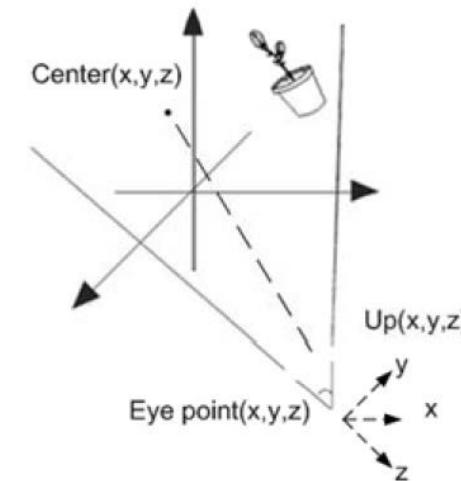
- Specify the location of camera

`gluLookAt(eyeX, eyeY, eyeZ, centerX, centerY, centerZ,  
upX, upY, upZ);`

(eyeX, eyeY, eyeZ) : Eye point position.

(centerX, centerY, centerZ) : Reference point.

(upX, upY, upZ) : Direction of up vector.

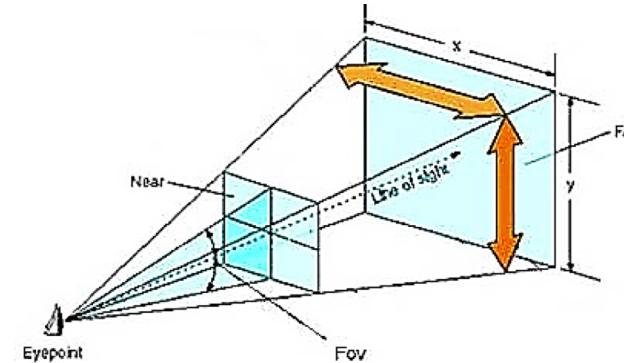


# 3D Rendering

- Define the viewing volume

Perspective projection

`gluPerspective(fov, aspect, near, far);`



Purpose: Define the perspective projection matrix

**fov**: specify the angle of scene view in model space.

**aspect**: specify the scene view height/width ratio;

**near** : distance of near plane from eye point(>0).

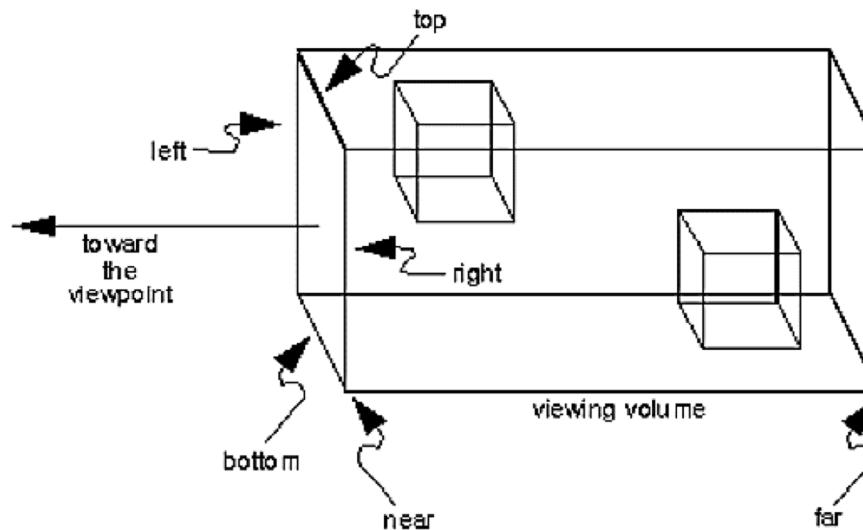
**far** : distance of far plane from eyepoint(>near).

# 3D Rendering

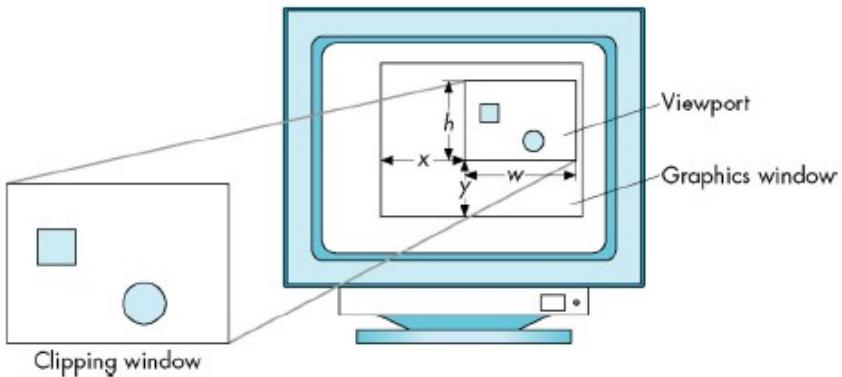
- Define the viewing volume

Orthogonal projection

`glOrtho(Xmin, Xmax, Ymin, Ymax, near, far)`



# 3D Rendering



**void glViewport(GLint x, GLint y, GLsizei w, GLsizei h);**

**Purpose:** Set viewport for model scene rendering.

( $x, y$ ) : define the left down point of a viewport.

( $w, h$ ) : define the height ( $h$ ) and width ( $w$ ) of the viewport.

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- 3D Modeling & Interface Design – Programming Assignment
  - About the Template
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# Template Provided Functions

- 3D Primitives Modeling
  - Triangular based models
    - Cube Pyramid Tetrahedron Octahedron Icosahedron Dodecahedron
  - Quadratics models
    - Sphere Cone Cylinder
- Object(s) Selection
- Navigate Control Mode
- Viewpoint rotation

# Outline

- 3D Modeling & 3D Rendering in OpenGL
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  - **About the Task**
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# Your Tasks

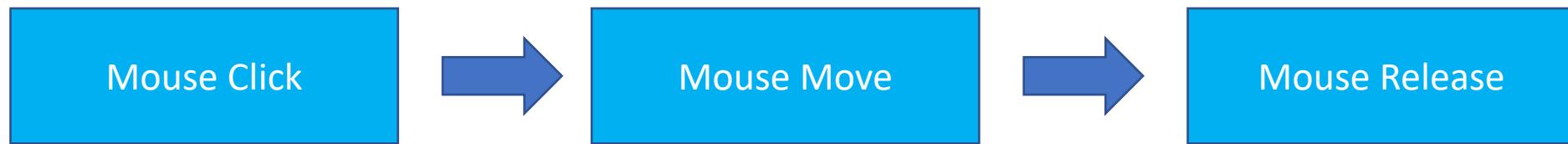
- Mouse controlled model editing (in ‘UserMouseMove’ function\*)
  - Translation (axis aligned)
  - Rotation (Trackball style)
  - Scaling (axis aligned)
- 3D solid handles (in ‘UserDrawControlHandle’ function\*)

\*Both functions are in ‘RayView.cpp’

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# Basic Mouse Control



UserLButtonDown(...)

UserRButtonDown(...)

*Setup Editing Mode*

UserMouseMove(...)

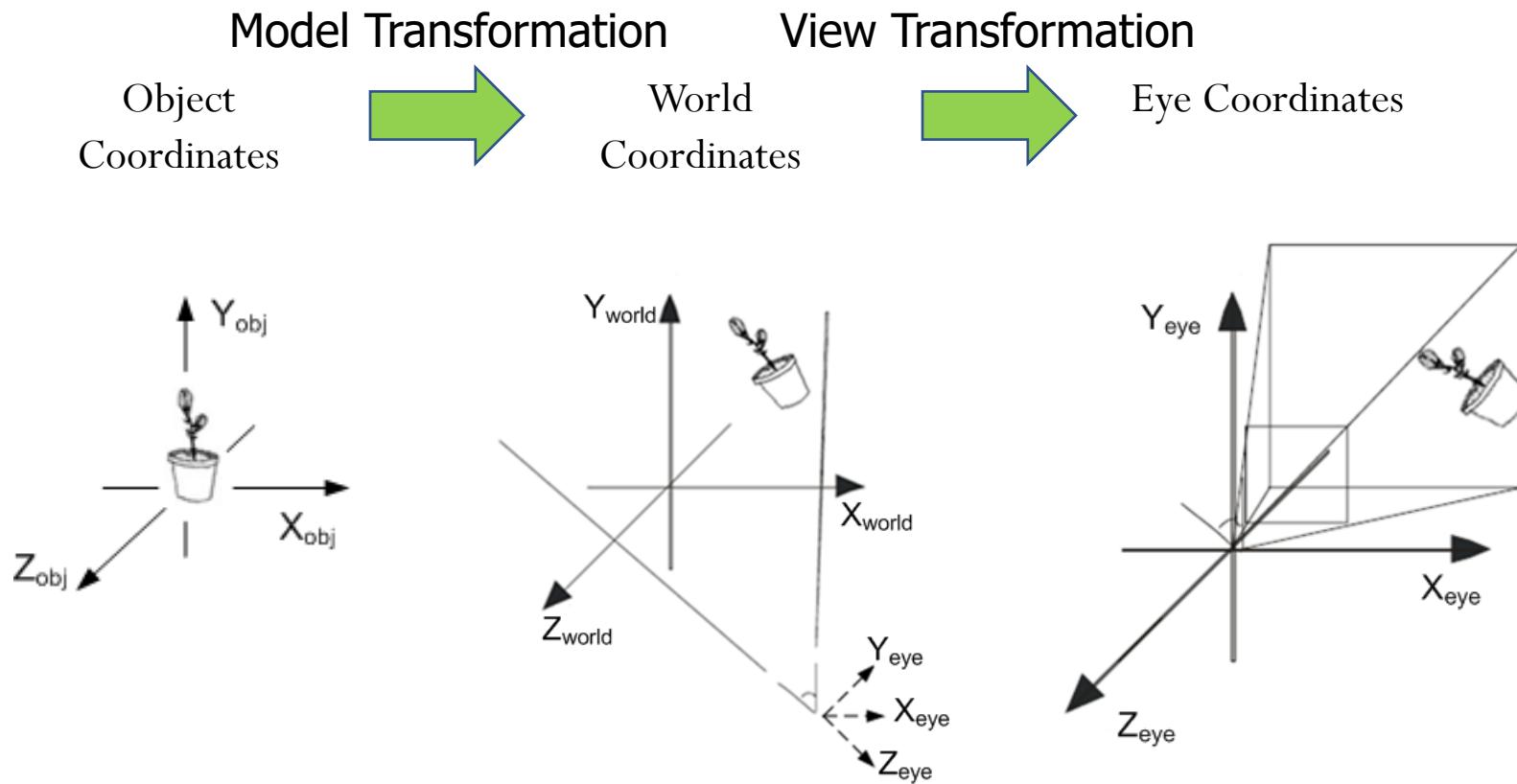
*Do Transformation*

UserLButtonUp(...)

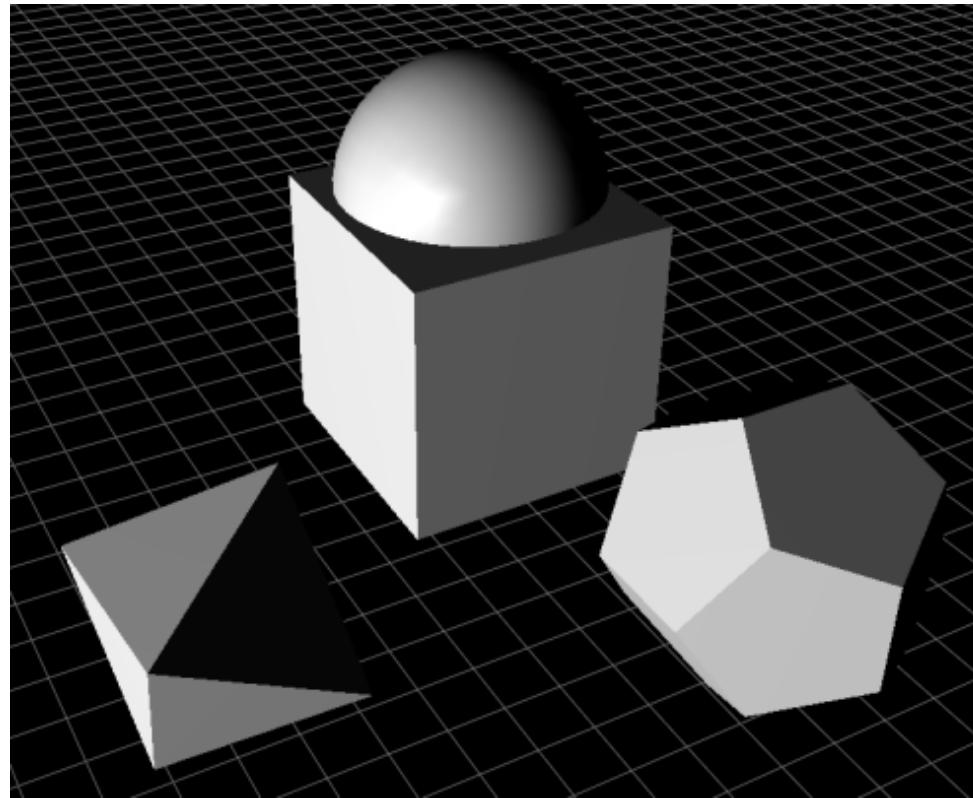
UserRButtonUp(...)

*Exit Editing Mode*

# Implementation Outline – Object transformation



# Implementation Outline – Object transformation



# Implementation Outline – Interface of UserMouseMove()

- Input
  - View information
    - `pDoc->m_camera.viewpoint`
  - 2D screen position
    - Start mouse position (Sstart): `m_nSx , m_nSy`
    - Current mouse position(Scurr): Function parameters `x,y`
- To-do
  - Form the transformation matrix and multiply it to each selected object.

# Implementation Outline – Conventions in this template

- We always use the start condition in *mousedown*.

- Model's transform matrix is saved on *mousedownevent*.

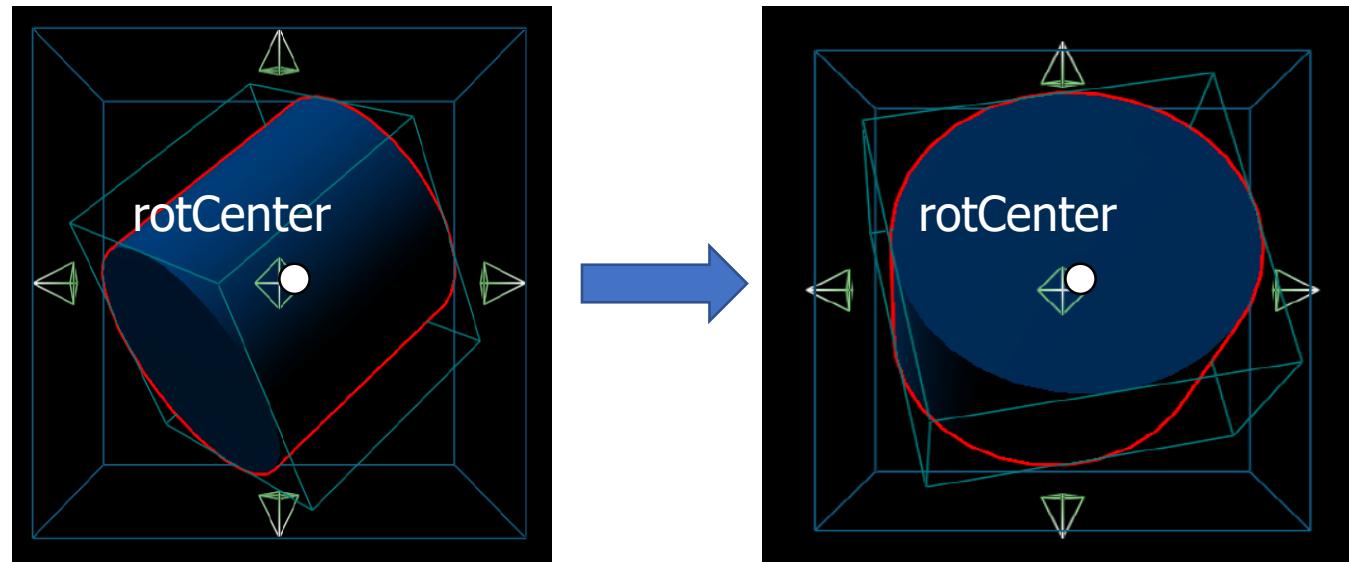
```
pDoc->SelectedObjectsBackupM();  
//backup all the matrices of selected objects
```

- Model's transform matrix should be restored on *mousemoveevent*. This is to ensure the object is unchanged if mouse returns to its start condition.

```
pDoc->SelectedObjectsRestoreM();  
//restore all the matrices of selected objects
```

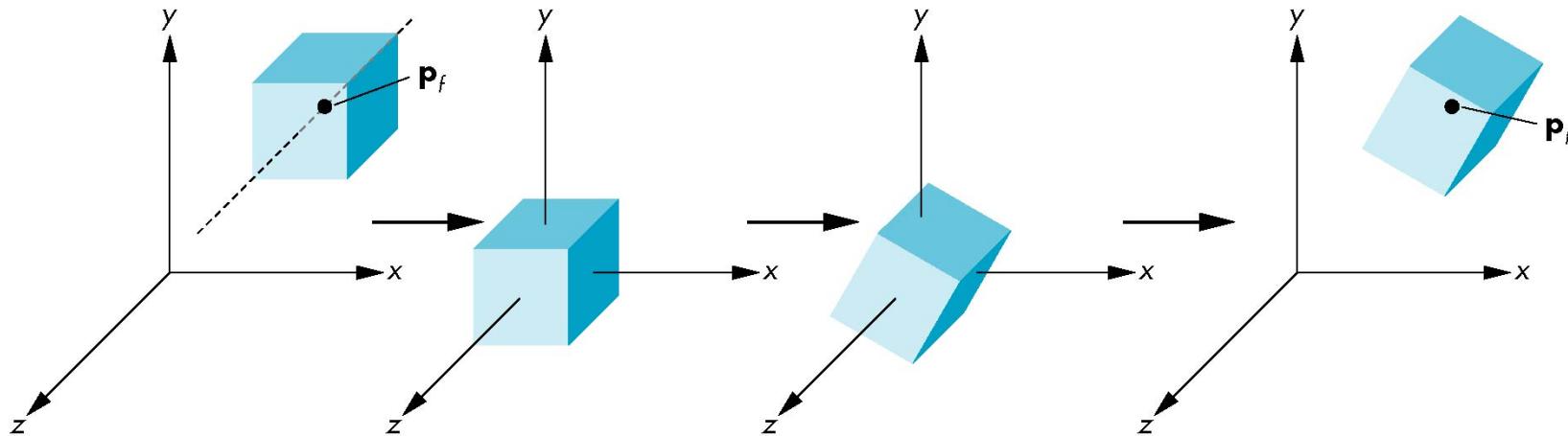
# Object Rotation

- **rotCenter** denotes the rotation center.
- **rotCenter** is a class member variable. You may use it directly.
- Rotation angle is proportional to the amount of mouse motion.



# Object Rotation – Rotation About a Fixed Point

- Move fixed point  $P_f$  to origin
- Rotate around the origin
- Move fixed point  $P_f$  back
- $\mathbf{M} = \mathbf{T}(p_f) \mathbf{R} \mathbf{T}(-p_f)$



# Object Rotation – Form the transformation matrix

- *rotCenter* is the fixed point. The overall transformation is

$$\begin{pmatrix} 1, 0, 0, \text{rotCenter}[0] \\ 0, 1, 0, \text{rotCenter}[1] \\ 0, 0, 1, \text{rotCenter}[2] \\ 0, 0, 0, \quad 1 \end{pmatrix} \begin{matrix} R \end{matrix} \begin{pmatrix} 1, 0, 0, -\text{rotCenter}[0] \\ 0, 1, 0, -\text{rotCenter}[1] \\ 0, 0, 1, -\text{rotCenter}[2] \\ 0, 0, 0, \quad 1 \end{pmatrix}$$

- Use CPrimitive's *MultM(N)* function to do the matrix multiplications.  
Note that MultM is a left matrix multiplication, i.e.  $M = N * M$

# Object Rotation - Sample Code

```
float tmat[16]={.0f}; float itmat[16]={.0f}; float rmat[16]={.0f};  
tmat[0] = tmat[5] = tmat[10] = tmat[15] = 1.0f;  
itmat[0] = itmat[5] = itmat[10] = itmat[15] = 1.0f;  
tmat[12] = rotCenter[0]; tmat[13] = rotCenter[1]; tmat[14] = rotCenter[2];  
itmat[12]=-rotCenter[0]; itmat[13]=-rotCenter[1]; itmat[14]=-rotCenter[2];  
  
//get rmat  
  
for(list<LPPRIMITIVE>::iterator it=pDoc->m_selectedobjects.begin();  
    it!=pDoc->m_selectedobjects.end(); it++)  
{      (*it)->MultM(itmat);  
      (*it)->MultM(rmat);  
      (*it)->MultM(tmat);  
}
```

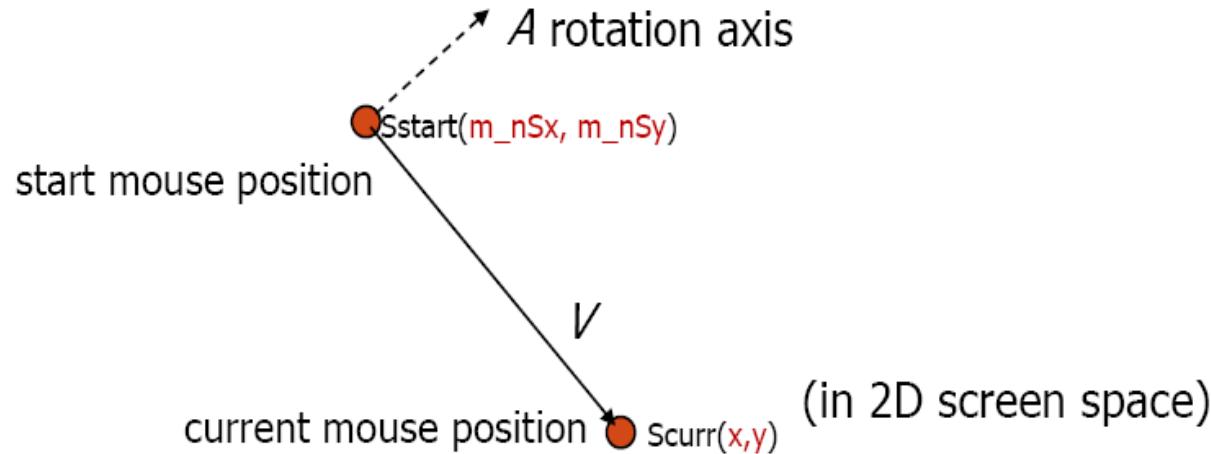
$$\begin{pmatrix} 1, 0, 0, & \text{rotCenter}[0] \\ 0, 1, 0, & \text{rotCenter}[1] \\ 0, 0, 1, & \text{rotCenter}[2] \\ 0, 0, 0, & 1 \end{pmatrix}$$

tmat

$$\begin{pmatrix} 1, 0, 0, & -\text{rotCenter}[0] \\ 0, 1, 0, & -\text{rotCenter}[1] \\ 0, 0, 1, & -\text{rotCenter}[2] \\ 0, 0, 0, & 1 \end{pmatrix}$$

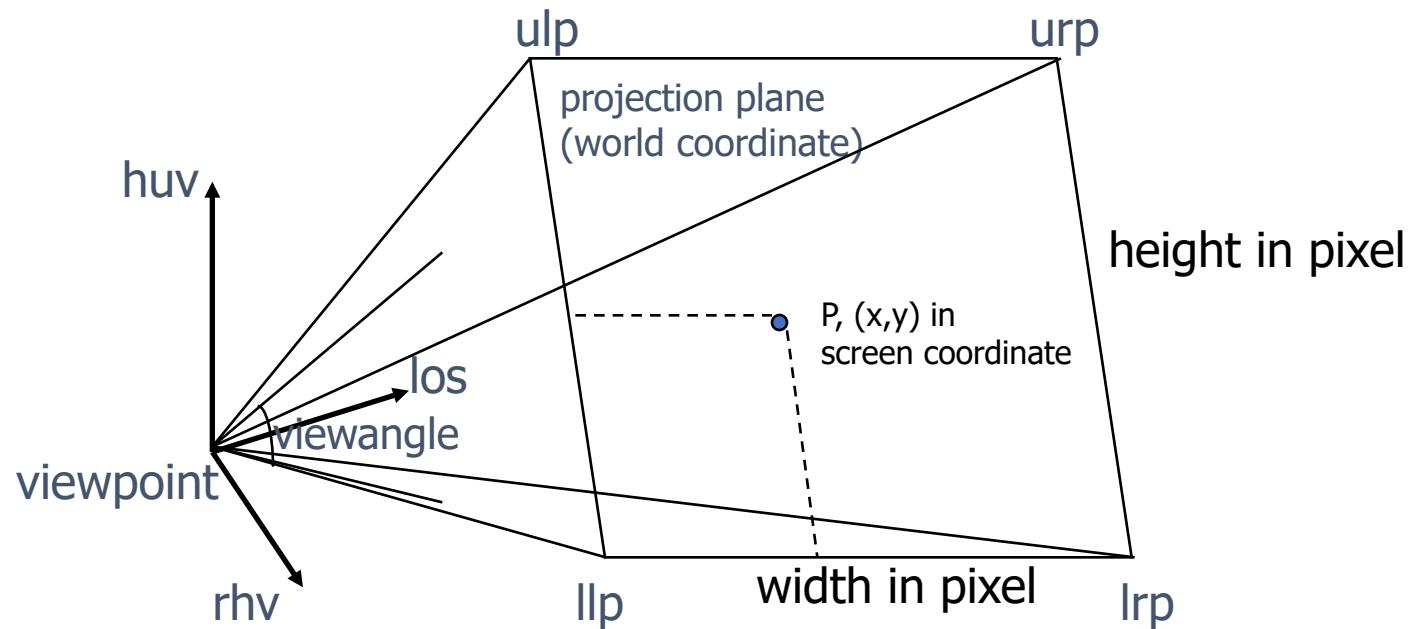
itmat

# Object Rotation – Find the rotation axis & rotation angle



- 2D vector  $V = S_{curr} - S_{start}$
- Rotate  $V$  by 90 degree to get vector  $A(A_x, A_y)$ , here  $A_x = -V_y$ ,  $A_y = V_x$ .
- Project  $S_{start}$  and  $S_{start} + A$  to world coordinates to get  $S_{start}'$  and  $(S_{start} + A)'$  with function '[ProjectScreenPoint](#)'.
- Rotation axis  $ra = (S_{start} + A)' - S_{start}'$
- Rotation angle  $= k \times |A| = k \times \sqrt{A_x^2 + A_y^2}$   
(assign  $k$  by yourself, suggested value: 0.5)

# Project screen coordinates to world coordinates



huv -- head up vector (unit vector)  
los -- line of sight (unit vector)  
rhv -- right hand vector (unit vector)

Calculate the corresponding world coordinate  $P'$  of a screen position  $P$   
$$P' = llp + (lrp - llp) * x / \text{width} + (ulp - llp) * y / \text{height}$$

Using Function `ProjectScreenPoint(x,y)`.

# Object Rotation – Finding the Rotational Matrix R

- Use OpenGL library to compute R

```
glPushMatrix();
glLoadIdentity();
//angle is the rotation angle, ra is the rotation axis
glRotatef(angle,ra[0],ra[1],ra[2]);
glGetFloatv(GL_MODELVIEW_MATRIX, R);
glPopMatrix();
```

# Object Rotation - Procedure

Step 1 : Find the rotation axis and determine the rotation degree

Step 2 : Get the rotation matrix about the origin

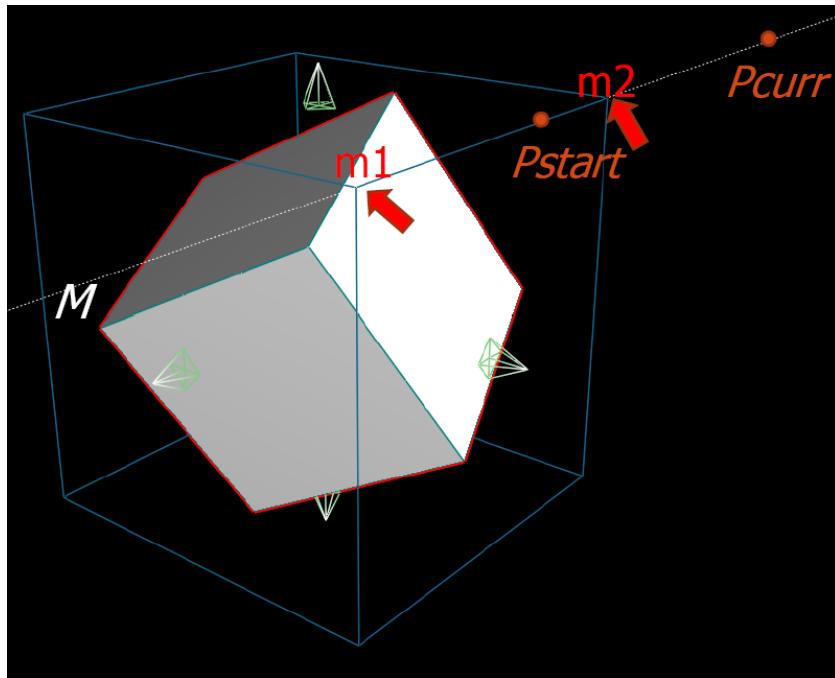
Step 3 : Restore all the matrices of selected objects

Step 4 : For each selected object:

- (a) Translate the rotation center to the origin
- (b) Rotate round the origin
- (c) Translate the rotation center back

# Object Translation

- Translate along the user selected line  $M$ , with two endpoints  $m_1, m_2$ .



$$T = \begin{pmatrix} 1 & 0 & 0 & Pcurr[0] - Pstart[0] \\ 0 & 1 & 0 & Pcurr[1] - Pstart[1] \\ 0 & 0 & 1 & Pcurr[2] - Pstart[2] \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

# Object Translation – Find the start & current position on M

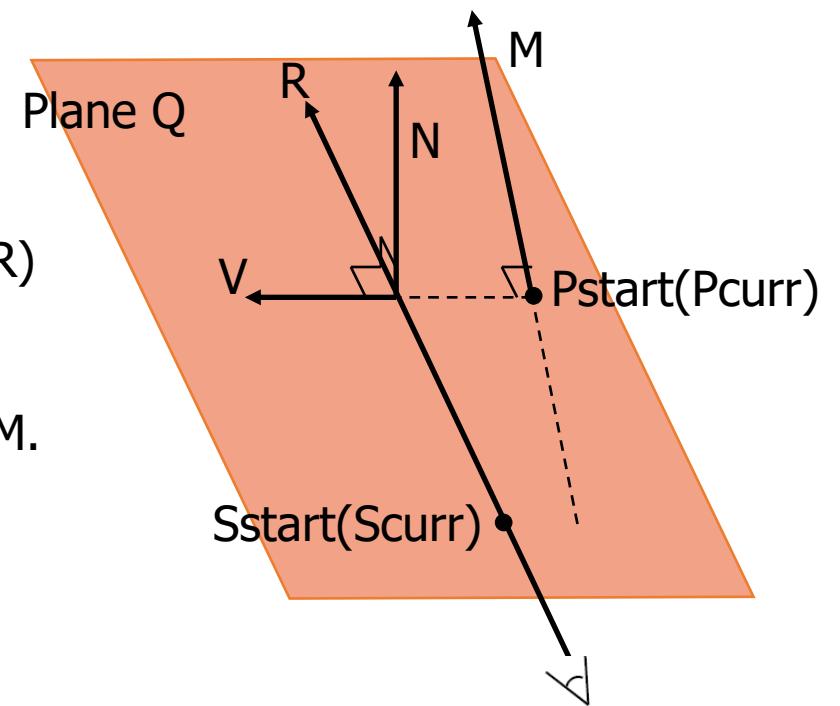
- Find Pstart and Pcurr corresponding to Sstart and Scurr respectively.
- Pstart and Pcurr are on the user selected line M.
- Pstart (Pcurr) is the closest point to ray R that goes through Sstart (Scurr).

$V = \text{cross}(M, R)$  ( $V$  means the shortest path between  $M$  and  $R$ )

$N = \text{cross}(R, V)$

Plane Q can be defined by N and viewpoint.

Pstart (or Pcurr) is the intersection point of Plane Q and line M.



# Object Translation - Procedure

Step 1: For the start mouse position Sstart, find Pstart on M

Step 2: For the current mouse position Scurr, find Pcurr on M

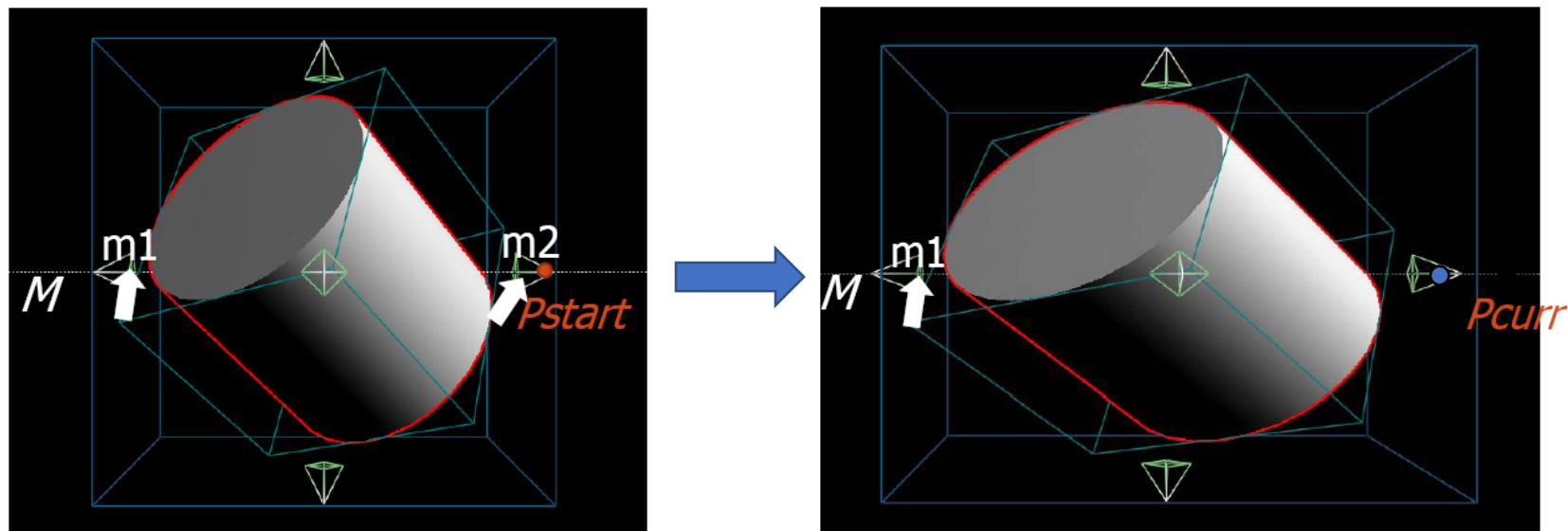
Step 3: Create the translation matrix

Step 4: Restore all the matrices of selected objects

Step 5: For each selected object,  
do the translation.

# Object Scaling (Axis aligned)

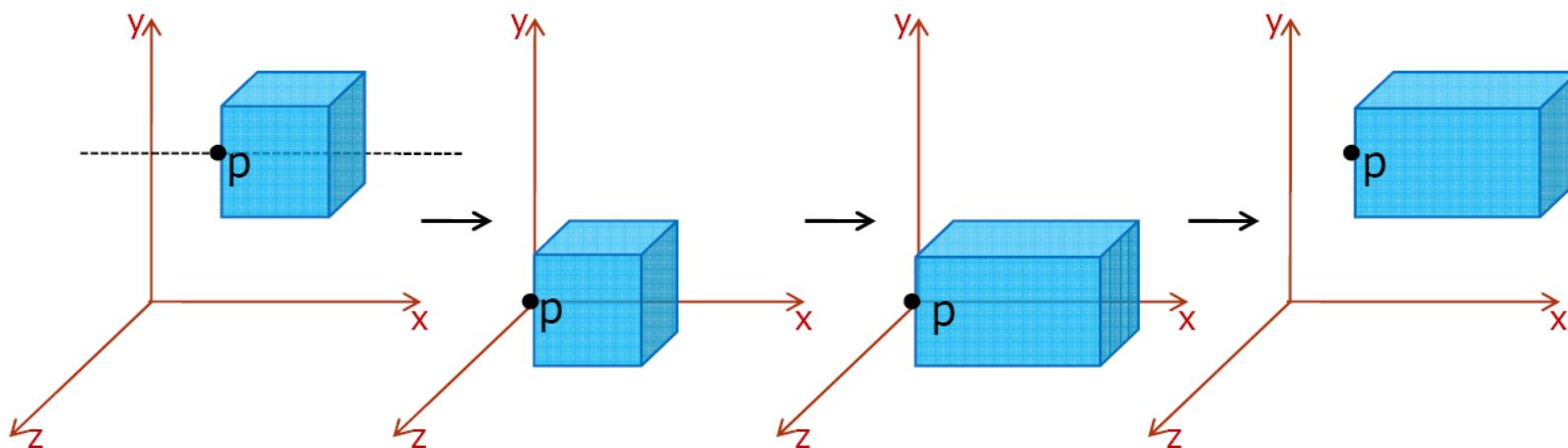
- Scale along the user selected line  $M$ , denoted by two points  $m_1, m_2$ . (here,  $M$  is one of the world axes.)
- Scale about the fixed point  $m_1$ .



# Object Scaling – Scaling About a Fixed Point P

- Move P to the origin
- Scale the object
- Move P back

Transformation Matrix =  $T(p) S T(-p)$



# Object Scaling – Form the transformation matrix

- $m1$  is the fixed point. The overall transformation is

$$\begin{bmatrix} 1 & 0 & 0 & m1[0] \\ 0 & 1 & 0 & m1[1] \\ 0 & 0 & 1 & m1[2] \\ 0 & 0 & 0 & 1 \end{bmatrix} \times S \times \begin{bmatrix} 1 & 0 & 0 & -m1[0] \\ 0 & 1 & 0 & -m1[1] \\ 0 & 0 & 1 & -m1[2] \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

- Use CPrimitive MultM(N) function to do the matrix multiplications. Note that MultM is a left matrix multiplication, i.e.  $M := N * M$ .

# Finding the Scaling Matrix S

- **ScaleDir** denotes the scaling direction.
- **ScaleDir** is a class member variable. You may use it directly.

- Compute the scaling value by:

$$svalue = \frac{(P_{curr} - m1).length()}{(P_{start} - m1).length()}$$

If **scaleDir** = 2:

$$\begin{bmatrix} Svalue & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

If **scaleDir** = 0:

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & Svalue & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

If **scaleDir** = 1:

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & Svalue & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

# Object Scaling – Find the start & current position on M

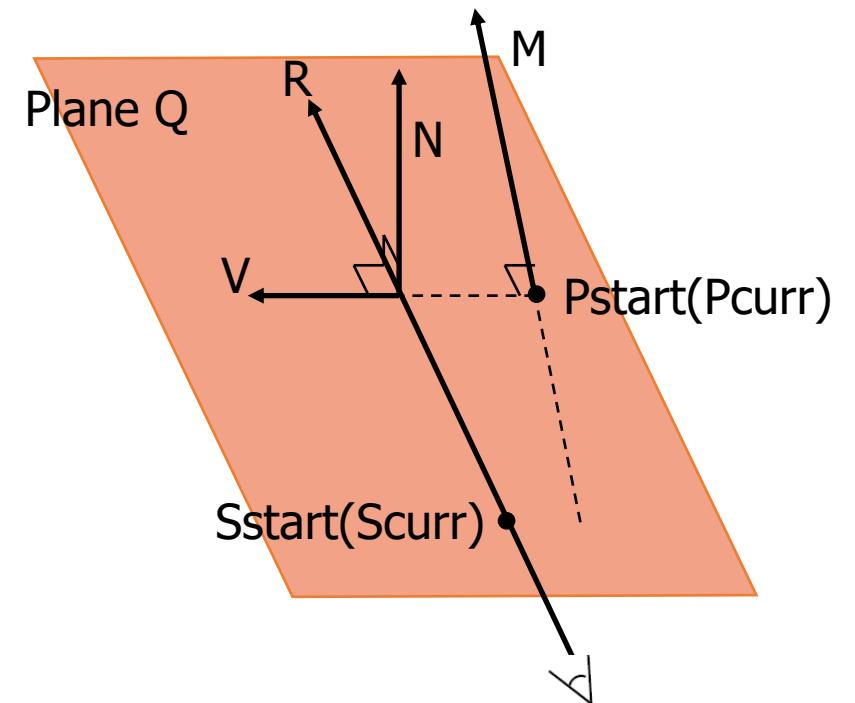
- Find  $P_{start}$  and  $P_{curr}$  corresponding to  $S_{start}$  and  $S_{curr}$  respectively.
- $P_{start}$  and  $P_{curr}$  are on the user selected line  $M$ .
- $P_{start}$  ( $P_{curr}$ ) is the closest point to ray  $R$  that goes through  $S_{start}$  ( $S_{curr}$ ).

$$V = \text{cross}(M, R)$$

$$N = \text{cross}(R, V)$$

Plane Q can be defined by N and viewpoint.

$P_{start}$  ( $P_{curr}$ ) is the intersection point of Plane Q and line M.



# Object Scaling - Procedure

Step 1: For the start mouse position  $S_{start}$ , find  $P_{start}$  on  $M$

Step 2: For the current mouse position  $S_{curr}$ , find  $P_{curr}$  on  $M$

Step 3: Determine the scaling value and create the scaling matrix

Step 4: Restore all the matrices of selected objects

Step 5: For each selected object:

(a) Translate the scaling fixed point to the origin.

(b) Do the scaling.

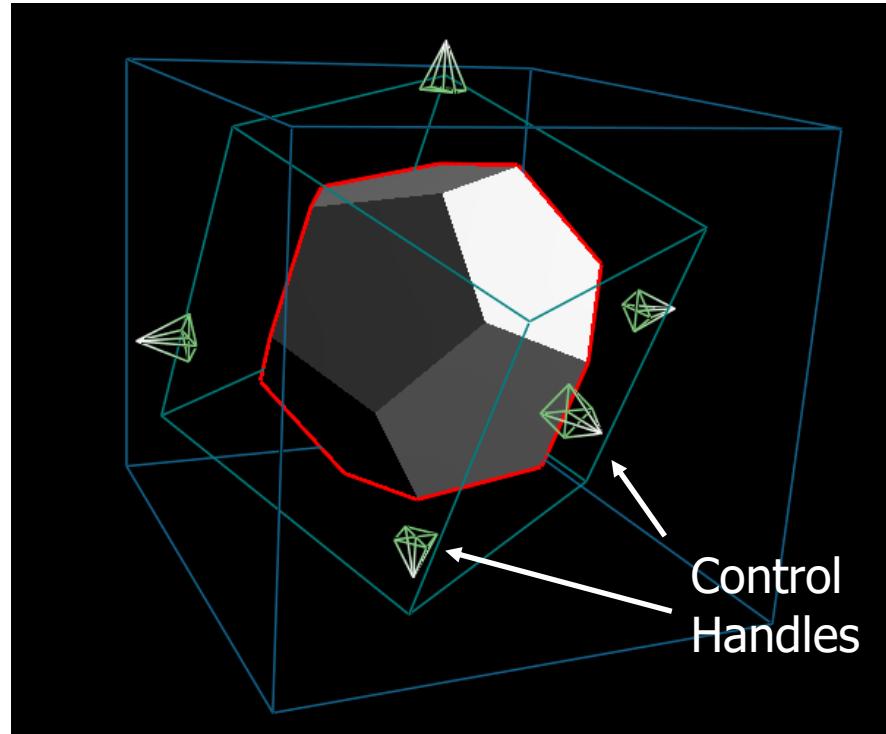
(c) Translate the scaling fixed point back.

# Outline

- 3D Modeling & 3D Rendering in OpenGL
- 3D Modeling & Interface Design – Programming Assignment
  - About the Template
  - About the Task
    - Mouse controlled model editing
    - 3D solid handles

# Control Handle

- Transformation modes are determined by clicking of different control handles



# Drawing control handles

- UserDrawControlHandle(...)
- Called in each frame to draw handles.

Add codes to function “UserDrawControlHandle” in file “rayView.cpp”

```
void CRayView::UserDrawControlHandle(V3 origin, V3 x-axis, V3 y-axis, V3 z-axis)
{ //The parameters form a local coordinate system.

    //Calculate Point Coordinates for the designed handle object.

    //Draw Designed 3D Handle,
}
```

# Provided Vector Operations

- Declaration: `V3 v0,v1,v2;`
- Normalize : `v0.normalize();`
- Length : `v0.length();`
- Dot product : `float x=v0.dot(v1);`
- Cross product : `v2=v0.cross(v1);`
- ... See more in “v3.h”

# Some Notes

- Matrix defined in OpenGL is like:

$$M = \begin{pmatrix} m_0, m_4, m_8, m_{12} \\ m_1, m_5, m_9, m_{13} \\ m_2, m_6, m_{10}, m_{14} \\ m_3, m_7, m_{11}, m_{15} \end{pmatrix}$$

- The origin of the screen coordinate you get is at the bottom left corner.

# Marking Scheme

- Model Transformation
  - Translation (axis aligned)
  - Rotation (Trackball style)
  - Scaling (axis aligned)
- Handle Design
- Programming Structure

# Hand-in

- Submit your rayView.cpp file through the Web-handin.
- Late Policy
  - 50% off for the delay of each day.
  - Re-submission after deadline is treated as late submission.
- NO PLAGIARISM!

# References

- OpenGL Official Site  
<http://www.opengl.org>
- GLU reference  
<http://pyopengl.sourceforge.net/documentation/manual/reference-GLU.html>
- Edward Angel, Interactive Computer Graphics, a top-down approach with OpenGL(5th edition), Addison Wesley, 2009
- Jackie Neider, Tom Davis, Mason Woo, OpenGL Programming Guide, Addison Wesley, 1996

Q & A!