
Flow-Based Policy for Online Reinforcement Learning

Anonymous Author(s)

Affiliation
Address
email

Abstract

We present **FlowRL**, a novel framework for online reinforcement learning that integrates flow-based policy representation with Wasserstein-2-regularized optimization. We argue that in addition to training signals, enhancing the expressiveness of the policy class is crucial for the performance gains in RL. Flow-based generative models offer such potential, excelling at capturing complex, multimodal action distributions. However, their direct application in online RL is challenging due to a fundamental objective mismatch: standard flow training optimizes for static data imitation, while RL requires value-based policy optimization through a dynamic buffer, leading to difficult optimization landscapes. FlowRL first models policies via a state-dependent velocity field, generating actions through deterministic ODE integration from noise. We derive a constrained policy search objective that jointly maximizes Q through the flow policy while bounding the Wasserstein-2 distance to a behavior-optimal policy implicitly derived from the replay buffer. This formulation effectively aligns the flow optimization with the RL objective, enabling efficient and value-aware policy learning despite the complexity of the policy class. Empirical evaluations on DMControl and Humanoidbench demonstrate that FlowRL achieves competitive performance in online reinforcement learning benchmarks.

1 Introduction

Recent advances in iterative generative models, particularly Diffusion Models (DM) [16, 37] and Flow Matching (FM) [22, 23, 40], have demonstrated remarkable success in capturing complex multimodal distributions. These models excel in tasks such as high-resolution image synthesis [7], robotic imitation learning [6, 2], and protein structure prediction [17, 3], owing to their expressivity and ability to model stochasticity. A promising yet underexplored application lies in leveraging their multimodal generation capabilities to enhance reinforcement learning (RL) policies, particularly in environments with highly stochastic or multimodal dynamics.

Traditional RL frameworks alternate between Q-function estimation and policy updates [38], often parameterizing policies as Gaussian [13] or deterministic policies [36, 12] to maximize expected returns. However, directly employing diffusion or flow-based models as policies introduces a fundamental challenge: the misalignment between RL objectives, which aim to optimize value-aware distributions, and generative modeling, which imitates static data distributions. This discrepancy

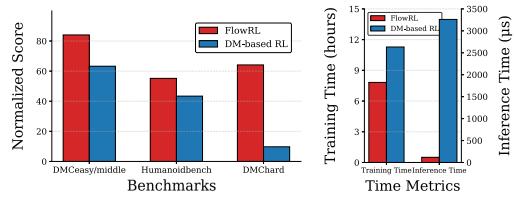


Figure 1: (left) Normalized scores comparing FlowRL and DM-based RL (QVPO) on 12 challenging DMControl and HumanoidBench tasks, and 3 DMC-easy & middle tasks. (right) Computational efficiency on the Dogrun task: 1M-step training time and single env step inference time.

39 becomes exacerbated in online RL, where nonstationary data distributions and evolving Q-value
40 estimates lead to unstable training [12].

41 While recent methods have pioneered the use of diffusion model (DM)-based policies in online
42 reinforcement learning [44, 8, 42], these approaches still suffer from high computational cost and
43 inefficient sample usage (see Section 2). By contrast, flow-based models (FMs), despite their ability
44 to represent complex and multimodal policies, have yet to be effectively integrated into online RL
45 frameworks.

46 Our method distinguishes itself by leveraging carefully selected replay buffer data as a reference
47 distribution to align flow-based policies with high-value behaviors while preserving multimodality.
48 Inspired by prior works such as SIL [27] and OBAC [25], which utilised behaviour policies to
49 guide policy optimization but limit policy expressivity to capture diverse behaviors, we propose a
50 unified framework that integrates flow-based action generation with Wasserstein-2-regularized [10]
51 distribution matching. Specifically, our policy extraction objective simultaneously maximizes Q-
52 values through flow-based actor and minimizes distribution distance from high-reward trajectories
53 identified in the replay buffer. By reformulating this dual objective as a guided flow-matching loss, we
54 enable the policy to adaptively imitate empirically optimal behaviors while exploring novel actions
55 that maximize future returns. Besides, this approach retains the simplicity of standard actor-critic
56 architectures, without requiring lengthy iterative sampling steps or auxiliary inference tricks [18,
57 8]—yet fully exploits the multimodality of flow models to discover diverse, high-performing policies.
58 We evaluate our approach on challenging DMControl [39] and HumanoidBench [35], demonstrating
59 competitive performance against state-of-the-art baselines. Notably, our framework achieves one-step
60 policy inference, significantly reducing computational overhead and training instability caused by
61 backpropagation through time (BPTT) [42, 30]. Experimental results highlight both the empirical
62 effectiveness of our method and its practical advantages in scalability and efficiency, establishing a
63 robust pathway for integrating expressive generative models into online RL.

64 2 Related Work

65 In this section, we provide a comprehensive survey of existing policy extraction paradigms based
66 on iterative generative models based policy, with a particular focus on recent advances that leverage
67 diffusion and flow-based models in offline or online reinforcement learning. We categorize these
68 approaches according to their underlying policy optimization objective and highlight their respective
69 advantages and limitations.

70 **Generalized Behavior Cloning** Generalized Behavior Cloning, often akin to weighted behavioral
71 cloning or weighted regression [32, 31], trains policies by imitating high-reward trajectories from a
72 replay buffer, weighted by advantage or value estimates, thereby avoiding BPTT. Previous methods
73 like EDP [18], QGPO [24], QVPO [8], and QIPO [45] implemented these paradigms, enhancing
74 computational efficiency by bypassing BPTT. However, as demonstrated in prior research, this
75 approach has been empirically shown to be inefficient [29, 30], and often leads to suboptimal
76 performance.

77 **Reverse process as policy parametrizations** These methods use reparameterized policy gradients,
78 computing gradients of the Q-function with respect to policy parameters directly through the genera-
79 tive model’s reverse sampling process, similar to the reparameterization trick commonly employed
80 in Gaussian-based policies [13]. Previous methods, such as DQL [43], DiffCPS [15], Consistency-
81 AC [19], and DACER [42], backpropagate gradients through the reverse diffusion process, which,
82 while flexible, incurs significant computational costs due to iterative denoising and backpropagation
83 through time (BPTT) [29]. These factors limit the scalability of such algorithms to more complex
84 environments. To address this, FQL [30] distills a one-step policy from a flow-matching policy,
85 reducing computational cost, but requires careful hyperparameter tuning.

86 **Other Approaches.** Beyond above methods, alternative methods include action gradients [44, 33],
87 hybrid Markov Decision Processes (MDPs) [34], rejection sampling [4] or combinations of above
88 strategies [26].

89 The distinction between these methods underscores an inherent trade-off between computational
90 simplicity and the efficiency of policy extraction. Generalized Behavior Cloning emphasizes ease

91 of implementation, often at the expense of policy extraction efficiency. In contrast, reparameterized
 92 policy gradients facilitate direct policy updates but incur increased complexity. These observations
 93 highlight the necessity for further research to achieve a better balance between expressivity and
 94 scalability when applying iterative generative models to reinforcement learning.

95 3 Preliminaries

96 3.1 Reinforcement Learning

97 Consider the Markov Decision Process (MDPs) [1] defined by a 5-tuple $\mathcal{M} = \langle \mathcal{S}, \mathcal{A}, \mathcal{P}, r, \gamma \rangle$, where
 98 $\mathcal{S} \in \mathbb{R}^n$ and $\mathcal{A} \in \mathbb{R}^m$ represent the continuous state and action spaces, $\mathcal{P}(s'|s, a) : \mathcal{S} \times \mathcal{A} \rightarrow \Delta(\mathcal{S})$
 99 denotes the dynamics distribution of the MDPs, $r(s, a) : \mathcal{S} \times \mathcal{A} \rightarrow \Delta(\mathbb{R})$ is a reward function,
 100 $\gamma \in [0, 1)$ gives the discounted factor for future rewards. The goal of RL is to find a policy
 101 $\pi(a|s) : \mathcal{S} \rightarrow \Delta(\mathcal{A})$ that maximizes the cumulative discounted reward:

$$J_\pi = \mathbb{E}_{\pi, \mathcal{P}} \left[\sum_{t=0}^{\infty} \gamma^t r(s_t, a_t) \right]. \quad (1)$$

102 In this paper, we focus on the online off-policy RL setting, where the agent interacts with the en-
 103 vironment and collects new data into a replay buffer $\mathcal{D} \leftarrow \mathcal{D} \cup \{(s, a, s', r)\}$. The replay buffer
 104 consequently maintains a distribution over trajectories induced by a mixture of historical behav-
 105 ior policies π_β . At the k -th iteration step, the online learning policy is denoted as π_k , with its
 106 corresponding Q value function defined by:

$$Q^{\pi_k}(s, a) = \mathbb{E}_{\pi_k, \mathcal{P}} \left[\sum_{t=0}^{\infty} \gamma^t r(s_t, a_t) | s_0 = s, a_0 = a \right], \quad (2)$$

107 and it can be derived by minimizing the TD error [38]:

$$\arg \min_{Q^{\pi_k}} \mathbb{E}_{(s, a, r, s') \sim \mathcal{D}} \left[(Q^{\pi_k}(s, a) - \mathcal{T}^{\pi_k} Q^{\pi_k}(s, a))^2 \right], \quad (3)$$

where $\mathcal{T}^{\pi_k} Q^{\pi_k}(s, a) = r(s, a) + \gamma \mathbb{E}_{s' \sim \mathcal{P}(\cdot|s, a), a' \sim \pi_k(\cdot|s')} [Q^{\pi_k}(s', a')]$.

108 Similarly, we distinguish the following key elements:

- 109 • **Optimal policy and Q-function:** The optimal policy π^* maximizes the expected cumulative
 110 reward, and the associated Q-function $Q^*(s, a)$ characterizes the highest achievable return.
- 111 • **Behavior policy and replay buffer:** The behavior policy π_β is responsible for generating the data
 112 stored in the replay buffer [21, 25]. Its Q-function, $Q^{\pi_\beta}(s, a)$, reflects the expected return when
 113 following π_β . Notably, \mathcal{D} is closely tied to the distribution of π_β , such that actions sampled from
 114 \mathcal{D} are supported by those sampled from π_β (i.e., $a \in \mathcal{D} \Rightarrow a \sim \pi_\beta$).
- 115 • **Behavior-optimal policy:** Among all behavior policies present in the buffer, we define π_{β^*} as the
 116 one that achieves the highest expected return, with Q-function $Q^{\pi_{\beta^*}}(s, a)$.

117 These definitions yield the following relationship, which holds for any state-action pair:

$$Q^*(s, a) \geq Q^{\pi_{\beta^*}}(s, a) \geq Q^{\pi_\beta}(s, a). \quad (4)$$

118 This relationship suggests that, although direct access to the optimal policy is typically infeasible, the
 119 value of the optimal behavior policy constitutes a theoretical lower bound [27] on the performance
 120 that can be achieved by policies derived from the replay buffer.

121 3.2 Flow Models

122 Continuous Normalizing Flows (CNF) [5] model the time-varying probability paths by defining
 123 a transformation between an initial distribution p_0 and a target data distribution p_1 [22, 23]. This
 124 transformation is parameterized by a flow $\psi_t(x)$ governed by a learned time-dependent vector field
 125 $v_t(x)$ [5], following the ordinary differential equation (ODE):

$$\frac{d}{dt} \psi_t(x) = v_t(\psi_t(x)), \quad (5)$$

126 and the continuity equation [41]:

$$\frac{d}{dt} p_t(x) + \nabla \cdot [p_t(x) v_t(x)] = 0, \quad \forall x \in \mathbb{R}^d. \quad (6)$$

127 **Flow Matching.** Flow matching provides a theoretically grounded framework for training
 128 continuous-time generative models through deterministic ordinary differential equations (ODEs).
 129 Unlike diffusion models that rely on stochastic dynamics governed by stochastic differential equa-
 130 tions (SDEs) [37], flow matching operates via a *deterministic* vector field, enabling simpler training
 131 objectives and more efficient sampling trajectories. The core objective is to learn a neural velocity
 132 field $v_\theta : [0, 1] \times \mathbb{R}^d \rightarrow \mathbb{R}^d$ that approximates a predefined conditional target velocity field $u(t, x|x^1)$.
 133 Given a source distribution $q(x^0)$ and target distribution $p(x^1)$, the training process involves mini-
 134 mizing the conditional flow matching objective [22]:

$$\mathcal{L}_{\text{CFM}}(\theta) = \mathbb{E}_{\substack{t \sim \mathcal{U}([0,1]) \\ x^1 \sim p, x^0 \sim q}} \|v_\theta(t, x^t) - u(t, x^t|x^1)\|_2^2, \quad (7)$$

135 where the linear interpolation path is defined as $x^t = tx^1 + (1-t)x^0$ with $u(t, x^t|x^1) = x^1 - x^0$.
 136 This formulation induces a *probability flow* governed by the ODE:

$$\frac{dx}{dt} = v_\theta(t, x), \quad x^0 \sim q, \quad (8)$$

137 which transports samples from q to p .

138 4 Method

139 In this section, we detail the design of our method. We first parameterize the policy as a flow model,
 140 where actions are generated by integrating a learned velocity field over time. For policy improvement,
 141 we model policy learning as a constrained policy search that maximizes expected returns while bound-
 142 ing the distance to an optimal behavior policy. Practically, we circumvent intractable distribution
 143 matching and optimal behavior policy by aligning velocity fields with elite historical actions through
 144 regularization and implicit guidance, enabling efficient constraint enforcement.

145 4.1 Flow Model based Policy Representation.

146 We parameterize π_θ with $v_\theta(t, s, a^t)$, a state-action-time dependent velocity field, as an actor for
 147 reinforcement learning. The policy π_θ can be derived by solving ODE (8) :

$$\pi_\theta(s, a^0) = a^0 + \int_0^1 v_\theta(t, s, a^t) dt, \quad (9)$$

148 where $a^0 \sim \mathcal{N}(0, I^2)$. The superscript t denotes the continuous time variable in the flow-based ODE
 149 process to distinguish it from discrete Markovian time steps in reinforcement learning. (For brevity,
 150 the terminal condition at $t = 1$ is omitted in the notation.) The Flow Model derives a deterministic
 151 velocity field v_θ from an ordinary differential equation (ODE). However, when a^0 is sampled from a
 152 random distribution, the model effectively functions as a stochastic actor, exhibiting diverse behaviors
 153 across sampling instances. This diversity in generated trajectories inherently promotes enhanced
 154 exploration in online reinforcement learning.

155 Recall the definition in Section 3.1. Following the notation of π_β and π_{β^*} , we can define the
 156 corresponding velocity fields as follows:

Let v_β be the velocity field induced by the behavior policy π_β , such that:

$$v_\beta(s, a) = a - a^0.$$

157 where $s, a \sim \mathcal{D}$, and $a^0 \sim \mathcal{N}(0, I^2)$.

Similarly, let v_{β^*} denote the velocity field induced by the behavior-optimal policy π_{β^*} :

$$v_{\beta^*}(s, a) = a - a^0.$$

158 where $a \sim \pi_{\beta^*}$, and $a^0 \sim \mathcal{N}(0, I^2)$.

159 **4.2 Optimal-Behavior Constrained Policy Search with Flow Models**

160 Building on the discussion in Section 3.1, where the optimal behavior policy is established as a lower
 161 bound for the optimal policy, we proceed to optimize the following objective under a constrained
 162 policy search setting:

$$\begin{aligned} \theta^* = \arg \max_{\theta} & \mathbb{E}_{a \sim \pi_{\theta}} [Q^{\pi_{\theta}}(s, a)], \\ \text{s.t. } & D(\pi_{\theta}, \pi_{\beta^*}) \leq \epsilon. \end{aligned} \quad (10)$$

163 Here, $D(\pi_{\theta}, \pi_{\beta^*})$ denotes a distance metric between the current policy and the optimal behavior
 164 policy distributions.

165 The objective is to maximize the expected reward $\mathbb{E}_{a \sim \pi_{\theta}} [Q^{\pi}(s, a)]$ while constraining the learned
 166 policy π_{θ} to remain within an ϵ -neighborhood of the optimal behavior policy π_{β^*} , i.e., $D(\pi_{\theta}, \pi_{\beta^*}) \leq \epsilon$.
 167 This formulation utilizes the Q-function, a widely used and effective approach for policy extraction,
 168 while ensuring fidelity to the optimal behavior policy. Despite its theoretical appeal, this optimization
 169 paradigm exhibits two inherent limitations:

- 170 • *Challenges in computing distributional distances:* For flow-based models, computing policy
 171 densities at arbitrary samples is computationally expensive, which limits the practicality of distance
 172 metrics such as the KL divergence for sample-based estimation and policy regularization.
- 173 • *Inaccessibility of the optimal behavior policy π_{β^*} :* The replay buffer contains trajectories from
 174 a mixture of policies, making it difficult to directly sample from π_{β^*} or to reliably estimate its
 175 associated velocity field, thereby complicating the computation of related quantities in practice.

176 **4.3 A Tractable Surrogate Objective**

177 To overcome the aforementioned challenges, we propose the following solutions:

- 178 • **Wasserstein Distance as Policy Constraints:** We introduce a policy regularization method based
 179 on the alignment of velocity fields. This approach bounds the Wasserstein distance between policies
 180 by characterizing their induced dynamic transport processes, thereby imposing direct empirical
 181 constraints on the evolution of policies without requiring density estimation.
- 182 • **Implicit Guidance for Optimal Behaviors:** Instead of explicitly constraining the policy to match
 183 the inaccessible π_{β^*} , we leverage implicit guidance from past best-performing behaviors in the
 184 buffer, enabling efficient revisiting of arbitrary samples and encouraging the policy to remain within
 185 a high-quality region of the action space.

186 In particular, we adopt the squared Wasserstein-2 distance for its convexity with respect to the
 187 policy distribution and ease of implementation. This metric is also well-suited for measuring the
 188 velocity field between policies and enables efficient sample-based regularization within the flow-based
 189 modeling framework. In general, we can define the Wasserstein-2 Distance [41] as follows :

190 **Definition 4.1 (Wasserstein-2 Distance)** Given two probability measures p and q on \mathbb{R}^n , the
 191 squared Wasserstein-2 distance between p and q is defined as:

$$W_2^2(p, q) = \inf_{\gamma \in \Pi(p, q)} \int_{\mathbb{R}^n \times \mathbb{R}^n} \gamma(x, y) \|x - y\|^2 dx dy, \quad (11)$$

192 where $\Pi(p, q)$ denotes the joint distributions of p and q , γ on $\mathbb{R}^n \times \mathbb{R}^n$ with marginals p and q .
 193 Specifically, we derive a tractable upper bound for the Wasserstein-2 distance (proof in A.1):

194 **Theorem 4.1 (W-2 Bound for Flow Matching)** Let v_{θ} and v_{β^*} be two velocity fields inducing
 195 time-evolving distributions $\pi_{\theta}^t(a|s)$ and $\pi_{\beta^*}^t(a|s)$, respectively. Assume v_{β^*} is Lipschitz continuous
 196 in a with constant L . $a^t = ta + (1-t)a^0$. Then, the squared Wasserstein-2 distance between π_{θ} and
 197 π_{β^*} at $t = 1$ satisfies:

$$W_2^2(\pi_{\theta}, \pi_{\beta^*}) \leq e^{2L} \int_0^1 \mathbb{E}_{a \sim \pi_{\beta^*}} [\|v_{\theta}(s, a^t, t) - v_{\beta^*}\|^2] dt. \quad (12)$$

198 By explicitly constraining the Wasserstein-2 distance, the model enforces proximity between the
 199 current policy and the optimal policy stored in the buffer. This objective is inherently consistent

200 with the generative modeling goal of minimizing distributional divergence. The regularization
 201 mechanism benefits from the representational expressiveness of flow-based models in capturing
 202 diverse, high-performing action distributions while systematically restricting policy updates.

203 However, while the upper bound of Wasserstein-2 distance above is theoretically tractable, sampling
 204 directly from π_{β^*} or evaluating its velocity field remains a computational barrier in practice. To
 205 circumvent this limitation, we introduce an implicit guidance (13) mechanism through the $Q^{\pi_{\beta^*}}$,
 206 which is more readily estimable:

$$\mathbb{E}_{\substack{a' \sim \pi_\theta, t \sim \mathcal{U}(0,1) \\ s, a \sim \mathcal{D}}} \left[f(Q^{\pi_{\beta^*}}(s, a) - Q^{\pi_\theta}(s, a')) \|v_\theta(s, a^t, t) - (a - a^0)\|^2 \right], \quad (13)$$

207

$$f \propto \max(Q^{\pi_{\beta^*}} - Q^{\pi_\theta}, 0). \quad (14)$$

208 The constraint incorporates a non-negative weighting function, as defined in Eq. (14), thereby
 209 establishing an adaptive regularization mechanism. A positive value of f signifies that the behavioral
 210 policy achieves superior performance relative to the current policy; under these circumstances, the
 211 constraint adaptively regularizes the current policy towards the optimal behavioral policy.

212 The implicit form of the constraints in Eq. (12) enables efficient utilization of arbitrary samples from
 213 the replay buffer, thus improving sample efficiency. Moreover, by relaxing the strict constraint on the
 214 Wasserstein-2 distance, the modified objective enhances computational efficiency. Notwithstanding
 215 this relaxation, policy improvement guarantees remain valid, as demonstrated in the following
 theorem (proof in Appendix A.2):

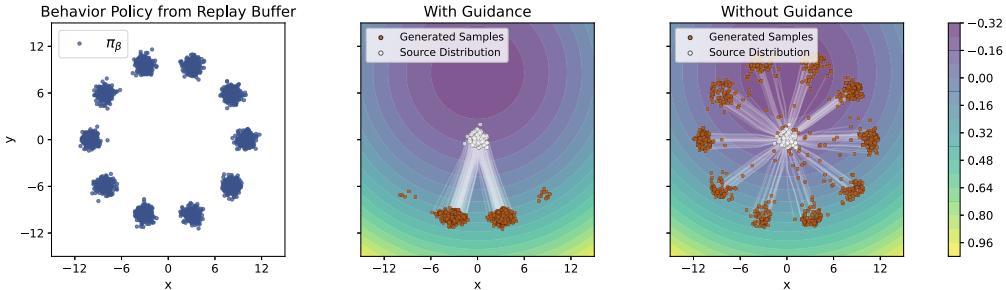


Figure 2: Illustration of Theorem 4.2 on a bandit toy example: (left) behavior data in the replay buffer;
 (middle) implicit value-guided flow matching steers the policy toward the high-performance behavior
 policy(π_{β^*}), heatmap shows $Q^{\pi_k} - Q^{\pi_{\beta^*}}$, white lines indicate transport paths; (right) standard flow
 matching leads to dispersed sampling with high variance under limited flow steps.

216

217 **Theorem 4.2 (Weighted CFM)** Let $\pi_k(a|s)$ be the current policy induced by velocity field v_{θ_k} ,
 218 and f , a non-negative weighting function with $f \propto Q^{\pi_{\beta^*}} - Q^{\pi_k}$. Minimizing the objective (13)
 219 yields an improved policy distribution:

$$\pi_{k+1}(a|s) = \frac{f(s, a)\pi_{\beta^*}(a|s)}{\mathcal{Z}(s)}, \quad (15)$$

220 where $\mathcal{Z}(s) = \int_{\mathcal{A}} f \cdot \pi_k(a|s) da$ is the normalization factor.

221 Figure 2 shows that, as guaranteed by Theorem 4.2, flow matching with guidance can steer the policy
 222 toward the π_{β^*} , even without direct sampling from it. For details of the toy example settings, see
 223 Appendix B.4.

224 4.4 A Practical Implementation

225 Building on the theoretical developments above, we now present a practical implementation of
 226 FlowRL, as detailed in Algorithm 1.

227 **Policy Evaluation** Recall the constraint in Eq. (13), which necessitates the evaluation of both the
 228 current policy value function Q^{π_θ} and the optimal behavioral policy value function $Q^{\pi_{\beta^*}}$. The value
 229 function Q^{π_θ} is estimated using standard Bellman residual minimization, as described in Eq. (3). For
 230 $Q^{\pi_{\beta^*}}$, leveraging the definition of π_{β^*} , we similarly adopt the following objective:

$$\arg \min_{Q^{\pi_{\beta^*}}} \mathbb{E}_{(s, a, r, s') \sim \mathcal{D}} \left[(Q^{\pi_{\beta^*}}(s, a) - \mathcal{T}^{\pi_{\beta^*}} Q^{\pi_{\beta^*}}(s, a))^2 \right], \quad (16)$$

$$\mathcal{T}^{\pi_{\beta^*}} Q^{\pi_{\beta^*}}(s, a) = r(s, a) + \gamma \mathbb{E}_{s' \sim \mathcal{D}} \left[\max_{a' \sim \mathcal{D}} Q^{\pi_{\beta^*}}(s', a') \right]. \quad (17)$$

231 To circumvent the difficulties of directly evaluating the max operator, we leverage techniques from
 232 offline reinforcement learning to estimate $Q^{\pi_{\beta^*}}$. Among these approaches, we adopt expectile
 233 regression [19] due to its simplicity and compatibility with unmodified data pipelines. Specifically,
 234 the value function $V^{\pi_{\beta^*}}$ and the action-value function $Q^{\pi_{\beta^*}}$ are estimated by solving the following
 235 optimization problems:

$$\arg \min_{V^{\pi_{\beta^*}}} \mathbb{E}_{(s, a) \sim \mathcal{D}} [L_2^\tau(Q^{\pi_{\beta^*}}(s, a) - V^{\pi_{\beta^*}}(s))], \quad (18)$$

$$\arg \min_{Q^{\pi_{\beta^*}}} \mathbb{E}_{(s, a, s', r) \sim \mathcal{D}} \left[(r + \gamma V^{\pi_{\beta^*}}(s') - Q^{\pi_{\beta^*}}(s, a))^2 \right], \quad (19)$$

237 where $L_2^\tau(x) = |\tau - \mathbb{1}(x < 0)|x^2$ denotes the expectile regression loss and τ is the expectile factor.

238 **Policy Extraction** Accordingly, the policy extraction problem for flow-based models can be
 239 formulated as the following constrained optimization:

$$\theta^* = \arg \max_{\theta} \mathbb{E}_{s \sim \mathcal{D}, a \sim \pi_\theta} [Q^{\pi_\theta}(s, a)], \quad (20)$$

$$\text{s.t. } \mathbb{E}_{s, a \sim \mathcal{D}, a' \sim \pi_\theta} \left[f(Q^{\pi_{\beta^*}} - Q^{\pi_\theta}) \|v_\theta(s, a^t, t) - (a - a^0)\|^2 \right] \leq \epsilon. \quad (21)$$

241 Although a closed-form solution can be derived using the Lagrangian multiplier and KKT conditions,
 242 it is generally intractable to apply in practice due to the unknown partition function [31, 32, 25].
 243 Therefore, we adopt a Lagrangian form, leading to the following objective:

$$\mathcal{L}(\theta) = \mathbb{E}_{s, a \sim \mathcal{D}, a' \sim \pi_\theta} \underbrace{[Q^{\pi_\theta}(s, a')]_{\text{exploration}} - \lambda \left(\underbrace{f(Q^{\pi_{\beta^*}} - Q^{\pi_\theta}) \|v_\theta - (a - a^0)\|^2}_{\text{exploitation}} - \epsilon \right)}_{\text{exploitation}}. \quad (22)$$

244 Where λ is the Lagrangian multiplier, which is often set as a constant in practice [11, 20].

245 Objective (22) can be interpreted as comprising two key components: (1) maximization of the
 246 learned Q-function, which encourages the agent to explore unknown regions and facilitates policy
 247 improvement; and (2) a policy distribution regularization term, which enforces alignment with optimal
 248 behavior policies and thereby promotes the exploitation of high-quality actions.

249 Conceptual similarities exist between our method and both self-imitation learning [27] and tandem
 250 learning [28]. Self-imitation learning focuses on exploiting high-reward behaviors by encouraging
 251 the policy to revisit successful past experiences, typically requiring complete trajectories and modifi-
 252 cations to the data pipeline. In contrast, our method operates directly on individual samples from
 253 the buffer, enabling more flexible and efficient sample utilization. Tandem learning, by comparison,
 254 decomposes the learning process into active and passive agents to facilitate knowledge transfer, with
 255 a primary emphasis on value learning, whereas our approach is centered on policy extraction.

256 5 Experiments

257 To comprehensively evaluate the effectiveness and generality of **FlowRL**, we conduct experiments
 258 on a diverse set of challenging tasks from DMControl [39] and HumanoidBench [35]. These
 259 benchmarks encompass high-dimensional locomotion and human-like robot (Unitree H1) control
 260 tasks. Our evaluation aims to answer the following key questions:

Algorithm 1 Flow RL

Require: Critic Q^{π_θ} , critic $Q^{\pi_\beta^*}$, value $V^{\pi_\beta^*}$, flow model v_θ , replay buffer $\mathcal{D} = \emptyset$, weighting function f

- 1: **repeat**
- 2: **for** each environment step **do**
- 3: $a \sim \pi_\theta(a|s)$, $r, s' \sim P(s'|s, a)$
- 4: $\mathcal{D} \leftarrow \mathcal{D} \cup \{(s, a, s', r)\}$
- 5: **end for**
- 6: **for** each gradient step **do**
- 7: **Estimate value for** π_θ : Update Q^{π_θ} by (3),
- 8: **Estimate value for** π_{β^*} : Update $Q^{\pi_{\beta^*}}$ by (19), update $V^{\pi_{\beta^*}}$ by (18)
- 9: Update v_θ by (22)
- 10: **end for**
- 11: **until** reach the max environment steps

261 1. How does FlowRL compare to previous online RL algorithms and existing diffusion-based online
262 algorithms?

263 2. Can the algorithm still demonstrate strong performance in the absence of any explicit exploration
264 mechanism?

265 3. How does the constraint affect the performance?

266 We compare **FlowRL** against two categories of baselines to ensure comprehensive evaluation: **(1) Model-free RL**:

267 We consider three representative policy parameterizations: deterministic policies (TD3 [12]), Gaussian policies (SAC [13]), and diffusion-based policies (QVPO [8], the previous
268 state-of-the-art for diffusion-based online RL). **(2) Model-based RL**: TD-MPC2 [14], a strong model-
269 based method on these benchmarks, is included for reference only, as it is not directly comparable to
270 model-free methods.

272 **5.1 Results and Analysis**

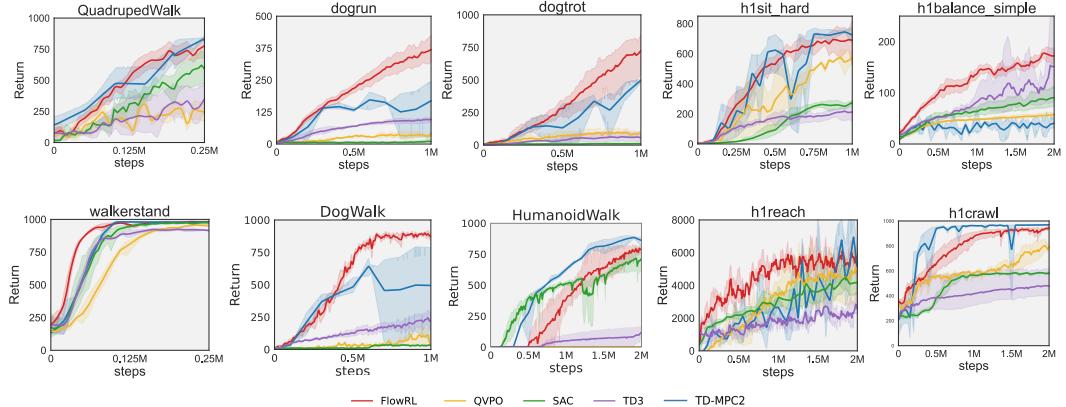
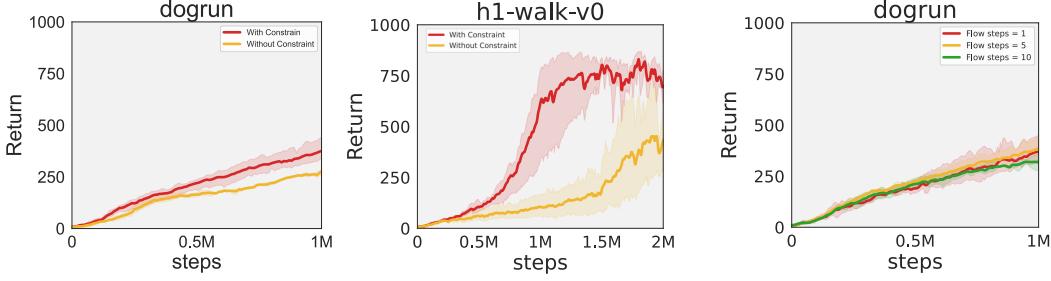


Figure 3: Main results. We provide performance comparisons for tasks (first column: DMC-easy/middle; second and third columns: DMC-hard; fourth and fifth columns: HumanoidBench). For comprehensive results, please refer to Appendix D. All model-free algorithms (FlowRL, SAC, QVPO, TD3) are evaluated with 5 random seeds, while the model-based algorithm (TD-MPC2) uses 3 seeds. Note that direct comparison between model-free methods and the model-based TD-MPC2 is not strictly fair; TD-MPC2 is included just as a reference.

273 The main results are summarized in Figure 3, which shows the learning curves across tasks. **FlowRL**
274 consistently outperforms or matches the model-free baselines on the majority of tasks, demonstrating
275 strong generalization and robustness, especially in challenging high-dimensional (e.g., the DMC dog
276 domain, where $s \in \mathbb{R}^{223}$ and $a \in \mathbb{R}^{38}$) and complex control settings (e.g., Unitree H1). Compared



(a) Effect of the constraint: FlowRL with the constraint achieves higher returns compared to the variant without the constraint.

(b) Sensitivity to flow steps: The number of flow steps has a limited effect on FlowRL performance.

Figure 4: Ablation studies

277 to strong model-based baselines, FlowRL achieves comparable results but is much more efficient
 278 in terms of wall-clock time. Notably, both during the training and evaluation stage, we use flow
 279 steps $N = 1$, and do not employ any sampling-based action selection used in [8, 18]. Despite the
 280 absence of any explicit exploration mechanism, FlowRL demonstrates strong results, which can be
 281 attributed to both the inherent stochasticity and exploratory capacity of the flow-based actor and the
 282 effective exploitation of advantageous actions identified by the policy constraint. These findings
 283 indicate that, while exploration facilitates the discovery of high-reward actions, the exploitation of
 284 previously identified advantageous behaviors is equally essential.

285 5.2 Ablation Studies

286 One of the central designs in FlowRL is the introduction of a policy constraint mechanism. This
 287 design aims to guide the policy towards optimal behavior by adaptively weighting the constraint based
 288 on the relative advantage of the optimal behavioral policy over the current policy. To rigorously assess
 289 the necessity and effectiveness of this component, we address **Q3** by conducting ablation studies
 290 in which the policy constraint is omitted from FlowRL. Experimental results in Figure 4a indicate
 291 that the presence of the policy constraint leads to improvements in performance and, by constraining
 292 the current policy towards the optimal behavioral policy, enhances sample efficiency. These benefits
 293 are especially pronounced in environments with complex dynamics (e.g., H1 control tasks from
 294 HumanoidBench), highlighting the importance of adaptive policy regularization in challenging task
 295 settings.

296 We also investigate the sensitivity of the algorithm to different choices of the number of flow steps
 297 ($N=1,5,10$). Experimental results in Figure 4b demonstrate that varying the number of flow steps has
 298 only a limited impact on the overall performance. Specifically, using a smaller number of flow steps
 299 does not substantially affect the final policy performance. On the other hand, increasing the number
 300 of flow steps results in longer backpropagation through time (BPTT) chains, which significantly
 301 increases computational complexity and training time. These findings suggest that FlowRL is robust
 302 to the choice of flow step and that single-step inference is generally sufficient for achieving stable
 303 and efficient learning in practice.

304 6 Conclusion

305 We introduce FlowRL, a practical framework that integrates flow-based generative models into online
 306 reinforcement learning through Wasserstein-2 distance constrained policy search. By parameterizing
 307 policies as state-dependent velocity fields, FlowRL leverages the expressivity of flow models to
 308 model action distributions. To align policy updates with value maximization, we propose an implicit
 309 guidance mechanism that regularizes the learned policy using high-performing actions from the
 310 replay buffer. This approach avoids explicit density estimation and reduces iterative sampling steps,
 311 achieving stable training and improved sample efficiency. Empirical results demonstrate that FlowRL
 312 achieves competitive performance.

313 **References**

- 314 [1] Richard Bellman. A markovian decision process. *Journal of mathematics and mechanics*, pages
315 679–684, 1957.
- 316 [2] Kevin Black, Noah Brown, Danny Driess, Adnan Esmail, Michael Equi, Chelsea Finn, Niccolo
317 Fusai, Lachy Groom, Karol Hausman, Brian Ichter, et al. A vision-languageaction flow model
318 for general robot control. *arXiv preprint arXiv:2410.24164*, 2(3):5, 2024.
- 319 [3] Avishek Joey Bose, Tara Akhound-Sadegh, Guillaume Huguet, Kilian Fatras, Jarrid Rector-
320 Brooks, Cheng-Hao Liu, Andrei Cristian Nica, Maksym Korablyov, Michael Bronstein, and
321 Alexander Tong. Se (3)-stochastic flow matching for protein backbone generation. *arXiv
322 preprint arXiv:2310.02391*, 2023.
- 323 [4] Huayu Chen, Cheng Lu, Chengyang Ying, Hang Su, and Jun Zhu. Offline reinforcement
324 learning via high-fidelity generative behavior modeling. *arXiv preprint arXiv:2209.14548*,
325 2022.
- 326 [5] Ricky TQ Chen, Yulia Rubanova, Jesse Bettencourt, and David K Duvenaud. Neural ordinary
327 differential equations. *Advances in neural information processing systems*, 31, 2018.
- 328 [6] Cheng Chi, Zhenjia Xu, Siyuan Feng, Eric Cousineau, Yilun Du, Benjamin Burchfiel, Russ
329 Tedrake, and Shuran Song. Diffusion policy: Visuomotor policy learning via action diffusion.
330 *The International Journal of Robotics Research*, page 02783649241273668, 2023.
- 331 [7] Prafulla Dhariwal and Alexander Nichol. Diffusion models beat gans on image synthesis.
332 *Advances in neural information processing systems*, 34:8780–8794, 2021.
- 333 [8] Shutong Ding, Ke Hu, Zhenhao Zhang, Kan Ren, Weinan Zhang, Jingyi Yu, Jingya Wang, and
334 Ye Shi. Diffusion-based reinforcement learning via q-weighted variational policy optimization.
335 *arXiv preprint arXiv:2405.16173*, 2024.
- 336 [9] Zihan Ding and Chi Jin. Consistency models as a rich and efficient policy class for reinforcement
337 learning. *arXiv preprint arXiv:2309.16984*, 2023.
- 338 [10] Jiajun Fan, Shuaike Shen, Chaoran Cheng, Yuxin Chen, Chumeng Liang, and Ge Liu. Online
339 reward-weighted fine-tuning of flow matching with wasserstein regularization. *arXiv preprint
340 arXiv:2502.06061*, 2025.
- 341 [11] Scott Fujimoto and Shixiang Shane Gu. A minimalist approach to offline reinforcement learning.
342 *Advances in neural information processing systems*, 34:20132–20145, 2021.
- 343 [12] Scott Fujimoto, Herke Hoof, and David Meger. Addressing function approximation error
344 in actor-critic methods. In *International conference on machine learning*, pages 1587–1596.
345 PMLR, 2018.
- 346 [13] Tuomas Haarnoja, Aurick Zhou, Pieter Abbeel, and Sergey Levine. Soft actor-critic: Off-
347 policy maximum entropy deep reinforcement learning with a stochastic actor. In *International
348 conference on machine learning*, pages 1861–1870. Pmlr, 2018.
- 349 [14] Nicklas Hansen, Hao Su, and Xiaolong Wang. Td-mpc2: Scalable, robust world models for
350 continuous control. *arXiv preprint arXiv:2310.16828*, 2023.
- 351 [15] Longxiang He, Li Shen, Linrui Zhang, Junbo Tan, and Xueqian Wang. Diffcps: Diffusion
352 model based constrained policy search for offline reinforcement learning. *arXiv preprint
353 arXiv:2310.05333*, 2023.
- 354 [16] Jonathan Ho, Ajay Jain, and Pieter Abbeel. Denoising diffusion probabilistic models. *Advances
355 in neural information processing systems*, 33:6840–6851, 2020.
- 356 [17] Bowen Jing, Bonnie Berger, and Tommi Jaakkola. Alphafold meets flow matching for generating
357 protein ensembles. *arXiv preprint arXiv:2402.04845*, 2024.

- 358 [18] Bingyi Kang, Xiao Ma, Chao Du, Tianyu Pang, and Shuicheng Yan. Efficient diffusion policies
 359 for offline reinforcement learning. *Advances in Neural Information Processing Systems*, 36:
 360 67195–67212, 2023.
- 361 [19] Ilya Kostrikov, Ashvin Nair, and Sergey Levine. Offline reinforcement learning with implicit
 362 q-learning. *arXiv preprint arXiv:2110.06169*, 2021.
- 363 [20] Aviral Kumar, Justin Fu, Matthew Soh, George Tucker, and Sergey Levine. Stabilizing off-
 364 policy q-learning via bootstrapping error reduction. *Advances in neural information processing*
 365 *systems*, 32, 2019.
- 366 [21] Sergey Levine, Aviral Kumar, George Tucker, and Justin Fu. Offline reinforcement learning:
 367 Tutorial, review, and perspectives on open problems. *arXiv preprint arXiv:2005.01643*, 2020.
- 368 [22] Yaron Lipman, Ricky TQ Chen, Heli Ben-Hamu, Maximilian Nickel, and Matt Le. Flow
 369 matching for generative modeling. *arXiv preprint arXiv:2210.02747*, 2022.
- 370 [23] Xingchao Liu, Chengyue Gong, and Qiang Liu. Flow straight and fast: Learning to generate
 371 and transfer data with rectified flow. *arXiv preprint arXiv:2209.03003*, 2022.
- 372 [24] Cheng Lu, Huayu Chen, Jianfei Chen, Hang Su, Chongxuan Li, and Jun Zhu. Contrastive
 373 energy prediction for exact energy-guided diffusion sampling in offline reinforcement learning.
 374 In *International Conference on Machine Learning*, pages 22825–22855. PMLR, 2023.
- 375 [25] Yu Luo, Tianying Ji, Fuchun Sun, Jianwei Zhang, Huazhe Xu, and Xianyuan Zhan. Offline-
 376 boosted actor-critic: Adaptively blending optimal historical behaviors in deep off-policy rl.
 377 *arXiv preprint arXiv:2405.18520*, 2024.
- 378 [26] Liyuan Mao, Haoran Xu, Xianyuan Zhan, Weinan Zhang, and Amy Zhang. Diffusion-dice: In-
 379 sample diffusion guidance for offline reinforcement learning. *arXiv preprint arXiv:2407.20109*,
 380 2024.
- 381 [27] Junhyuk Oh, Yijie Guo, Satinder Singh, and Honglak Lee. Self-imitation learning. In *International*
 382 *conference on machine learning*, pages 3878–3887. PMLR, 2018.
- 383 [28] Georg Ostrovski, Pablo Samuel Castro, and Will Dabney. The difficulty of passive learning
 384 in deep reinforcement learning. *Advances in Neural Information Processing Systems*, 34:
 385 23283–23295, 2021.
- 386 [29] Seohong Park, Kevin Frans, Sergey Levine, and Aviral Kumar. Is value learning really the main
 387 bottleneck in offline rl? *arXiv preprint arXiv:2406.09329*, 2024.
- 388 [30] Seohong Park, Qiyang Li, and Sergey Levine. Flow q-learning. *arXiv preprint*
 389 *arXiv:2502.02538*, 2025.
- 390 [31] Xue Bin Peng, Aviral Kumar, Grace Zhang, and Sergey Levine. Advantage-weighted regression:
 391 Simple and scalable off-policy reinforcement learning. *arXiv preprint arXiv:1910.00177*, 2019.
- 392 [32] Jan Peters and Stefan Schaal. Reinforcement learning by reward-weighted regression for
 393 operational space control. In *Proceedings of the 24th international conference on Machine*
 394 *learning*, pages 745–750, 2007.
- 395 [33] Michael Psenka, Alejandro Escontrela, Pieter Abbeel, and Yi Ma. Learning a diffusion model
 396 policy from rewards via q-score matching. *arXiv preprint arXiv:2312.11752*, 2023.
- 397 [34] Allen Z Ren, Justin Lidard, Lars L Ankile, Anthony Simeonov, Pulkit Agrawal, Anirudha
 398 Majumdar, Benjamin Burchfiel, Hongkai Dai, and Max Simchowitz. Diffusion policy policy
 399 optimization. *arXiv preprint arXiv:2409.00588*, 2024.
- 400 [35] Carmelo Sferrazza, Dun-Ming Huang, Xingyu Lin, Youngwoon Lee, and Pieter Abbeel. Hu-
 401 manoidbench: Simulated humanoid benchmark for whole-body locomotion and manipulation.
 402 *arXiv preprint arXiv:2403.10506*, 2024.

- 403 [36] David Silver, Guy Lever, Nicolas Heess, Thomas Degris, Daan Wierstra, and Martin Riedmiller.
 404 Deterministic policy gradient algorithms. In *International conference on machine learning*,
 405 pages 387–395. Pmlr, 2014.
- 406 [37] Yang Song, Jascha Sohl-Dickstein, Diederik P Kingma, Abhishek Kumar, Stefano Ermon, and
 407 Ben Poole. Score-based generative modeling through stochastic differential equations. *arXiv*
 408 preprint arXiv:2011.13456, 2020.
- 409 [38] Richard S Sutton, Andrew G Barto, et al. Reinforcement learning. *Journal of Cognitive*
 410 *Neuroscience*, 11(1):126–134, 1999.
- 411 [39] Yuval Tassa, Yotam Doron, Alistair Muldal, Tom Erez, Yazhe Li, Diego de Las Casas, David
 412 Budden, Abbas Abdolmaleki, Josh Merel, Andrew Lefrancq, et al. Deepmind control suite.
 413 *arXiv preprint arXiv:1801.00690*, 2018.
- 414 [40] Alexander Tong, Kilian Fatras, Nikolay Malkin, Guillaume Huguet, Yanlei Zhang, Jarrid Rector-
 415 Brooks, Guy Wolf, and Yoshua Bengio. Improving and generalizing flow-based generative
 416 models with minibatch optimal transport. *arXiv preprint arXiv:2302.00482*, 2023.
- 417 [41] Cédric Villani et al. *Optimal transport: old and new*, volume 338. Springer, 2008.
- 418 [42] Yinuo Wang, Likun Wang, Yuxuan Jiang, Wenjun Zou, Tong Liu, Xujie Song, Wenxuan Wang,
 419 Liming Xiao, Jiang Wu, Jingliang Duan, et al. Diffusion actor-critic with entropy regulator.
 420 *Advances in Neural Information Processing Systems*, 37:54183–54204, 2024.
- 421 [43] Zhendong Wang, Jonathan J Hunt, and Mingyuan Zhou. Diffusion policies as an expressive
 422 policy class for offline reinforcement learning. *arXiv preprint arXiv:2208.06193*, 2022.
- 423 [44] Long Yang, Zhixiong Huang, Fenghao Lei, Yucun Zhong, Yiming Yang, Cong Fang, Shiting
 424 Wen, Binbin Zhou, and Zhouchen Lin. Policy representation via diffusion probability model for
 425 reinforcement learning. *arXiv preprint arXiv:2305.13122*, 2023.
- 426 [45] Shiyuan Zhang, Weitong Zhang, and Quanquan Gu. Energy-weighted flow matching for offline
 427 reinforcement learning. *arXiv preprint arXiv:2503.04975*, 2025.

428 **A Proofs in the Main Text**

429 Here, we present a sketch of theoretical analyses in Figure 5. We model the policy learning as a
 430 constrained policy search that maximizes expected returns while bounding the distance to an optimal
 431 behavior policy. To avoid sampling from π_β^* , we employ guided flow matching, which allows the
 432 constraint to utilize arbitrary data from the buffer. Finally, we solve the problem using Lagrangian
 433 relaxation.

434 **A.1 Proof for Theorem 4.1**

435 Before the proof, we first introduce the following lemma [10]:

436 **Lemma 1** :Let $\psi_1^t(x_0)$ and $\psi_2^t(x_0)$ be the two different flow maps induced by v_1^t and v_2^t starting
 437 from x^0 , and assume v_2^t are Lipschitz continuous in x with constant L . Define their difference as
 438 $\Delta_t(x^0) = \psi_1^t(x^0) - \psi_2^t(x^0)$. (For notational consistency, we denote the time variable as a superscript.)
 439 Then the difference satisfies the following inequality:

$$\frac{d}{dt} \Delta_t(x_0) \leq \|v_1^t(\psi_1^t(x^0)) - v_2^t(\psi_1^t(x^0))\| + L\|\Delta_t(x_0)\|$$

440 By rewriting equivalently, we have:

$$\frac{d}{dt} \Delta_t(x^0) = \underbrace{v_1^t(\psi_1^t(x^0)) - v_2^t(\psi_1^t(x^0))}_{\delta_v(t)} + \underbrace{v_2^t(\psi_1^t(x^1)) - v_2^t(\psi_2^t(x^0))}_{\delta_\psi(t)}$$

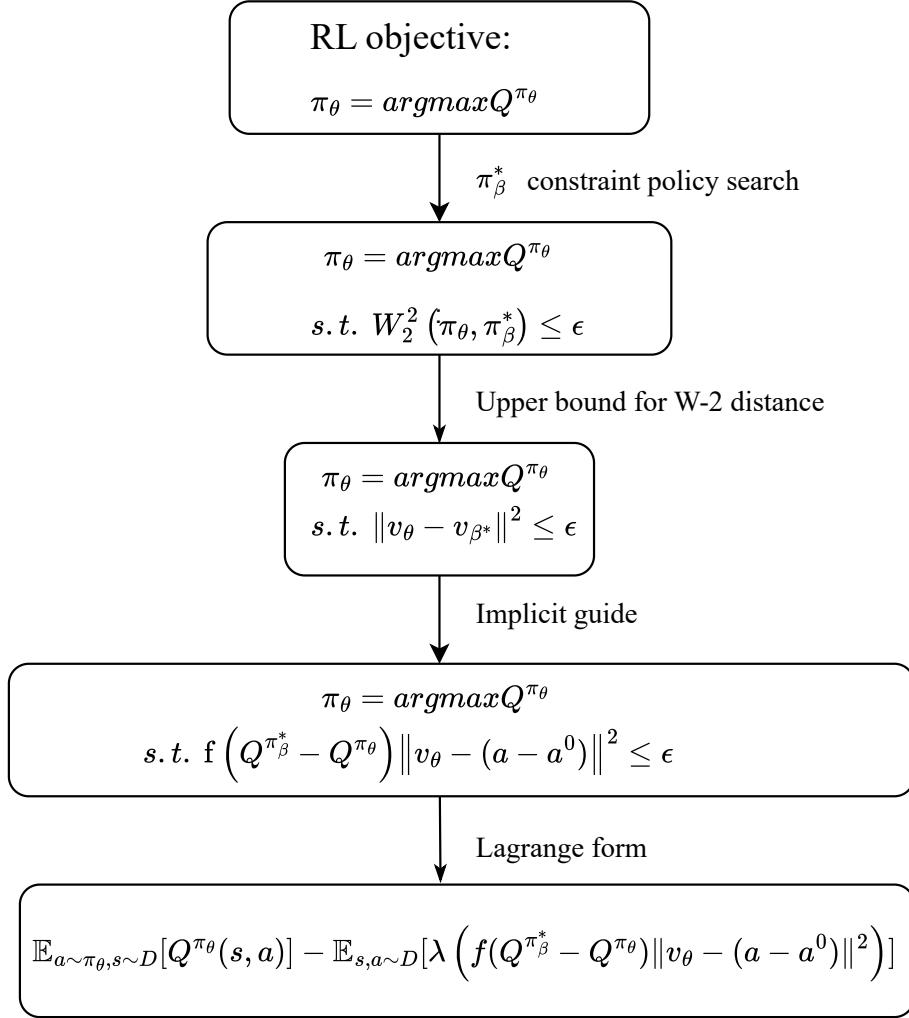


Figure 5: Theoretical sketch of FlowRL

⁴⁴¹ Since v_2^t is Lipschitz continuous in x with constant L , we have:

$$\|v_2^t(x) - v_2^t(y)\| \leq L\|x - y\|$$

⁴⁴² By Lipschitz continuity,

$$\|\delta_\psi(t)\| \leq L\|\Delta_t(x^0)\|$$

⁴⁴³ Then,

$$\left\| \frac{d}{dt} \Delta_t(x^0) \right\| \leq \|\delta_v(t)\| + L\|\Delta_t(x^0)\|$$

⁴⁴⁴ This concludes the proof of the inequality satisfied by the difference of the two flow maps.

⁴⁴⁵ Let v_θ and v_{β^*} be two velocity fields that induce time-evolving distributions $\pi_\theta^t(a|s)$ and $\pi_{\beta^*}^t(a|s)$,

⁴⁴⁶ respectively((we omit the superscript $t = 1$ for policy distributions, i.e., $\pi_\theta(a|s) := \pi_\theta^1(a|s)$)).

⁴⁴⁷ Assume v_{β^*} is Lipschitz continuous with constant L . Then, define $f(t) = \|\Delta_t(x_0)\|$, by Lemma 448 1, we have:

$$\frac{d}{dt} f(t) \leq \|\delta_v(t)\| + Lf(t),$$

449 where $\delta_v(t) = v_\theta(t, \psi_t^\theta(s, a^0)) - v_{\beta^*}$. Then, we have,

$$\frac{d}{dt} (e^{-Lt} f(t)) \leq e^{-Lt} \|\delta_v(t)\|.$$

450 Then we can get (by simply intergrating from 0 to t both side and multiplying e^{-Lt}):

$$e^{-Lt} f(t) - f(0) \leq \int_0^t e^{-Lm} \|\delta_v(m)\| dm.$$

451 The initial policy distribution $a^0 \sim p(a^0)$ is shared between the two velocity fields, so $f(0) = 0$.

452 Therefore,

$$f(t) \leq e^{Lt} \int_0^t e^{-Lm} \|\delta_v(m)\| dm.$$

453 At $t = 1$,

$$f(1) \leq e^L \int_0^1 e^{-Lm} \|v_\theta(s, \psi_\theta^t(s, a^0), m) - v_{\beta^*}\| dm.$$

454 By taking the expectation and using Jensen's inequality:

$$\mathbb{E}_{a^0}[f(1)^2] \leq e^{2L} \int_0^1 \mathbb{E}_{a \sim \pi_\theta^t} [\|v_\theta(s, a, t) - v_{\beta^*}\|^2] dt.$$

455 And use the definition of the Wasserstein-2 distance:

$$W_2^2(\pi_\theta, \pi_{\beta^*}) = \inf_{\gamma \in \Pi(\pi_\theta, \pi_{\beta^*})} \int_{\mathbb{R}^n \times \mathbb{R}^n} \|x - y\|^2 d\gamma(x, y),$$

456 where $\Pi(\pi_\theta, \pi_{\beta^*})$ denotes the set of all couplings between π_θ and π_{β^*} . Construct the following
457 coupling γ and define:

- 458 • $a_\theta^1 = \psi_\theta^1(x_0)$,
- 459 • $a_{\beta^*}^1 = \psi_{\beta^*}^1(x_0)$.

460 By definition, the coupling γ is defined via the joint distribution of $(a \sim \pi_\theta, a \sim \pi_{\beta^*})$ induced by
461 $a_0 \sim p_0$. So, for any coupling γ ,

$$W_2^2(\pi_\theta, \pi_{\beta^*}) \leq \int_{\mathbb{R}^n \times \mathbb{R}^n} \|x - y\|^2 d\gamma(x, y).$$

462 With the constructed coupling substituted, we have

$$\int_{\mathbb{R}^n \times \mathbb{R}^n} \|x - y\|^2 d\gamma(x, y) = \mathbb{E}_{a^0} [\|\psi_\theta^1(a^0) - \psi_{\beta^*}^1(a^0)\|^2] = \mathbb{E}_{a^0}[f(1)^2].$$

463 Recall that the flow-based policy models transport the initial distribution $p_0(a^0)$ to the final policy
464 distributions π_θ and π_{β^*} at $t = 1$. The squared Wasserstein-2 distance between π_θ and π_{β^*} can be
465 bounded as

$$W_2^2(\pi_\theta, \pi_{\beta^*}) \leq \mathbb{E}_{a^0}[f(1)^2]. \quad (23)$$

466 Thus,

$$W_2^2(\pi_\theta, \pi_{\beta^*}) \leq e^{2L} \int_0^1 \mathbb{E}_{a \sim \pi_\theta^t} [\|v_\theta(s, a^t) - v_{\beta^*}(s, a)\|^2] ds. \quad (24)$$

467 A.2 Proof for Theorem 4.2

468 The weighted loss can be written as:

$$\mathcal{L}_W(\theta) = \int_{s \sim D} \rho(s) \int_{s, a \sim D} f(s, a) \pi_k(a|s) \|v_\theta(s, a^t, t) - (a - a^0)\| da ds$$

469 where $\rho(s)$ is the state distribution in replay buffer, $a^0 \sim \mathcal{N}(0, I^2)$, $t \sim \mathcal{U}(0, 1)$, $a^t = ta + (1-t)a^0$.

470 Assuming the weighted policy distribution is:

$$\pi_{k+1}(a'|s) = \frac{f(s, a) \pi_k(a|s)}{\mathcal{Z}(s)}, \quad \text{where } \mathcal{Z}(s) = \int_{s, a \sim D} f(s, a) \pi_k(a|s) da.$$

471 Substituting above $\pi_{k+1}(a'|s)$ into the loss function, we have:

$$\mathcal{L}_W(\theta) = \int_{s \sim D} \rho(s) \mathcal{Z}(s) \int_{s, a \sim D} \pi_{k+1}(a'|s) \|v_\theta(s, a^t, t) - (a - a^0)\| da ds.$$

472 The expectation form:

$$\mathcal{L}_W(\theta) = \mathbb{E}_{s \sim \mathcal{D}, a \sim \pi_{k+1}(a|s)} [\mathcal{Z}(s) \|v_\theta(s, a^t, t) - (a - a^0)\|].$$

473 The gradient of $\mathcal{L}_W(\theta)$ is:

$$\nabla_\theta \mathcal{L}_W(\theta) = \mathbb{E}_{s \sim \mathcal{D}, a \sim \pi_{k+1}(a|s)} [\mathcal{Z}(s) \nabla_\theta \|v_\theta(s, a, t) - (a - a^0)\|].$$

474 $\mathcal{Z}(s)$ does not depend on θ , that means, minimizing $\mathcal{L}_W(\theta)$ is equivalent to minimizing the expected

475 loss under the new distribution $\pi_{k+1}(a|s)$, provided that our assumption holds.

476 B Hyperparameters and Experiment Settings

477 In this section, we provide comprehensive details regarding the implementation of FlowRL, the
478 baseline algorithms, and the experimental environments. All experiments are conducted on a single
479 NVIDIA H100 GPU and an Intel(R) Platinum 8480C CPU, with two tasks running in parallel on the
480 GPU.

481 B.1 Hyperparameters

482 The hyperparameters used in our experiments are summarized in Table 1. For the choice of the
483 weighting function, we use $f(x) = \mathbb{I}(x) \cdot \exp(x)$, where $\mathbb{I}(x)$ is the indicator function, i.e.,

$$\mathbb{I}(x) = \begin{cases} 1, & \text{if } x > 0 \\ 0, & \text{otherwise} \end{cases}$$

484 For numerical stability, the Q function is normalized by subtracting its mean exclusively during the
485 computation of the weighting function.

486 B.2 Baselines

487 In our experiments, we have implemented SAC, TD3, QVPO and TD-MPC2 using their original
488 code bases and slightly tuned them to match our evaluation protocol to ensure a fair and consistent
489 comparison.

- 490 • For SAC [13], we utilized the open-source PyTorch implementation, available at <https://github.com/pranz24/pytorch-soft-actor-critic>.
- 492 • TD3 [12] was integrated into our experiments through its official codebase, accessible at <https://github.com/sfujim/TD3>.
- 494 • QVPO [8] was integrated into our experiments through its official codebase, accessible at <https://github.com/wadx2019/qvpo>.
- 496 • TD-MPC2 [14] was employed with its official implementation from <https://github.com/nicklashansen/tdmpc2> and used their official results.

498 B.3 Environment Details

499 We validate our algorithm on the DMControl [39] and HumanoidBench [35], including the most
500 challenging high-dimensional and Unitree H1 humanoid robot control tasks. On DMControl, tasks
501 are categorized into DMC easy & middle (walker and quadruped domains), and DMC hard (dog and
502 humanoid domains). On HumanoidBench, we focus on tasks that do not require dexterous hands.

Table 1: Hyperparameters

	Hyperparameter	Value
Hyperparameters	Optimizer	Adam
	Critic learning rate	3×10^{-4}
	Actor learning rate	3×10^{-4}
	Discount factor	0.99
	Batchsize	256
	Replay buffer size	1×10^6
	Expectile factor τ	0.9
	Lagrangian multiplier λ	0.1
	Flow steps N	1
	ODE Slover	Midpoint Euler
Value network	Network hidden dim	512
	Network hidden layers	3
	Network activation function	mish
Policy network	Network hidden dim	512
	Network hidden layers	2
	Network activation function	elu

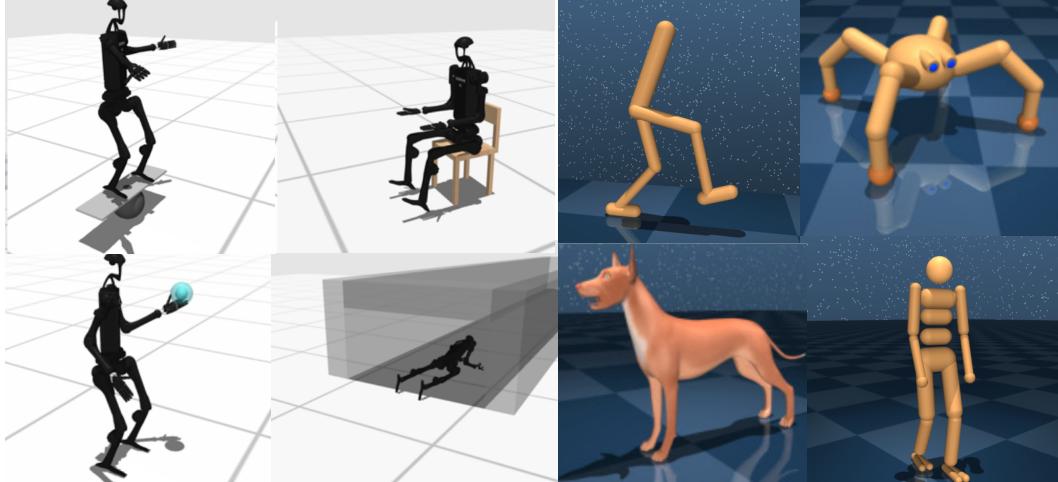


Figure 6: Task domain visualizations

503 B.4 Toy Example Setup

504 We consider a 2D toy example as follows. The behavior policy is a Gaussian mixture model with 10
505 components, each with mean

$$\mu_k = (10 \cos(2\pi k/10), 10 \sin(2\pi k/10)), \quad k = 0, 1, \dots, 9,$$

506 and covariance I . The initial distribution is a Gaussian $\mathcal{N}((0, 0), I)$. $Q^{\pi_{\beta^*}} - Q^{\pi_\theta}$ is defined as

$$\frac{1}{600} \|x - (0, 8.66)\|^2 - 3,$$

507 and $f(x) = \mathbb{I}(x) \cdot x$. Flow steps $N = 5$.

508 C Limitation and Future Work

509 In this work, we propose a flow-based reinforcement learning framework that leverages the behavior-
510 optimal policy as a constraint. Although competitive performance is achieved even without explicit
511 exploration, investigating efficient adaptive exploration mechanisms remains a promising direction
512 for future research.

Task	State dim	Action dim
Walker Run	24	6
Walker Stand	24	6
Quadruped Walk	78	12
Humanoid Run	67	24
Humanoid Walk	67	24
Dog Run	223	38
Dog Trot	223	38
Dog Stand	223	38
Dog Walk	223	38

Table 2: Task dimensions for DMControl.

Task	Observation dim	Action dim
H1 Balance Hard	77	19
H1 Balance Simple	64	19
H1 Crawl	51	19
H1 Maze	51	19
H1 Reach	57	19
H1 Sit Hard	64	19

Table 3: Task dimensions for HumanoidBench.

513 D More Experimental Results

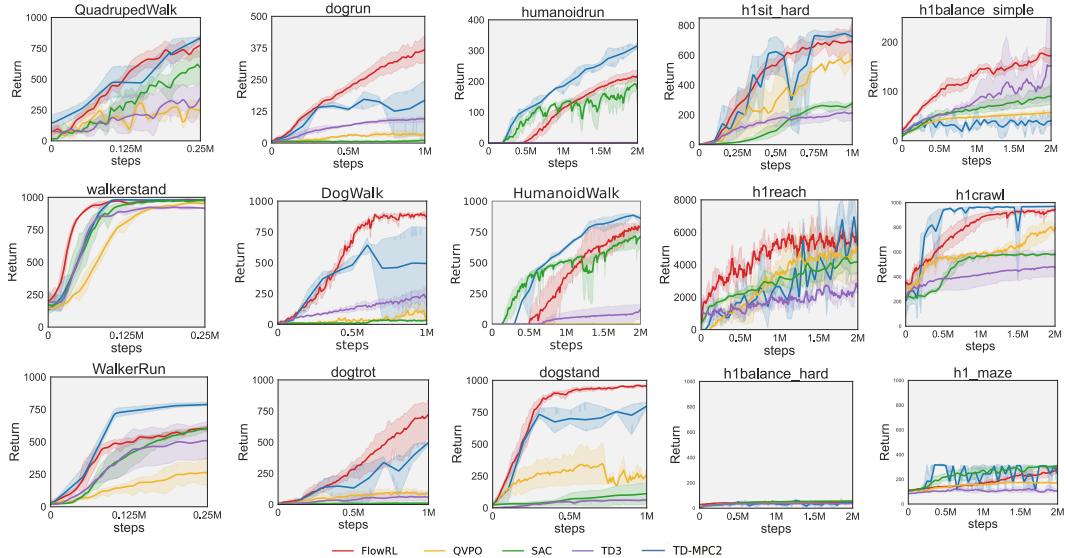


Figure 7: Experimental results are reported on 12 tasks drawn from HumanoidBench and DMC-hard, 3 tasks from DMC-easy & middle.

514 **NeurIPS Paper Checklist**

515 **1. Claims**

516 Question: Do the main claims made in the abstract and introduction accurately reflect the
517 paper's contributions and scope?

518 Answer: [Yes]

519 Justification: Yes, the main claims made in the abstract and introduction accurately reflect
520 the paper's contributions and scope.

521 Guidelines:

- 522 • The answer NA means that the abstract and introduction do not include the claims
523 made in the paper.
- 524 • The abstract and/or introduction should clearly state the claims made, including the
525 contributions made in the paper and important assumptions and limitations. A No or
526 NA answer to this question will not be perceived well by the reviewers.
- 527 • The claims made should match theoretical and experimental results, and reflect how
528 much the results can be expected to generalize to other settings.
- 529 • It is fine to include aspirational goals as motivation as long as it is clear that these goals
530 are not attained by the paper.

531 **2. Limitations**

532 Question: Does the paper discuss the limitations of the work performed by the authors?

533 Answer: [Yes]

534 Justification: Yes, the paper discusses its limitations in the appendix. Although competitive
535 performance is achieved without explicit exploration mechanisms, the exploration
536 regularization mechanism remains an important direction for future work.

537 Guidelines:

- 538 • The answer NA means that the paper has no limitation while the answer No means that
539 the paper has limitations, but those are not discussed in the paper.
- 540 • The authors are encouraged to create a separate "Limitations" section in their paper.
- 541 • The paper should point out any strong assumptions and how robust the results are to
542 violations of these assumptions (e.g., independence assumptions, noiseless settings,
543 model well-specification, asymptotic approximations only holding locally). The authors
544 should reflect on how these assumptions might be violated in practice and what the
545 implications would be.
- 546 • The authors should reflect on the scope of the claims made, e.g., if the approach was
547 only tested on a few datasets or with a few runs. In general, empirical results often
548 depend on implicit assumptions, which should be articulated.
- 549 • The authors should reflect on the factors that influence the performance of the approach.
550 For example, a facial recognition algorithm may perform poorly when image resolution
551 is low or images are taken in low lighting. Or a speech-to-text system might not be
552 used reliably to provide closed captions for online lectures because it fails to handle
553 technical jargon.
- 554 • The authors should discuss the computational efficiency of the proposed algorithms
555 and how they scale with dataset size.
- 556 • If applicable, the authors should discuss possible limitations of their approach to
557 address problems of privacy and fairness.
- 558 • While the authors might fear that complete honesty about limitations might be used by
559 reviewers as grounds for rejection, a worse outcome might be that reviewers discover
560 limitations that aren't acknowledged in the paper. The authors should use their best
561 judgment and recognize that individual actions in favor of transparency play an impor-
562 tant role in developing norms that preserve the integrity of the community. Reviewers
563 will be specifically instructed to not penalize honesty concerning limitations.

564 **3. Theory Assumptions and Proofs**

565 Question: For each theoretical result, does the paper provide the full set of assumptions and
566 a complete (and correct) proof?

567 Answer: [Yes]

568 Justification: Yes, the paper provides the full set of assumptions and complete proofs for all
569 theorems in the appendix.

570 Guidelines:

- 571 • The answer NA means that the paper does not include theoretical results.
- 572 • All the theorems, formulas, and proofs in the paper should be numbered and cross-
573 referenced.
- 574 • All assumptions should be clearly stated or referenced in the statement of any theorems.
- 575 • The proofs can either appear in the main paper or the supplemental material, but if
576 they appear in the supplemental material, the authors are encouraged to provide a short
577 proof sketch to provide intuition.
- 578 • Inversely, any informal proof provided in the core of the paper should be complemented
579 by formal proofs provided in appendix or supplemental material.
- 580 • Theorems and Lemmas that the proof relies upon should be properly referenced.

581 4. Experimental Result Reproducibility

582 Question: Does the paper fully disclose all the information needed to reproduce the main ex-
583 perimental results of the paper to the extent that it affects the main claims and/or conclusions
584 of the paper (regardless of whether the code and data are provided or not)?

585 Answer: [Yes]

586 Justification: Yes, the paper fully discloses all information needed to reproduce the main
587 experimental results. Pseudocode is provided in the main text, and all experimental settings,
588 hyperparameters, and baseline details are included in the appendix.

589 Guidelines:

- 590 • The answer NA means that the paper does not include experiments.
- 591 • If the paper includes experiments, a No answer to this question will not be perceived
592 well by the reviewers: Making the paper reproducible is important, regardless of
593 whether the code and data are provided or not.
- 594 • If the contribution is a dataset and/or model, the authors should describe the steps taken
595 to make their results reproducible or verifiable.
- 596 • Depending on the contribution, reproducibility can be accomplished in various ways.
597 For example, if the contribution is a novel architecture, describing the architecture fully
598 might suffice, or if the contribution is a specific model and empirical evaluation, it may
599 be necessary to either make it possible for others to replicate the model with the same
600 dataset, or provide access to the model. In general, releasing code and data is often
601 one good way to accomplish this, but reproducibility can also be provided via detailed
602 instructions for how to replicate the results, access to a hosted model (e.g., in the case
603 of a large language model), releasing of a model checkpoint, or other means that are
604 appropriate to the research performed.
- 605 • While NeurIPS does not require releasing code, the conference does require all submis-
606 sions to provide some reasonable avenue for reproducibility, which may depend on the
607 nature of the contribution. For example
 - 608 (a) If the contribution is primarily a new algorithm, the paper should make it clear how
609 to reproduce that algorithm.
 - 610 (b) If the contribution is primarily a new model architecture, the paper should describe
611 the architecture clearly and fully.
 - 612 (c) If the contribution is a new model (e.g., a large language model), then there should
613 either be a way to access this model for reproducing the results or a way to reproduce
614 the model (e.g., with an open-source dataset or instructions for how to construct
615 the dataset).
 - 616 (d) We recognize that reproducibility may be tricky in some cases, in which case
617 authors are welcome to describe the particular way they provide for reproducibility.
618 In the case of closed-source models, it may be that access to the model is limited in
619 some way (e.g., to registered users), but it should be possible for other researchers
620 to have some path to reproducing or verifying the results.

621 **5. Open access to data and code**

622 Question: Does the paper provide open access to the data and code, with sufficient instructions
623 to faithfully reproduce the main experimental results, as described in supplemental
624 material?

625 Answer: [Yes]

626 Justification: Yes, the code will be made available after the open-source approval process is
627 completed.

628 Guidelines:

- 629 • The answer NA means that paper does not include experiments requiring code.
- 630 • Please see the NeurIPS code and data submission guidelines (<https://nips.cc/public/guides/CodeSubmissionPolicy>) for more details.
- 632 • While we encourage the release of code and data, we understand that this might not be
633 possible, so “No” is an acceptable answer. Papers cannot be rejected simply for not
634 including code, unless this is central to the contribution (e.g., for a new open-source
635 benchmark).
- 636 • The instructions should contain the exact command and environment needed to run to
637 reproduce the results. See the NeurIPS code and data submission guidelines (<https://nips.cc/public/guides/CodeSubmissionPolicy>) for more details.
- 639 • The authors should provide instructions on data access and preparation, including how
640 to access the raw data, preprocessed data, intermediate data, and generated data, etc.
- 641 • The authors should provide scripts to reproduce all experimental results for the new
642 proposed method and baselines. If only a subset of experiments are reproducible, they
643 should state which ones are omitted from the script and why.
- 644 • At submission time, to preserve anonymity, the authors should release anonymized
645 versions (if applicable).
- 646 • Providing as much information as possible in supplemental material (appended to the
647 paper) is recommended, but including URLs to data and code is permitted.

648 **6. Experimental Setting/Details**

649 Question: Does the paper specify all the training and test details (e.g., data splits, hyper-
650 parameters, how they were chosen, type of optimizer, etc.) necessary to understand the
651 results?

652 Answer: [Yes]

653 Justification: Yes, all hyperparameters and experimental setup details necessary to under-
654 stand the results are provided in the appendix.

655 Guidelines:

- 656 • The answer NA means that the paper does not include experiments.
- 657 • The experimental setting should be presented in the core of the paper to a level of detail
658 that is necessary to appreciate the results and make sense of them.
- 659 • The full details can be provided either with the code, in appendix, or as supplemental
660 material.

661 **7. Experiment Statistical Significance**

662 Question: Does the paper report error bars suitably and correctly defined or other appropriate
663 information about the statistical significance of the experiments?

664 Answer: [Yes]

665 Justification: Yes, for all model-free algorithms, five random seeds are used, and for model-
666 based algorithm, three random seeds are used. All results are presented as mean \pm standard
667 deviation.

668 Guidelines:

- 669 • The answer NA means that the paper does not include experiments.
- 670 • The authors should answer "Yes" if the results are accompanied by error bars, confi-
671 dence intervals, or statistical significance tests, at least for the experiments that support
672 the main claims of the paper.

- The factors of variability that the error bars are capturing should be clearly stated (for example, train/test split, initialization, random drawing of some parameter, or overall run with given experimental conditions).
- The method for calculating the error bars should be explained (closed form formula, call to a library function, bootstrap, etc.)
- The assumptions made should be given (e.g., Normally distributed errors).
- It should be clear whether the error bar is the standard deviation or the standard error of the mean.
- It is OK to report 1-sigma error bars, but one should state it. The authors should preferably report a 2-sigma error bar than state that they have a 96% CI, if the hypothesis of Normality of errors is not verified.
- For asymmetric distributions, the authors should be careful not to show in tables or figures symmetric error bars that would yield results that are out of range (e.g. negative error rates).
- If error bars are reported in tables or plots, The authors should explain in the text how they were calculated and reference the corresponding figures or tables in the text.

689 8. Experiments Compute Resources

690 Question: For each experiment, does the paper provide sufficient information on the
 691 computer resources (type of compute workers, memory, time of execution) needed to reproduce
 692 the experiments?

693 Answer: [Yes]

694 Justification: Yes, the appendix provides detailed information about the specific computational
 695 devices used for the experiments.

696 Guidelines:

- The answer NA means that the paper does not include experiments.
- The paper should indicate the type of compute workers CPU or GPU, internal cluster, or cloud provider, including relevant memory and storage.
- The paper should provide the amount of compute required for each of the individual experimental runs as well as estimate the total compute.
- The paper should disclose whether the full research project required more compute than the experiments reported in the paper (e.g., preliminary or failed experiments that didn't make it into the paper).

705 9. Code Of Ethics

706 Question: Does the research conducted in the paper conform, in every respect, with the
 707 NeurIPS Code of Ethics <https://neurips.cc/public/EthicsGuidelines>?

708 Answer: [Yes]

709 Justification: We make sure the code was anonymous

710 Guidelines:

- The answer NA means that the authors have not reviewed the NeurIPS Code of Ethics.
- If the authors answer No, they should explain the special circumstances that require a deviation from the Code of Ethics.
- The authors should make sure to preserve anonymity (e.g., if there is a special consideration due to laws or regulations in their jurisdiction).

716 10. Broader Impacts

717 Question: Does the paper discuss both potential positive societal impacts and negative
 718 societal impacts of the work performed?

719 Answer: [Yes]

720 Justification: Yes, the appendix discusses both potential positive societal impacts and
 721 limitations of the work.

722 Guidelines:

- The answer NA means that there is no societal impact of the work performed.

- 724 • If the authors answer NA or No, they should explain why their work has no societal
 725 impact or why the paper does not address societal impact.
 726 • Examples of negative societal impacts include potential malicious or unintended uses
 727 (e.g., disinformation, generating fake profiles, surveillance), fairness considerations
 728 (e.g., deployment of technologies that could make decisions that unfairly impact specific
 729 groups), privacy considerations, and security considerations.
 730 • The conference expects that many papers will be foundational research and not tied
 731 to particular applications, let alone deployments. However, if there is a direct path to
 732 any negative applications, the authors should point it out. For example, it is legitimate
 733 to point out that an improvement in the quality of generative models could be used to
 734 generate deepfakes for disinformation. On the other hand, it is not needed to point out
 735 that a generic algorithm for optimizing neural networks could enable people to train
 736 models that generate Deepfakes faster.
 737 • The authors should consider possible harms that could arise when the technology is
 738 being used as intended and functioning correctly, harms that could arise when the
 739 technology is being used as intended but gives incorrect results, and harms following
 740 from (intentional or unintentional) misuse of the technology.
 741 • If there are negative societal impacts, the authors could also discuss possible mitigation
 742 strategies (e.g., gated release of models, providing defenses in addition to attacks,
 743 mechanisms for monitoring misuse, mechanisms to monitor how a system learns from
 744 feedback over time, improving the efficiency and accessibility of ML).

745 11. Safeguards

746 Question: Does the paper describe safeguards that have been put in place for responsible
 747 release of data or models that have a high risk for misuse (e.g., pretrained language models,
 748 image generators, or scraped datasets)?

749 Answer: [NA]

750 Justification:

751 Guidelines:

- 752 • The answer NA means that the paper poses no such risks.
- 753 • Released models that have a high risk for misuse or dual-use should be released with
 754 necessary safeguards to allow for controlled use of the model, for example by requiring
 755 that users adhere to usage guidelines or restrictions to access the model or implementing
 756 safety filters.
- 757 • Datasets that have been scraped from the Internet could pose safety risks. The authors
 758 should describe how they avoided releasing unsafe images.
- 759 • We recognize that providing effective safeguards is challenging, and many papers do
 760 not require this, but we encourage authors to take this into account and make a best
 761 faith effort.

762 12. Licenses for existing assets

763 Question: Are the creators or original owners of assets (e.g., code, data, models), used in
 764 the paper, properly credited and are the license and terms of use explicitly mentioned and
 765 properly respected?

766 Answer: [Yes]

767 Justification: Yes, all sources of data and code are properly credited in the appendix, with
 768 licenses and terms of use clearly indicated.

769 Guidelines:

- 770 • The answer NA means that the paper does not use existing assets.
- 771 • The authors should cite the original paper that produced the code package or dataset.
- 772 • The authors should state which version of the asset is used and, if possible, include a
 773 URL.
- 774 • The name of the license (e.g., CC-BY 4.0) should be included for each asset.
- 775 • For scraped data from a particular source (e.g., website), the copyright and terms of
 776 service of that source should be provided.

- 777 • If assets are released, the license, copyright information, and terms of use in the
778 package should be provided. For popular datasets, paperswithcode.com/datasets
779 has curated licenses for some datasets. Their licensing guide can help determine the
780 license of a dataset.
781 • For existing datasets that are re-packaged, both the original license and the license of
782 the derived asset (if it has changed) should be provided.
783 • If this information is not available online, the authors are encouraged to reach out to
784 the asset's creators.

785 **13. New Assets**

786 Question: Are new assets introduced in the paper well documented and is the documentation
787 provided alongside the assets?

788 Answer: [NA]

789 Justification:

790 Guidelines:

- 791 • The answer NA means that the paper does not release new assets.
792 • Researchers should communicate the details of the dataset/code/model as part of their
793 submissions via structured templates. This includes details about training, license,
794 limitations, etc.
795 • The paper should discuss whether and how consent was obtained from people whose
796 asset is used.
797 • At submission time, remember to anonymize your assets (if applicable). You can either
798 create an anonymized URL or include an anonymized zip file.

799 **14. Crowdsourcing and Research with Human Subjects**

800 Question: For crowdsourcing experiments and research with human subjects, does the paper
801 include the full text of instructions given to participants and screenshots, if applicable, as
802 well as details about compensation (if any)?

803 Answer:[NA]

804 Justification:

805 Guidelines:

- 806 • The answer NA means that the paper does not involve crowdsourcing nor research with
807 human subjects.
808 • Including this information in the supplemental material is fine, but if the main contribu-
809 tion of the paper involves human subjects, then as much detail as possible should be
810 included in the main paper.
811 • According to the NeurIPS Code of Ethics, workers involved in data collection, curation,
812 or other labor should be paid at least the minimum wage in the country of the data
813 collector.

814 **15. Institutional Review Board (IRB) Approvals or Equivalent for Research with Human
815 Subjects**

816 Question: Does the paper describe potential risks incurred by study participants, whether
817 such risks were disclosed to the subjects, and whether Institutional Review Board (IRB)
818 approvals (or an equivalent approval/review based on the requirements of your country or
819 institution) were obtained?

820 Answer: [NA]

821 Justification:

822 Guidelines:

- 823 • The answer NA means that the paper does not involve crowdsourcing nor research with
824 human subjects.
825 • Depending on the country in which research is conducted, IRB approval (or equivalent)
826 may be required for any human subjects research. If you obtained IRB approval, you
827 should clearly state this in the paper.

- 828
- We recognize that the procedures for this may vary significantly between institutions
- 829
- and locations, and we expect authors to adhere to the NeurIPS Code of Ethics and the
- 830
- guidelines for their institution.
- 831
- For initial submissions, do not include any information that would break anonymity (if
- 832
- applicable), such as the institution conducting the review.