

1. Qual é o conjunto solução da equação exponencial  $5^{X+2} = 125^X$ ?

$$5^{X+2} = 5^X 5^3$$

$$5^{X+2} = 5^{3X}$$

Bases iguais, logo:

$$x + 2 = 3x$$

$$2 = 3x - x$$

$$2x = 2$$

$$\mathbf{R: x = 1}$$

2. Determinar o conjunto solução da equação  $3^X 7^X = 441^{1/4}$ ?

$$3^X 7^X = (3^2 7^2)^{1/4}$$

$$21^X = (21^2)^{1/4}$$

$$21^X = 21^{2 \cdot 1/4}$$

$$21^X = 21^{1/2}$$

Bases iguais, logo:

$$\mathbf{x = 1/2}$$

3. Resolva:

$$\text{a) } \sum_{l=1}^{10000} \sum_{i=1}^{n-5} \sum_{j=i+1}^{n/2} \sum_{k=1}^n 1$$

$$\sum_{k=1}^n 1 = n - 1 + 1 = n$$

$$\sum_{j=i+1}^{n/2} n = n \sum_{j=i+1}^{n/2} 1 = n(n/2 - i - 1 + 1) = n(n/2 - i) = \frac{n^2}{2} - in$$

$$\sum_{i=1}^{n-5} \left( \frac{n^2}{2} - in \right) = \sum_{i=1}^{n-5} \left( \frac{n^2}{2} \right) - \sum_{i=1}^{n-5} (in) = \left( \frac{n^2}{2} \right) \sum_{i=1}^{n-5} 1 - n \sum_{i=1}^{n-5} (i)$$

$$\left( \frac{n^2}{2} \right) \sum_{i=1}^{n-5} 1 = \left( \frac{n^2}{2} \right) (n - 5 - 1 + 1) = \left( \frac{n^2}{2} \right) (n - 5) = \frac{n^3}{2} - \frac{5n^2}{2} = \frac{n^3 - 5n^2}{2}$$

$$n \sum_{i=1}^{n-5} (i) = \frac{(n-5)(n-4)}{2} = \frac{(n^2 - 4n - 5n + 20)}{2} = n \frac{(n^2 - 9n + 20)}{2}$$

$$\frac{n^3 - 5n^2}{2} - \frac{(n^3 - 9n^2 + 20n)}{2} = \frac{n^3 - 5n^2 - n^3 + 9n^2 - 20n}{2} = \frac{4n^2 - 20n}{2} = 2n^2 - 10n$$

$$\sum_{l=1}^{10000} 2n^2 - 10n = (2n^2 - 10n)(10000 - 1 + 1) = \mathbf{20000n^2 - 100000n}$$

$$\text{b) } \sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6} = \frac{n(2n^2+n+2n+1)}{6} = \frac{(2n^3+3n^2+n)}{6}$$

$$\text{c) } \sum_{i=1}^n ia^i = \frac{na^{n+2} - a^{n+1}(1+n) + a}{(1-a)^2}, a \neq 1$$