

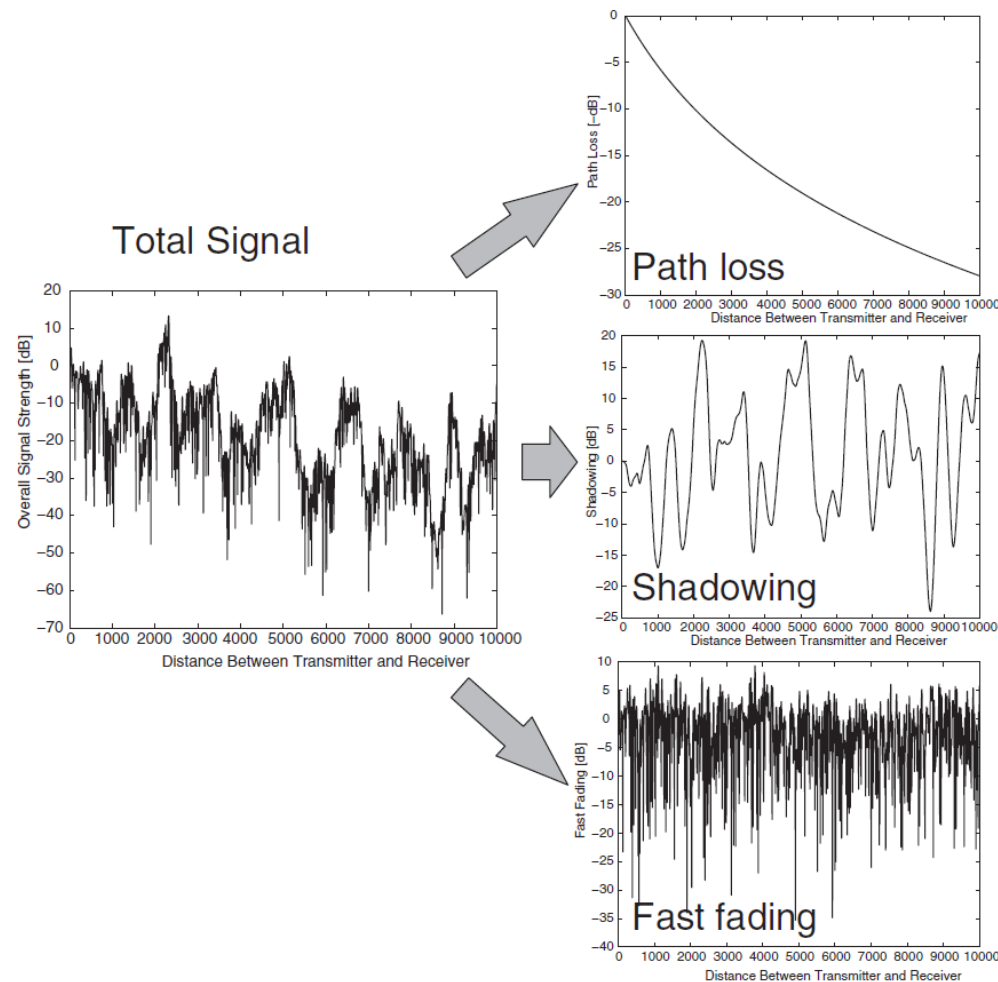
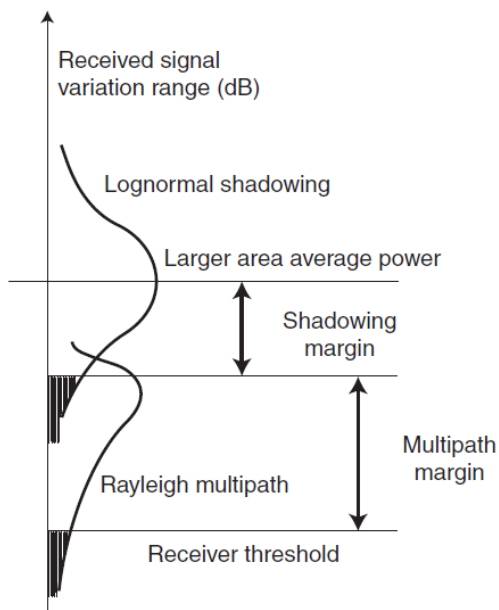
Project II

Narrowband Mobile Propagation Channel: Measurement and Modelling

Introduction

Narrowband UHF Mobile Propagation Channel

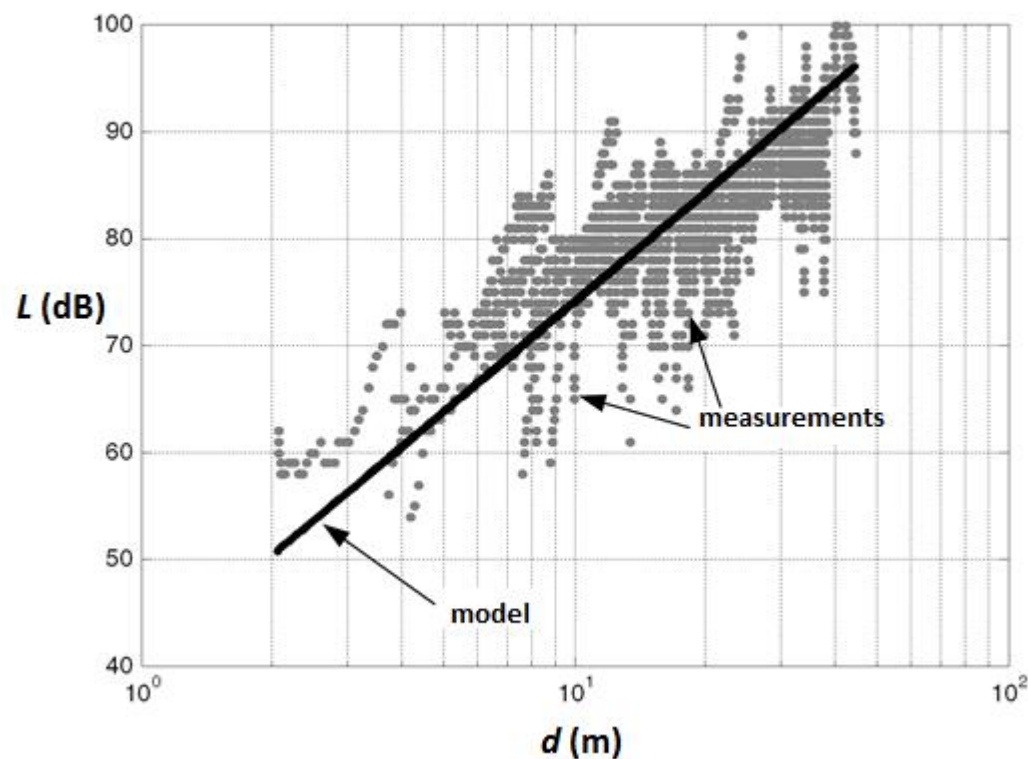
- Basic path loss (the mean for the given location)
 - ◆ (Semi-)Empirical models
 - ◆ (Semi-)Deterministic models
- Large-scale variations
 - ◆ Log-normal shadowing
- Small-scale variations
 - ◆ Rayleigh fading



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Mean Path Loss - Basic Empirical Model

(Log-distance Model, One Slope Model)



Environment	n (-)
Free space	2.0
suburban	2.5 – 4.0
dense urban	3.0 – 5.0
indoor – LOS	1.6 – 1.8
indoor – NLOS	3.0 – 6.0

$$\overline{L(d)} = \overline{L_1(d_1)} + 10n \log\left(\frac{d}{d_1}\right)$$

$$P_p \approx \frac{1}{d^n}$$

Log-normal Shadowing

- **Long-term / Large-scale** variations from the **mean** due to **shadowing**
- Log-normal shadowing = measured signal levels **in dB** in the given area shows **normal** (Gaussian) distribution about the mean

$$L(d) = \overline{L(d)} + X_\sigma = \overline{L_1(d_1)} + 10n\log\left(\frac{d}{d_1}\right) + X_\sigma$$

$$L(d, p) = \overline{L(d)} + L_{ln}(\sigma, p)$$

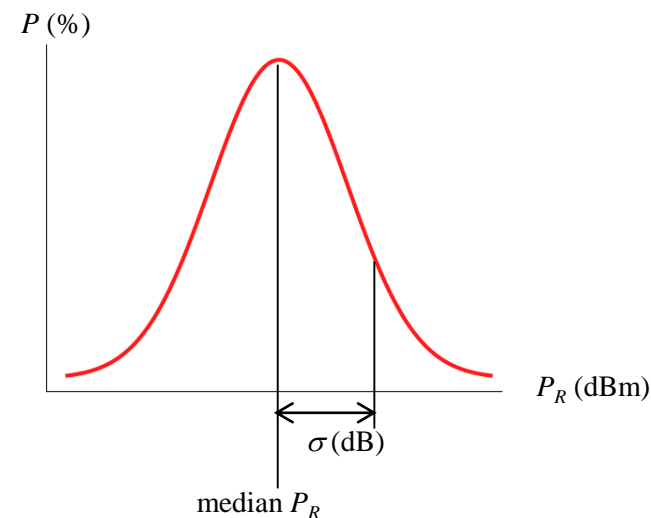
X_σ - zero-mean Gaussian distributed random variable in dB with standard deviation σ (dB); σ is given by the environment (urban ~8 dB, rural ~4 dB);

L_{ln} - value of X_σ for probability of p (%)

- Received power

$$P_R(d) = P_0 - L(d)$$

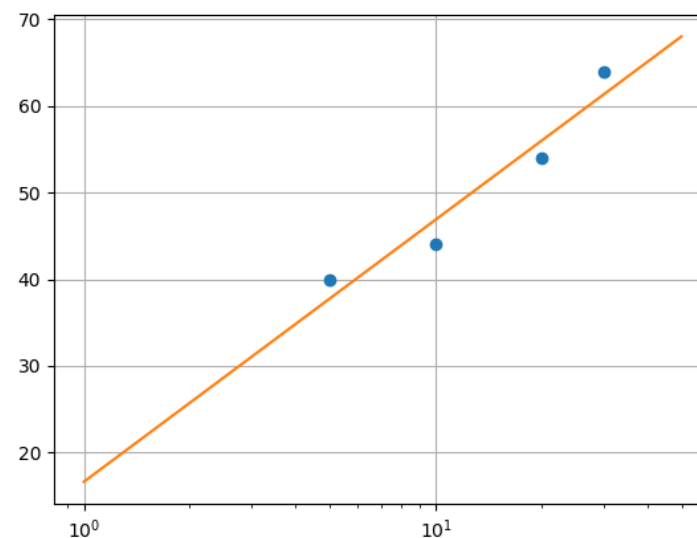
$$P[P_R(d) > \gamma] = Q\left(\frac{\gamma - \overline{P_R(d)}}{\sigma}\right)$$



Example (not real and PRIMITIVE!)

- Measurement (distance [m], path loss[dB]):
[(5, 40), (10, 44), (20, 54), (30, 64)]
- Fitting $\overline{L(d)} = \overline{L_1(d_1)} + 10n\log\left(\frac{d}{d_1}\right)$ for $d_1 = 1$ m:
 $L_1 = 16.6$ dB; $n = 3.0$
- Calculating standard deviation σ :
 $\sigma^2 = \{(37.8 - 40)^2 + (46.9 - 44)^2 + (56.0 - 54)^2 + (61.3 - 64)^2\} / 4 = 6.1 \Rightarrow \sigma = \mathbf{2.5}$ dB

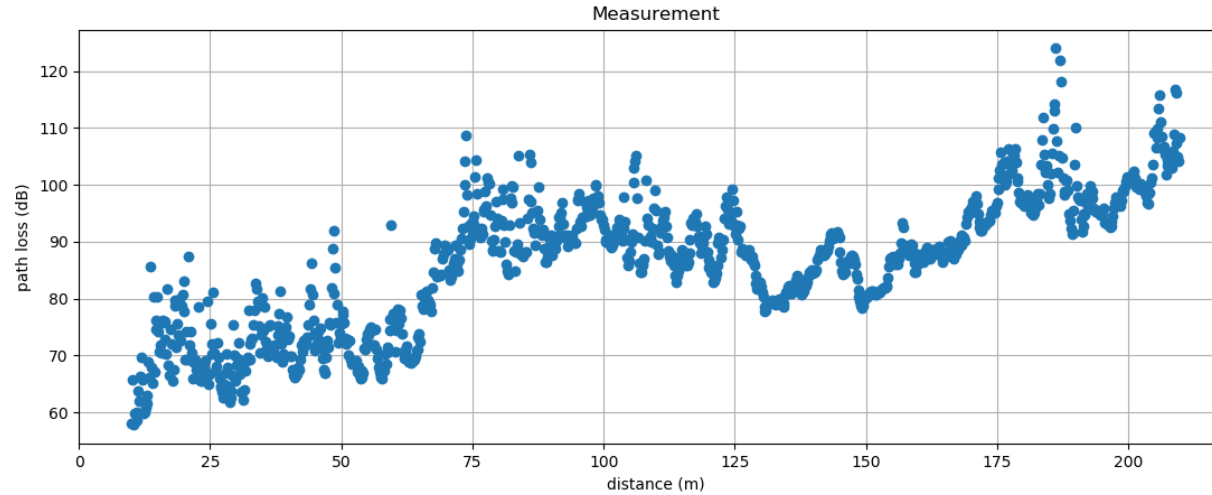
Distance (m)	Measured (dB)	Predicted (dB)	Error (dB)
5	40	37.8	-2.2
10	44	46.9	2.9
20	54	56.0	2.0
30	64	61.3	-2.7



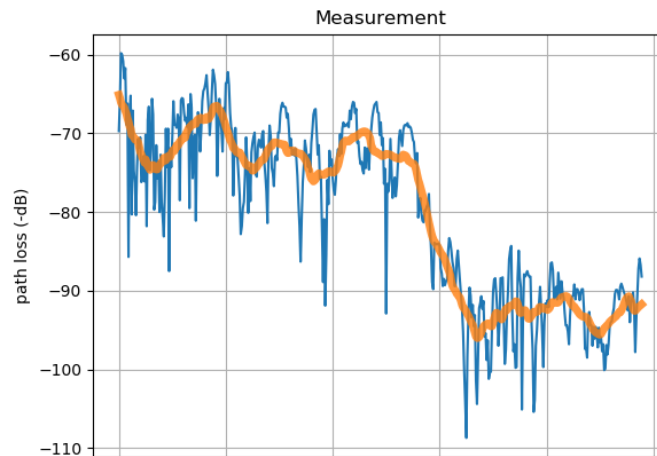
$$L(d) = \overline{L(d)} + X_\sigma = 16.6 + 30\log(d) + X_{2.5} \quad [\text{dB}, \text{m}, \text{dB}]$$

Example I

- Calculation of measured path loss vs. distance from the link budget and geometry



- If fast fading present (dynamic scene, speed) apply filtering first



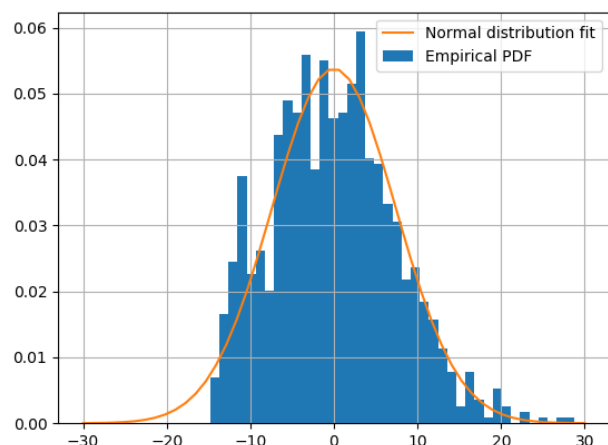
Note the path loss given in $-dB$
and the difference between relative path loss
and received signal strengths (RSS) in dB

Example I (contd.)

- Fit the one slope empirical model

$$\overline{L(d)} = 30.8 + 28 \log(d) \quad [\text{dB, m}]$$

- Calculate prediction error



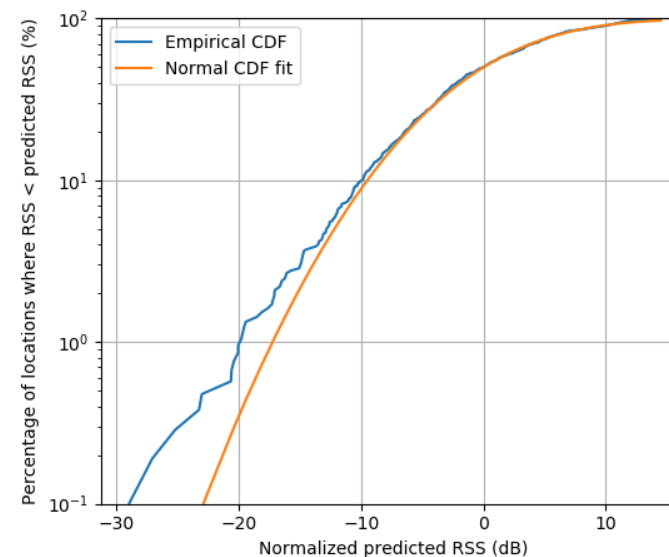
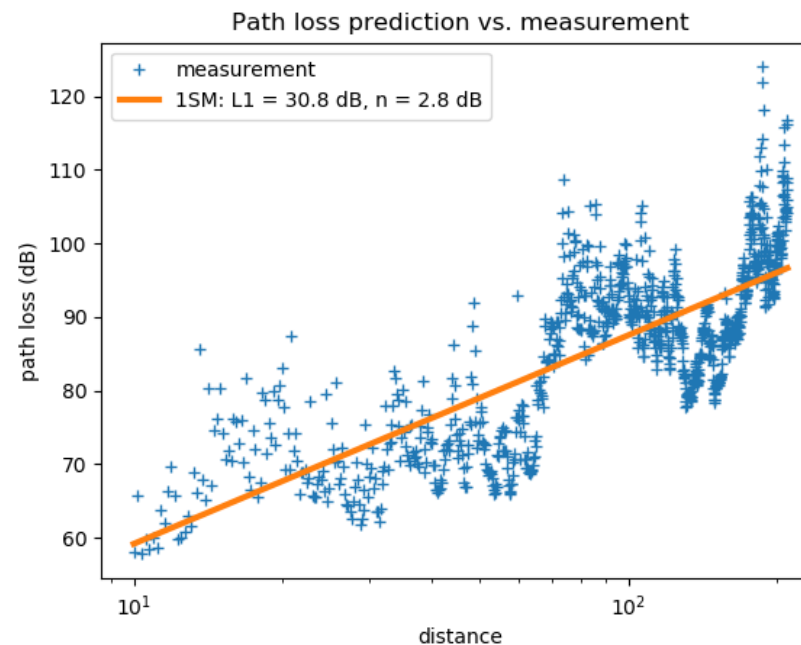
$$\sigma = 7.4 \text{ dB}$$

$$L(d) = \overline{L(d)} + X_{\sigma} = 30.8 + 28 \log(d) + X_{7.4} \quad [\text{dB, m, dB}]$$

- Provide CDF and required predictions, e.g.:

a) predicted path loss at $d = 100 \text{ m}$

b) max distance where $L < 80 \text{ dB}$ for 90% locations

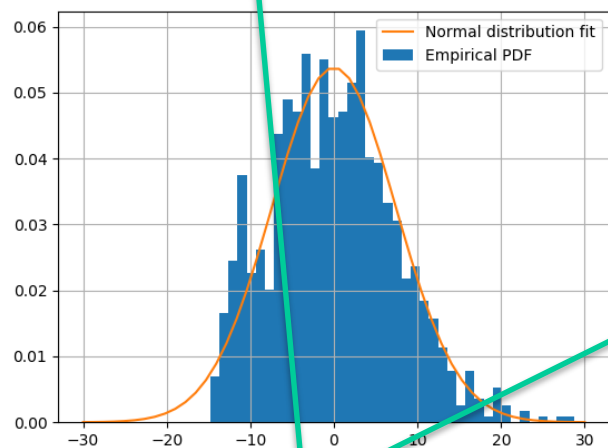


Example I (contd.)

- Fit the one slope empirical model

$$\overline{L(d)} = 30.8 + 28 \log(d) \quad [\text{dB, m}]$$

- Calculate prediction error



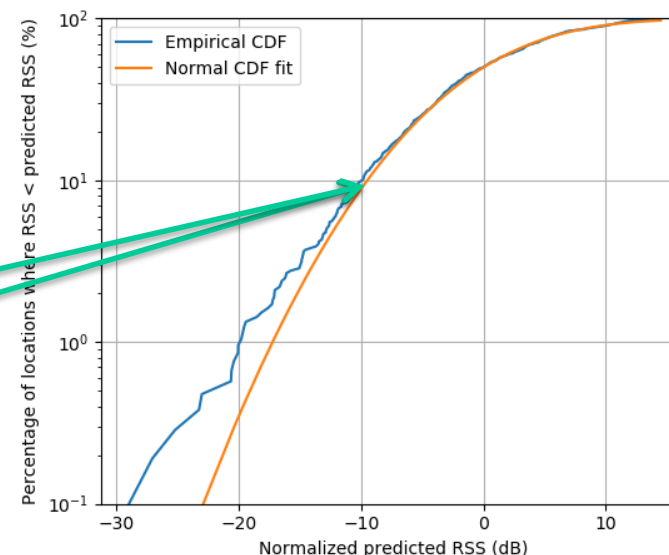
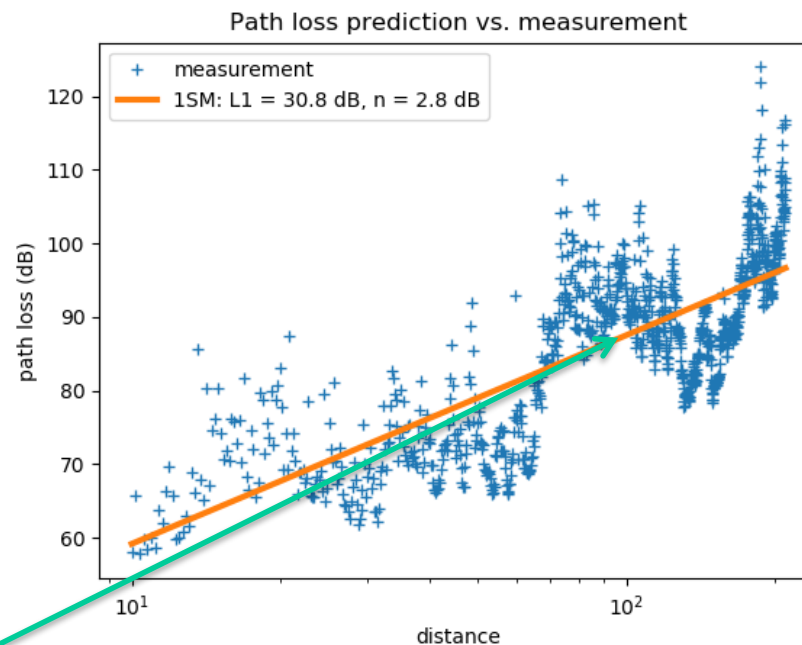
$$\sigma = 7.4 \text{ dB}$$

$$L(d) = \overline{L(d)} + X_{\sigma} = 30.8 + 28 \log(d) + X_{7.4} \quad [\text{dB, m, dB}]$$

- Provide CDF and required predictions, e.g.:

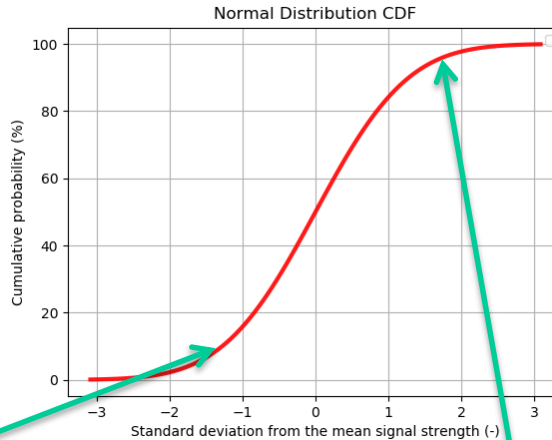
a) predicted path loss at $d = 100$ m
mean = 86.8 dB; for 10% locations higher than 96 dB

b) max distance where $L < 80$ dB for 90% locations
mean = $80 + 10 = 90$ dB $\Rightarrow d = 130$ m



Example I (contd.)

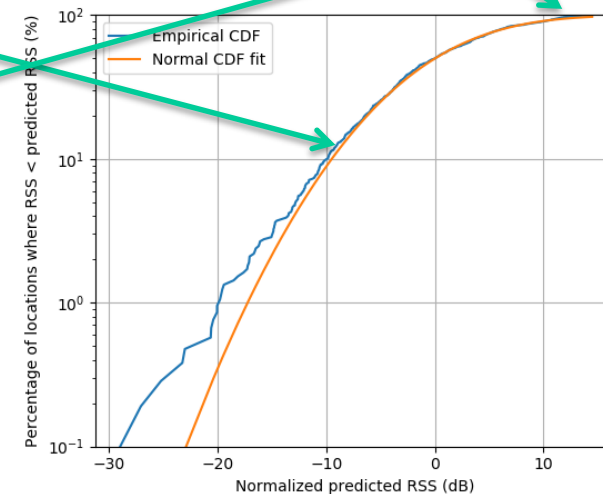
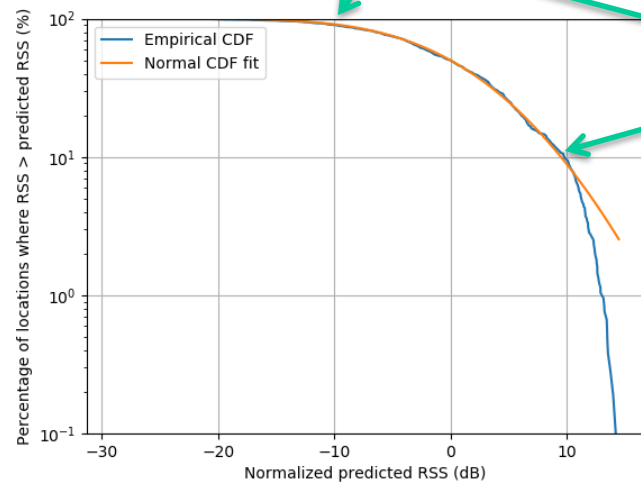
- Standard Gaussian distribution $m = 0, \sigma = 1$



1%	-2.33
5%	-1.65
10%	-1.28
20%	-0.84
30%	-0.52
50%	0.00
70%	0.52
80%	0.84
90%	1.28
95%	1.65
99%	2.33

- $\sigma = 7.4$ dB

$$L_M(7.4 \text{ dB}, 10 \%) = -1.28 \times 7.4 \text{ dB} = -9.5 \text{ dB} \quad L_M(7.4 \text{ dB}, 95 \%) = 1.65 \times 7.4 \text{ dB} = 12.2 \text{ dB}$$

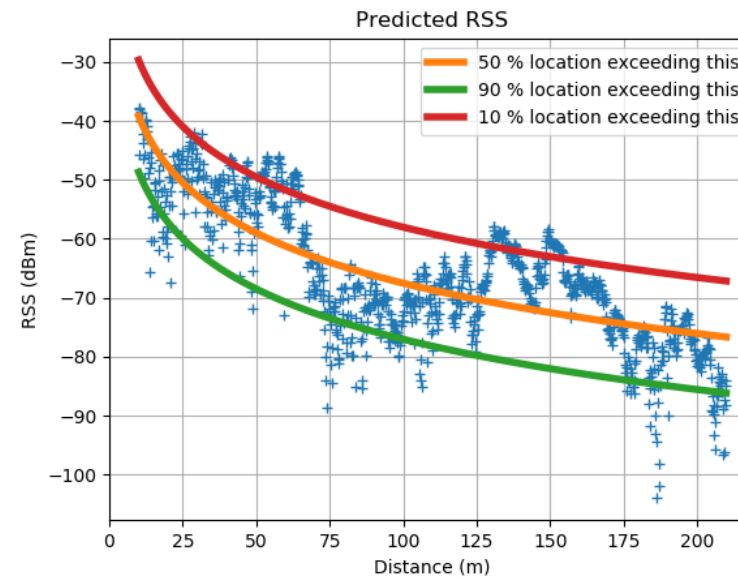
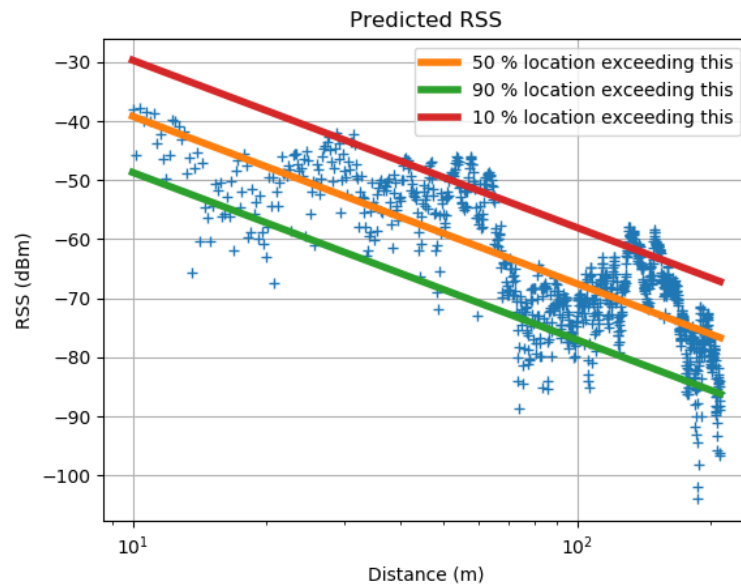


Example I (contd.)

$$L(d, p) = \overline{L(d)} + L_{ln}(\sigma, p) = 30.8 + 28 \log(d) + L_{ln}(7.4, p) \quad [\text{dB, m, \%, dB}]$$

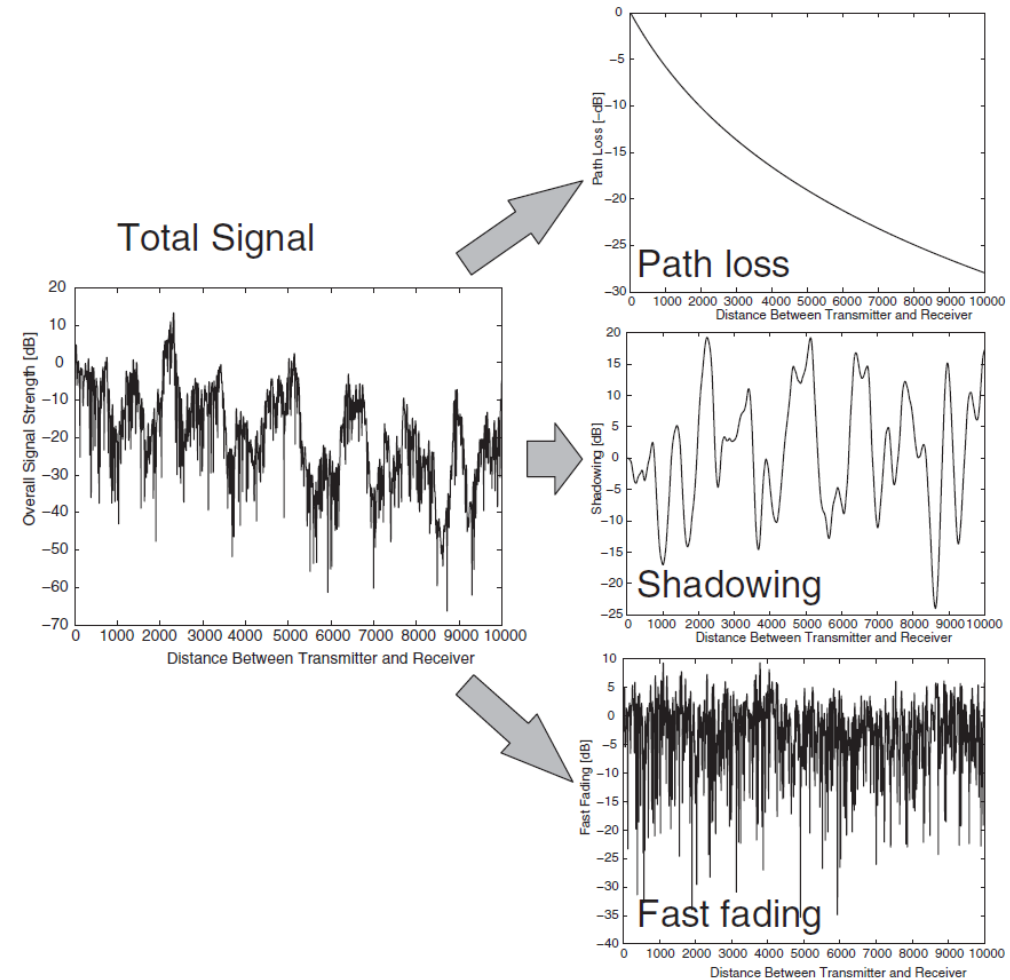
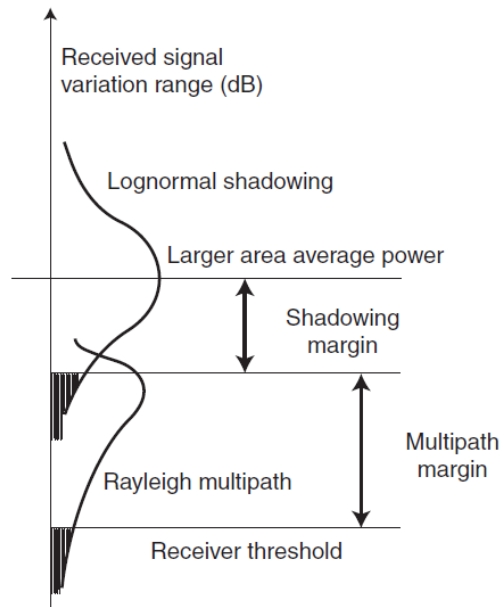
$$P_R(d, p) = P_T + G_T + G_R - L_{sys} - L(d, p) \quad [\text{dBm, m, \%, dBm, dB}]$$

$$P(P_R > x) = p = 10\%, 50\%, 90\% :$$



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Rayleigh fading

$$r(t) = \sqrt{I(t)^2 + Q(t)^2}$$

$$p_R(r) = \frac{r}{\sigma^2} e^{-\frac{r^2}{2\sigma^2}}$$

Mode

Median

Mean

RMS value

Standard deviation

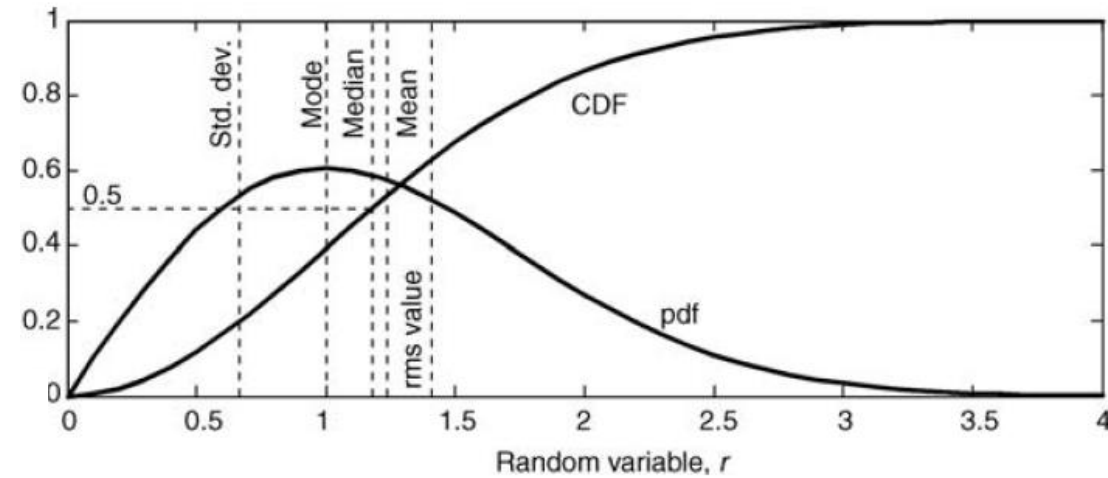
σ

$$\sigma\sqrt{2\ln 2} = 1.18\sigma$$

$$\sigma\sqrt{\pi/2} = 1.25\sigma$$

$$\sigma\sqrt{2} = 1.41\sigma$$

$$\sigma\sqrt{2 - \pi/2} = 0.655\sigma$$



Modeling the Wireless Propagation Channel, © F. P. Fontan, P. M. Espineira, 20087

$$P[r \leq R] = P_R(R) = 1 - e^{-\frac{R^2}{2\sigma^2}}$$

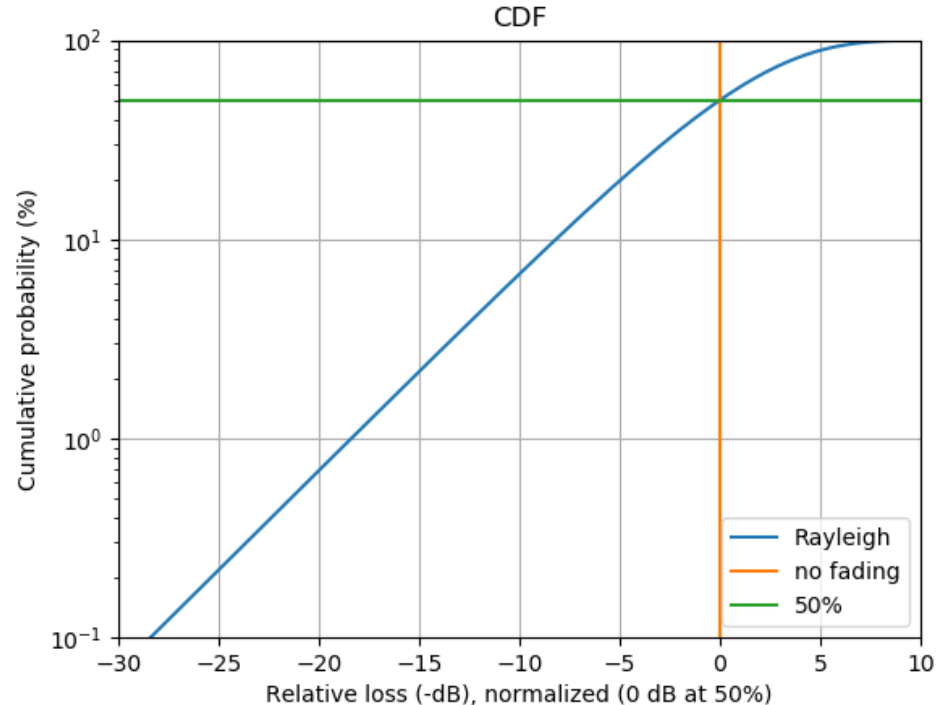
Note:

$r(t)$ models *voltage* (V)

$\text{power (W)} = \text{voltage}^2 / (2 \cdot 50 \Omega)$

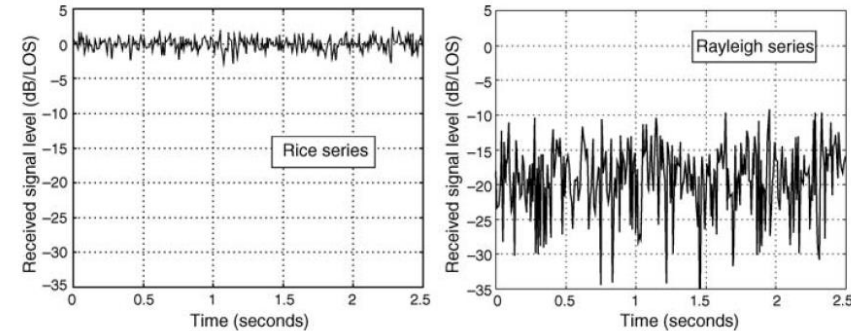
$\text{power (dBm)} = 10 \log [\text{power (W)} / 10^{-3}]$

$$R_{dB} = 20 \log_{10} \left(\frac{R}{R_{50}} \right)$$



Rice channel

- Adding two components
 - ◆ Coherent LOS (constant power; path loss + shadowing)
 - ◆ Random multipath (Rayleigh distributed)



$$p_R(r) = \frac{r}{\sigma^2} e^{-\frac{r^2+a^2}{2\sigma^2}} I_0\left(\frac{ar}{\sigma^2}\right)$$

$$k = \frac{a^2}{2\sigma^2}, \quad K(\text{dB}) = 10 \log(k)$$

r – magnitude of complex envelope

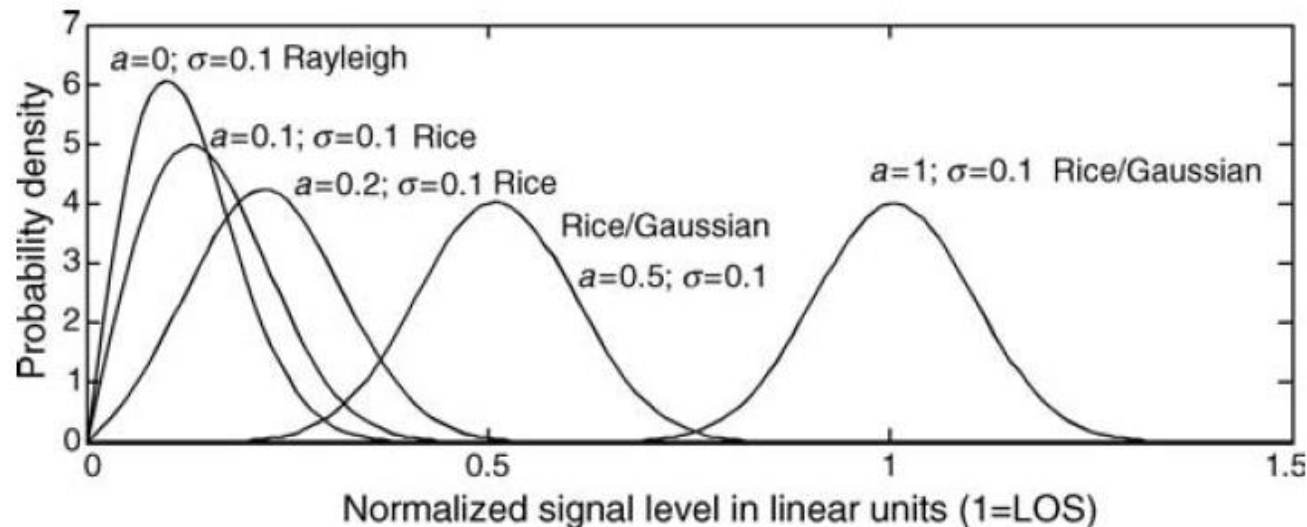
a – amplitude of the direct LOS signal

σ – mode of Rayleigh distribution when $a = 0$

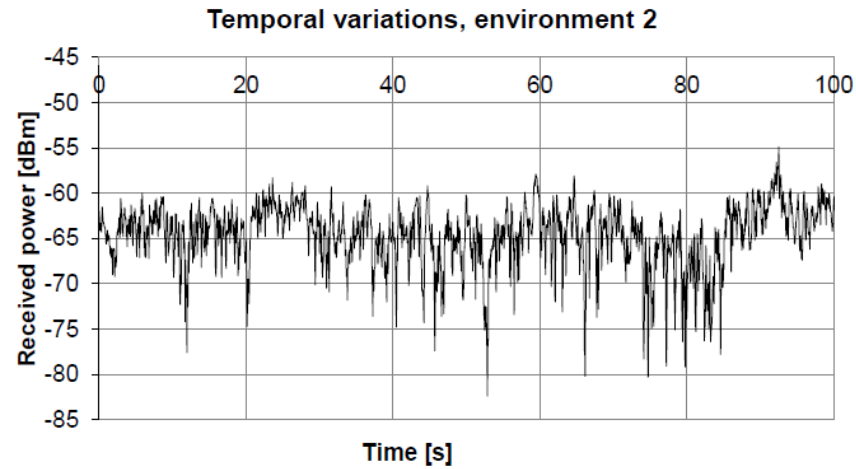
$2\sigma^2$ – normalized average power of the multipath component

I_0 – modified Bessel f. of the first kind and zeroth order

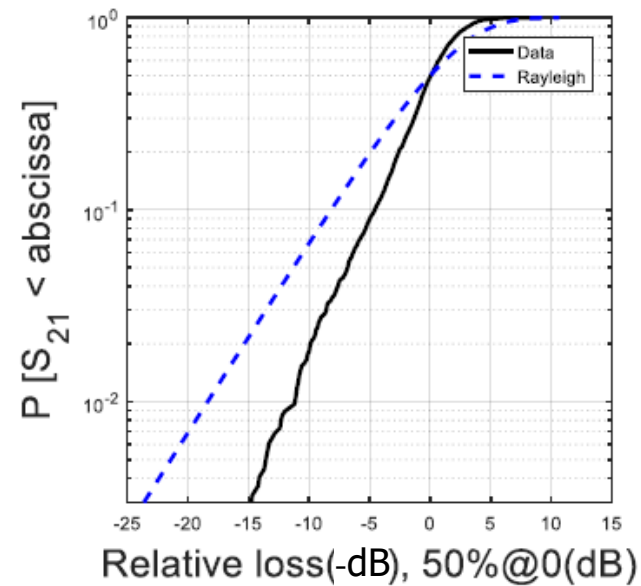
k, K – Rice k -factor; Carrier-to-Multipath ratio (C/M)



Example II



Minimum [dBm]	-82.5
Maximum [dBm]	-54.9
Median [dBm]	-64
Maximum fade [dB]	18.4



$P(\%)$	$RSS(\text{dB})$
50	0
10	-5
1	-12