

Chapter 1

Appendix

he error term in the by [Gelman *et al.* \(2017\)](#) proposed definition of the R^2 is defined as $\text{Var}(\sum_{i=1}^n e_n^s)$. I think we could also use $\sum (y - \hat{y}^s)^2 / (n - 1)$ as an estimate for the error. For the maximum likelihood estimate $\text{Var}(y_i - \hat{y}_i) = \sum (y_i - \hat{y}_i)^2 / (n - 1)$. This is because the mean of the residuals is 0. When samples of the posterior parameters are used, the mean of the residuals is not exactly zero. $\text{Var}(y_i - \hat{y}_i) = \sum (y_i - \hat{y}_i)^2 / (n - 1)$ is than a little bit bigger than $\text{Var}(y_i - \hat{y}_i)$. In practice the values should only differ by a very small amount. We do not expect the errors to have a systematic bias. However, the residuals are just a sample of the error. The mean of the residuals must not be exactly 0 when the samples of the posteriors are used for the regression coefficients.

Bibliography

Gelman, A., Goodrich, B., Gabry, J., and Ali, I. (2017). R-squared for Bayesian regression models *. Technical report. [1](#)