

The General Nesting Logit (GNL) Model using Aggregate Data

Andre de Palma and Julien Monardo (2017)

Presented by Silvio Ravaioli

June 27, 2019

Preview of the Paper

- ▶ Demand estimation with aggregate data (representative agent)
- ▶ General equivalence between discrete choice and rational inattention model
- ▶ In the General Nesting Logit products can be independent, substitutable, or complementary
- ▶ Linear regression of market shares on product characteristics and “nesting” terms
- ▶ Pro: good parsimony/flexibility compromise to add compl.
- ▶ Con: it requires external definition of criteria (nests)
- ▶ Simple application: brand/segment substitutability for cereals (Dominick’s database)

Thoughts for the Discussion

- ▶ **General equivalence between discrete choice and rational inattention model**
- ▶ What does RI represent in a traditional market (e.g. cereals)?
- ▶ In the General Nesting Logit products can be independent, substitutable, or complementary
- ▶ When do we need this flexibility?
- ▶ How can we *really* connect discrete choice and rational inattention?

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Key References - Matejka & McKay (AER 2015)

- ▶ **Rational Inattention to Discrete Choices: A New Foundation for the Multinomial Logit Model**
- ▶ Equivalence between discrete choice model with ARUM and rational inattention (RI) model with Shannon Entropy
- ▶ Information friction: it is costly to learn true payoffs
- ▶ Choice is probabilistic, based on true payoffs, prior beliefs, and attention cost
- ▶ Representative agent
- ▶ One-shot decision (no memory, learning, or communication)
- ▶ Continuous state and signals [State-Signal-Action model]
- ▶ Shannon Entropy assumption

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► Generalized Entropy Models

- Extension of Matejka-McKay based on a generalization of Shannon entropy
- Entropy cost component expresses *taste for variety* rich complementarity/substitutability pattern
- Dual representation of discrete choice ARUM (requires substitutability)
- Some generalized entropy models lead to demand systems that cannot be rationalized under any ARUM
- Demand models can be estimated by linear regressions - invert market shares to find implied mean utility as in Berry (1994)
- Theoretical backbone for this paper

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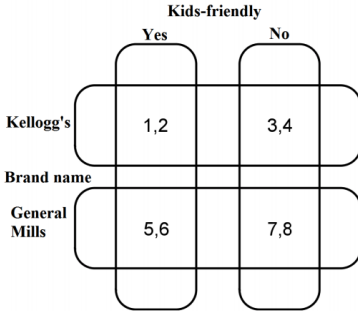
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- ▶ **Fosgerau, Melo, De Palma, and Shum (WP 2017) Discrete Choice and RI: A General Equivalence Result**
- ▶ *When information costs are modelled using a class of generalized entropy functions, the choice probabilities in any rational inattention model are observationally equivalent to some additive random utility discrete choice model and vice versa*
- ▶ *Any ARUM can be given an interpretation in terms of boundedly rational behavior [...although RI is not a case of bounded rationality...]*
- ▶ **Joo (JMP 2019) RI as an Empirical Framework** with an application to the welfare effects of new product introduction and endogenous promotion
- ▶ Welfare calculation differs between RI and RUM
- ▶ Role of information shifters (promotion and consumer inertia)

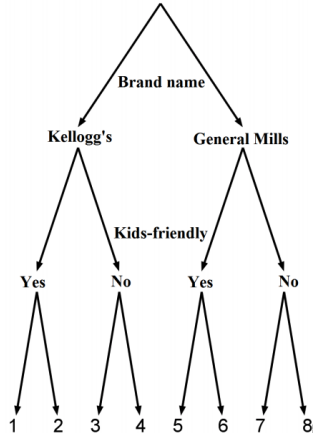
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Example: Market Segmentation for Cereals



Symmetric Structure



Hierarchical Structure

Figure 1: Cereals: symmetric vs. hierarchical structure

Introduction

- ▶ Benchmark: the **nested logit model** accounts for multiple discrete characteristics (criteria) used to partition the choice set into groups (nests).
- ▶ Product choice follows a two (or more)-steps process: choose a group (e.g. cereal segment), then a product from the group
- ▶ **Concerns:** arbitrary hierarchy, restrictive substitution constraints, independence from irrelevant alternatives
- ▶ **Solution:** General Nesting Logit: product differentiation + segmentation (discrete criteria) + no hierarchy + no generalized extreme value
- ▶ Possible applications: incentive to introduce a new product on the market, incentive to bundle products

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Generalized Entropy Model

- ▶ Representative consumer with income y
- ▶ Choice set of differentiated products $\mathcal{J} = \{0, 1, \dots, J\}$
- ▶ Maximization of consumer's utility function: sum of expected utility and a generalized entropy function [deterministic function of the choice vector $q = (q_0, \dots, q_J)$]

$$\max_{q \in \Delta} u(q, y) = \alpha z + \sum_j v_j q_j + \Omega(q)$$

$$\text{subject to budget constraint } y \geq \sum_j p_j q_j + z$$

- ▶ z consumption of the numeraire good
- ▶ α marginal utility of income
- ▶ v_j and p_j are the quality and price of product j
- ▶ $\Omega(q)$ is a generalized entropy function

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Entropy Function

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- ▶ $\Omega : [0, \infty)^{J+1} \rightarrow \mathbb{R} \cup \{-\infty\}$
- ▶ $\Omega(q) = -\sum_j q_j \ln S^{(j)}(q)$ if $q \in \Delta$
- ▶ $\Omega(q) = -\infty$ if $q \notin \Delta$ (feasibility)
- ▶ $S(\cdot) = (S^{(0)}(\cdot), \dots, S^{(J)}(\cdot))$ is a flexible generator which satisfies four conditions [Axiom 1, page 8]
- ▶ $S(q)$ is twice continuously differentiable, homogeneous of degree 1, and globally invertible, the Jacobian of $\ln S$ is positive semi-definite and symmetric, and $-\frac{\partial \Omega(q)}{\partial q_k} = \ln S^{(k)}(q) + 1$
- ▶ The last assumption is crucial to derive a tractable demand

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Main Result: Theorem 1

- ▶ We can define the net utility $\delta_j = v_j - \alpha p_j$ and rewrite the problem as maximization of the utility

$$u(q, y) = \alpha y + \sum_j \delta_j q_j - \sum_j q_j \ln S^{(j)}(q)$$

- ▶ **Theorem 1.** [page 9] Let $S(q)$ be a flexible generator satisfying the conditions above. Maximization of utility leads to a demand system with interior solution

$$q_i(\delta) = \frac{H^{(i)}(e^\delta)}{\sum_j H^{(j)}(e^\delta)} \quad \text{where } H^{(i)} = S^{-1(i)}$$

- ▶ When $S(q) = q$ we get Shannon entropy and we are back to logit demand [end of page 9]

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Implications of Theorem 1

- ▶ The demand system generalizes the logit demand
- ▶ RUM may differ in the RU distribution assumptions
- ▶ GEM may differ in the specifications of S
- ▶ For any ARUM there exists a GEM that leads to the same demand
- ▶ Some GEM are not consistent with any ARUM
- ▶ Properties of the GEM [pp 10-12]

General Nesting Logit

- ▶ Use product segmentation to add structure to the entropy function
- ▶ Market for differentiated products with segmentation in C criteria (dimensions) that generate nests. Products of the same type (i.e. grouped in all the dimensions) are in the same group
- ▶ Dimensions capture *similarity*: products of the same type are closer substitutes
- ▶ $\sigma_c(j)$ is the set of products grouped together with j on dimension c

$$S^j(q) = \begin{cases} q_0, & \text{if } q \in \Delta, j = 0 \\ q_j^{\mu_0} \prod_c q_{\sigma_c(j)}^{\mu_c}, & \text{if } q \in \Delta, j > 0 \\ -\infty & \text{if } q \notin \Delta \end{cases}$$

By imposing $\mu_c > 0$ and $\mu_0 + \sum_c \mu_c = 1$, $S(\cdot)$ satisfies axiom 1

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Issues with GNL model

- ▶ There is an analytic formula for the **inverse** market shares only. Recovering the market shares requires inverting a system of nonlinear equations (it cannot be performed analytically)
- ▶ A priori symmetric restrictions on the substitution patterns (at the market level) that may hold only at the individual level [same problem as in the family of generalized extreme value models]

Market for Cereals

- ▶ Two dimensions: brand name (Kellogg's or General Mills) and segment (family or kids)
- ▶ The 3-levels NL assumes a hierarchical structure, requires the a priori assumption between two cases, and its generator becomes $S^{(j)}(q) = q_j^{\mu_0} q_{\sigma_1(j)}^{\mu_1} q_{\sigma_2(j)}^{\mu_2}$
- ▶ Note that $\sigma_2(j)$ is a subset of $\sigma_1(j)$
- ▶ GNL model removes the hierarchy assumption and treats the dimensions symmetrically and independently
- ▶ Key difference: $\sigma_2(j)$ is not necessarily a subset of $\sigma_1(j)$
- ▶ GNL is observationally equivalent to the 3-lv NL with nested parameters (γ_1, γ_2) when $\gamma_1 = \mu_1$ and $\gamma_2 = \mu_1 + \mu_2$

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Elasticities [Page 17, Appendix B.2]

- ▶ We can compute the analytic formula for the matrix of own- and cross-price elasticities (not market shares, though)
- ▶ Each criteria has a nesting structure matrix Θ_c
- ▶ Build a market structure matrix

$$\rho(\mu, \Theta) = \left[\mu_0 I_J + \sum_c \mu_c \frac{q_j}{q_{\sigma_c(j)}} \Theta_c \right]^{-1}$$

- ▶ Obtain the matrix of own- and cross- price elasticities

$$\Sigma = \left[\frac{\partial q_j}{\partial p_i} \frac{p_i}{q_j} \right] = -\alpha \text{diag}(pq) \rho(\mu, \Theta) (\text{diag}(1/q) - J_J)$$

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Econometric Setting

- ▶ Net utility for product j

$$\delta_{jt}(\cdot) = \beta_0 + \mathbf{X}_{jt}\beta - \alpha p_{jt} + \xi_{jt}$$

- ▶ Some confusion about ξ_{jt} (unobserved product characteristic):
consider $\xi_{jt} = \xi_j + \xi_t + u_{jt}$
- ▶ Relation between utility and market shares

$$\ln S^{jt}(q; \theta_2) = \delta_{jt}(X, p, \xi; \theta_1) + c_t$$

- ▶ It follows that

$$\ln S^{jt}(q; \theta_2) - \ln S^{0t}(q; \theta_2) = \delta_{jt}(X, p, \xi; \theta_1)$$

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Empirical Application: Demand for Cereals

► Data

- Dominick's Database: ready-to-eat cereals, Chicago, 1991-92
- Segmentation as in Nevo 2001
- Nutrient content from USDA Nutrient Database for Standard Reference
- Price of sugar (instrument)
- Restriction on top 50 brands (73% of sales)
- Market shares calculated based on number of servings

► Descriptive statistics

- Four segments (family, kids, health, taste enhanced)
- Six brand names (General Mills, Kellogg's, Quakers, Post, Nabisco, Ralston)
- 17 types of products

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Identification [pp. 23-25]

- ▶ Unobserved product characteristic $\xi_{jt} = \xi_j + \xi_t + u_{jt}$
- ▶ u_{jt} (residual term) includes advertising, shelf-space, positioning,...
- ▶ Endogeneity: prices and nesting terms
- ▶ Instruments z_t
- ▶ **Characteristics-based instruments:** promotional activity (heterogeneous across stores and time)
- ▶ Number of promoted products in the same segment (NL and GNL) and same type (GNL only)
- ▶ **Cost-based instrument:** input prices. Sugar \times sugar content
- ▶ Instruments are not weak

Results: GNL vs 3-levels NL models

	(1) GNL	(2) 3NL1	(3) 3NL2				
Price ($-\alpha$)	-1.114*** (0.0896)	-2.499*** (0.118)	-2.642*** (0.130)	Fixed Effects Brand Names (θ)			
Segment/nest (μ_1)	0.608*** (0.0102)	0.778*** (0.00882)	0.768*** (0.00996)	Kellogg's (θ_K)	0.0541*** (0.00422)	-0.0429*** (0.00340)	0.160*** (0.00536)
Company/subnest (μ_2)	0.293*** (0.0103)	0.818*** (0.00715)	0.807*** (0.00802)	Nabisco (θ_N)	-0.867*** (0.0275)	-0.207*** (0.0118)	-2.277*** (0.0191)
Promotion (β)	0.0704*** (0.00272)	0.0924*** (0.00326)	0.107*** (0.00348)	Post (θ_P)	-0.545*** (0.0165)	-0.185*** (0.00946)	-1.451*** (0.00858)
Fixed Effects Segments (γ)				Quaker (θ_Q)	-0.573*** (0.0166)	-0.308*** (0.0150)	-1.511*** (0.00669)
Health/nutrition (γ_H)	-0.647*** (0.0110)	-0.876*** (0.00752)	-0.0569*** (0.00567)	Ralston (θ_R)	-0.871*** (0.0277)	-0.228*** (0.0131)	-2.382*** (0.0175)
Kids (γ_K)	-0.435*** (0.00886)	-0.554*** (0.00868)	0.0336*** (0.00443)	Constant (β_0)	-0.141* (0.0570)	0.221*** (0.0668)	-0.102 (0.0678)
Taste enhanced (γ_T)	-0.683*** (0.0114)	-0.926*** (0.00753)	-0.0682*** (0.00586)	Observations	99281	99281	99281
				RMSE	0.237	0.267	0.274
				F-test for price	464.47	514.32	471.42
				F-test for segment/nest	359.01	468.09	467.46
				F-test for brand/subnest	326.60	488.31	464.10

* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$

Parameter estimates from the main specifications

Results: Substitution Patterns

Type	Brand	Segment	Own	Cross							
				General Mills				Kellogg's			
				Family 1	Health 2	Kids 3	Taste 4	Family 5	Health 6	Kids 7	Taste 8
1	General Mills	Family	-2.7524	0.2396	0.1179	0.0896	0.0990	0.0792	-0.0425	-0.0708	-0.0613
2	General Mills	Health/nutrition	-2.7123	0.0775	0.3844	0.0760	0.0815	-0.0455	0.2615	-0.0469	-0.0414
3	General Mills	Kids	-2.9885	0.0664	0.0858	0.2999	0.0799	-0.0286	-0.0092	0.2049	-0.0150
4	General Mills	Taste enhanced	-2.5691	0.0688	0.0864	0.0749	0.3592	-0.0375	-0.0199	-0.0313	0.2529
5	Kelloggs	Family	-2.2305	0.0810	-0.0717	-0.0396	-0.0554	0.2035	0.0509	0.0829	0.0671
6	Kelloggs	Health/nutrition	-2.3392	-0.0312	0.2917	-0.0091	-0.0207	0.0365	0.3594	0.0586	0.0470
7	Kelloggs	Kids	-2.9261	-0.0411	-0.0416	0.1615	-0.0267	0.0475	0.0469	0.2500	0.0618
8	Kelloggs	Taste enhanced	-2.1892	-0.0454	-0.0468	-0.0156	0.2704	0.0488	0.0474	0.0786	0.3643
9	Nabisco	Health/nutrition	-1.5646	0.0011	0.0469	0.0007	0.0013	-0.0022	0.0436	-0.0025	-0.0020
10	Post	Health/nutrition	-1.2850	0.0085	0.1959	-0.0528	-0.0300	-0.0104	0.1770	-0.0718	-0.0489
11	Post	Kids	-2.7172	-0.0054	-0.0516	0.0824	-0.0310	0.0054	-0.0407	0.0932	-0.0201
12	Post	Taste enhanced	-1.6185	-0.0019	-0.0532	-0.0503	0.1695	-0.0012	-0.0525	-0.0496	0.1701
13	Quaker	Family	-1.9753	0.0486	-0.0024	-0.0566	-0.0314	0.0426	-0.0084	-0.0626	-0.0374
14	Quaker	Kids	-1.9466	-0.0111	-0.0033	0.0750	-0.0320	-0.0041	0.0037	0.0820	-0.0249
15	Quaker	Taste enhanced	-1.5042	-0.0073	0.0009	-0.0609	0.1574	-0.0118	-0.0035	-0.0653	0.1529
16	Ralston	Family	-2.1511	0.0211	-0.0016	-0.0209	-0.0018	0.0188	-0.0039	-0.0232	-0.0041
17	Ralston	Kids	-2.8539	-0.0224	-0.0018	0.0649	0.0008	-0.0158	0.0048	0.0715	0.0075

Average price elasticities for the GNL models

Summary

- ▶ Very preliminary version of the paper (no Conclusions)
- ▶ Model (GNL): additional flexibility wrt classic NL allows to generate complementarity, accommodates for more violations of IIA, and requires less a priori assumptions
- ▶ Application (cereals): estimated parameters are highly sensitive to the order of nesting. Top nesting is always estimated as less important (higher substitutability)
- ▶ Relevant implications for counterfactual analysis, product introduction, and bundling

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