RGESolver

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Chapter 1

Class Index

1.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

Chapter 2

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2.1 File List

Here is a list of all files with brief descriptions:

Chapter 3

Class Documentation

3.1 RGESolver Class Reference

A class that performs renormalization group evolution in the context of the SMEFT.

`#include <RGESolver.h>`

Public Member Functions

- RGESolver ()
  The default constructor.
- ~RGESolver ()
  The default destructor.
- double epsrel ()
  Getter for the relative error used in the numerical integration.
- double epsabs ()
  Getter for the absolute error used in the numerical integration.
- double step ()
  Getter for the step used in the numerical integration.
- void Set_epsrel (double epsrel)
  Setter for the relative error used in the numerical integration.
- void Set_epsabs (double epsabs)
  Setter for the absolute error used in the numerical integration.
- void Set_step (double step)
  Setter for the step used in the numerical integration.
- void SetCKMTheta12 (double val)
  Setter function for the CKM matrix angle θ_{12}. The assignation is completed only if $\theta_{12} \in [0, \frac{\pi}{2}]$.
- void SetCKMTheta13 (double val)
  Setter function for the CKM matrix angle θ_{13}. The assignation is completed only if $\theta_{13} \in [0, \frac{\pi}{2}]$.
- void SetCKMTheta23 (double val)
  Setter function for the CKM matrix angle θ_{23}. The assignation is completed only if $\theta_{23} \in [0, \frac{\pi}{2}]$.
- void SetCKMPhase (double val)
  Setter function for the CKM matrix phase δ. The assignation is completed only if $\delta \in (-\pi, \pi]$.
- double GetCKMTheta12 ()
  Getter function for the CKM matrix angle θ_{12}.

- double GetCKMTheta13 ()

  Getter function for the CKM matrix angle θ_{13}.
- double GetCKMTheta23 ()

  Getter function for the CKM matrix angle θ_{23}.
- double GetCKMPhase ()

  Getter function for the CKM matrix delta δ.
- void SetCoefficient (std::string name, double val)

  Setter function for scalar/0F parameters (no flavour indices).
- void SetCoefficient (std::string name, double val, int i, int j)

  Setter function for 2F parameters (2 flavour indices).
- void SetCoefficient (std::string name, double val, int i, int j, int k, int l)

  Setter function for 4F parameters (4 flavour indices).
- double GetCoefficient (std::string name)

  Getter function for scalar/0F parameters (no flavour indices).
- double GetCoefficient (std::string name, int i, int j)

  Getter function for 2F parameters (2 flavour indices).
- double GetCoefficient (std::string name, int i, int j, int k, int l)

  Getter function for 4F parameters (4 flavour indices).
- void Evolve (std::string method, double muI, double muF)

  Command to perform the RGE evolution.
- void GenerateSMInitialConditions (double mu, std::string basis, std::string method, bool inputCKM=true)

  Generates the initial conditions for Standard Model's parameters (gauge couplings, Yukawa coupling, quartic coupling and Higgs' boson mass).
- void EvolveSMOnly (std::string method, double muI, double muF)

  Same as Evolve(std::string method, double muI, double muF), but only for the SM parameters. The user should use this method instead of `Evolve` when interested in pure SM running.
- void SetSMInputScale (double mu)

  Setter method for the scale at which the method `GenerateSMInitialConditions` takes the input values for SM parameters.
- double GetSMInputScale ()

  Getter method for the scale at which the method `GenerateSMInitialConditions` takes the input values for SM parameters.
- void SaveOutputFile (std::string filename, std::string format)

  Saves the current values of parameters in a file.
- void Reset ()

  Resets all the SMEFT coefficients to 0 and the SM parameters to their default value.

Private Member Functions

- void GoToBasisSMOnly (std::string basis)
- void ExtractParametersFromCKM ()
- void UpdateCKM ()
- void InitSMOnly ()
- void UpdateSMOnly ()
- void FromMassesToYukawas (std::string basis)
- void SetSMDefaultInput ()
- void Init ()

  Inserts the initial values of the parameters in the array `x`.
- void Update ()

  Saves the evolved values of the coefficients from `x`.

Static Private Member Functions

- static int funcSMOnly (double logmu, const double y[ ], double f[ ], void ∗params)
- static int func (double logmu, const double y[ ], double f[ ], void ∗params)

  Computes the beta functions for the SMEFT.

Output file

Stuff for output on file

- static void Print (double ∗c, std::string name, std::string sym, std::string format, std::ofstream &f)

  Prints on file the coefficient `c`.

Setters and Getters

Setter and getter function for each symmetry class.

- static void Yukawa_set (double y[3][3], int i, int j, double val)
- static double Yukawa (double y[3][3], int i, int j)
- static void WC1_set (double ∗c, int i, int j, double val)
- static double WC1 (double ∗c, int i, int j)
- static double WC2R (double ∗c, int i, int j)
- static void WC2R_set (double ∗c, int i, int j, double val)
- static double WC2I (double ∗c, int i, int j)
- static void WC2I_set (double ∗c, int i, int j, double val)
- static double WC3 (double ∗c, int i, int j)
- static void WC3_set (double ∗c, int i, int j, double val)
- static void WC5_set (double ∗c, int i, int j, int k, int l, double val)
- static double WC5 (double ∗c, int i, int j, int k, int l)
- static double WC6R (double ∗c, int i, int j, int k, int l)
- static void WC6R_set (double ∗c, int i, int j, int k, int l, double val)
- static double WC6I (double ∗c, int i, int j, int k, int l)
- static void WC6I_set (double ∗c, int i, int j, int k, int l, double val)
- static void WC7R_set (double ∗c, int i, int j, int k, int l, double val)
- static double WC7R (double ∗c, int i, int j, int k, int l)
- static double WC7I (double ∗c, int i, int j, int k, int l)
- static void WC7I_set (double ∗c, int i, int j, int k, int l, double val)
- static double WC8R (double ∗c, int i, int j, int k, int l)
- static void WC8R_set (double ∗c, int i, int j, int k, int l, double val)
- static double WC8I (double ∗c, int i, int j, int k, int l)
- static void WC8I_set (double ∗c, int i, int j, int k, int l, double val)

Private Attributes

- gslpp::matrix< gslpp::complex > CKM = gslpp::matrix<gslpp::complex>(3, 3, 0.)

  The CKM matrix.
- double InputScale_SM

  the scale at which the method `GenerateSMInitialConditions` *takes the input values for SM parameters.*
- double CKM_theta12

  θ_{12} *of the CKM matrix (in radians). The default value is ???*
- double CKM_theta13
- double CKM_theta23
- double CKM_delta
- double c12

  $\cos\theta_{12}$
- double s12

  $\sin\theta_{12}$
- double c13

$\cos\theta_{13}$

- double s13

  $\sin\theta_{13}$
- double c23

  $\cos\theta_{23}$
- double s23

  $\sin\theta_{23}$
- double mu

  m_u , *the mass of up quark in GeV (default value ?????).*
- double mc
- double mt
- double md
- double ms
- double mb
- double mel
- double mmu
- double mtau

GSL Objects

- double epsrel_ = 0.0000000000000001

  Relative error used in the integrator with its default value.
- double epsabs_ = 0.0001

  Absolute error used in the integrator with its default value.
- double step_

  Last step used in the integrator.
- gsl_odeiv2_system sys_ = {func, NULL, 3}
- gsl_odeiv2_step * s_
- gsl_odeiv2_control * con_
- gsl_odeiv2_evolve * evo_ = gsl_odeiv2_evolve_alloc(2558)
- double x [2558]

  1D array for the integration

Standard Model parameters

- double g1

  g_1
- double g2

  g_2
- double g3

  g_3
- double mh2

  m_h^2 *(Higgs boson mass squared)*
- double lambda

  λ *(Higgs quartic coupling)*
- double yuR [3][3]
- double yuI [3][3]
- double ydR [3][3]
- double ydI [3][3]
- double yeR [3][3]
- double yeI [3][3]

SMEFT dimension-six operators

By default, all SMEFT dimension-six operators' coefficients are set to 0. See https://arxiv.org/abs/1308.2627 tab. 1 for the full list of operators. Each member has a class from 1 to 8 depending on its field contents, as well as a flavour symmetry classification (WC1, WC2R, WC2I...).

- double cG = 0.
  C_G *(class 1, scalar)*
- double cGT = 0.
  $C_{\tilde{G}}$ *(class 1, scalar)*
- double cW = 0.
  C_W *(class 1, scalar)*
- double cWT = 0.
  $C_{\tilde{W}}$ *(class 1, scalar)*
- double cH = 0.
  C_H *(class 2, scalar)*
- double cHBOX = 0.
  $C_{H\Box}$ *(class 3, scalar)*
- double cHD = 0.
  C_{HD} *(class 3, scalar)*
- double cHG = 0.
  C_{HG} *(class 4, scalar)*
- double cHGT = 0.
  $C_{H\tilde{G}}$ *(class 4, scalar)*
- double cHW = 0.
  C_{HW} *(class 4, scalar)*
- double cHWT = 0.
  $C_{H\tilde{W}}$ *(class 4, scalar)*
- double cHB = 0.
  C_{HB} *(class 4, scalar)*
- double cHBT = 0.
  $C_{H\tilde{B}}$ *(class 4, scalar)*
- double cHWB = 0.
  C_{HWB} *(class 4, scalar)*
- double cHWBT = 0.
  $C_{H\tilde{W}B}$ *(class 4, scalar)*
- double ceHR [3 ∗3] = {0.}
  $\Re\left[C_{eH}\right]$ *(class 5, WC1)*
- double ceHI [3 ∗3] = {0.}
  $\Im\left[C_{eH}\right]$ *(class 5, WC1)*
- double cuHR [3 ∗3] = {0.}
  $\Re\left[C_{uH}\right]$ *(class 5, WC1)*
- double cuHI [3 ∗3] = {0.}
  $\Im\left[C_{uH}\right]$ *(class 5, WC1)*
- double cdHR [3 ∗3] = {0.}
  $\Re\left[C_{dH}\right]$ *(class 5, WC1)*
- double cdHI [3 ∗3] = {0.}
  $\Im\left[C_{dH}\right]$ *(class 5, WC1)*
- double ceWR [3 ∗3] = {0.}
  $\Re\left[C_{eW}\right]$ *(class 6, WC1)*
- double ceWI [3 ∗3] = {0.}
  $\Im\left[C_{eW}\right]$ *(class 6, WC1)*
- double ceBR [3 ∗3] = {0.}
  $\Re\left[C_{eB}\right]$ *(class 6, WC1)*
- double ceBI [3 ∗3] = {0.}
  $\Im\left[C_{eB}\right]$ *(class 6, WC1)*
- double cuGR [3 ∗3] = {0.}
  $\Re\left[C_{uG}\right]$ *(class 6, WC1)*
- double cuGI [3 ∗3] = {0.}

$\Im[C_{uG}]$ *(class 6, WC1)*
- double cuWR [3 ∗3] = {0.}

$\Re[C_{uW}]$ *(class 6, WC1)*
- double cuWI [3 ∗3] = {0.}

$\Im[C_{uW}]$ *(class 6, WC1)*
- double cuBR [3 ∗3] = {0.}

$\Re[C_{uB}]$ *(class 6, WC1)*
- double cuBI [3 ∗3] = {0.}

$\Im[C_{uB}]$ *(class 6, WC1)*
- double cdGR [3 ∗3] = {0.}

$\Re[C_{dG}]$ *(class 6, WC1)*
- double cdGI [3 ∗3] = {0.}

$\Im[C_{dG}]$ *(class 6, WC1)*
- double cdWR [3 ∗3] = {0.}

$\Re[C_{dW}]$ *(class 6, WC1)*
- double cdWI [3 ∗3] = {0.}

$\Im[C_{dW}]$ *(class 6, WC1)*
- double cdBR [3 ∗3] = {0.}

$\Re[C_{dB}]$ *(class 6, WC1)*
- double cdBI [3 ∗3]

$\Im[C_{dW}]$ *(class 6, WC1)*
- double cHl1R [3 ∗3] = {0.}

$\Re[C_{Hl1}]$ *(class 7, WC2R)*
- double cHl1I [3 ∗3] = {0.}

$\Im[C_{Hl1}]$ *(class 7, WC2I)*
- double cHl3R [3 ∗3] = {0.}

$\Re[C_{Hl3}]$ *(class 7, WC2R)*
- double cHl3I [3 ∗3] = {0.}

$\Im[C_{Hl3}]$ *(class 7, WC2I)*
- double cHeR [3 ∗3] = {0.}

$\Re[C_{He}]$ *(class 7, WC2R)*
- double cHeI [3 ∗3] = {0.}

$\Im[C_{He}]$ *(class 7, WC2I)*
- double cHq1R [3 ∗3] = {0.}

$\Re[C_{Hq1}]$ *(class 7, WC2R)*
- double cHq1I [3 ∗3] = {0.}

$\Im[C_{Hq1}]$ *(class 7, WC2I)*
- double cHq3R [3 ∗3] = {0.}

$\Re[C_{Hq3}]$ *(class 7, WC2R)*
- double cHq3I [3 ∗3] = {0.}

$\Im[C_{Hq3}]$ *(class 7, WC2I)*
- double cHuR [3 ∗3] = {0.}

$\Re[C_{Hu}]$ *(class 7, WC2R)*
- double cHuI [3 ∗3] = {0.}

$\Im[C_{Hu}]$ *(class 7, WC2I)*
- double cHdR [3 ∗3] = {0.}

$\Re[C_{Hd}]$ *(class 7, WC2R)*
- double cHdI [3 ∗3] = {0.}

$\Im[C_{Hd}]$ *(class 7, WC2I)*
- double cHudR [3 ∗3] = {0.}

$\Re[C_{Hud}]$ *(class 7, WC1)*
- double cHudI [3 ∗3] = {0.}

$\Im[C_{Hud}]$ *(class 7, WC1)*
- double cllR [3 ∗3 ∗3 ∗3] = {0.}

$\Re[C_{ll}]$ *(class 8-[LL][LL], WC6R)*
- double cllI [3 ∗3 ∗3 ∗3] = {0.}

$\Im[C_{ll}]$ *(class 8-[LL][LL], WC6I)*
- double cqq1R [3 ∗3 ∗3 ∗3] = {0.}

$\Re[C_{qq1}]$ *(class 8-[LL][LL], WC6R)*

- double cqq1I [3 ∗3 ∗3 ∗3] = {0.}
  $\Im[C_{qq1}]$ *(class 8-[LL][LL], WC6I)*
- double cqq3R [3 ∗3 ∗3 ∗3] = {0.}
  $\Re[C_{qq3}]$ *(class 8-[LL][LL], WC6R)*
- double cqq3I [3 ∗3 ∗3 ∗3] = {0.}
  $\Im[C_{qq3}]$ *(class 8-[LL][LL], WC6I)*
- double clq1R [3 ∗3 ∗3 ∗3] = {0.}
  $\Re[C_{lq1}]$ *(class 8-[LL][LL], WC7R)*
- double clq1I [3 ∗3 ∗3 ∗3] = {0.}
  $\Im[C_{lq1}]$ *(class 8-[LL][LL], WC7I)*
- double clq3R [3 ∗3 ∗3 ∗3] = {0.}
  $\Re[C_{lq3}]$ *(class 8-[LL][LL], WC7R)*
- double clq3I [3 ∗3 ∗3 ∗3] = {0.}
  $\Im[C_{lq3}]$ *(class 8-[LL][LL], WC7I)*
- double cuuR [3 ∗3 ∗3 ∗3] = {0.}
  $\Re[C_{uu}]$ *(class 8-[RR][RR], WC6R)*
- double cuuI [3 ∗3 ∗3 ∗3] = {0.}
  $\Im[C_{uu}]$ *(class 8-[RR][RR], WC6I)*
- double cddR [3 ∗3 ∗3 ∗3] = {0.}
  $\Re[C_{dd}]$ *(class 8-[RR][RR], WC6R)*
- double cddI [3 ∗3 ∗3 ∗3] = {0.}
  $\Im[C_{dd}]$ *(class 8-[RR][RR], WC6I)*
- double ceeR [3 ∗3 ∗3 ∗3] = {0.}
  $\Re[C_{ee}]$ *(class 8-[RR][RR], WC8R)*
- double ceeI [3 ∗3 ∗3 ∗3] = {0.}
  $\Im[C_{ee}]$ *(class 8-[RR][RR], WC8I)*
- double ceuR [3 ∗3 ∗3 ∗3] = {0.}
  $\Re[C_{eu}]$ *(class 8-[RR][RR], WC7R)*
- double ceuI [3 ∗3 ∗3 ∗3] = {0.}
  $\Im[C_{eu}]$ *(class 8-[RR][RR], WC7I)*
- double cedR [3 ∗3 ∗3 ∗3] = {0.}
  $\Re[C_{ed}]$ *(class 8-[RR][RR], WC7R)*
- double cedI [3 ∗3 ∗3 ∗3] = {0.}
  $\Im[C_{ed}]$ *(class 8-[RR][RR], WC7I)*
- double cud1R [3 ∗3 ∗3 ∗3] = {0.}
  $\Re[C_{ud1}]$ *(class 8-[RR][RR], WC7R)*
- double cud1I [3 ∗3 ∗3 ∗3] = {0.}
  $\Im[C_{ud1}]$ *(class 8-[RR][RR], WC7I)*
- double cud8R [3 ∗3 ∗3 ∗3] = {0.}
  $\Re[C_{ud8}]$ *(class 8-[RR][RR], WC7R)*
- double cud8I [3 ∗3 ∗3 ∗3] = {0.}
  $\Im[C_{ud1}]$ *(class 8-[RR][RR], WC7I)*
- double cleR [3 ∗3 ∗3 ∗3] = {0.}
  $\Re[C_{le}]$ *(class 8-[LL][RR], WC7R)*
- double cleI [3 ∗3 ∗3 ∗3] = {0.}
  $\Im[C_{le}]$ *(class 8-[LL][RR], WC7I)*
- double cluR [3 ∗3 ∗3 ∗3] = {0.}
  $\Re[C_{lu}]$ *(class 8-[LL][RR], WC7R)*
- double cluI [3 ∗3 ∗3 ∗3] = {0.}
  $\Im[C_{lu}]$ *(class 8-[LL][RR], WC7I)*
- double cldR [3 ∗3 ∗3 ∗3] = {0.}
  $\Re[C_{ld}]$ *(class 8-[LL][RR], WC7R)*
- double cldI [3 ∗3 ∗3 ∗3] = {0.}
  $\Im[C_{ld}]$ *(class 8-[LL][RR], WC7I)*
- double cqeR [3 ∗3 ∗3 ∗3] = {0.}
  $\Re[C_{qe}]$ *(class 8-[LL][RR], WC7R)*
- double cqeI [3 ∗3 ∗3 ∗3] = {0.}
  $\Im[C_{qe}]$ *(class 8-[LL][RR], WC7I)*
- double cqu1R [3 ∗3 ∗3 ∗3] = {0.}

$\Re\,[C_{qu1}]$ *(class 8-[LL][RR], WC7R)*
- double cqu1I [3 ∗3 ∗3 ∗3] = {0.}

  $\Im\,[C_{qu1}]$ *(class 8-[LL][RR], WC7I)*
- double cqu8R [3 ∗3 ∗3 ∗3] = {0.}

  $\Re\,[C_{qu8}]$ *(class 8-[LL][RR], WC7R)*
- double cqu8I [3 ∗3 ∗3 ∗3] = {0.}

  $\Im\,[C_{qu8}]$ *(class 8-[LL][RR], WC7I)*
- double cqd1R [3 ∗3 ∗3 ∗3] = {0.}

  $\Re\,[C_{qd1}]$ *(class 8-[LL][RR], WC7R)*
- double cqd1I [3 ∗3 ∗3 ∗3] = {0.}

  $\Im\,[C_{qd1}]$ *(class 8-[LL][RR], WC7I)*
- double cqd8R [3 ∗3 ∗3 ∗3] = {0.}

  $\Re\,[C_{qd8}]$ *(class 8-[LL][RR], WC7R)*
- double cqd8I [3 ∗3 ∗3 ∗3] = {0.}

  $\Im\,[C_{qd8}]$ *(class 8-[LL][RR], WC7I)*
- double cledqR [3 ∗3 ∗3 ∗3] = {0.}

  $\Re\,[C_{ledq}]$ *(class 8-[LR][RL], WC5)*
- double cledqI [3 ∗3 ∗3 ∗3] = {0.}

  $\Im\,[C_{ledq}]$ *(class 8-[LR][RL], WC5)*
- double clequ1R [3 ∗3 ∗3 ∗3] = {0.}

  $\Re\,[C_{lequ1}]$ *(class 8-[LR][LR], WC5)*
- double clequ1I [3 ∗3 ∗3 ∗3] = {0.}

  $\Im\,[C_{lequ1}]$ *(class 8-[LR][LR], WC5)*
- double clequ3R [3 ∗3 ∗3 ∗3] = {0.}

  $\Re\,[C_{lequ3}]$ *(class 8-[LR][LR], WC5)*
- double clequ3I [3 ∗3 ∗3 ∗3] = {0.}

  $\Im\,[C_{lequ3}]$ *(class 8-[LR][LR], WC5)*
- double cquqd1R [3 ∗3 ∗3 ∗3] = {0.}

  $\Re\,[C_{quqd1}]$ *(class 8-[LR][LR], WC5)*
- double cquqd1I [3 ∗3 ∗3 ∗3] = {0.}

  $\Im\,[C_{quqd1}]$ *(class 8-[LR][LR], WC5)*
- double cquqd8R [3 ∗3 ∗3 ∗3] = {0.}

  $\Re\,[C_{quqd8}]$ *(class 8-[LR][LR], WC5)*
- double cquqd8I [3 ∗3 ∗3 ∗3] = {0.}

  $\Im\,[C_{quqd8}]$ *(class 8-[LR][LR], WC5)*

Maps for I/O

Maps that connects the coefficients with the appropriate getter/setter functions (based on their symmetry properties)

- std::unordered_map< std::string, double ∗ > Operators0F
- std::unordered_map< std::string, boost::function< void(int, int, double) > > Setter2F
- std::unordered_map< std::string, boost::function< double(int, int) > > Getter2F
- std::unordered_map< std::string, boost::function< void(int, int, int, int, double) > > Setter4F
- std::unordered_map< std::string, boost::function< double(int, int, int, int) > > Getter4F

Static Private Attributes

Independent entries

We follow https://arxiv.org/abs/2010.16341 *tab. 15, 16 for the symmetry class of the operators.*
Notice that operators in classes WC1 and WC5 have no restrictions for neither real nor imaginary part, each having N_G^2 (for WC1) or N_G^4 (for WC5).

- static const int DWC2R = 6

  Number of independent entries of the real part of operators in symmetry class WC2.

- static const int DWC2I = 3
  Number of independent entries of the imaginary part of operators in symmetry class WC2.
- static const int DWC6R = 27
  Number of independent entries of the real part of operators in symmetry class WC6.
- static const int DWC6I = 18
  Number of independent entries of the imaginary part of operators in symmetry class WC6.
- static const int DWC7R = 45
  Number of independent entries of the real part of operators in symmetry class WC7.
- static const int DWC7I = 36
  Number of independent entries of the imaginary part of operators in symmetry class WC7.
- static const int DWC8R = 21
  Number of independent entries of the real part of operators in symmetry class WC8.
- static const int DWC8I = 15
  Number of independent entries of the imaginary part of operators in symmetry class WC8.

Indices chosen as independent entries

the element `WCn_indices[a][b]` must be interpretated as : the b-th index (there are 4 in 4F operators and 2 in 2F) of the a-th independent entry for the WCn category, where n = 1,2R,2I...

- static const int WC2R_indices [DWC2R][2]
  Independent indices for WC2R.
- static const int WC2I_indices [DWC2I][2]
  Independent indices for WC2I.
- static const int WC6R_indices [DWC6R][4]
  Independent indices for WC6R.
- static const int WC6I_indices [DWC6I][4]
  Independent indices for WC6I.
- static const int WC7R_indices [DWC7R][4]
  Independent indices for WC7R.
- static const int WC7I_indices [DWC7I][4]
  Independent indices for WC7I.
- static const int WC8R_indices [DWC8R][4]
  Independent indices for WC8R.
- static const int WC8I_indices [DWC8I][4]
  Independent indices for WC8I.

Number of operators for each class

See `https://arxiv.org/abs/1308.2627` tab. 1 for the full list of operators. There are 8 different classes, depending on the field content. This classification is different from the symmetry classification WC1, WC2R, ...
For each class `N` is the number of operators and `E` the number of independent entries. When E is not explicitely defined is understood `E=N` (no flavour structure)

- static const int NG = 3
  Number of fermion flavours.
- static const int DF = 9
  Dimension of matrices in flavour space.
- static const int DFs = (NG∗NG + NG) / 2
  Independent entries of a $N_G \times N_G$ real symmetric matrix.
- static const int DFa = (NG∗NG - NG) / 2
  Independent entries of a $N_G \times N_G$ real anti-symmetric matrix.
- static const int Ngauge = 3
  Number of gauge couplings.
- static const int Nh = 2
  Number of Higgs' sector parameters.
- static const int Nyukawa = 3
  Number of Yukawa matrices.

- static const int Eyuk = (Nyukawa $*$ 2 $*$ DF)

  Number of real parameters for each Yukawa matrix.
- static const int N1 = 4
- static const int N23 = 3
- static const int N4 = 8
- static const int N5 = 3
- static const int E5 = (N5 $*$ 2 $*$ DF)
- static const int N6 = 8
- static const int E6 = (N6 $*$ 2 $*$ DF)
- static const int N7 = 8
- static const int N7H = 7

  Number of Hermitian operators in class 7.
- static const int N7NH = 1

  Number of non-Hermitian operators in class 7.
- static const int E7 = (N7H$*$(DWC2R + DWC2I) + N7NH $*$ 2 $*$ DF)
- static const int N8_LLLL = 5
- static const int E8_LLLL = 2 $*$ (DWC7R + DWC7I) + 3 $*$ (DWC6R + DWC6I)
- static const int N8_RRRR = 7
- static const int E8_RRRR = 4 $*$ (DWC7R + DWC7I) + 2 $*$ (DWC6R + DWC6I) + 1 $*$ (DWC8R + DWC8I)
- static const int N8_LLRR = 8
- static const int E8_LLRR = 8 $*$ (DWC7R + DWC7I)
- static const int N8_LRRL = 1
- static const int E8_LRRL = 2 $*$ NG$*$NG$*$NG$*$NG$*$N8_LRRL
- static const int N8_LRLR = 4
- static const int E8_LRLR = 2 $*$ NG$*$NG$*$NG$*$NG$*$N8_LRLR

Fractions

Recurring fractions defined in order to increase efficiency

- static const double TWO_THIRDS = (2. / 3.)
- static const double FOUR_THIRDS = (4. / 3.)
- static const double EIGHT_THIRDS = (8. / 3.)
- static const double ONE_THIRD = (1. / 3.)
- static const double ONE_SIXTH = (1. / 6.)
- static const double TEN_THIRDS = (10. / 3.)

Miscellaneous parameters

- static const double delta [3][3]

  Kroenecker delta in flavour space.
- static const int dim = (Ngauge + Nh + Eyuk + N1 + N23 + N4 + E5 + E6 + E7 + E8_LLLL + E8_RRRR + E8_LLRR + E8_LRRL + E8_LRLR)

  Dimension of the system.
- static const double NC = 3.

  Number of colors.
- static const double NC2 = 9.

  Number of colors squared.
- static const double b01 = (- 1. / 6. - 3. $*$ 20. / 9.)

  Leading-order g_1 beta function (with g_1 normalized as usual and not as in GUT theories)
- static const double b02 = (43. / 6. - 4. $*$ 3. / 3.)

  Leading-order g_2 beta function.
- static const double b03 = (11. - 4. $*$ 3. / 3.)

  Leading-order g_3 beta function.
- static const double cA2 = double(2.)

  $\mathbf{SU(2)}$ *adjoint Casimir*
- static const double cA3 = double(NC)

  $\mathbf{SU(3)}$ *adjoint Casimir*
- static const double cF2 = double(3. / 4.)

  $\mathbf{SU(2)}$ *fundamental Casimir*
- static const double cF3 = double(0.5 $*$ (NC$*$NC - 1) / NC)

$\mathbf{SU(3)}$ *fundamental Casimir*

Hypercharges (and products of hypercharges)

We use $Q = T_3 + Y$, being T_3 the z-component of the weak isospin and Q the electric charge. The other possibility is $Q = T_3 + \frac{Y}{2}$ as in https://arxiv.org/abs/1308.2627

- static const double Yh = (0.5)
- static const double Yh2 = Yh∗Yh
- static const double Yq = (1. / 6.)
- static const double Yq2 = Yq∗Yq
- static const double Yl = (- 0.5)
- static const double Yl2 = Yl∗Yl
- static const double Yu = (2. / 3.)
- static const double Yu2 = Yu∗Yu
- static const double Yd = (- 1. / 3.)
- static const double Yd2 = Yd∗Yd
- static const double Ye = (- 1.)
- static const double Ye2 = Ye∗Ye
- static const double YhYu = Yh∗Yu
- static const double YhYd = Yh∗Yd
- static const double YhYe = Yh∗Ye
- static const double YhYq = Yh∗Yq
- static const double YhYl = Yh∗Yl
- static const double YuYd = Yu∗Yd
- static const double YuYe = Yu∗Ye
- static const double YuYq = Yu∗Yq
- static const double YuYl = Yu∗Yl
- static const double YdYe = Yd∗Ye
- static const double YdYq = Yd∗Yq
- static const double YdYl = Yd∗Yl
- static const double YeYq = Ye∗Yq
- static const double YeYl = Ye∗Yl
- static const double YlYq = Yl∗Yq

3.1.1 Detailed Description

A class that performs renormalization group evolution in the context of the SMEFT.

The class solves the Renormalization Group Equations (RGEs) both numerically and in the leading-log approximations. Only operators up to dimension six that preserve lepton and baryon numbers are considered. The operator basis is the Warsaw basis, defined in https://arxiv.org/abs/1008.4884.
The user must set separately real and imaginary part of each complex parameter.
In tables 3.1, 3.2, 3.3 and 3.4 are listed all the parameters, together with their name (that must be used to correctly invoke getter and setter functions).
The numerical integration is performed with an adaptive step-size routine (the Explicit embedded Runge-Kutta-↩ Fehlberg method), using the tools in the GNU Scientific Library.
See https://www.gnu.org/software/gsl/doc/html/ode-initval.html for all the details.
The accuracy level of the numerical integration can be tuned selecting the parameters $\epsilon_{rel}, \epsilon_{abs}$ and the integration step using the dedicated getter functions.

Author

HEPfit Collaboration

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Coefficient	Name
g_1	g1
g_2	g2
g_3	g3
λ	lambda
m_h^2 [GeV^2]	mh2
$\Re(\mathcal{Y}_u)$	YuR
$\Im(\mathcal{Y}_u)$	YuI
$\Re(\mathcal{Y}_d)$	YdR
$\Im(\mathcal{Y}_d)$	YdI
$\Re(\mathcal{Y}_e)$	YeR
$\Im(\mathcal{Y}_e)$	YeI

Table 3.1 Standard Model parameters

Classes 1-3		Class 4	
Coefficient	Name	Coefficient	Name
C_G	CG	C_{HG}	CHG
$C_{\tilde{G}}$	CGtilde	$C_{H\tilde{G}}$	CHGtilde
C_W	CW	C_{HW}	CHW
$C_{\tilde{W}}$	CWtilde	$C_{H\tilde{W}}$	CHWtilde
C_H	CH	C_{HB}	CHB
$C_{H\Box}$	CHbox	$C_{H\tilde{B}}$	CHBtilde
C_{HD}	CHD	C_{HWB}	CHWB
		$C_{H\tilde{W}B}$	CHWtildeB

Table 3.2 Scalar (and real) SMEFT operators.

Class 5		
Coefficient	Name	Symmetry
$\Re(C_{eH})$	CeHR	WC1
$\Im(C_{eH})$	CeHI	WC1
$\Re(C_{uH})$	CuHR	WC1
$\Im(C_{uH})$	CuHI	WC1
$\Re(C_{dH})$	CdHR	WC1
$\Im(C_{dH})$	CdHI	WC1

Class 6		
Coefficient	Name	Symmetry
$\Re(C_{eW})$	CeWR	WC1
$\Im(C_{eW})$	CeWI	WC1
$\Re(C_{eB})$	CeBR	WC1
$\Im(C_{eB})$	CeBI	WC1
$\Re(C_{uG})$	CuGR	WC1
$\Im(C_{uG})$	CuGI	WC1
$\Re(C_{uW})$	CuWR	WC1
$\Im(C_{uW})$	CuWI	WC1
$\Re(C_{uB})$	CuBR	WC1
$\Im(C_{uB})$	CuBI	WC1
$\Re(C_{dG})$	CdGR	WC1
$\Im(C_{dG})$	CdGI	WC1
$\Re(C_{dW})$	CdWR	WC1
$\Im(C_{dW})$	CdWI	WC1
$\Re(C_{dB})$	CdBR	WC1
$\Im(C_{dB})$	CdBI	WC1

Class 7		
Coefficient	Name	Symmetry
$\Re(C_{Hl1})$	CHl1R	WC2R
$\Im(C_{Hl1})$	CHl1I	WC2I
$\Re(C_{Hl3})$	CHl3R	WC2R
$\Im(C_{Hl3})$	CHl3I	WC2I
$\Re(C_{He})$	CHeR	WC2R
$\Im(C_{He})$	CHeI	WC2I
$\Re(C_{Hq1})$	CHq1R	WC2R
$\Im(C_{Hq1})$	CHq1I	WC2I
$\Re(C_{Hq3})$	CHq3R	WC2R
$\Im(C_{Hq3})$	CHq3I	WC2I
$\Re(C_{Hu})$	CHuR	WC2R
$\Im(C_{Hu})$	CHuI	WC2I
$\Re(C_{Hd})$	CHdR	WC2R
$\Im(C_{Hd})$	CHdI	WC2I
$\Re(C_{Hud})$	CHudR	WC1
$\Im(C_{Hud})$	CHudI	WC1

Table 3.3 2F SMEFT operators

Class 8 $(\bar{L}L)(\bar{L}L)$

Coefficient	Name	Symmetry
$\Re(C_{ll})$	`CllR`	WC6R
$\Im(C_{ll})$	`CllI`	WC6I
$\Re(C_{qq1})$	`Cqq1R`	WC6R
$\Im(C_{qq1})$	`Cqq1I`	WC6I
$\Re(C_{qq3})$	`Cqq3R`	WC6R
$\Im(C_{qq3})$	`Cqq3I`	WC6I
$\Re(C_{lq1})$	`Clq1R`	WC7R
$\Im(C_{lq1})$	`Clq1I`	WC7I
$\Re(C_{lq3})$	`Clq3R`	WC7R
$\Im(C_{lq3})$	`Clq3I`	WC7I

Class 8 $(\bar{L}R)(\bar{L}R)$

Coefficient	Name	Symmetry
$\Re(C_{quqd1})$	`Cquqd1R`	WC5
$\Im(C_{quqd1})$	`Cquqd1I`	WC5
$\Re(C_{quqd8})$	`Cquqd8R`	WC5
$\Im(C_{quqd8})$	`Cquqs8I`	WC5
$\Re(C_{lequ1})$	`Clequ1R`	WC5
$\Im(C_{lequ1})$	`Clequ1I`	WC5
$\Re(C_{lequ3})$	`Clequ3R`	WC5
$\Im(C_{lequ3})$	`Clequ3I`	WC5

Class 8 $(\bar{R}R)(\bar{R}R)$

Coefficient	Name	Symmetry
$\Re(C_{ee})$	`CeeR`	WC8R
$\Im(C_{ee})$	`CeeI`	WC8I
$\Re(C_{uu})$	`CuuR`	WC6R
$\Im(C_{uu})$	`CuuI`	WC6I
$\Re(C_{dd})$	`CddR`	WC6R
$\Im(C_{dd})$	`CddI`	WC6I
$\Re(C_{eu})$	`CeuR`	WC7R
$\Im(C_{eu})$	`CeuI`	WC7I
$\Re(C_{ed})$	`CedR`	WC7R
$\Im(C_{ed})$	`CedI`	WC7I
$\Re(C_{ud1})$	`Cud1R`	WC7R
$\Im(C_{ud1})$	`Cud1I`	WC7I
$\Re(C_{ud8})$	`Cud8R`	WC7R
$\Im(C_{ud8})$	`Cud8I`	WC7I

Class 8 $(\bar{L}R)(\bar{R}L)$

Coefficient	Name	Symmetry
$\Re(C_{ledq})$	`CledqR`	WC5
$\Im(C_{ledq})$	`CledqI`	WC5

Class 8 $(\bar{L}L)(\bar{R}R)$

Coefficient	Name	Symmetry
$\Re(C_{le})$	`CleR`	WC7R
$\Im(C_{le})$	`CleI`	WC7I
$\Re(C_{lu})$	`CluR`	WC7R
$\Im(C_{lu})$	`CluI`	WC7I
$\Re(C_{ld})$	`CldR`	WC7R
$\Im(C_{ld})$	`CldI`	WC7I
$\Re(C_{qe})$	`CqeR`	WC7R
$\Im(C_{qe})$	`CqeI`	WC7I
$\Re(C_{qu1})$	`Cqu1R`	WC7R
$\Im(C_{qu1})$	`Cqu1I`	WC7I
$\Re(C_{qu8})$	`Cqu8R`	WC7R
$\Im(C_{qu8})$	`Cqu8I`	WC7I
$\Re(C_{qd1})$	`Cqd1R`	WC7R
$\Im(C_{qd1})$	`Cqd1I`	WC7I
$\Re(C_{qd8})$	`Cqd8R`	WC7R
$\Im(C_{qd8})$	`Cqd8I`	WC7I

Table 3.4 4F SMEFT Operators.

3.1.2 Constructor & Destructor Documentation

3.1.2.1 RGESolver()

```
RGESolver::RGESolver ( )
```

The default constructor.

3.1.2.2 ∼RGESolver()

```
RGESolver::∼RGESolver ( )  [inline]
```

The default destructor.

3.1.3 Member Function Documentation

3.1.3.1 epsabs()

```
double RGESolver::epsabs ( )  [inline]
```

Getter for the absolute error used in the numerical integration.

3.1.3.2 epsrel()

```
double RGESolver::epsrel ( )  [inline]
```

Getter for the relative error used in the numerical integration.

3.1.3.3 Evolve()

```
void RGESolver::Evolve (
            std::string method,
            double muI,
            double muF )
```

Command to perform the RGE evolution.

RGEs are solved with the chosen method from `muI` to `muF`. Currently, the available methods are "Numeric" and "Leading-Log".
The evolutor takes as initial values the current values of the parameters, set with the `SetCoefficient(...)` function. After completing the evolution the values of the parameters are updated and are accessible with the `GetCoefficient(...)` function.

Parameters

method	resolution method
muI	initial energy scale
muF	final energy scale

3.1.3.4 EvolveSMOnly()

```
void RGESolver::EvolveSMOnly (
            std::string method,
```

```
            double muI,
            double muF )
```

Same as Evolve(std::string method, double muI, double muF), but only for the SM parameters. The user should use this method instead of `Evolve` when interested in pure SM running.

Parameters

method	
muI	
muF	

3.1.3.5 ExtractParametersFromCKM()

```
void RGESolver::ExtractParametersFromCKM ( )  [private]
```

3.1.3.6 FromMassesToYukawas()

```
void RGESolver::FromMassesToYukawas (
            std::string basis )  [private]
```

3.1.3.7 func()

```
int RGESolver::func (
            double logmu,
            const double y[],
            double f[],
            void * params )  [static], [private]
```

Computes the beta functions for the SMEFT.

Parameters

logmu	value of the logarithm of the energy scale at which the beta functions are computed
y	1D array in which are stored the current values of the parameters
f	1D array in which the beta functions for each parameters are saved
params	eventual additional parameters (not used)

Returns

GSL_SUCCESS

3.1.3.8 funcSMOnly()

```
static int RGESolver::funcSMOnly (
              double logmu,
              const double y[],
              double f[],
              void * params )  [static], [private]
```

3.1.3.9 GenerateSMInitialConditions()

```
void RGESolver::GenerateSMInitialConditions (
              double mu,
              std::string basis,
              std::string method,
              bool inputCKM = true )
```

Generates the initial conditions for Standard Model's parameters (gauge couplings, Yukawa coupling, quartic coupling and Higgs' boson mass).

Parameters

mu	Scale (in GeV) at which the initial conditions are generated. If mu is different from the scale at which the input is given, RGESolver will use the pure SM RGEs to run the parameters to the scale mu.
basis	Flavour basis ("UP"or "DOWN")
method	Method used by RGESolver to run the SM parameters to the scale mu ("Numeric" or "Leading-Log")
inputCKM	If set to true (default), the input for the Yukawa matrices will be generated from the current value of the CKM matrix and the masses of the fermions (default).

3.1.3.10 GetCKMPhase()

```
double RGESolver::GetCKMPhase ( )  [inline]
```

Getter function for the CKM matrix delta δ.

Returns

δ.

3.1.3.11 GetCKMTheta12()

```
double RGESolver::GetCKMTheta12 ( )  [inline]
```

Getter function for the CKM matrix angle θ_{12}.

Returns

θ_{12}.

3.1.3.12 GetCKMTheta13()

```
double RGESolver::GetCKMTheta13 ( )  [inline]
```

Getter function for the CKM matrix angle θ_{13}.

Returns

θ_{13}.

3.1.3.13 GetCKMTheta23()

```
double RGESolver::GetCKMTheta23 ( )  [inline]
```

Getter function for the CKM matrix angle θ_{23}.

Returns

θ_{23}.

3.1.3.14 GetCoefficient() [1/3]

```
double RGESolver::GetCoefficient (
            std::string name )
```

Getter function for scalar/0F parameters (no flavour indices).

If the parameter name does not match with any of the parameters, an error message is printed and the value 0 is returned.

Parameters

name	name of the parameter

Returns

the requested parameter (if it exists), otherwise returns 0.

3.1.3.15 GetCoefficient() [2/3]

```
double RGESolver::GetCoefficient (
            std::string name,
            int i,
            int j )
```

Getter function for 2F parameters (2 flavour indices).

If the parameter name does not match with any of the parameters or if at least one of the inserted indices is outside the [0:2] range,
an error message is printed and the value 0 is returned.

Parameters

name	name of the parameter
i	first flavour index
j	second flavour index

Returns

the requested parameter (if it exists), otherwise returns 0.

3.1.3.16 GetCoefficient() [3/3]

```
double RGESolver::GetCoefficient (
            std::string name,
            int i,
            int j,
            int k,
            int l )
```

Getter function for 4F parameters (4 flavour indices).

If the parameter name does not match with any of the parameters or if at least one of the inserted indices is outside the [0:2] range,
an error message is printed and the value 0 is returned.

Parameters

name	name of the parameter
i	first flavour index
j	second flavour index
k	third flavour index
l	fourth flavour index

Returns

the requested parameter (if it exists), otherwise returns 0.

3.1.3.17 GetSMInputScale()

```
double RGESolver::GetSMInputScale ( )  [inline]
```

Getter method for the scale at which the method `GenerateSMInitialConditions` takes the input values for SM parameters.

3.1.3.18 GoToBasisSMOnly()

```
void RGESolver::GoToBasisSMOnly (
            std::string basis )  [private]
```

3.1.3.19 Init()

```
void RGESolver::Init ( )  [private]
```

Inserts the initial values of the parameters in the array `x`.

Only used in `Evolve`

3.1.3.20 InitSMOnly()

```
void RGESolver::InitSMOnly ( )  [private]
```

3.1.3.21 Print()

```
void RGESolver::Print (
            double * c,
            std::string name,
            std::string sym,
            std::string format,
            std::ofstream & f )  [inline], [static], [private]
```

Prints on file the coefficient `c`.

This function is used only in the function `SaveOutputFile`. Currently only "SLHA" printing for WC1,WC2R/I, WC5,WC6R/I,WC7R/I,WC8R/I is implemented.

Parameters

c	coefficient
name	printed name
sym	symmetry category of the operator
format	chosen format
f	pointer to file

3.1.3.22 Reset()

```
void RGESolver::Reset ( )
```

Resets all the SMEFT coefficients to 0 and the SM parameters to their default value.

3.1.3.23 SaveOutputFile()

```
void RGESolver::SaveOutputFile (
            std::string filename,
            std::string format )
```

Saves the current values of parameters in a file.

Currently, only "SLHA" format is implemented

Parameters

filename	Name of the output file
format	Format of the output file

3.1.3.24 Set_epsabs()

```
void RGESolver::Set_epsabs (
            double epsabs )  [inline]
```

Setter for the absolute error used in the numerical integration.

3.1.3.25 Set_epsrel()

```
void RGESolver::Set_epsrel (
            double epsrel )  [inline]
```

Setter for the relative error used in the numerical integration.

3.1.3.26 Set_step()

```
void RGESolver::Set_step (
            double step )  [inline]
```

Setter for the step used in the numerical integration.

3.1.3.27 SetCKMPhase()

```
void RGESolver::SetCKMPhase (
            double val )
```

Setter function for the CKM matrix phase δ. The assignation is completed only if $\delta \in (-\pi, \pi]$.

Parameters

val	

3.1.3.28 SetCKMTheta12()

```
void RGESolver::SetCKMTheta12 (
            double val )
```

Setter function for the CKM matrix angle θ_{12}. The assignation is completed only if $\theta_{12} \in [0, \frac{\pi}{2}]$.

Parameters

val	

3.1.3.29 SetCKMTheta13()

```
void RGESolver::SetCKMTheta13 (
            double val )
```

Setter function for the CKM matrix angle θ_{13}. The assignation is completed only if $\theta_{13} \in [0, \frac{\pi}{2}]$.

Parameters

val	

3.1.3.30 SetCKMTheta23()

```
void RGESolver::SetCKMTheta23 (
            double val )
```

Setter function for the CKM matrix angle θ_{23}. The assignation is completed only if $\theta_{23} \in [0, \frac{\pi}{2}]$.

Parameters

val	

3.1.3.31 SetCoefficient() [1/3]

```
void RGESolver::SetCoefficient (
            std::string name,
            double val )
```

Setter function for scalar/0F parameters (no flavour indices).

If the parameter name does not match with any of the parameters, an error message is printed and no assignation is performed.

Parameters

name	name of the parameter
val	its value

3.1.3.32 SetCoefficient() [2/3]

```
void RGESolver::SetCoefficient (
            std::string name,
            double val,
            int i,
            int j )
```

Setter function for 2F parameters (2 flavour indices).

If the parameter name does not match with any of the parameters or if at least one of the inserted indices is outside the [0:2] range,

Parameters

name	name of the parameter
val	its value
i	first flavour index
j	second flavour index

3.1.3.33 SetCoefficient() [3/3]

```
void RGESolver::SetCoefficient (
            std::string name,
            double val,
            int i,
            int j,
            int k,
            int l )
```

Setter function for 4F parameters (4 flavour indices).

If the parameter name does not match with any of the parameters or if at least one of the inserted indices is outside the [0:2] range, an error message is printed and no assignation is performed.

Parameters

name	name of the parameter
val	its value
i	first flavour index
j	second flavour index
k	third flavour index
l	fourth flavour index

3.1.3.34 SetSMDefaultInput()

```
void RGESolver::SetSMDefaultInput ( )  [private]
```

3.1.3.35 SetSMInputScale()

```
void RGESolver::SetSMInputScale (
            double mu )  [inline]
```

Setter method for the scale at which the method `GenerateSMInitialConditions` takes the input values for SM parameters.

Parameters

mu	

3.1.3.36 step()

```
double RGESolver::step ( )  [inline]
```

Getter for the step used in the numerical integration.

3.1.3.37 Update()

```
void RGESolver::Update ( )  [private]
```

Saves the evolved values of the coefficients from `x`.

Only used in `Evolve`

3.1.3.38 UpdateCKM()

```
void RGESolver::UpdateCKM ( )  [private]
```

3.1.3.39 UpdateSMOnly()

```
void RGESolver::UpdateSMOnly ( )  [private]
```

3.1.3.40 WC1()

```
double RGESolver::WC1 (
            double * c,
            int i,
            int j )  [inline], [static], [private]
```

3.1.3.41 WC1_set()

```
void RGESolver::WC1_set (
            double * c,
            int i,
            int j,
            double val )  [inline], [static], [private]
```

3.1.3.42 WC2I()

```
double RGESolver::WC2I (
            double * c,
            int i,
            int j )  [inline], [static], [private]
```

3.1.3.43 WC2I_set()

```
void RGESolver::WC2I_set (
            double * c,
            int i,
            int j,
            double val )  [inline], [static], [private]
```

3.1.3.44 WC2R()

```
double RGESolver::WC2R (
            double * c,
            int i,
            int j )  [inline], [static], [private]
```

3.1.3.45 WC2R_set()

```
void RGESolver::WC2R_set (
            double * c,
            int i,
            int j,
            double val )  [inline], [static], [private]
```

3.1.3.46 WC3()

```
double RGESolver::WC3 (
            double * c,
            int i,
            int j )  [inline], [static], [private]
```

3.1.3.47 WC3_set()

```
void RGESolver::WC3_set (
            double * c,
            int i,
            int j,
            double val )  [inline], [static], [private]
```

3.1.3.48 WC5()

```
double RGESolver::WC5 (
            double * c,
            int i,
            int j,
            int k,
            int l )  [inline], [static], [private]
```

3.1.3.49 WC5_set()

```
void RGESolver::WC5_set (
            double * c,
            int i,
            int j,
            int k,
            int l,
            double val )  [inline], [static], [private]
```

3.1.3.50 WC6I()

```
double RGESolver::WC6I (
            double * c,
            int i,
            int j,
            int k,
            int l )  [inline], [static], [private]
```

3.1.3.51 WC6I_set()

```
void RGESolver::WC6I_set (
            double * c,
            int i,
            int j,
            int k,
            int l,
            double val )  [inline], [static], [private]
```

3.1.3.52 WC6R()

```
double RGESolver::WC6R (
            double * c,
            int i,
            int j,
            int k,
            int l )  [inline], [static], [private]
```

3.1.3.53 WC6R_set()

```
void RGESolver::WC6R_set (
            double * c,
            int i,
            int j,
            int k,
            int l,
            double val )  [inline], [static], [private]
```

3.1.3.54 WC7I()

```
double RGESolver::WC7I (
            double * c,
            int i,
            int j,
            int k,
            int l )  [inline], [static], [private]
```

3.1.3.55 WC7I_set()

```
void RGESolver::WC7I_set (
            double * c,
            int i,
            int j,
            int k,
            int l,
            double val )  [inline], [static], [private]
```

3.1.3.56 WC7R()

```
double RGESolver::WC7R (
            double * c,
            int i,
            int j,
            int k,
            int l )  [inline], [static], [private]
```

3.1.3.57 WC7R_set()

```
void RGESolver::WC7R_set (
            double * c,
            int i,
            int j,
            int k,
            int l,
            double val )  [inline], [static], [private]
```

3.1.3.58 WC8I()

```
double RGESolver::WC8I (
            double * c,
            int i,
            int j,
            int k,
            int l )  [inline], [static], [private]
```

3.1.3.59 WC8I_set()

```
void RGESolver::WC8I_set (
            double * c,
            int i,
            int j,
            int k,
            int l,
            double val )  [inline], [static], [private]
```

3.1.3.60 WC8R()

```
double RGESolver::WC8R (
            double * c,
            int i,
            int j,
            int k,
            int l )  [inline], [static], [private]
```

3.1.3.61 WC8R_set()

```
void RGESolver::WC8R_set (
            double * c,
            int i,
            int j,
            int k,
            int l,
            double val )  [inline], [static], [private]
```

3.1.3.62 Yukawa()

```
double RGESolver::Yukawa (
            double y[3][3],
            int i,
            int j )  [inline], [static], [private]
```

3.1.3.63 Yukawa_set()

```
void RGESolver::Yukawa_set (
            double y[3][3],
            int i,
            int j,
            double val )  [inline], [static], [private]
```

3.1.4 Member Data Documentation

3.1.4.1 b01

```
const double RGESolver::b01 = (- 1.  / 6.  - 3.  * 20.  / 9.)  [static], [private]
```

Leading-order g_1 beta function (with g_1 normalized as usual and not as in GUT theories)

3.1.4.2 b02

```
const double RGESolver::b02 = (43.  / 6.  - 4.  * 3.  / 3.)  [static], [private]
```

Leading-order g_2 beta function.

3.1.4.3 b03

```
const double RGESolver::b03 = (11.  - 4.  * 3.  / 3.)  [static], [private]
```

Leading-order g_3 beta function.

3.1.4.4 c12

```
double RGESolver::c12  [private]
```

$\cos\theta_{12}$

3.1.4.5 c13

```
double RGESolver::c13  [private]
```

$\cos\theta_{13}$

3.1.4.6 c23

```
double RGESolver::c23  [private]
```

$\cos\theta_{23}$

3.1.4.7 cA2

```
const double RGESolver::cA2 = double(2.)  [static], [private]
```

$\mathbf{SU}(\mathbf{2})$ adjoint Casimir

3.1.4.8 cA3

```
const double RGESolver::cA3 = double(NC)  [static], [private]
```

$\mathbf{SU}(\mathbf{3})$ adjoint Casimir

3.1.4.9 cdBI

```
double RGESolver::cdBI[3 *3]  [private]
```

$\Im\left[C_{dW}\right]$ (class 6, WC1)

3.1.4.10 cdBR

```
double RGESolver::cdBR[3 *3] = {0.}  [private]
```

$\Re\left[C_{dB}\right]$ (class 6, WC1)

3.1.4.11 cddI

```
double RGESolver::cddI[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{dd}\right]$ (class 8-[RR][RR], WC6I)

3.1.4.12 cddR

```
double RGESolver::cddR[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{dd}\right]$ (class 8-[RR][RR], WC6R)

3.1.4.13 cdGI

```
double RGESolver::cdGI[3 *3] = {0.}  [private]
```

$\Im\left[C_{dG}\right]$ (class 6, WC1)

3.1.4.14 cdGR

```
double RGESolver::cdGR[3 *3] = {0.}  [private]
```

$\Re\left[C_{dG}\right]$ (class 6, WC1)

3.1.4.15 cdHI

```
double RGESolver::cdHI[3 *3] = {0.}  [private]
```

$\Im\left[C_{dH}\right]$ (class 5, WC1)

3.1.4.16 cdHR

```
double RGESolver::cdHR[3 *3] = {0.}  [private]
```

$\Re\left[C_{dH}\right]$ (class 5, WC1)

3.1.4.17 cdWI

```
double RGESolver::cdWI[3 *3] = {0.}  [private]
```

$\Im\left[C_{dW}\right]$ (class 6, WC1)

3.1.4.18 cdWR

```
double RGESolver::cdWR[3 *3] = {0.}  [private]
```

$\Re\left[C_{dW}\right]$ (class 6, WC1)

3.1.4.19 ceBI

```
double RGESolver::ceBI[3 *3] = {0.}  [private]
```

$\Im\left[C_{eB}\right]$ (class 6, WC1)

3.1.4.20 ceBR

```
double RGESolver::ceBR[3 *3] = {0.}  [private]
```

$\Re\left[C_{eB}\right]$ (class 6, WC1)

3.1.4.21 cedI

```
double RGESolver::cedI[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{ed}\right]$ (class 8-[RR][RR], WC7I)

3.1.4.22 cedR

```
double RGESolver::cedR[3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{ed}\right]$ (class 8-[RR][RR], WC7R)

3.1.4.23 ceeI

```
double RGESolver::ceeI[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{ee}\right]$ (class 8-[RR][RR], WC8I)

3.1.4.24 ceeR

```
double RGESolver::ceeR[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{ee}\right]$ (class 8-[RR][RR], WC8R)

3.1.4.25 ceHI

```
double RGESolver::ceHI[3 *3] = {0.}  [private]
```

$\Im\left[C_{eH}\right]$ (class 5, WC1)

3.1.4.26 ceHR

```
double RGESolver::ceHR[3 *3] = {0.}  [private]
```

$\Re\left[C_{eH}\right]$ (class 5, WC1)

3.1.4.27 ceuI

```
double RGESolver::ceuI[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{eu}\right]$ (class 8-[RR][RR], WC7I)

3.1.4.28 ceuR

```
double RGESolver::ceuR[3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{eu}\right]$ (class 8-[RR][RR], WC7R)

3.1.4.29 ceWI

```
double RGESolver::ceWI[3 *3] = {0.}  [private]
```

$\Im\left[C_{eW}\right]$ (class 6, WC1)

3.1.4.30 ceWR

```
double RGESolver::ceWR[3 *3] = {0.}  [private]
```

$\Re\left[C_{eW}\right]$ (class 6, WC1)

3.1.4.31 cF2

```
const double RGESolver::cF2 = double(3.  / 4.)  [static], [private]
```

$\mathbf{SU}(\mathbf{2})$ fundamental Casimir

3.1.4.32 cF3

```
const double RGESolver::cF3 = double(0.5 * (NC*NC - 1) / NC)  [static], [private]
```

$\mathbf{SU}(\mathbf{3})$ fundamental Casimir

3.1.4.33 cG

```
double RGESolver::cG = 0.  [private]
```

C_G (class 1, scalar)

3.1.4.34 cGT

```
double RGESolver::cGT = 0.  [private]
```

$C_{\tilde{G}}$ (class 1, scalar)

3.1.4.35 cH

```
double RGESolver::cH = 0.  [private]
```

C_H (class 2, scalar)

3.1.4.36 cHB

```
double RGESolver::cHB = 0.  [private]
```

C_{HB} (class 4, scalar)

3.1.4.37 cHBOX

```
double RGESolver::cHBOX = 0.  [private]
```

$C_{H\Box}$ (class 3, scalar)

3.1.4.38 cHBT

```
double RGESolver::cHBT = 0.  [private]
```

$C_{H\tilde{B}}$ (class 4, scalar)

3.1.4.39 cHD

```
double RGESolver::cHD = 0.  [private]
```

C_{HD} (class 3, scalar)

3.1.4.40 cHdI

```
double RGESolver::cHdI[3 *3] = {0.}  [private]
```

$\Im\left[C_{Hd}\right]$ (class 7, WC2I)

3.1.4.41 cHdR

```
double RGESolver::cHdR[3 *3] = {0.}  [private]
```

$\Re\left[C_{Hd}\right]$ (class 7, WC2R)

3.1.4.42 cHeI

```
double RGESolver::cHeI[3 *3] = {0.}  [private]
```

$\Im\left[C_{He}\right]$ (class 7, WC2I)

3.1.4.43 cHeR

```
double RGESolver::cHeR[3 *3] = {0.}  [private]
```

$\Re\left[C_{He}\right]$ (class 7, WC2R)

3.1.4.44 cHG

```
double RGESolver::cHG = 0.  [private]
```

C_{HG} (class 4, scalar)

3.1.4.45 cHGT

```
double RGESolver::cHGT = 0.  [private]
```

$C_{H\tilde{G}}$ (class 4, scalar)

3.1.4.46 cHl1I

```
double RGESolver::cHl1I[3 *3] = {0.}  [private]
```

$\Im\left[C_{Hl1}\right]$ (class 7, WC2I)

3.1.4.47 cHl1R

```
double RGESolver::cHl1R[3 *3] = {0.}  [private]
```

$\Re\left[C_{Hl1}\right]$ (class 7, WC2R)

3.1.4.48 cHl3I

```
double RGESolver::cHl3I[3 *3] = {0.}  [private]
```

$\Im\left[C_{Hl3}\right]$ (class 7, WC2I)

3.1.4.49 cHl3R

```
double RGESolver::cHl3R[3 *3] = {0.}  [private]
```

$\Re\left[C_{Hl3}\right]$ (class 7, WC2R)

3.1.4.50 cHq1I

```
double RGESolver::cHq1I[3 *3] = {0.}  [private]
```

$\Im\left[C_{Hq1}\right]$ (class 7, WC2I)

3.1.4.51 cHq1R

```
double RGESolver::cHq1R[3 *3] = {0.}  [private]
```

$\Re\left[C_{Hq1}\right]$ (class 7, WC2R)

3.1.4.52 cHq3I

```
double RGESolver::cHq3I[3 *3] = {0.}  [private]
```

$\Im\left[C_{Hq3}\right]$ (class 7, WC2I)

3.1.4.53 cHq3R

```
double RGESolver::cHq3R[3 *3] = {0.}  [private]
```

$\Re\left[C_{Hq3}\right]$ (class 7, WC2R)

3.1.4.54 cHudI

```
double RGESolver::cHudI[3 *3] = {0.}  [private]
```

$\Im\left[C_{Hud}\right]$ (class 7, WC1)

3.1.4.55 cHudR

```
double RGESolver::cHudR[3 *3] = {0.}  [private]
```

$\Re\left[C_{Hud}\right]$ (class 7, WC1)

3.1.4.56 cHuI

```
double RGESolver::cHuI[3 *3] = {0.}  [private]
```

$\Im\left[C_{Hu}\right]$ (class 7, WC2I)

3.1.4.57 cHuR

```
double RGESolver::cHuR[3 *3] = {0.}  [private]
```

$\Re\left[C_{Hu}\right]$ (class 7, WC2R)

3.1.4.58 cHW

```
double RGESolver::cHW = 0.  [private]
```

C_{HW} (class 4, scalar)

3.1.4.59 cHWB

```
double RGESolver::cHWB = 0.  [private]
```

C_{HWB} (class 4, scalar)

3.1.4.60 cHWBT

```
double RGESolver::cHWBT = 0.  [private]
```

$C_{H\tilde{W}B}$ (class 4, scalar)

3.1.4.61 cHWT

```
double RGESolver::cHWT = 0.  [private]
```

$C_{H\tilde{W}}$ (class 4, scalar)

3.1.4.62 CKM

```
gslpp::matrix<gslpp::complex> RGESolver::CKM = gslpp::matrix<gslpp::complex>(3, 3, 0.)  [private]
```

The CKM matrix.

3.1.4.63 CKM_delta

```
double RGESolver::CKM_delta  [private]
```

3.1.4.64 CKM_theta12

```
double RGESolver::CKM_theta12  [private]
```

θ_{12} of the CKM matrix (in radians). The default value is ???

3.1.4.65 CKM_theta13

```
double RGESolver::CKM_theta13  [private]
```

3.1.4.66 CKM_theta23

```
double RGESolver::CKM_theta23  [private]
```

3.1.4.67 cldI

```
double RGESolver::cldI[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{ld}\right]$ (class 8-[LL][RR], WC7I)

3.1.4.68 cldR

```
double RGESolver::cldR[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{ld}\right]$ (class 8-[LL][RR], WC7R)

3.1.4.69 cledqI

```
double RGESolver::cledqI[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{ledq}\right]$ (class 8-[LR][RL], WC5)

3.1.4.70 cledqR

```
double RGESolver::cledqR[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{ledq}\right]$ (class 8-[LR][RL], WC5)

3.1.4.71 cleI

```
double RGESolver::cleI[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{le}\right]$ (class 8-[LL][RR], WC7I)

3.1.4.72 clequ1I

```
double RGESolver::clequ1I[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{lequ1}\right]$ (class 8-[LR][LR], WC5)

3.1.4.73 clequ1R

```
double RGESolver::clequ1R[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{lequ1}\right]$ (class 8-[LR][LR], WC5)

3.1.4.74 clequ3I

```
double RGESolver::clequ3I[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{lequ3}\right]$ (class 8-[LR][LR], WC5)

3.1.4.75 clequ3R

```
double RGESolver::clequ3R[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{lequ3}\right]$ (class 8-[LR][LR], WC5)

3.1.4.76 cleR

```
double RGESolver::cleR[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{le}\right]$ (class 8-[LL][RR], WC7R)

3.1.4.77 cllI

```
double RGESolver::cllI[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{ll}\right]$ (class 8-[LL][LL], WC6I)

3.1.4.78 cllR

```
double RGESolver::cllR[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{ll}\right]$ (class 8-[LL][LL], WC6R)

3.1.4.79 clq1I

```
double RGESolver::clq1I[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{lq1}\right]$ (class 8-[LL][LL], WC7I)

3.1.4.80 clq1R

```
double RGESolver::clq1R[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{lq1}\right]$ (class 8-[LL][LL], WC7R)

3.1.4.81 clq3I

```
double RGESolver::clq3I[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{lq3}\right]$ (class 8-[LL][LL], WC7I)

3.1.4.82 clq3R

```
double RGESolver::clq3R[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{lq3}\right]$ (class 8-[LL][LL], WC7R)

3.1.4.83 cluI

```
double RGESolver::cluI[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{lu}\right]$ (class 8-[LL][RR], WC7I)

3.1.4.84 cluR

```
double RGESolver::cluR[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{lu}\right]$ (class 8-[LL][RR], WC7R)

3.1.4.85 con_

```
gsl_odeiv2_control* RGESolver::con_  [private]
```

Initial value:

```
= gsl_odeiv2_control_standard_new(
            epsabs_, epsrel_, 1, 1)
```

3.1.4.86 cqd1I

```
double RGESolver::cqd1I[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{qd1}\right]$ (class 8-[LL][RR], WC7I)

3.1.4.87 cqd1R

```
double RGESolver::cqd1R[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{qd1}\right]$ (class 8-[LL][RR], WC7R)

3.1.4.88 cqd8I

```
double RGESolver::cqd8I[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{qd8}\right]$ (class 8-[LL][RR], WC7I)

3.1.4.89 cqd8R

```
double RGESolver::cqd8R[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{qd8}\right]$ (class 8-[LL][RR], WC7R)

3.1.4.90 cqeI

```
double RGESolver::cqeI[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{qe}\right]$ (class 8-[LL][RR], WC7I)

3.1.4.91 cqeR

```
double RGESolver::cqeR[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{qe}\right]$ (class 8-[LL][RR], WC7R)

3.1.4.92 cqq1I

```
double RGESolver::cqq1I[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{qq1}\right]$ (class 8-[LL][LL], WC6I)

3.1.4.93 cqq1R

```
double RGESolver::cqq1R[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{qq1}\right]$ (class 8-[LL][LL], WC6R)

3.1.4.94 cqq3I

```
double RGESolver::cqq3I[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{qq3}\right]$ (class 8-[LL][LL], WC6I)

3.1.4.95 cqq3R

```
double RGESolver::cqq3R[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{qq3}\right]$ (class 8-[LL][LL], WC6R)

3.1.4.96 cqu1I

```
double RGESolver::cqu1I[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{qu1}\right]$ (class 8-[LL][RR], WC7I)

3.1.4.97 cqu1R

```
double RGESolver::cqu1R[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{qu1}\right]$ (class 8-[LL][RR], WC7R)

3.1.4.98 cqu8I

```
double RGESolver::cqu8I[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{qu8}\right]$ (class 8-[LL][RR], WC7I)

3.1.4.99 cqu8R

```
double RGESolver::cqu8R[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{qu8}\right]$ (class 8-[LL][RR], WC7R)

3.1.4.100 cquqd1I

```
double RGESolver::cquqd1I[3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{quqd1}\right]$ (class 8-[LR][LR], WC5)

3.1.4.101 cquqd1R

```
double RGESolver::cquqd1R[3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{quqd1}\right]$ (class 8-[LR][LR], WC5)

3.1.4.102 cquqd8I

```
double RGESolver::cquqd8I[3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{quqd8}\right]$ (class 8-[LR][LR], WC5)

3.1.4.103 cquqd8R

```
double RGESolver::cquqd8R[3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{quqd8}\right]$ (class 8-[LR][LR], WC5)

3.1.4.104 cuBI

```
double RGESolver::cuBI[3 *3] = {0.}  [private]
```

$\Im\left[C_{uB}\right]$ (class 6, WC1)

3.1.4.105 cuBR

```
double RGESolver::cuBR[3 *3] = {0.}  [private]
```

$\Re\left[C_{uB}\right]$ (class 6, WC1)

3.1.4.106 cud1I

```
double RGESolver::cud1I[3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{ud1}\right]$ (class 8-[RR][RR], WC7I)

3.1.4.107 cud1R

```
double RGESolver::cud1R[3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{ud1}\right]$ (class 8-[RR][RR], WC7R)

3.1.4.108 cud8I

```
double RGESolver::cud8I[3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{ud1}\right]$ (class 8-[RR][RR], WC7I)

3.1.4.109 cud8R

```
double RGESolver::cud8R[3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{ud8}\right]$ (class 8-[RR][RR], WC7R)

3.1.4.110 cuGI

```
double RGESolver::cuGI[3 *3] = {0.}  [private]
```

$\Im\left[C_{uG}\right]$ (class 6, WC1)

3.1.4.111 cuGR

```
double RGESolver::cuGR[3 *3] = {0.}  [private]
```

$\Re\left[C_{uG}\right]$ (class 6, WC1)

3.1.4.112 cuHI

```
double RGESolver::cuHI[3 *3] = {0.}  [private]
```

$\Im\left[C_{uH}\right]$ (class 5, WC1)

3.1.4.113 cuHR

```
double RGESolver::cuHR[3 *3] = {0.}  [private]
```

$\Re\left[C_{uH}\right]$ (class 5, WC1)

3.1.4.114 cuuI

```
double RGESolver::cuuI[3 *3 *3 *3] = {0.}  [private]
```

$\Im\left[C_{uu}\right]$ (class 8-[RR][RR], WC6I)

3.1.4.115 cuuR

```
double RGESolver::cuuR[3 *3 *3 *3] = {0.}  [private]
```

$\Re\left[C_{uu}\right]$ (class 8-[RR][RR], WC6R)

3.1.4.116 cuWI

```
double RGESolver::cuWI[3 *3] = {0.}  [private]
```

$\Im\left[C_{uW}\right]$ (class 6, WC1)

3.1.4.117 cuWR

```
double RGESolver::cuWR[3 *3] = {0.}  [private]
```

$\Re\left[C_{uW}\right]$ (class 6, WC1)

3.1.4.118 cW

```
double RGESolver::cW = 0.  [private]
```

C_W (class 1, scalar)

3.1.4.119 cWT

```
double RGESolver::cWT = 0.  [private]
```

$C_{\tilde{W}}$ (class 1, scalar)

3.1.4.120 delta

```
const double RGESolver::delta  [static], [private]
```

Initial value:

```
= {
    {1., 0., 0.},
    { 0., 1., 0.},
    { 0., 0., 1.}
}
```

Kroenecker delta in flavour space.

3.1.4.121 DF

```
const int RGESolver::DF = 9  [static], [private]
```

Dimension of matrices in flavour space.

3.1.4.122 DFa

```
const int RGESolver::DFa = (NG*NG - NG) / 2  [static], [private]
```

Independent entries of a $N_G \times N_G$ real anti-symmetric matrix.

3.1.4.123 DFs

```
const int RGESolver::DFs = (NG*NG + NG) / 2  [static], [private]
```

Independent entries of a $N_G \times N_G$ real symmetric matrix.

3.1.4.124 dim

```
const int RGESolver::dim = (Ngauge + Nh + Eyuk + N1 + N23 + N4 + E5 + E6 + E7 + E8_LLLL +
E8_RRRR + E8_LLRR + E8_LRRL + E8_LRLR)  [static], [private]
```

Dimension of the system.

3.1.4.125 DWC2I

```
const int RGESolver::DWC2I = 3  [static], [private]
```

Number of independent entries of the imaginary part of operators in symmetry class WC2.

3.1.4.126 DWC2R

```
const int RGESolver::DWC2R = 6  [static], [private]
```

Number of independent entries of the real part of operators in symmetry class WC2.

3.1.4.127 DWC6I

```
const int RGESolver::DWC6I = 18  [static], [private]
```

Number of independent entries of the imaginary part of operators in symmetry class WC6.

3.1.4.128 DWC6R

```
const int RGESolver::DWC6R = 27  [static], [private]
```

Number of independent entries of the real part of operators in symmetry class WC6.

3.1.4.129 DWC7I

```
const int RGESolver::DWC7I = 36  [static], [private]
```

Number of independent entries of the imaginary part of operators in symmetry class WC7.

3.1.4.130 DWC7R

```
const int RGESolver::DWC7R = 45  [static], [private]
```

Number of independent entries of the real part of operators in symmetry class WC7.

3.1.4.131 DWC8I

```
const int RGESolver::DWC8I = 15  [static], [private]
```

Number of independent entries of the imaginary part of operators in symmetry class WC8.

3.1.4.132 DWC8R

```
const int RGESolver::DWC8R = 21  [static], [private]
```

Number of independent entries of the real part of operators in symmetry class WC8.

3.1.4.133 E5

```
const int RGESolver::E5 = (N5 * 2 * DF)  [static], [private]
```

3.1.4.134 E6

```
const int RGESolver::E6 = (N6 * 2 * DF)  [static], [private]
```

3.1.4.135 E7

```
const int RGESolver::E7 = (N7H*(DWC2R + DWC2I) + N7NH * 2 * DF)  [static], [private]
```

3.1.4.136 E8_LLLL

```
const int RGESolver::E8_LLLL = 2 * (DWC7R + DWC7I) + 3 * (DWC6R + DWC6I)  [static], [private]
```

3.1.4.137 E8_LLRR

```
const int RGESolver::E8_LLRR = 8 * (DWC7R + DWC7I)  [static], [private]
```

3.1.4.138 E8_LRLR

```
const int RGESolver::E8_LRLR = 2 * NG*NG*NG*NG*N8_LRLR  [static], [private]
```

3.1.4.139 E8_LRRL

```
const int RGESolver::E8_LRRL = 2 * NG*NG*NG*NG*N8_LRRL  [static], [private]
```

3.1.4.140 E8_RRRR

```
const int RGESolver::E8_RRRR = 4 * (DWC7R + DWC7I) + 2 * (DWC6R + DWC6I) + 1 * (DWC8R + DWC8I)
[static], [private]
```

3.1.4.141 EIGHT_THIRDS

```
const double RGESolver::EIGHT_THIRDS = (8.  / 3.)  [static], [private]
```

3.1.4.142 epsabs_

```
double RGESolver::epsabs_ = 0.0001  [private]
```

Absolute error used in the integrator with its default value.

3.1.4.143 epsrel_

```
double RGESolver::epsrel_ = 0.0000000000000001  [private]
```

Relative error used in the integrator with its default value.

().

3.1.4.144 evo_

```
gsl_odeiv2_evolve* RGESolver::evo_ = gsl_odeiv2_evolve_alloc(2558)  [private]
```

3.1.4.145 Eyuk

```
const int RGESolver::Eyuk = (Nyukawa * 2 * DF)  [static], [private]
```

Number of real parameters for each Yukawa matrix.

3.1.4.146 FOUR_THIRDS

```
const double RGESolver::FOUR_THIRDS = (4.  / 3.)  [static], [private]
```

3.1.4.147 g1

```
double RGESolver::g1  [private]
```

g_1

3.1.4.148 g2

```
double RGESolver::g2  [private]
```

g_2

3.1.4.149 g3

```
double RGESolver::g3  [private]
```

g_3

3.1.4.150 Getter2F

```
std::unordered_map<std::string, boost::function<double(int, int) > > RGESolver::Getter2F
[private]
```

3.1.4.151 Getter4F

```
std::unordered_map<std::string, boost::function<double(int, int, int, int) > > RGESolver::↩
Getter4F [private]
```

3.1.4.152 InputScale_SM

```
double RGESolver::InputScale_SM [private]
```

the scale at which the method `GenerateSMInitialConditions` takes the input values for SM parameters.

3.1.4.153 lambda

```
double RGESolver::lambda [private]
```

λ (Higgs quartic coupling)

See https://arxiv.org/pdf/1308.2627.pdf for the normalization

3.1.4.154 mb

```
double RGESolver::mb [private]
```

3.1.4.155 mc

```
double RGESolver::mc [private]
```

3.1.4.156 md

```
double RGESolver::md [private]
```

3.1.4.157 mel

```
double RGESolver::mel  [private]
```

3.1.4.158 mh2

```
double RGESolver::mh2  [private]
```

m_h^2 (Higgs boson mass squared)

See https://arxiv.org/pdf/1308.2627.pdf for the normalization

3.1.4.159 mmu

```
double RGESolver::mmu  [private]
```

3.1.4.160 ms

```
double RGESolver::ms  [private]
```

3.1.4.161 mt

```
double RGESolver::mt  [private]
```

3.1.4.162 mtau

```
double RGESolver::mtau  [private]
```

3.1.4.163 mu

```
double RGESolver::mu  [private]
```

m_u , the mass of up quark in GeV (default value ?????).

3.1.4.164 N1

```
const int RGESolver::N1 = 4  [static], [private]
```

3.1.4.165 N23

```
const int RGESolver::N23 = 3  [static], [private]
```

3.1.4.166 N4

```
const int RGESolver::N4 = 8  [static], [private]
```

3.1.4.167 N5

```
const int RGESolver::N5 = 3  [static], [private]
```

3.1.4.168 N6

```
const int RGESolver::N6 = 8  [static], [private]
```

3.1.4.169 N7

```
const int RGESolver::N7 = 8  [static], [private]
```

3.1.4.170 N7H

```
const int RGESolver::N7H = 7  [static], [private]
```

Number of Hermitian operators in class 7.

3.1.4.171 N7NH

```
const int RGESolver::N7NH = 1  [static], [private]
```

Number of non-Hermitian operators in class 7.

3.1.4.172 N8_LLLL

```
const int RGESolver::N8_LLLL = 5  [static], [private]
```

3.1.4.173 N8_LLRR

```
const int RGESolver::N8_LLRR = 8  [static], [private]
```

3.1.4.174 N8_LRLR

```
const int RGESolver::N8_LRLR = 4  [static], [private]
```

3.1.4.175 N8_LRRL

```
const int RGESolver::N8_LRRL = 1  [static], [private]
```

3.1.4.176 N8_RRRR

```
const int RGESolver::N8_RRRR = 7  [static], [private]
```

3.1.4.177 NC

```
const double RGESolver::NC = 3.  [static], [private]
```

Number of colors.

3.1.4.178 NC2

```
const double RGESolver::NC2 = 9.  [static], [private]
```

Number of colors squared.

3.1.4.179 NG

```
const int RGESolver::NG = 3  [static], [private]
```

Number of fermion flavours.

3.1.4.180 Ngauge

```
const int RGESolver::Ngauge = 3  [static], [private]
```

Number of gauge couplings.

3.1.4.181 Nh

```
const int RGESolver::Nh = 2  [static], [private]
```

Number of Higgs' sector parameters.

3.1.4.182 Nyukawa

```
const int RGESolver::Nyukawa = 3  [static], [private]
```

Number of Yukawa matrices.

3.1.4.183 ONE_SIXTH

```
const double RGESolver::ONE_SIXTH = (1.  / 6.)  [static], [private]
```

3.1.4.184 ONE_THIRD

```
const double RGESolver::ONE_THIRD = (1.  / 3.)  [static], [private]
```

3.1.4.185 Operators0F

```
std::unordered_map<std::string, double*> RGESolver::Operators0F  [private]
```

3.1.4.186 s12

```
double RGESolver::s12  [private]
```

$\sin\theta_{12}$

3.1.4.187 s13

```
double RGESolver::s13  [private]
```

$\sin\theta_{13}$

3.1.4.188 s23

```
double RGESolver::s23  [private]
```

$\sin\theta_{23}$

3.1.4.189 s_

```
gsl_odeiv2_step* RGESolver::s_  [private]
```

Initial value:

```
= gsl_odeiv2_step_alloc(
            gsl_odeiv2_step_rkf45, 2558)
```

3.1.4.190 Setter2F

```
std::unordered_map<std::string, boost::function<void(int, int, double) > > RGESolver::↩
Setter2F  [private]
```

3.1.4.191 Setter4F

```
std::unordered_map<std::string, boost::function<void(int, int, int, int, double) > > RGE↩
Solver::Setter4F  [private]
```

3.1.4.192 step_

```
double RGESolver::step_  [private]
```

Last step used in the integrator.

3.1.4.193 sys_

```
gsl_odeiv2_system RGESolver::sys_ = {func, NULL, 3}  [private]
```

3.1.4.194 TEN_THIRDS

```
const double RGESolver::TEN_THIRDS = (10.  / 3.)  [static], [private]
```

3.1.4.195 TWO_THIRDS

```
const double RGESolver::TWO_THIRDS = (2.  / 3.)  [static], [private]
```

3.1.4.196 WC2I_indices

```
const int RGESolver::WC2I_indices  [static], [private]
```

Initial value:

```
= {
    {0, 1},
    {0, 2},
    {1, 2}
}
```

Independent indices for WC2I.

3.1.4.197 WC2R_indices

```
const int RGESolver::WC2R_indices  [static], [private]
```

Initial value:

```
= {
    {0, 0},
    {0, 1},
    {0, 2},
    {1, 1},
    {1, 2},
    {2, 2}
}
```

Independent indices for WC2R.

3.1.4.198 WC6I_indices

```
const int RGESolver::WC6I_indices  [static], [private]
```

Initial value:

```
= {
    {0, 0, 0, 1},
    {0, 0, 0, 2},
    {0, 0, 1, 2},
    {0, 1, 0, 1},
    {0, 1, 0, 2},
    {0, 1, 1, 1},
    {0, 1, 1, 2},
    {0, 1, 2, 0},
    {0, 1, 2, 1},
    {0, 1, 2, 2},
    {0, 2, 0, 2},
    {0, 2, 1, 1},
    {0, 2, 1, 2},
    {0, 2, 2, 1},
    {0, 2, 2, 2},
    {1, 1, 1, 2},
    {1, 2, 1, 2},
    {1, 2, 2, 2}
}
```

Independent indices for WC6I.

3.1.4.199 WC6R_indices

```
const int RGESolver::WC6R_indices  [static], [private]
```

Initial value:

```
= {
    {0, 0, 0, 0},
    {0, 0, 0, 1},
    {0, 0, 0, 2},
    {0, 0, 1, 1},
    {0, 0, 1, 2},
    {0, 0, 2, 2},
    {0, 1, 0, 1},
    {0, 1, 0, 2},
    {0, 1, 1, 0},
    {0, 1, 1, 1},
    {0, 1, 1, 2},
    {0, 1, 2, 0},
    {0, 1, 2, 1},
    {0, 1, 2, 2},
    {0, 2, 0, 2},
    {0, 2, 1, 1},
```

```
    {0, 2, 1, 2},
    {0, 2, 2, 0},
    {0, 2, 2, 1},
    {0, 2, 2, 2},
    {1, 1, 1, 1},
    {1, 1, 1, 2},
    {1, 1, 2, 2},
    {1, 2, 1, 2},
    {1, 2, 2, 1},
    {1, 2, 2, 2},
    {2, 2, 2, 2}
}
```

Independent indices for WC6R.

3.1.4.200 WC7I_indices

```
const int RGESolver::WC7I_indices  [static], [private]
```

Independent indices for WC7I.

3.1.4.201 WC7R_indices

```
const int RGESolver::WC7R_indices  [static], [private]
```

Independent indices for WC7R.

3.1.4.202 WC8I_indices

```
const int RGESolver::WC8I_indices  [static], [private]
```

Initial value:

```
= {
    {0, 0, 0, 1},
    {0, 0, 0, 2},
    {0, 0, 1, 2},
    {0, 1, 0, 1},
    {0, 1, 0, 2},
    {0, 1, 1, 1},
    {0, 1, 1, 2},
    {0, 1, 2, 1},
    {0, 1, 2, 2},
    {0, 2, 0, 2},
    {0, 2, 1, 2},
    {0, 2, 2, 2},
    {1, 1, 1, 2},
    {1, 2, 1, 2},
    {1, 2, 2, 2}
}
```

Independent indices for WC8I.

3.1.4.203 WC8R_indices

```
const int RGESolver::WC8R_indices  [static], [private]
```

Initial value:

```
= {
    {0, 0, 0, 0},
    {0, 0, 0, 1},
    {0, 0, 0, 2},
    {0, 0, 1, 1},
    {0, 0, 1, 2},
    {0, 0, 2, 2},
    {0, 1, 0, 1},
    {0, 1, 0, 2},
    {0, 1, 1, 1},
    {0, 1, 1, 2},
    {0, 1, 2, 1},
    {0, 1, 2, 2},
    {0, 2, 0, 2},
    {0, 2, 1, 2},
    {0, 2, 2, 2},
    {1, 1, 1, 1},
    {1, 1, 1, 2},
    {1, 1, 2, 2},
    {1, 2, 1, 2},
    {1, 2, 2, 2},
    {2, 2, 2, 2}
}
```

Independent indices for WC8R.

3.1.4.204 x

```
double RGESolver::x[2558]  [private]
```

1D array for the integration

3.1.4.205 Yd

```
const double RGESolver::Yd = (- 1.  / 3.)  [static], [private]
```

3.1.4.206 Yd2

```
const double RGESolver::Yd2 = Yd*Yd  [static], [private]
```

3.1.4.207 ydI

```
double RGESolver::ydI[3][3]  [private]
```

3.1.4.208 ydR

```
double RGESolver::ydR[3][3]  [private]
```

3.1.4.209 YdYe

```
const double RGESolver::YdYe = Yd*Ye  [static], [private]
```

3.1.4.210 YdYl

```
const double RGESolver::YdYl = Yd*Yl  [static], [private]
```

3.1.4.211 YdYq

```
const double RGESolver::YdYq = Yd*Yq  [static], [private]
```

3.1.4.212 Ye

```
const double RGESolver::Ye = (- 1.)  [static], [private]
```

3.1.4.213 Ye2

```
const double RGESolver::Ye2 = Ye*Ye  [static], [private]
```

3.1.4.214 yeI

```
double RGESolver::yeI[3][3]  [private]
```

3.1.4.215 yeR

```
double RGESolver::yeR[3][3]  [private]
```

3.1.4.216 YeYl

```
const double RGESolver::YeYl = Ye*Yl  [static], [private]
```

3.1.4.217 YeYq

```
const double RGESolver::YeYq = Ye*Yq  [static], [private]
```

3.1.4.218 Yh

```
const double RGESolver::Yh = (0.5)  [static], [private]
```

3.1.4.219 Yh2

```
const double RGESolver::Yh2 = Yh*Yh  [static], [private]
```

3.1.4.220 YhYd

```
const double RGESolver::YhYd = Yh*Yd  [static], [private]
```

3.1.4.221 YhYe

```
const double RGESolver::YhYe = Yh*Ye  [static], [private]
```

3.1.4.222 YhYl

```
const double RGESolver::YhYl = Yh*Yl  [static], [private]
```

3.1.4.223 YhYq

```
const double RGESolver::YhYq = Yh*Yq  [static], [private]
```

3.1.4.224 YhYu

```
const double RGESolver::YhYu = Yh*Yu  [static], [private]
```

3.1.4.225 Yl

```
const double RGESolver::Yl = (- 0.5)  [static], [private]
```

3.1.4.226 Yl2

```
const double RGESolver::Yl2 = Yl*Yl  [static], [private]
```

3.1.4.227 YlYq

```
const double RGESolver::YlYq = Yl*Yq  [static], [private]
```

3.1.4.228 Yq

```
const double RGESolver::Yq = (1.  / 6.)  [static], [private]
```

3.1.4.229 Yq2

```
const double RGESolver::Yq2 = Yq*Yq  [static], [private]
```

3.1.4.230 Yu

```
const double RGESolver::Yu = (2.  / 3.)  [static], [private]
```

3.1.4.231 Yu2

```
const double RGESolver::Yu2 = Yu*Yu  [static], [private]
```

3.1.4.232 yuI

```
double RGESolver::yuI[3][3]  [private]
```

3.1.4.233 yuR

```
double RGESolver::yuR[3][3]  [private]
```

3.1.4.234 YuYd

```
const double RGESolver::YuYd = Yu*Yd  [static], [private]
```

3.1.4.235 YuYe

```
const double RGESolver::YuYe = Yu*Ye  [static], [private]
```

3.1.4.236 YuYl

```
const double RGESolver::YuYl = Yu*Yl  [static], [private]
```

3.1.4.237 YuYq

```
const double RGESolver::YuYq = Yu*Yq  [static], [private]
```

The documentation for this class was generated from the following files:

- RGESolver.h
- RGESolver.cc
- StaticMembers.cc
- BetaFunction.cc
- SettersAndGetters.cc

Chapter 4

File Documentation

4.1 BetaFunction.cc File Reference

4.2 RGESolver.cc File Reference

```
#include "RGESolver.h"
#include <boost/bind/bind.hpp>
#include "StaticMembers.cc"
#include "SettersAndGetters.cc"
#include "SMInput.cc"
#include "BetaFunction.cc"
```

4.3 RGESolver.h File Reference

```
#include <iostream>
#include <cmath>
#include <fstream>
#include <sstream>
#include <gsl/gsl_errno.h>
#include <gsl/gsl_matrix.h>
#include <gsl/gsl_odeiv2.h>
#include <unordered_map>
#include <boost/function.hpp>
#include "src/gslpp.h"
```

Classes

- class RGESolver

  A class that performs renormalization group evolution in the context of the SMEFT.

4.4 SettersAndGetters.cc File Reference

4.5 StaticMembers.cc File Reference

Index