

# Ejercicio 2.3: Detección y tratamiento de datos atípicos univariante y bivariante

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## Lectura Fichero de datos

```
data <- read.csv("ozone.csv") # import data  
data$Month<-as.factor(data$Month)  
data$Day_of_month<-as.factor(data$Day_of_month)  
data$Day_of_week<-as.factor(data$Day_of_week)
```

## Uso de la función outliers() y extreme()

```
source("Funciones_propias.R")
```

```
Attaching package: 'dplyr'
```

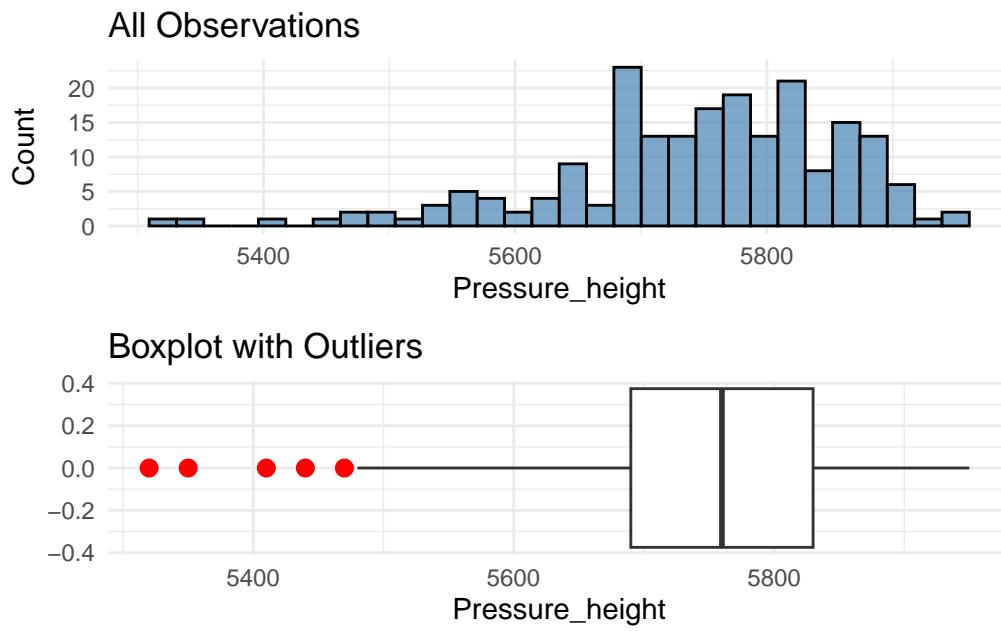
```
The following objects are masked from 'package:stats':
```

```
filter, lag
```

```
The following objects are masked from 'package:base':
```

```
intersect, setdiff, setequal, union
```

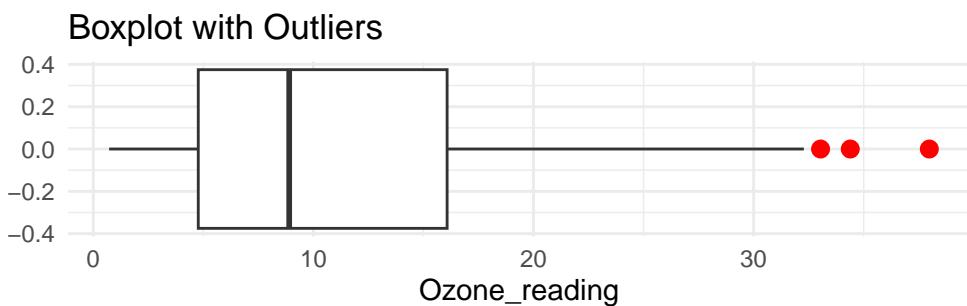
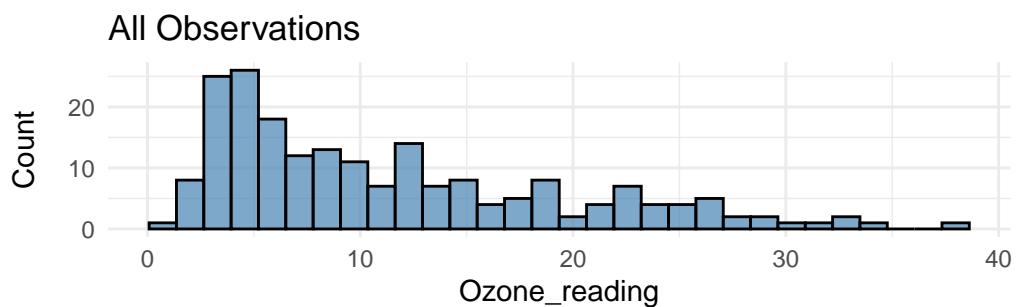
```
outliers(data, "Pressure_height")
```



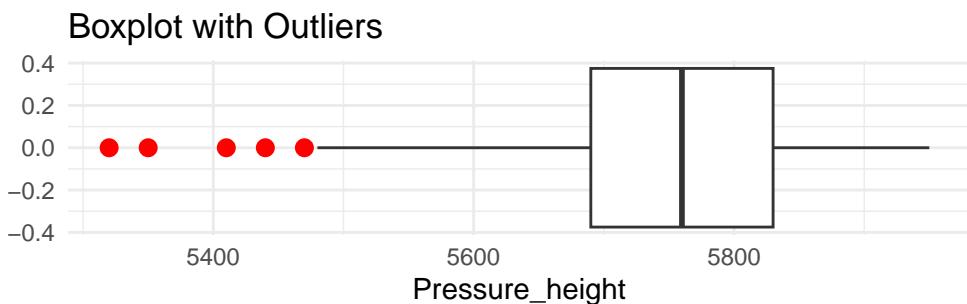
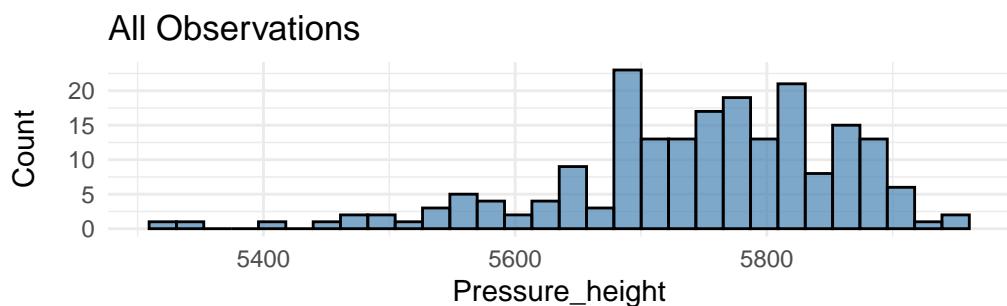
Outliers identified in Pressure\_height : 5 outliers  
 Proportion (%) of outliers: 2.46 %

```
[1] 5410 5350 5470 5320 5440
```

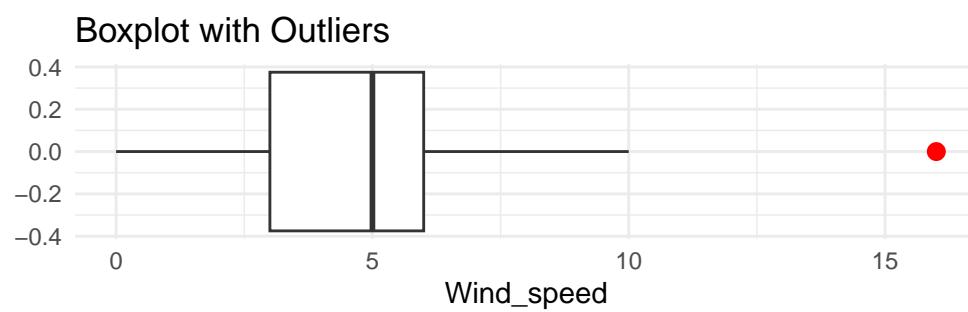
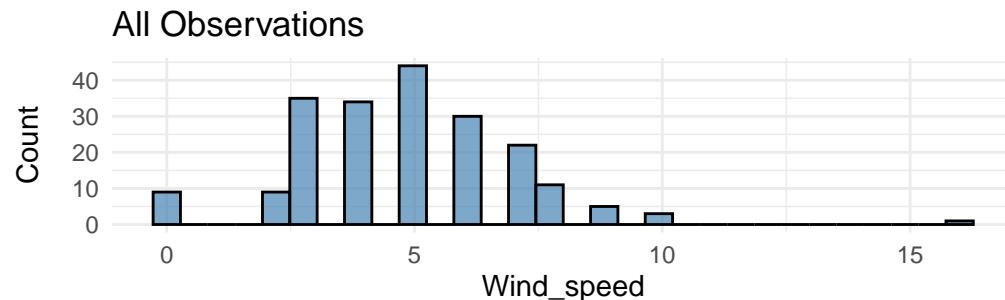
```
# Aplicar la función a múltiples variables numéricas o enteras
numeric_integer_vars <- names(which(sapply(data, is.numeric) | sapply(data, is.integer)))
# Aplicar la función 'outliers' a cada una de las variables numéricas
outliers_results <- lapply(numeric_integer_vars, function(var) {
  outliers(data, var) # Llamar a la función pasando el nombre de la variable
})
```



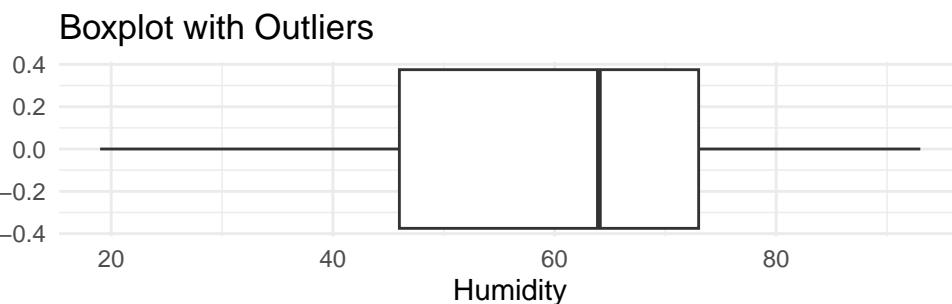
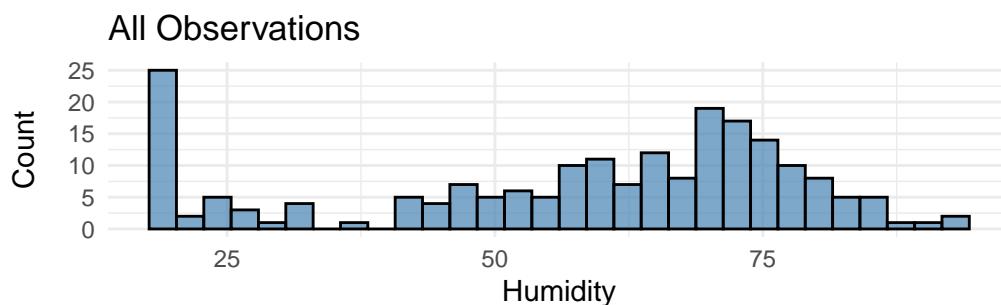
Outliers identified in Ozone\_reading : 3 outliers  
 Proportion (%) of outliers: 1.48 %



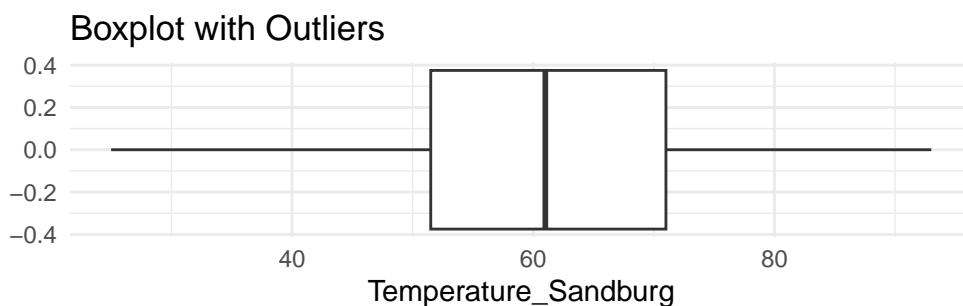
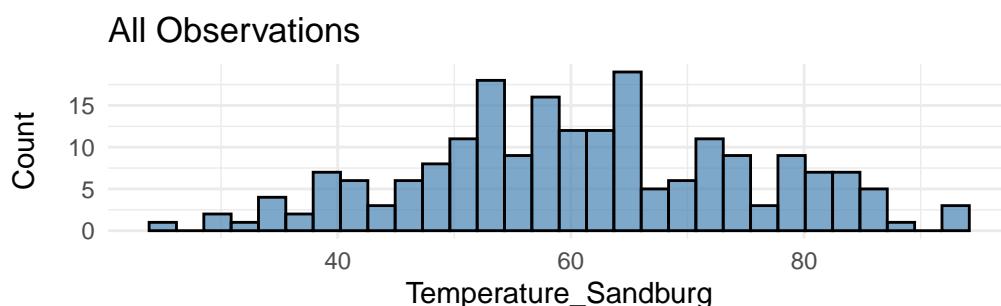
Outliers identified in Pressure\_height : 5 outliers  
Proportion (%) of outliers: 2.46 %



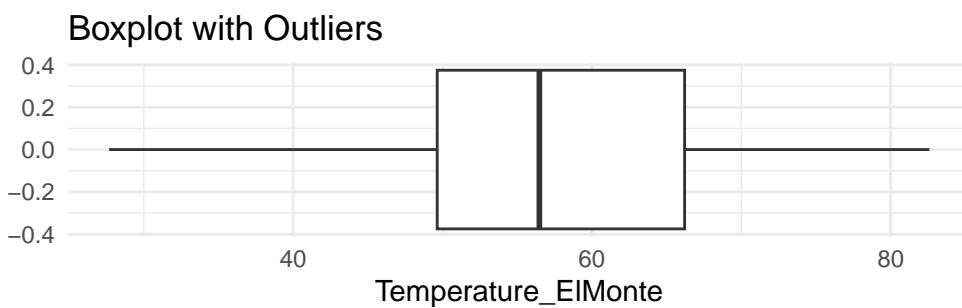
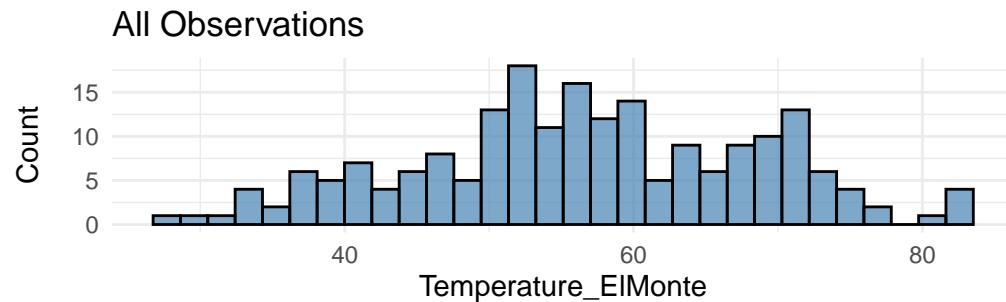
Outliers identified in Wind\_speed : 1 outliers  
Proportion (%) of outliers: 0.49 %



Outliers identified in Humidity : 0 outliers  
 Proportion (%) of outliers: 0 %



Outliers identified in Temperature\_Sandburg : 0 outliers  
Proportion (%) of outliers: 0 %

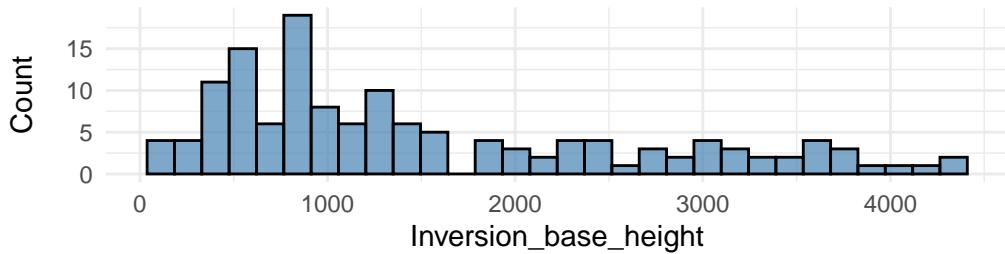


Outliers identified in Temperature\_ElMonte : 0 outliers  
Proportion (%) of outliers: 0 %

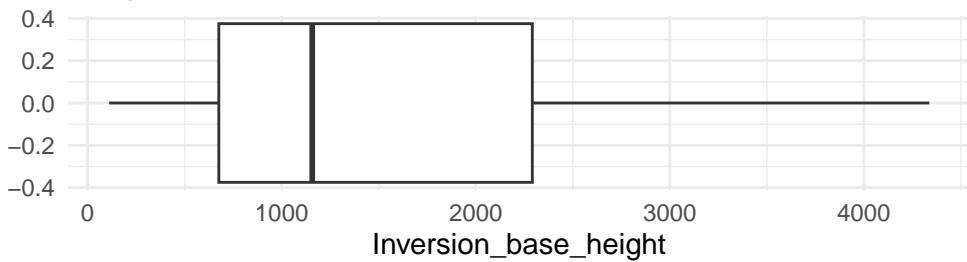
Warning: Removed 63 rows containing non-finite outside the scale range  
(`stat\_bin()`).

Warning: Removed 63 rows containing non-finite outside the scale range  
(`stat\_boxplot()`).

All Observations

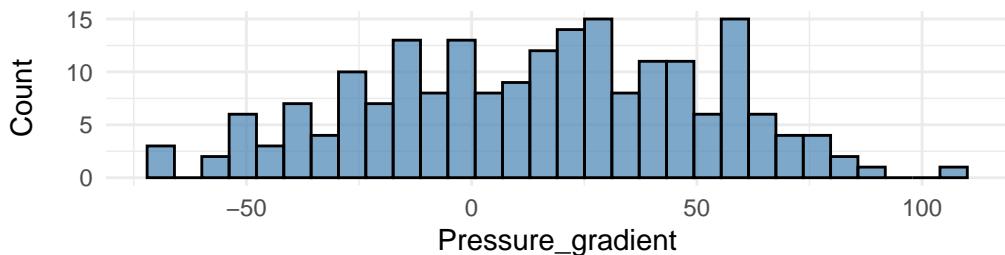


Boxplot with Outliers

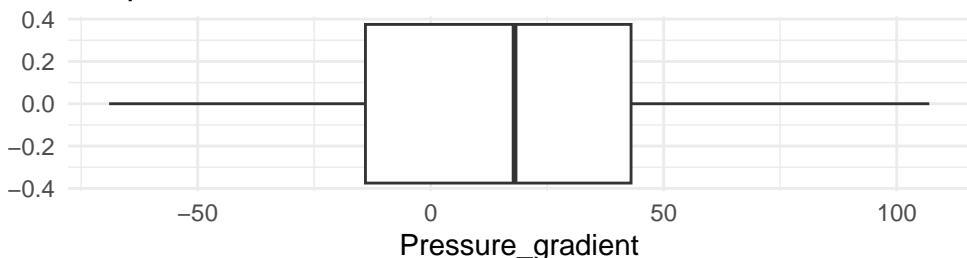


Outliers identified in Inversion\_base\_height : 0 outliers  
Proportion (%) of outliers: 0 %

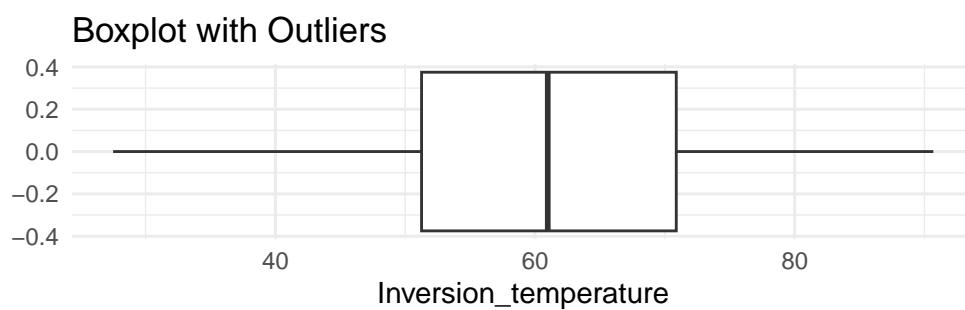
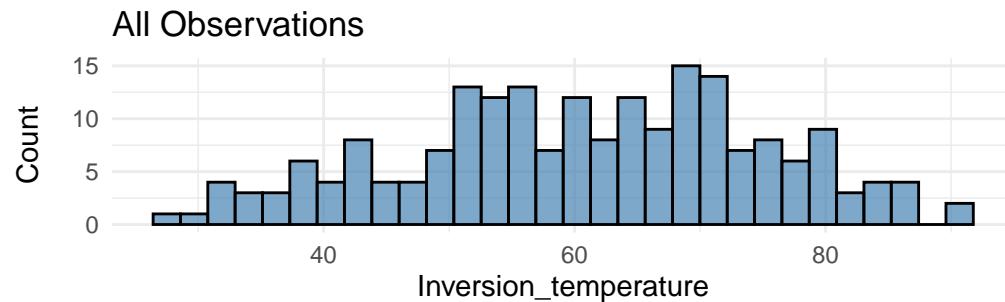
All Observations



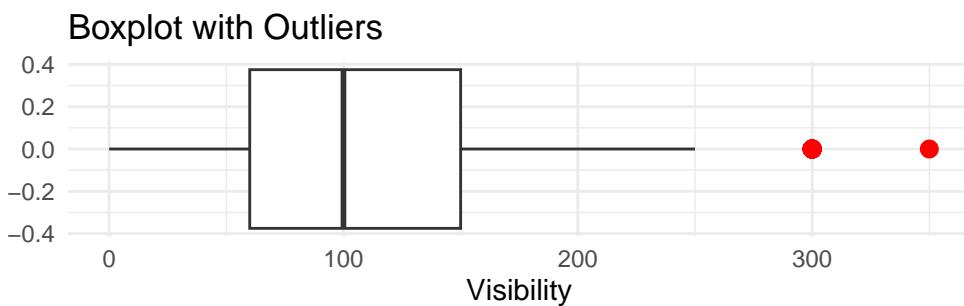
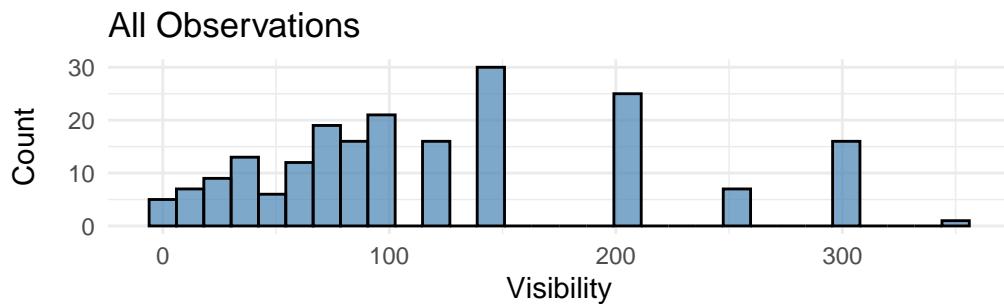
Boxplot with Outliers



Outliers identified in Pressure\_gradient : 0 outliers  
Proportion (%) of outliers: 0 %

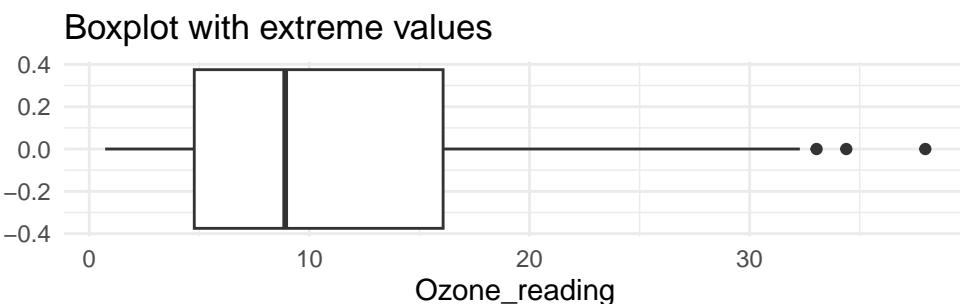
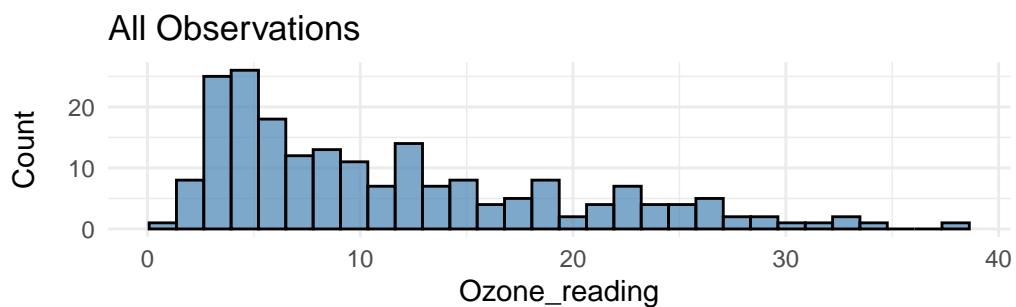


Outliers identified in Inversion\_temperature : 0 outliers  
Proportion (%) of outliers: 0 %

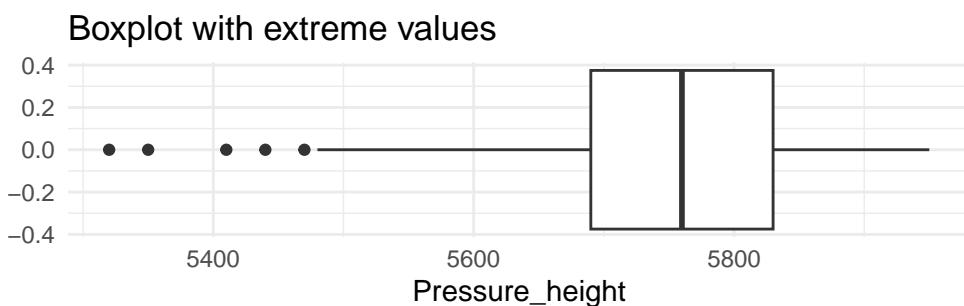
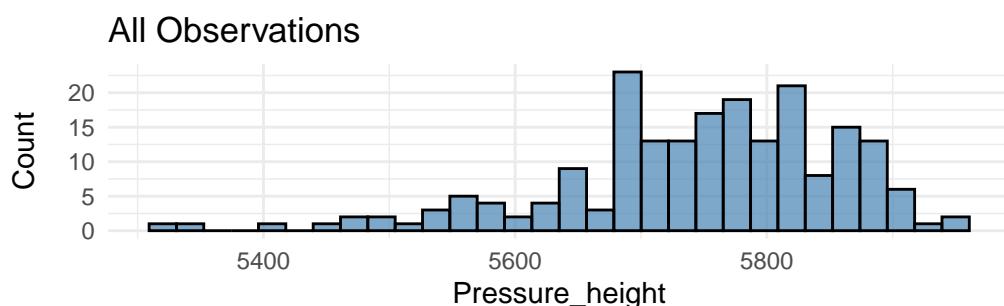


Outliers identified in Visibility : 17 outliers  
 Proportion (%) of outliers: 8.37 %

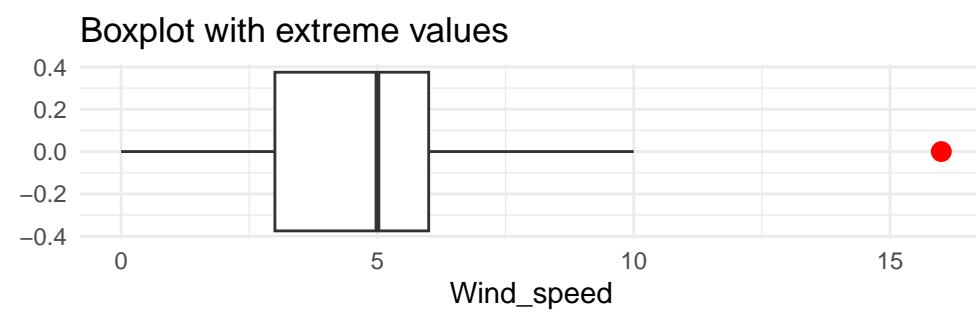
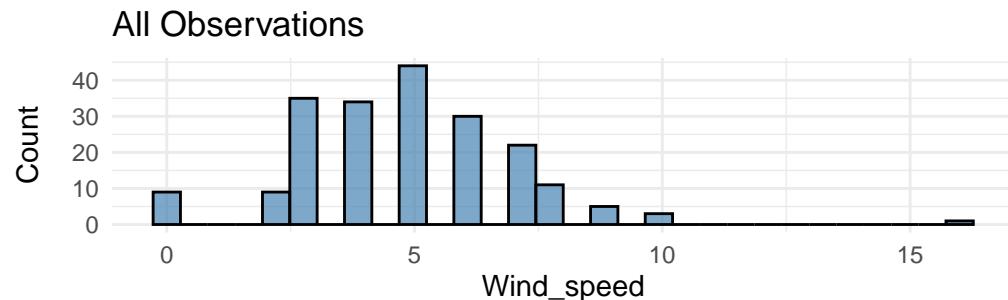
```
extreme_results <- lapply(numeric_integer_vars, function(var) {
  extreme(data, var) # Llamar a la función pasando el nombre de la variable
})
```



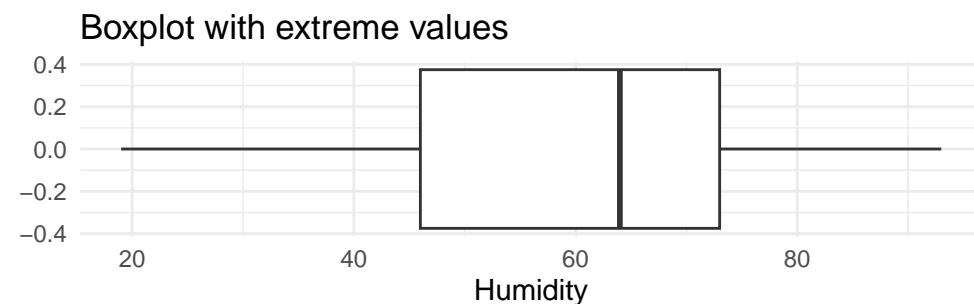
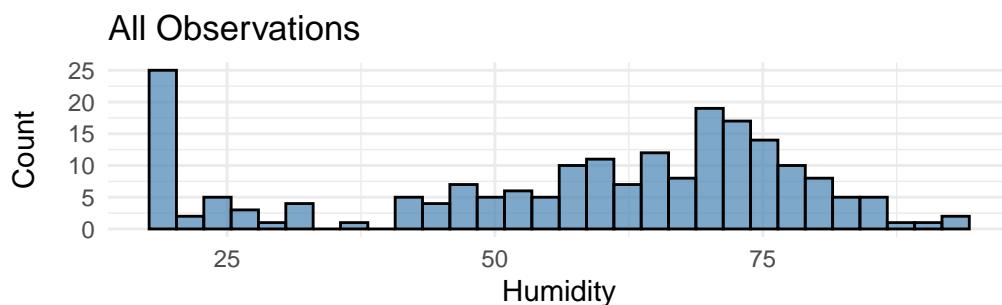
Outliers identified in Ozone\_reading : 0 extreme values  
 Proportion (%) of extreme values: 0 %



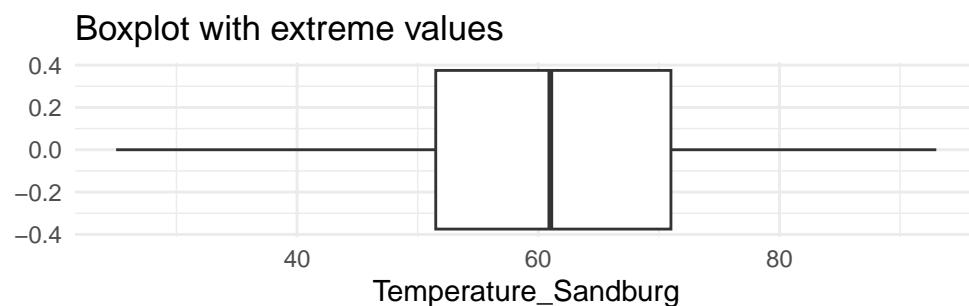
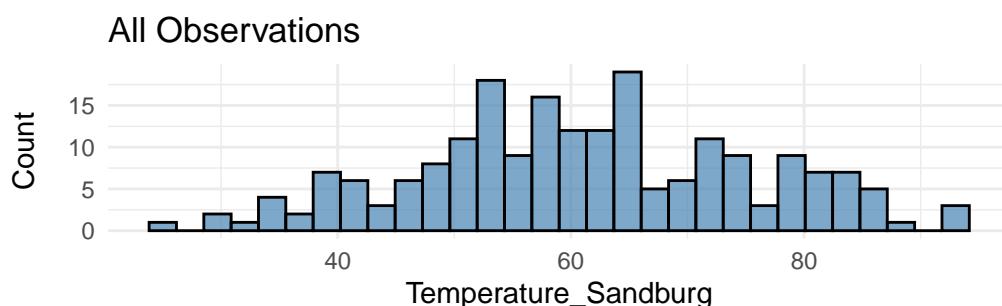
Outliers identified in Pressure\_height : 0 extreme values  
Proportion (%) of extreme values: 0 %



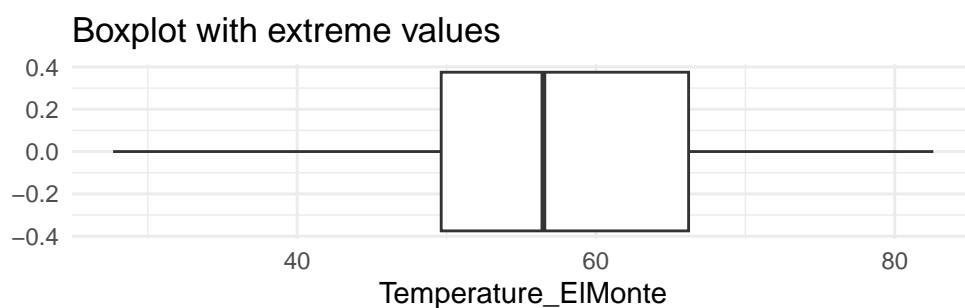
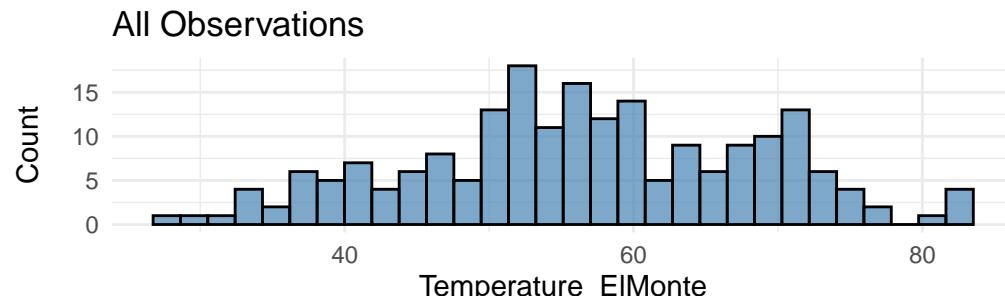
Outliers identified in Wind\_speed : 1 extreme values  
Proportion (%) of extreme values: 0.49 %



Outliers identified in Humidity : 0 extreme values  
 Proportion (%) of extreme values: 0 %

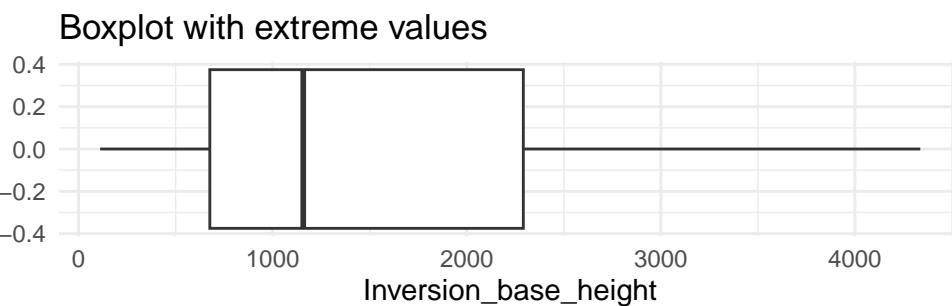
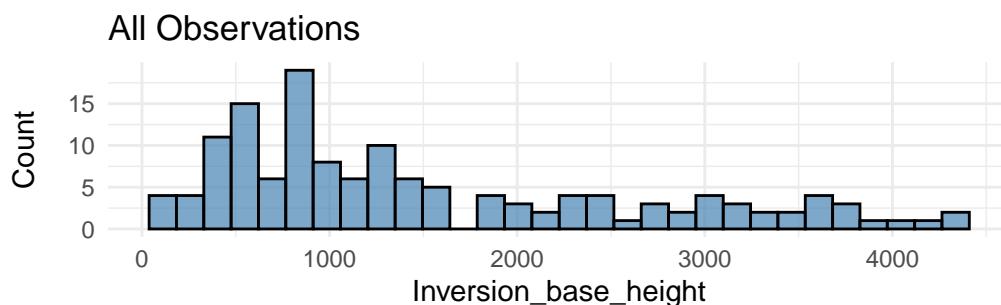


Outliers identified in Temperature\_Sandburg : 0 extreme values  
Proportion (%) of extreme values: 0 %

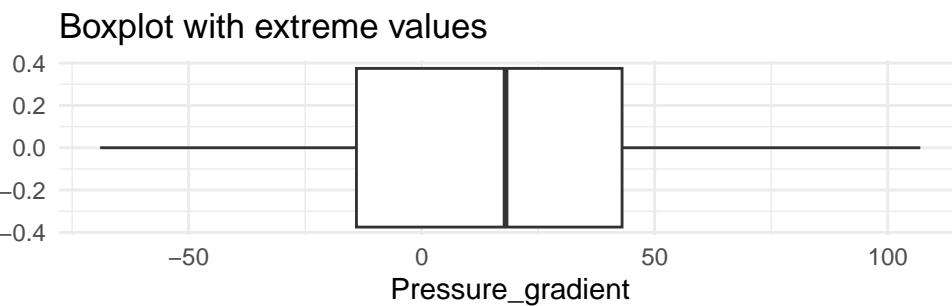
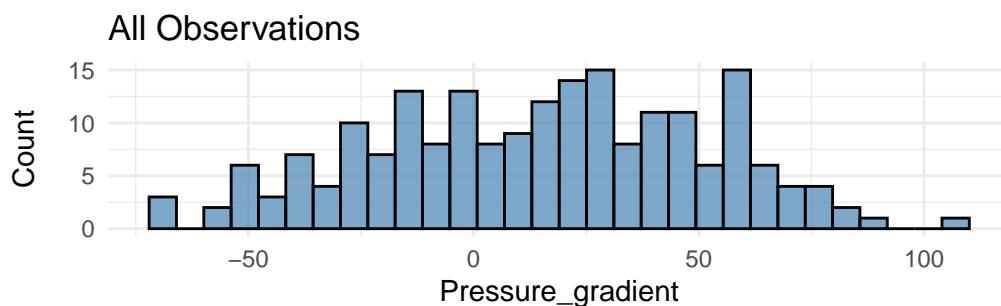


Outliers identified in Temperature\_ElMonte : 0 extreme values  
Proportion (%) of extreme values: 0 %

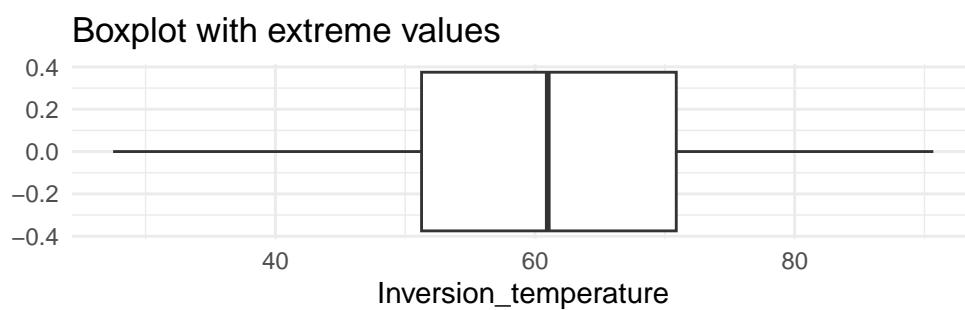
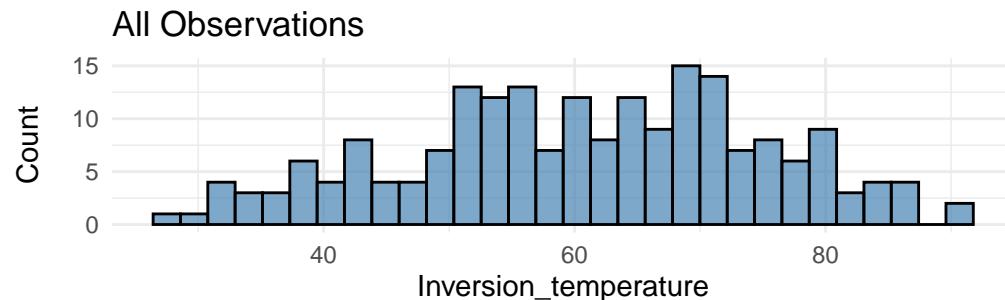
Warning: Removed 63 rows containing non-finite outside the scale range (`stat\_bin()`).  
Removed 63 rows containing non-finite outside the scale range  
(`stat\_boxplot()`).



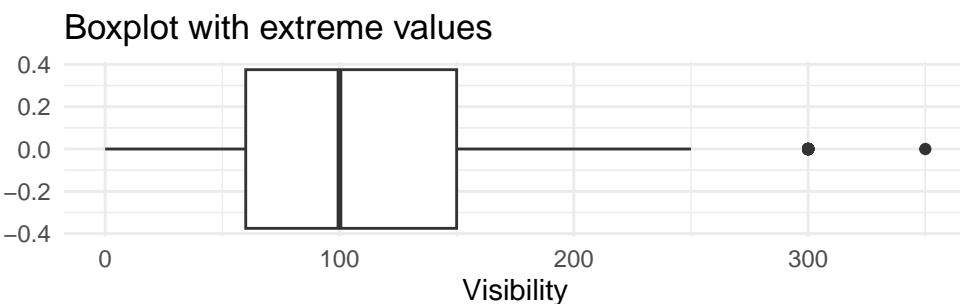
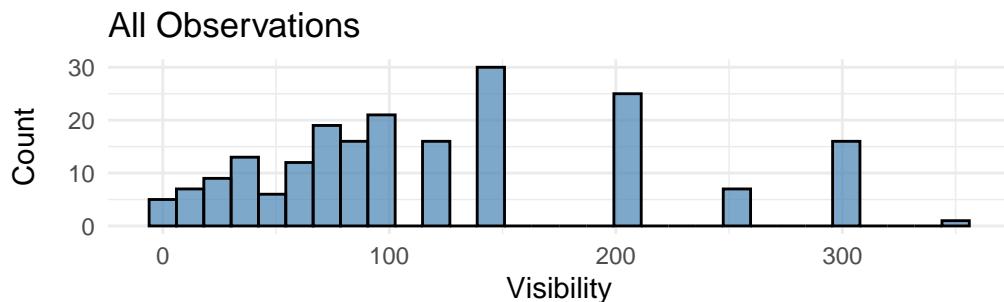
Outliers identified in Inversion\_base\_height : 0 extreme values  
Proportion (%) of extreme values: 0 %



Outliers identified in Pressure\_gradient : 0 extreme values  
Proportion (%) of extreme values: 0 %



Outliers identified in Inversion\_temperature : 0 extreme values  
Proportion (%) of extreme values: 0 %



Outliers identified in Visibility : 0 extreme values  
 Proportion (%) of extreme values: 0 %

Las variables con datos atípicos son:

**Pressure\_height** (2.46%): valores muy pequeños que parecen parte de una distribución asimétrica

**Ozone\_reading** (1.48%): valores muy grandes que parecen parte de una distribución asimétrica

**Wind\_speed** (0.49%): Valor que es también extremo y que se sale completamente de la distribución

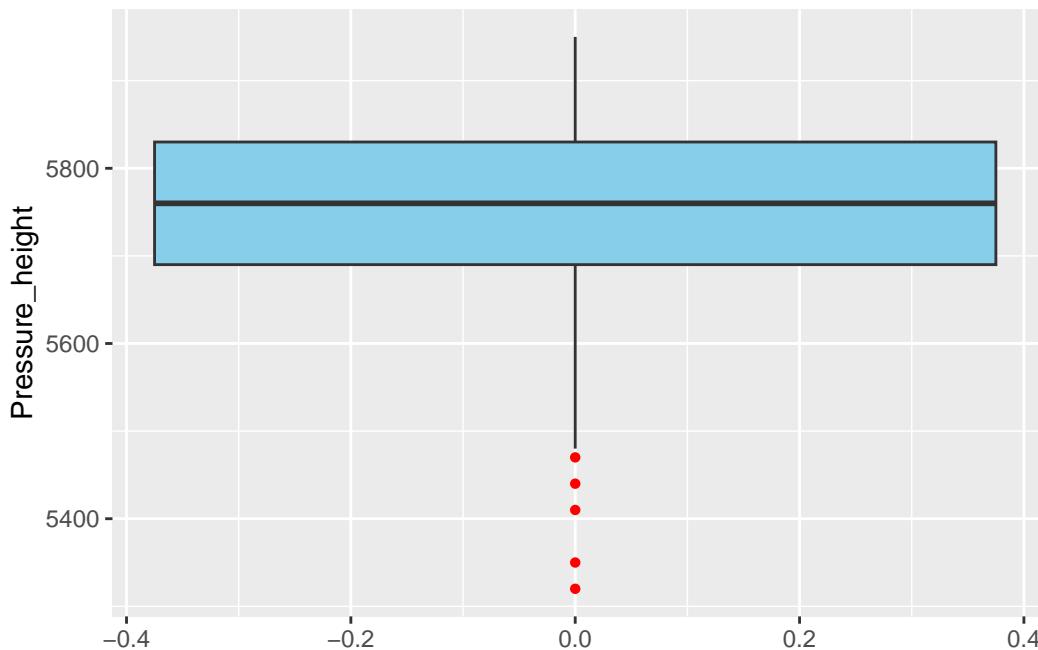
**Visibility** (8.37%): Valores que corresponden a los mismos valores de 300 y 350 que parecen claramente parte de la variable. Además es un número muy elevado como para ser dato atípico.

De todos los outliers el único que se ve como extremo es un valor en **Wind\_speed**

Vamos por tanto a realizar el estudio bivariante de **Pressure\_height**, **Ozone\_reading** y **Wind\_speed**

## Estudio de la variable Pressure\_height

```
##### Pressure height #####
ggplot(data, aes(y = Pressure_height)) +
  geom_boxplot(fill = "skyblue", outlier.color = "red", outlier.shape = 16)
```



```
## Los valores atípicos son:
outlier_values <- boxplot.stats(data$Pressure_height)$out # outlier values.
out_ind <- which(data$Ozone_reading %in% c(outlier_values))
data[out_ind,]
```

```
[1] Month           Day_of_month      Day_of_week
[4] Ozone_reading   Pressure_height    Wind_speed
[7] Humidity         Temperature_Sandburg Temperature_ElMonte
[10] Inversion_base_height Pressure_gradient Inversion_temperature
[13] Visibility
<0 rows> (or 0-length row.names)
```

```
## Los valores extremos son:
extreme_values <- boxplot.stats(data$Pressure_height, coef=3)$out # extreme values.
```

```
ext_ind <- which(data$Pressure_height %in% c(extreme_values))
data[ext_ind,]
```

```
[1] Month           Day_of_month      Day_of_week
[4] Ozone_reading  Pressure_height   Wind_speed
[7] Humidity        Temperature_Sandburg Temperature_ElMonte
[10] Inversion_base_height Pressure_gradient Inversion_temperature
[13] Visibility
<0 rows> (or 0-length row.names)
```

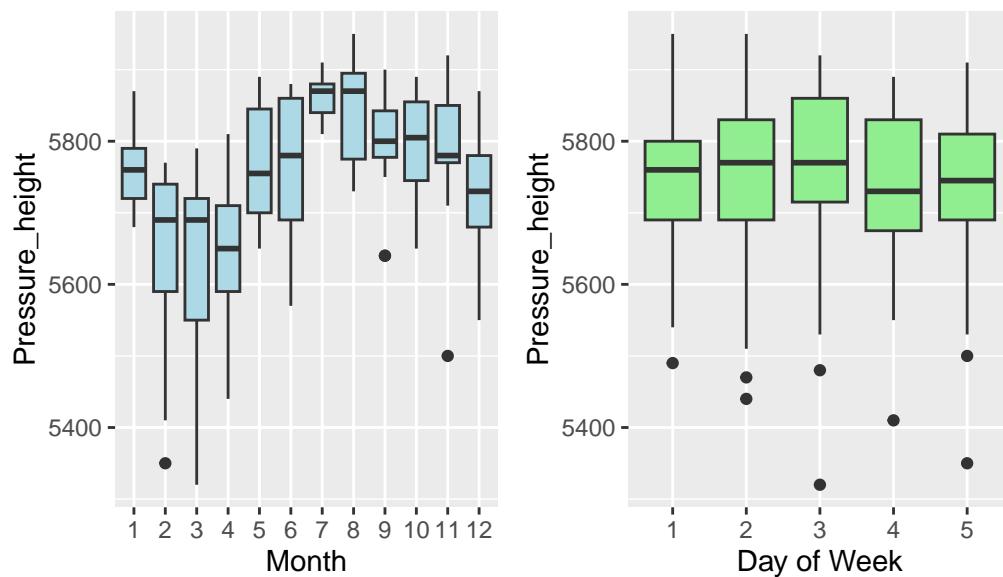
```
library(patchwork) # Para combinar gráficos fácilmente

# Gráfico 1: Pressure Height por mes
p1 <- ggplot(data, aes(x = as.factor(Month), y = Pressure_height)) +
  geom_boxplot(fill = "lightblue") +
  labs(title = "Pressure_height across months", x = "Month", y = "Pressure_height")

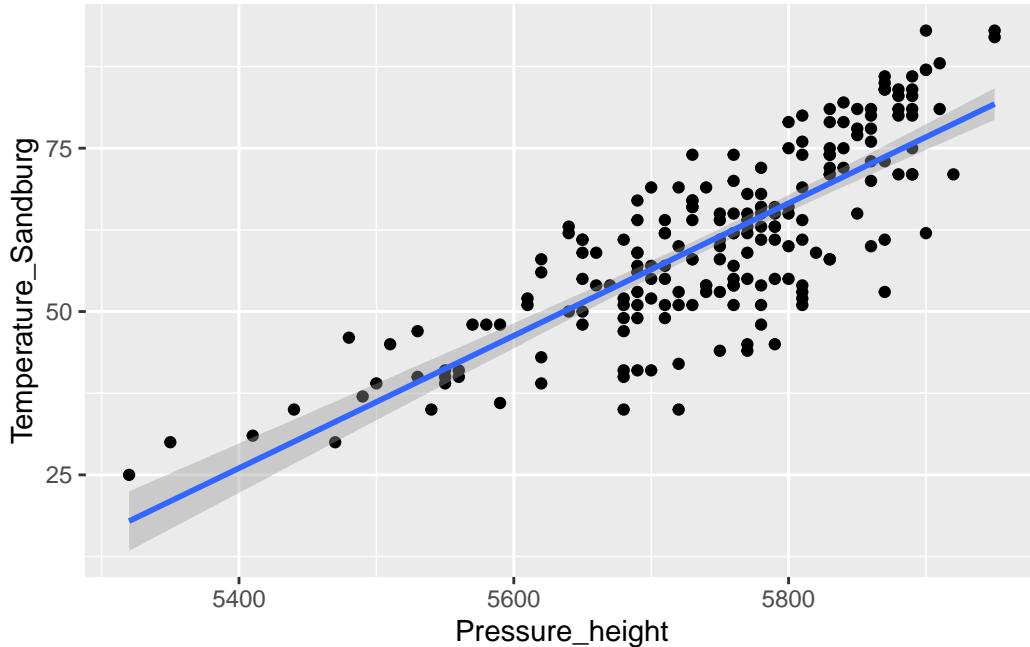
# Gráfico 2: Pressure Height por día de la semana
p2 <- ggplot(data, aes(x = as.factor(Day_of_week), y = Pressure_height)) +
  geom_boxplot(fill = "lightgreen") +
  labs(title = "Pressure_height for days of week", x = "Day of Week", y = "Pressure_height")

# Combinar ambos gráficos en una fila
p1 + p2
```

Pressure\_height across months Pressure\_height for days o



```
ggp <- ggplot(data,aes(Pressure_height, Temperature_Sandburg)) + geom_point()
ggp + stat_smooth(method = "lm",
                  formula = y ~ x,
                  geom = "smooth")
```



```
summary(lm(data$Pressure_height~data$Temperature_Sandburg))
```

Call:

```
lm(formula = data$Pressure_height ~ data$Temperature_Sandburg)
```

Residuals:

Min	1Q	Median	3Q	Max
-196.559	-41.846	1.171	39.099	175.891

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	5354.1021	20.8228	257.13	<2e-16 ***
data\$Temperature_Sandburg	6.4152	0.3319	19.33	<2e-16 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 67.02 on 201 degrees of freedom

Multiple R-squared: 0.6502, Adjusted R-squared: 0.6484

F-statistic: 373.6 on 1 and 201 DF, p-value: < 2.2e-16

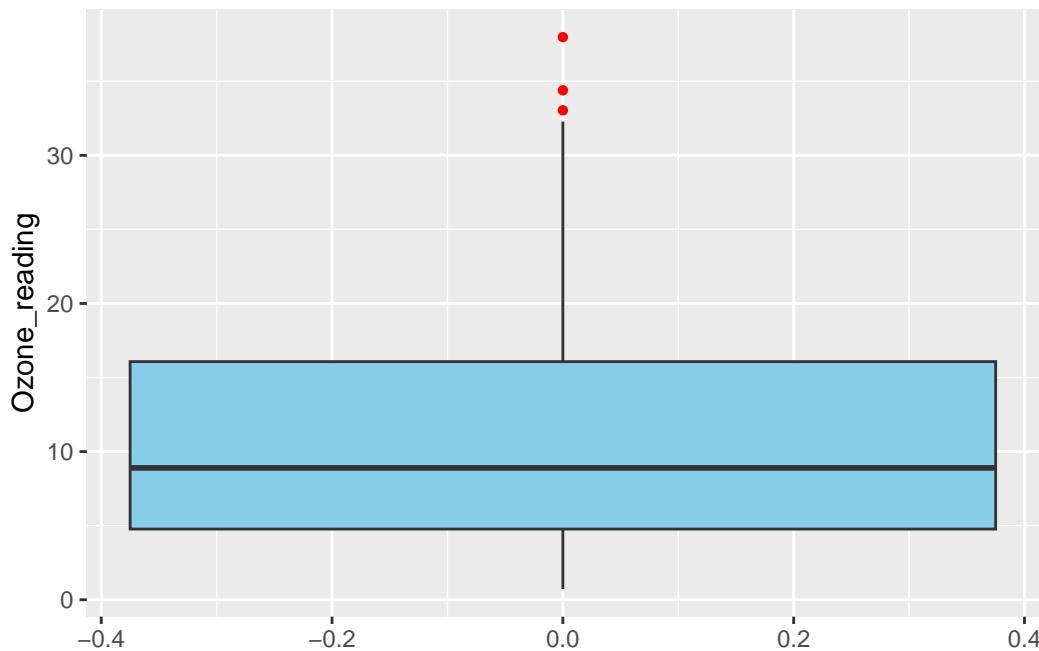
Esta variable está claramente asociada con los meses del año, perteneciendo los valores más

altos de esta variable a los meses de verano. Además vemos una clara asoaciación con la variable de temperatura.

CONCLUSIÓN: No borramos estos valores atípicos porque son parte de una asociación,

## Estudio de la variable Ozone Reading

```
##### OZONE READING #####
ggplot(data, aes(y = Ozone_reading)) +
  geom_boxplot(fill = "skyblue", outlier.color = "red", outlier.shape = 16)
```



```
##Los valores atípicos son:
outlier_values <- boxplot.stats(data$Ozone_reading)$out # outlier values.
out_ind <- which(data$Ozone_reading %in% c(outlier_values))
data[out_ind,]
```

Month	Day_of_month	Day_of_week	Ozone_reading	Pressure_height	Wind_speed
82	5	12	3	33.04	5880
104	7	6	2	34.39	5900
130	8	30	1	37.98	5950

	Humidity	Temperature_Sandburg	Temperature_ElMonte	Inversion_base_height
82	80	80	73.04	436
104	86	87	81.68	990
130	62	92	82.40	557
	Pressure_gradient	Inversion_temperature	Visibility	
82	0	86.36	40	
104	22	85.10	40	
130	0	90.68	70	

```
###Los valores extremos son:
extreme_values <- boxplot.stats(data$Ozone_reading,coef=3)$out # extreme values.
ext_ind <- which(data$Ozone_reading %in% c(extreme_values))
data[ext_ind,]
```

```
[1] Month                  Day_of_month          Day_of_week
[4] Ozone_reading         Pressure_height       Wind_speed
[7] Humidity               Temperature_Sandburg Temperature_ElMonte
[10] Inversion_base_height Pressure_gradient     Inversion_temperature
[13] Visibility
<0 rows> (or 0-length row.names)
```

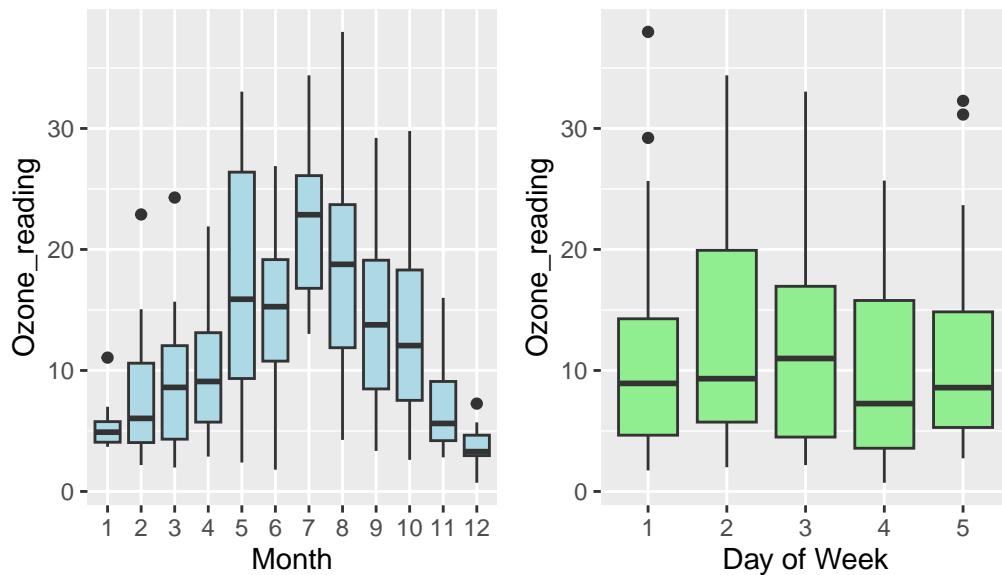
```
library(patchwork) # Para combinar gráficos fácilmente

# Gráfico 1: Ozone_reading por mes
p1 <- ggplot(data, aes(x = as.factor(Month), y = Ozone_reading)) +
  geom_boxplot(fill = "lightblue") +
  labs(title = "Ozone_reading across months", x = "Month", y = "Ozone_reading")

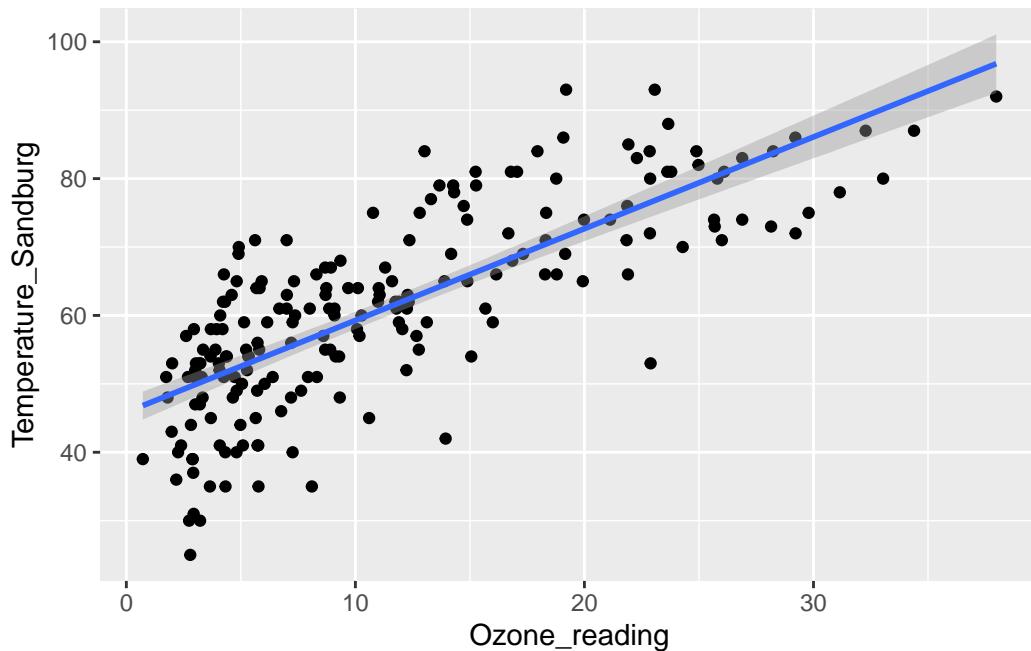
# Gráfico 2: Ozone_reading por día de la semana
p2 <- ggplot(data, aes(x = as.factor(Day_of_week), y = Ozone_reading)) +
  geom_boxplot(fill = "lightgreen") +
  labs(title = "Ozone_reading for days of week", x = "Day of Week", y = "Ozone_reading")

# Combinar ambos gráficos en una fila
p1 + p2
```

Ozone\_reading across months      Ozone\_reading for days of w



```
ggp <- ggplot(data,aes(Ozone_reading, Temperature_Sandburg)) + geom_point()
ggp + stat_smooth(method = "lm",
                  formula = y ~ x,
                  geom = "smooth")
```



```
summary(lm(data$Ozone_reading ~ data$Temperature_Sandburg))
```

Call:

```
lm(formula = data$Ozone_reading ~ data$Temperature_Sandburg)
```

Residuals:

Min	1Q	Median	3Q	Max
-10.4273	-3.8316	-0.4737	3.2197	15.1344

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-15.88133	1.61779	-9.817	<2e-16 ***
data\$Temperature_Sandburg	0.44598	0.02579	17.294	<2e-16 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 5.207 on 201 degrees of freedom

Multiple R-squared: 0.5981, Adjusted R-squared: 0.5961

F-statistic: 299.1 on 1 and 201 DF, p-value: < 2.2e-16

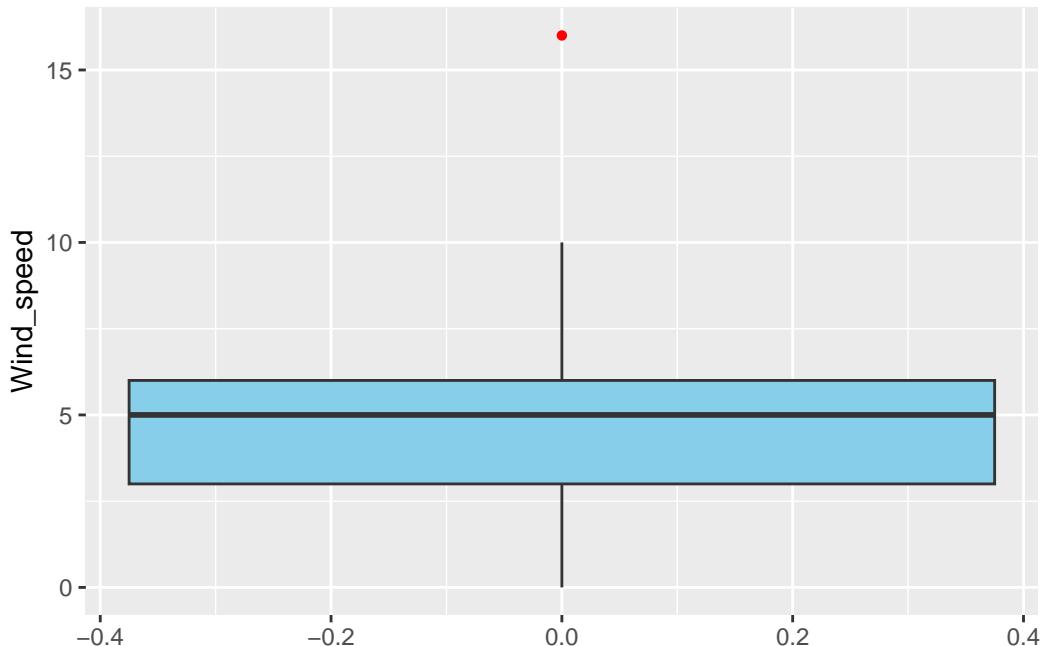
De la misma forma que la variable anterior, esta variable está claramente asociada con los

meses del año, perteneciendo los valores más altos de esta variable a los meses de verano. Además vemos una clara asoaciación con la variable de temperatura.

CONCLUSIÓN: No borramos estos valores atípicos porque son parte de una asociación

## Estudio de la variable WIND SPEED

```
ggplot(data, aes(y = Wind_speed)) +  
  geom_boxplot(fill = "skyblue", outlier.color = "red", outlier.shape = 16)
```



```
###Los valores atípicos son:  
outlier_values <- boxplot.stats(data$Wind_speed)$out # outlier values.  
out_ind <- which(data$Wind_speed %in% c(outlier_values))  
data[out_ind,]
```

	Month	Day_of_month	Day_of_week	Ozone_reading	Pressure_height	Wind_speed
37	3	3	3	2.79	5320	16
	Humidity	Temperature_Sandburg	Temperature_ElMonte	Inversion_base_height		
37	45		25	27.68		NA
	Pressure_gradient	Inversion_temperature	Visibility			
37		39		27.5	200	

```

###Los valores extremos son:
extreme_values <- boxplot.stats(data$Wind_speed,coef=3)$out # extreme values.
ext_ind <- which(data$Wind_speed %in% c(extreme_values))
data[ext_ind,]

```

	Month	Day_of_month	Day_of_week	Ozone_reading	Pressure_height	Wind_speed
37	3	3	3	2.79	5320	16
	Humidity	Temperature_Sandburg	Temperature_ElMonte	Inversion_base_height		
37	45		25	27.68		NA
	Pressure_gradient	Inversion_temperature	Visibility			
37		39		27.5	200	

```

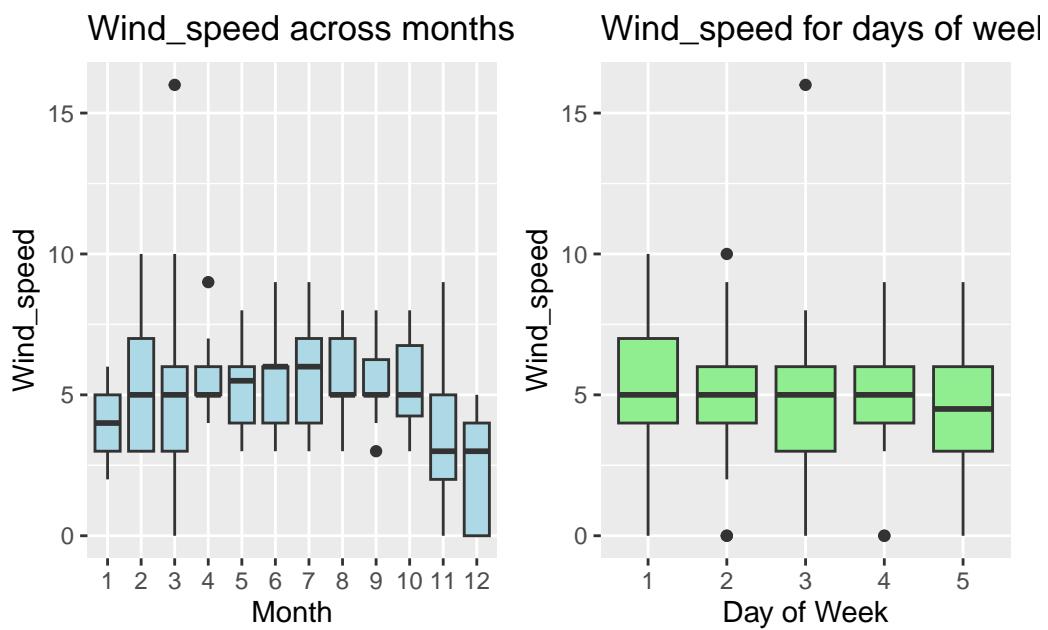
library(patchwork) # Para combinar gráficos fácilmente

# Gráfico 1: Pressure Height por mes
p1 <- ggplot(data, aes(x = as.factor(Month), y = Wind_speed)) +
  geom_boxplot(fill = "lightblue") +
  labs(title = "Wind_speed across months", x = "Month", y = "Wind_speed")

# Gráfico 2: Pressure Height por día de la semana
p2 <- ggplot(data, aes(x = as.factor(Day_of_week), y = Wind_speed)) +
  geom_boxplot(fill = "lightgreen") +
  labs(title = "Wind_speed for days of week", x = "Day of Week", y = "Wind_speed")

# Combinar ambos gráficos en una fila
p1 + p2

```



En este caso vemos que el outlier de `wind_speed` no está asociado con las variables de interés y además es un extremo.

**CONCLUSIÓN:** Este outlier no tiene ninguna asociación aparente, por tanto este dato missing si lo quitamos

```
outlier_values <- boxplot.stats(data$Wind_speed)$out # outlier values.
out_ind <- which(data$Wind_speed %in% c(outlier_values))
data[out_ind,"Wind_speed"]<-NA
```