2021 2 학기
자료구조개론
기말고사
문제지

1. You will get +1 point for each correct answer.

2. Assume that each program includes proper header files such as stdio.h and math.h.

3. All the variables and arrays are properly initialized by 0 at the beginning.

Q1. Read the following program, and answer the questions.

```
void Sort(int *arr, int len)
{
    int tmp = 0;
    for(int i = len - 1; i >= 0; i--){
        for(int j = 0; j < i; j++){
            if(Ⓐ){
                tmp = arr[j];
                Ⓑ
                arr[j + 1] = tmp;
            }
        }
    }
}
```

```
int main(void){
    int n = 10;

    int a[10] = {9, 11, 4, 2, 3, 1, 5 ,7 ,10, 6};

    // Sort ascending order
    Sort(a, n);

    for(int i = 0; i < n; i++){
        printf("%d₩n", a[i]);
    }
}
```

1. What is time complexity of the sort program? (n is the number of items in the list)
   ① Θ(1) ② Θ(n) ③ Θ($\log_2 n$)
   ④ Θ($n\log_2 n$) ⑤ Θ(n^2)

2. What is the name of this sort algorithm?
   ① Selection sort
   ② Insertion sort
   ③ Bubble sort
   ④ Quick sort
   ⑤ Merge sort

3. What is the value of a[4] after sort?
   ① 1 ② 3 ③ 5 ④ 7 ⑤ 9

4. What is the correct statement at Ⓐ?
   ① a[j+1] < a[j];
   ② a[j+1] > a[j];
   ③ a[j+1] == a[j];
   ④ a[j-1] > a[j];
   ⑤ a[j-1] < a[j];

5. What is the correct statement at Ⓑ?
   ① a[j] = a[j+1];
   ② a[j] = a[j-1];
   ③ a[j+1] = a[j];
   ④ a[j-1] = a[j];
   ⑤ a[j+1] = a[j-1];

Q2. Given static hash with open addressing, bucket size 17 and slot size 1, answer the questions

Index	Key
0	
1	Ⓐ
2	
3	
4	
5	Ⓑ
6	
7	
8	Ⓒ
9	
10	
11	
12	Ⓓ
13	
14	
15	
16	

Hash descriptions

- Static hashing
- Bucket size 17
- Slot size 1
- Open addressing
- Linear probe
- Empty slots have NULL

Hash functions

H1(key)

⇨ **key % 17**

H2(key)

⇨ **(key * key) % 17**

Insert following keys in order

17
24
29
0
3
4
87
54
15
35
12
48
65

6. After insertion, what is the value at Ⓐ when hash function is H1

① NULL ② 17 ③ 0 ④ 65 ⑤ 48

7. After insertion, what is the value at Ⓓ when hash function is H1

① NULL ② 4 ③ 48 ④ 35 ⑤ 29

8. After insertion, what is the value at Ⓑ when hash function is H1

① NULL ② 0 ③ 15 ④ 54 ⑤ 87

9. After insertion, what is the value at Ⓑ when hash function is H2

① NULL ② 0 ③ 17 ④ 15 ⑤ 48

10. After insertion, what is the value at Ⓓ when hash function is H2

① NULL ② 48 ③ 65 ④ 35 ⑤ 87

11. After insertion, what is the value at Ⓒ when hash function is H2

① NULL ② 24 ③ 29 ④ 17 ⑤ 54

Q3. Read the following program, and answer the questions.

```
#define MAX_SIZE 10

void fct1(int list1[], int list2[], int i, int m, int n)
{
	int j,k,t;
	j = m + 1;
	k = i;
	while(i <= m && j <= n) {
		if (list1[i] <= list1[j]){
			list2[k++] = list1[i++];
		}
		else{
			list2[k++] = list1[j++];
		}
	}

	Ⓐ

	if (i > m){
		for(t = j; t <= n; t++){
			list2[t] = list1[t];
		}
	}
	else{
		for(t = i; t <= m; t++){
			list2[k+t-i] = list1[t];
		}
	}
}

void fct2(int list1[], int list2[], int n, int s)
{
	int i ;
	int j ;

	for (i = 0; i <= n - 2 * s + 1; i += 2 * s){
		fct1(list1, list2, i, i + s - 1, i + 2 * s - 1);
	}

	Ⓑ

	if((i + s - 1) < n){
		fct1(list1, list2, i, i + s - 1, n);
	}
	else{
		for(j=i; j <= n; j++){
			list2[j] = list1[j];
		}
	}
}
```

```
void Sort(int a[], int n)
{
	int s = 1;
	int extra[MAX_SIZE];

	while (s<n) {
		fct2(a, extra, n, s);
		s *= 2;

		Ⓒ

		fct2(extra, a, n, s);
		s *= 2;

		Ⓓ

	}
}

int main(void)
{
	int arr[MAX_SIZE] = {13, 26, 41, 72, 23, 1, 0, 65, 32, 55};

	Sort(arr, MAX_SIZE - 1);
}
```

12. What is the name of this sorting algorithm?

① Merge Sort ④ LSD Radix Sort

② Heap Sort ⑤ List Sort

③ MSD Radix Sort

13. What is the time complexity of this algorithm?

① $\Theta(1)$ ② $\Theta(n)$ ③ $\Theta(\log_2 n)$

④ $\Theta(n\log_2 n)$ ⑤ $\Theta(n^2)$

14. How many times fct1 is called?

① 8 ② 9 ③ 10 ④ 11 ⑤ 12

15. How many times fct2 is called?

① 3 ② 4 ③ 5 ④ 6 ⑤ 7

16. When fct1 is called twice, what is the value of list1[4] at Ⓐ?

① 26 ② 23 ③ 1 ④ 0 ⑤ 55

17. When fct1 is called 5 times, what is the value of list2 [8] at Ⓐ?

① 32 ② 72 ③ 26 ④ 13 ⑤ 65

18. When fct2 is called for the first time, what is the value of list1[3] at Ⓑ?

① 26 ② 32 ③ 72 ④ 41 ⑤ 55

19. When fct2 is called 3 times, what is the value of list1[5] at Ⓑ?

① 41 ② 0 ③ 1 ④ 13 ⑤ 23

20. When s is 2, what is the value of a[3] at Ⓒ?

① 26 ② 32 ③ 41 ④ 72 ⑤ 13

21. When s is 4, what is the value of a[5] at Ⓓ?

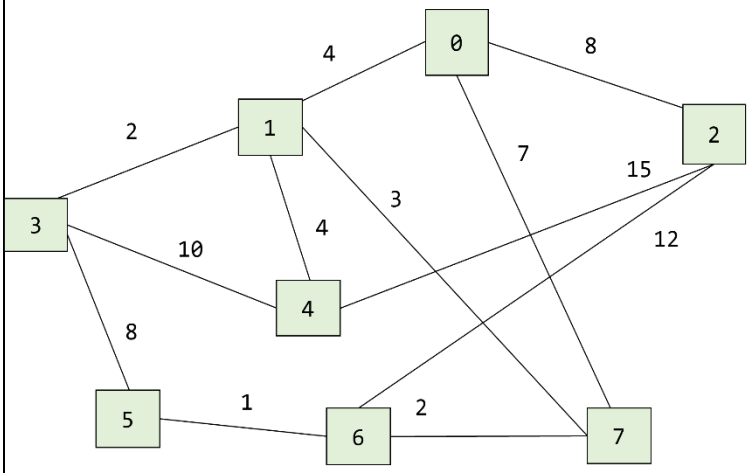
① 0 ② 23 ③ 1 ④ 55 ⑤ 65

Q4. Read the following graph program, and answer the questions. **Assume "func" is called with <u>v = 0</u>**.

```
#define VERY_LARGE_NUMBER 1000000
#define MAX_VERTICES 8

typedef struct __edge{
    int x;
    int y;
}edge;

typedef struct __treeData{
    edge T[MAX_VERTICES * MAX_VERTICES];
    int top;
}treeData;

void init_treeData(treeData *tree)
{
    edge tmp = {-1, -1};
    for(int i = 0; i < MAX_VERTICES * MAX_VERTICES; i++)
        tree->T[i] = tmp;
    tree->top = 0;
}
void fct(int graph[MAX_VERTICES][MAX_VERTICES]);

void push_to_T(treeData *tree, int x, int y)
{
    edge tmp;
    for(int i = 0; i < tree->top; i++){
        tmp = tree->T[i];
        if((tmp.x == x && tmp.y == y) || (tmp.x == y && tmp.y == x)){
            return;
        }
    }
    tree->T[tree->top].x = x;
    tree->T[tree->top].y = y;

    tree->top++;
}
```

```
void fct(int graph[MAX_VERTICES][MAX_VERTICES])
{
    int no_edge = 0;

    treeData tree;
    int TV[MAX_VERTICES] = {0};

    init_treeData(&tree);

    TV[0] = true;

    while(no_edge < MAX_VERTICES - 1) {
        int min = VERY_LARGE_NUMBER;
        edge tmp = {0, 0};

        for (int i = 0; i < MAX_VERTICES; i++) {
            if (TV[i]) {
                for (int j = 0; j < MAX_VERTICES; j++) {
                    if (!TV[j] && graph[i][j] != -1) {
                        if (min > graph[i][j]) {
                            min = graph[i][j];

                            push_to_T(&tree, i, j);

                            tmp.x = i;
                            tmp.y = j;

                            Ⓐ
                        }
                    }
                }
            }
        }
        TV[tmp.y] = true;
        no_edge++;
    }
}
```

```
int main(void)
{
/* -1 implies there is no connection between the vertices. */
    int graph[MAX_VERTICES][MAX_VERTICES] = {
        { 0,  4,  8, -1, -1, -1, -1,  7},
        { 4,  0, -1,  2,  4, -1, -1,  3},
        { 8, -1,  0, -1, 15, -1, 12, -1},
        {-1,  2, -1,  0, 10,  8, -1, -1},
        {-1,  4, 15, 10,  0, -1, -1, -1},
        {-1, -1, -1,  8, -1,  0,  1, -1},
        {-1, -1, 12, -1, -1,  1,  0,  2},
        { 7,  3, -1, -1, -1, -1,  2,  0}};

    fct(graph);

    return 0;
}
```



22. What is the name of this graph algorithm?

① Kruskal's Algorithm

② Prim's Algorithm

③ Dijkstra's Algorithm

④ Bellman-Ford Algorithm

⑤ Floyd-Warshall Algorithm

23. Find the edge that is in the MST made by the above code.

① (4, 2) ② (1, 4) ③ (5, 3) ④ (3, 4) ⑤ (0, 7)

24. What is tree.top after the fct ended?

① 6 ② 7 ③ 8 ④ 9 ⑤ 10

25. Find the edge that cannot be in the tree.T when tree.top is 3 at Ⓐ.

① (0, 1) ② (0, 7) ③ (1, 4) ④ (1, 7) ⑤ (6, 5)

26. Find the edge that cannot be in the tree.T when tree.top is 6 at Ⓐ.

① (0, 1) ② (0, 2) ③ (1, 7) ④ (6, 5) ⑤ (3, 4)

27. Suppose that node 1 and node 7 are not connected.
Find the edge that is in the MST made by the above code and given assumption.

① (0, 1) ② (2, 6) ③ (5, 3) ④ (3, 4) ⑤ (4, 2)

28. Suppose that node 1 and node 7 are not connected.
What is tree.top after the fct ended?

① 6 ② 7 ③ 8 ④ 9 ⑤ 10

29. Suppose that node 1 and node 7 are not connected.

Find the edge that cannot be in the tree.T when tree.top is 3 at Ⓐ.

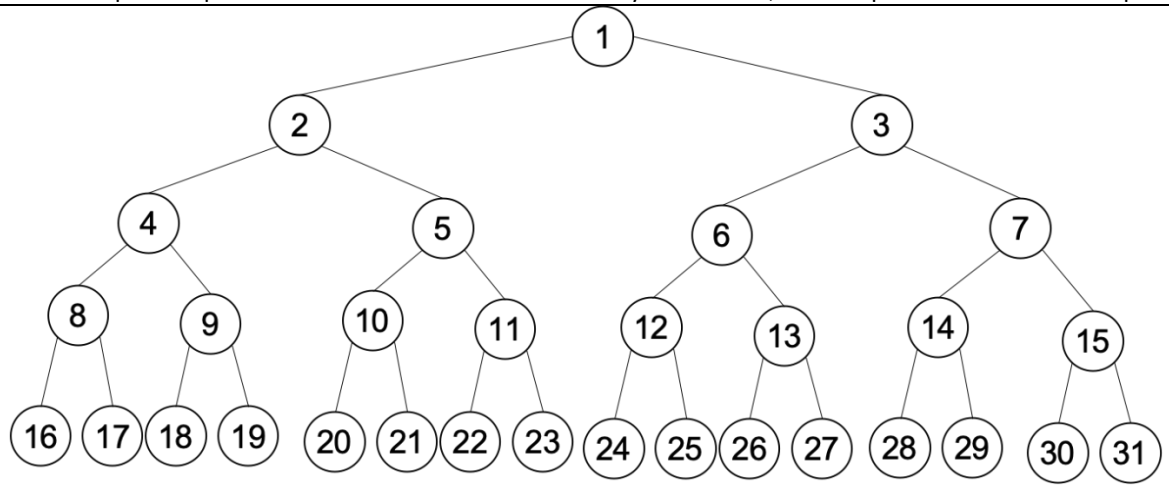
① (0, 1) ② (0, 2) ③ (1, 3) ④ (0, 7) ⑤ (2, 4)

30. Suppose that node 1 and node 7 are not connected.

Find the edge that cannot be in the tree.T when tree.top is 6 at Ⓐ.

① (0, 1) ② (7, 6) ③ (3, 4) ④ (6, 5) ⑤ (1, 4)

Q5. Graph below represent position of the Nodes. Make each Binary search tree, Min heap tree and answer the questions



Binary search tree operations	Max heap tree operations (Heapify after every insert)
Insert 17 Insert 5 Insert 24 Insert 15 Insert 30 Insert 34 Insert 2 Insert 1 Insert 19 Insert 22 Insert 28 Insert 37 Insert 11 Insert 13 Insert 4	Insert 17 Insert 5 Insert 24 Insert 15 Insert 30 Insert 34 Insert 2 Insert 1 Insert 19 Insert 22 Insert 28 Insert 37

31. [BINARY_TREE]
What is the value of Node 7 after all operations
① NULL ② 34 ③ 13 ④ 30 ⑤ 22

32. [BINARY_TREE]
What is the value of Node 15 after all operations
① NULL ② 34 ③ 13 ④ 30 ⑤ 22

33. [BINARY_TREE]
What is the value of Node 19 after all operations
① NULL ② 34 ③ 13 ④ 30 ⑤ 22

34. [MAX_HEAP]
What is the value of Node 1 after all operations
① NULL ② 28 ③ 34 ④ 30 ⑤ 37

35. [MAX_HEAP]
What is the value of Node 5 after all operations
① NULL ② 24 ③ 19 ④ 30 ⑤ 22

36. [MAX_HEAP]
What is the value of Node 9 after all operations
① NULL ② 5 ③ 15 ④ 22 ⑤ 17