## Ex3

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# 1 Estruturas Criptográficas - Criptografia e Segurança da Informação

#### Grupo 03

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#### 1.1 TP4 - Exercício 3

Construir tabelas de comparações das suas implementações, para os vários níveis de segurança NIST e em termos dos seguintes parâmetros:

- 1. Tempos: geração das chaves, produção da assinatura e verificação da assinatura.
- 2. Tamanhos: da chave pública, da chave privada e da assinatura.

**Librarias Utilizadas** Esta secção é dedicada ao import das librarias necessárias para a realização do exercício.

```
[]: from sage.all import *
  import hashlib
  import time
  import matplotlib.pyplot as plt
  import numpy as np
```

#### 1.1.1 Implementação Dilithium

Implementação do esquema de assinaturas Dilithium em Pythob+Sagemath como descrita no exercicio 1.

```
[]: def bits_to_integer(y):
    alpha = len(y)
    x = 0
    for i in range(1, alpha + 1):
        x = y[alpha - i] + 2 * x
    return x

def bits_to_bytes(y):
    c = len(y)
```

```
num_bytes = ceil(c / 8)
    z = [0] * num_bytes
    for i in range(c):
        z[i // 8] = z[i // 8] + y[i] * 2**(i % 8)
    return z
def bit_reverse(x, bits):
   y = 0
    for i in range(bits):
        y = (y << 1) | (x & 1)
        x >>= 1
    return y
def bytes_to_bits(z):
    d = len(z)
    y = [0] * (d * 8)
    for i in range(d):
        for j in range(8):
            y[8*i + j] = z[i] \% 2
            z[i] = z[i] // 2
    return y
def bitlen(x):
   return x.nbits()
def simple_bit_pack(w, b):
    z = []
    for i in range (256):
        z = z+integer_to_bits(w[i], bitlen(b))
    return bits_to_bytes(z)
def simple_bit_unpack(v, b):
   c = bitlen(b)
    z = bytes_to_bits(v)
    w = [0] * 256
    for i in range(256):
        # BitsToInteger((z[ic], z[ic + 1], ... z[ic + c - 1]), c)
        w[i] = bits_to_integer(z[i*c:(i+1)*c])
    return w
def bit_pack(w, a, b):
   z = []
    for i in range (256):
        z = z+integer_to_bits(b - w[i], bitlen(a + b))
    return bits_to_bytes(z)
def bit_unpack(v, a, b):
```

```
c = bitlen(a+b)
    z = bytes_to_bits(v)
    w = []
    for i in range(256):
       wi = b - bits_to_integer(z[i*c:(i+1)*c])
        w.append(wi)
    return w
def H1024(input bytes):
    hash_output = hashlib.sha256(input_bytes).digest()
    concatenated_output = hash_output
    while len(concatenated_output) < 128:</pre>
        hash_output = hashlib.sha256(hash_output).digest()
        concatenated_output += hash_output
    concatenated_output = concatenated_output[:128]
    bit_array = []
    for byte in concatenated_output:
        bits = bin(byte)[2:].zfill(8)
        bit_array.extend(int(bit) for bit in bits)
    return bit_array
def integer_to_bits(x, alpha):
    y = [0] * alpha
    for i in range(alpha):
        y[i] = Integer(x) % Integer(2)
        x = x // 2
    return y
def coef_from_three_bytes(b0, b1, b2, q):
    if b2 > 127:
       b2 -= 128
    z = 2 ** 16 * b2 + 2 ** 8 * b1 + b0
    if z < q:
        return z
    else:
       return None
def coef_from_half_byte(b, n):
    if n == 2 and b < 15:
       return 2 - (b % 5)
    elif n == 4 and b < 9:
       return 4 - b
    else:
        return None
```

```
def rej_ntt_poly(seed, q):
    a_hat = [None] * 256
    j = 0
    c = 0
    hsh=bits_to_bytes(H1024(bytearray(seed)))
    while j < 256:
        a_hat[j] =
 \negcoef_from_three_bytes(hsh[c%128],hsh[(c+1)%128],hsh[(c+2)%128],q)
        if a_hat[j] is not None:
            j += 1
    return a_hat
def rej_bounded_poly(seed, q, n):
    a = [0] * 256
    j = 0
    c = 0
    hsh=bits_to_bytes(H1024(bytearray(seed)))
    while j < 256:
        z = hsh[c\%128]
        z0 = coef from half byte(z % 16, n)
        z1 = coef_from_half_byte(z // 16, n)
        if z0 is not None:
            a[j] = z0
            j += 1
        if z1 is not None and j < 256:
            a[j] = z1
            j += 1
        c += 1
    return a
def expand_a(p, q, k, 1):
    A_hat = [[None for _ in range(1)] for _ in range(k)]
    for r in range(k):
        for s in range(1):
            bits_s = integer_to_bits(s, 8)
            bits_r = integer_to_bits(r, 8)
            combined_bytes = bytearray(p) + bytearray(bits_s) +__
 ⇒bytearray(bits_r)
            A_hat[r][s] = rej_ntt_poly(combined_bytes, q)[s]
    return A_hat
def expand_s(p, 1, k,q,n):
    s1 = [rej_bounded_poly(p + integer_to_bits(r, 16),q,n) for r in range(1)]
    s2 = [rej_bounded_poly(p + integer_to_bits(r + 1, 16),q,n) for r in_
 →range(k)]
    return (s1, s2)
```

```
def polynomial_mul(a, b, q):
    return [(a[i] * b[i]) % q for i in range(len(a))]
def ntt(w, q):
    w_hat = [0 for _ in range(256)]
    for j in range(256):
        w_hat[j] = w[j]
    z=1753
    k = 0
    length = 128
    while length >= 1:
        start = 0
        while start < 256:
            k += 1
            zeta = Integer(z**bit_reverse(k, 8)) % Integer(q)
            for j in range(start, start + length):
                 t = zeta * w_hat[j + length]
                 w_{hat}[j + length] = (w_{hat}[j] - t)
                 w_{hat}[j] = (w_{hat}[j] + t) % q
            start += 2 * length
        length = length // 2
    return w_hat
def ntt_inverse(w_hat, q):
    w = [0 \text{ for } \underline{\text{in }} \text{ range}(256)]
    for j in range(256):
        w[j] = w_hat[j]
    z = 1753
    k = 256
    length = 1
    while length < 256:
        start = 0
        while start < 256:
            zeta = (-1 * Integer(z**bit_reverse(k, 8))) % Integer(q)
            for j in range(start, start + length):
                 t = w[j]
                 w[j] = (t + w[j + length])
                 w[j + length] = (t - w[j + length])
                 w[j + length] = zeta * w[j + length]
            start += 2 * length
        length *= 2
    f = 8347681
    for j in range(256):
        w[j] = f * w[j] % q
    return w
```

```
def mod_plus_minus(m, alpha):
    m_prime = Integer(m) % Integer(alpha)
    if m_prime > alpha // 2:
        m_prime -= alpha
    return m_prime
def power2_round(r, q, d):
    r_plus = Integer(r) % Integer(q)
    r0 = mod_plus_minus(r_plus,2**d)
    r1 = (r_plus - r0) // (2**d)
    return (r1, r0)
def pk_encode(p, t1, q, d, k):
    pk = bits_to_bytes(p)
    \max_{\text{value}} = (2 ** (bitlen(q - 1) - d)) - 1
    for i in range(k):
        pk += simple_bit_pack(t1[i], max_value)
    return pk
def pk_decode(pk, q, d, k):
   y = pk[:32]
    len_z = 32*(bitlen(q - 1)-d)
    z = []
    for i in range(k):
        z.append(pk[32+i*len_z:32+(i+1)*len_z])
    p = bytes_to_bits(y)
    \max_{\text{value}} = (2 ** (bitlen(q - 1) - d)) - 1
    t = [None for _ in range(k)]
    for i in range(k):
        t[i] = simple_bit_unpack(z[i], max_value)
    return p, t
def sk_encode(p, K, tr, s1, s2, t0, d, n):
    sk = bits_to_bytes(p) + bits_to_bytes(K) + bits_to_bytes(tr)
    for si in s1:
        sk = sk + bit_pack(si, n, n)
    for si in s2:
        sk = sk + bit_pack(si, n, n)
    for ti in t0:
        sk = sk + bit_pack(ti, (2**(d-1))-1, 2**(d-1))
    return sk
def sk_decode(sk, d, n, l, k):
   f = sk[:32]
    g = sk[32:64]
    h = sk[64:128]
```

```
a_len = 32 * bitlen(2*n)
    y=[]
    for i in range(1):
        y.append(sk[128+i*a_len:128+(i+1)*a_len])
    z = []
    for i in range(k):
        z.append(sk[128+1*a_len+i*a_len:128+1*a_len+(i+1)*a_len])
    w_len = 32*d
    w = \Gamma
    for i in range(k):
        w.append(sk[128+(1+k)*a_len+i*w_len:128+(1+k)*a_len+(i+1)*w_len])
    p = bytes_to_bits(f)
    K = bytes_to_bits(g)
    tr = bytes_to_bits(h)
    s1 = [bit_unpack(yi, n, n) for yi in y]
    s2 = [bit_unpack(zi, n, n) for zi in z]
    t0 = [bit\_unpack(wi, (2**(d-1))-1, 2**(d-1)) for wi in w]
    return p, K, tr, s1, s2, t0
def matrix_mutl(m_a,m_b,q):
    m_c = [[0 for _ in range(len(m_b[0]))] for _ in range(len(m_a))]
    for i in range(len(m_a)):
        for j in range(len(m_b[0])):
            for k in range(len(m b)):
                m_c[i][j] += m_a[i][k] * m_b[k][j]
                m_c[i][j] \%= q
    return m_c
def decompose(r,q,y2):
    r_plus = Integer(r) % Integer(q)
    r0 = mod_plus_minus(r_plus,(2*y2))
    if r_plus - r0 == q - 1:
       r1 = 0
        r0 = r0 - 1
    else:
        r1 = (r_plus - r0) // (2*y2)
    return (r1, r0)
def high_bits(r,q,y2):
    (r1,r0) = decompose(r, q, y2)
    return r1
def low_bits(r,q,y2):
   (r1,r0) = decompose(r, q, y2)
    return r0
def expand_mask(seed, mu, l, gamma_1):
```

```
c = 1 + bitlen(gamma_1-1)
    s = [None for _ in range(1)]
    for r in range(1):
        n = integer_to_bits(mu+r, 16)
        v = [None for _in range(32*c)]
        byts = bits_to_bytes(H1024(bytearray(seed+n)))
        for i in range(32*c):
            v[i] = byts[(32*r*c + i)%128]
        s[r] = bit_unpack(v, gamma_1 - 1, gamma_1)
    return s
def w1_encode(w1, k, q, y2):
    w1_tilde = []
    for i in range(k):
        w1_tilde = w1_tilde + bytes_to_bits(simple_bit_pack(w1[i], Integer(((q_
 \rightarrow 1) / (2 * y2)) - 1)))
    return w1 tilde
def sample_in_ball(seed, tau):
    c = [0 \text{ for } \underline{\text{in }} \text{ range}(256)]
    k = 8
    for i in range (256 - tau, 256):
        while bits_to_bytes(H1024(bytearray(seed)))[k%128] > i:
        j = bits_to_bytes(H1024(bytearray(seed)))[k%128]
        c[i] = c[j]
        c[j] = (-1) ** (H1024(bytearray(seed))[i+tau-256])
        k += 1
    return c
def make_hint(z, r, q, y2):
    r1 = high_bits(r,q,y2)
    v1 = high_bits(r + z,q,y2)
    if r1 != v1:
        return 1
    return 0
def use_hint(h, r, q, gamma_2):
    m = (q - 1) // (2 * gamma_2)
    r1,r0 = decompose(r, q, gamma_2)
    if h==1 and r0 > 0:
        return (r1 + 1) % m
    elif h==1 and r0 <= 0:
        return (r1 - 1) % m
    else:
        return r1
```

```
def hint_bit_pack(h,omega,k):
    y = [0] * (omega + k)
    index = 0
    for i in range(k):
        for j in range(256):
            if h[i][j] != 0:
                y[index] = j
                index += 1
        y[omega + i] = index
    return y
def sig_encode(c_til, z, h, l, y1, omega, k):
    o = bits_to_bytes(c_til)
    for i in range(1):
        o = o + bit_pack(z[i], y1 - 1, y1)
    o = o + hint_bit_pack(h,omega,k)
    return o
def hint_bit_unpack(y, k, omega):
    h = [[0]*256 \text{ for } _in \text{ range(k)}]
    index = 0
    for i in range(k):
        if y[omega + i] < index or y[omega + i] > omega:
            return None
        while index < y[omega + i]:</pre>
            h[i][y[index]] = 1
            index += 1
    while index < omega:
        if y[index] != 0:
            return None
        index += 1
    return h
def sig_decode(o, y1, lbd, l, k, omega):
    1bd = 1bd // 4
    w = o[:lbd]
    x = []
    for i in range(1):
        x.append(o[lbd + 32*(1+bitlen(y1-1))*i:lbd + 32*(1+bitlen(y1-1))*(i+1)])
    y = o[1bd + 1*32*(1+bitlen(y1-1)):]
    c_til = bytes_to_bits(w)
    z = [None for _ in range(1)]
    for i in range(1):
        z[i] = bit_unpack(x[i], y1 - 1, y1)
    h = hint_bit_unpack(y,k,omega)
    return c_til, z, h
```

```
def ML_DSA_KeyGen(k, 1, q, d, n):
    eps = [randint(0, 1) for _ in range(256)]
    H_output = H1024(bytearray(eps))
    p = H_output[:256]
    p_ = H_output[256:768]
    K = H_output[768:]
    A_hat = expand_a(p, q, k, 1)
    s1, s2 = expand_s(p_1, l, k,q,n)
    NTT_s1 = []
    for i in range(1):
        s1_poly = PolynomialRing(Zmod(q), 'x')(s1[i])
        NTT_s1.append(ntt(s1_poly, q))
    A_NTT_s1 = matrix_mutl(A_hat, NTT_s1, q)
    t = [ntt_inverse(PolynomialRing(Zmod(q), 'x')(A_NTT_s1_row), q) for_
 →A_NTT_s1_row in A_NTT_s1]
    for i in range(k):
        for j in range(256):
            t[i][j] = (t[i][j] + s2[i][j])
    t1, t0 = [], []
    for tt in t:
        tt1, tt0 = [], []
        for ti in tt:
            t1i, t0i = power2_round(ti, q, d)
            tt1.append(t1i)
            tt0.append(t0i)
        t1.append(tt1)
        t0.append(tt0)
    pk = pk_encode(p, t1, q, d,k)
    tr = H1024(bytearray(pk))[:512]
    sk = sk_encode(p, K, tr, s1, s2, t0, d, n)
    return pk, sk
def ML_DSA_Sign(sk, M, Tq, q, d, n, 1, k, tau, gamma_1, gamma_2, omega, beta):
    rho, K, tr, s1, s2, t0 = sk_decode(sk, d, n, l, k)
    mu = H1024(bytearray(tr+M))[:512]
    s1_hat = [ntt(poly, q) for poly in s1]
    s2_hat = [ntt(poly, q) for poly in s2]
    t0_hat = [ntt(poly, q) for poly in t0]
    A_hat = expand_a(rho, q, k, 1)
    rnd = [randint(0, 1) for _ in range(256)]
    rho_prime = H1024(bytearray(K + rnd + mu))[:512]
    kappa = 0
    z, zz, h = None, None, None
    while z is None or h is None:
        y = expand_mask(rho_prime, kappa, 1, gamma_1)
        NTT_y = []
```

```
for i in range(1):
            y_poly = PolynomialRing(Zmod(q), 'x')(y[i])
            NTT_y.append(ntt(y_poly, q))
       A_NTT = matrix_mutl(A_hat, NTT_y, q)
       w = [ntt_inverse(PolynomialRing(Zmod(q), 'x')(A_NTT_row), q) for__
 →A_NTT_row in A_NTT]
       w1 = [[high_bits(n,q,gamma_2) for n in poly] for poly in w]
       c_til = H1024(bytearray(mu + w1_encode(w1, k, q, gamma_2)))[:(2*Tq)]
       c_til_1, c_til_2 = c_til[:256], c_til[256:]
       c = sample_in_ball(c_til_1, tau)
       c_poly = PolynomialRing(Zmod(q), 'x')(c)
        c_hat = ntt(c_poly, q)
        cs1_hat = [ntt_inverse(PolynomialRing(Zmod(q),__

    'x')(polynomial_mul(c_hat,s_hat,q)), q) for s_hat in s1_hat]

        cs2_hat = [ntt_inverse(PolynomialRing(Zmod(q),__

    'x')(polynomial_mul(c_hat,s_hat,q)), q) for s_hat in s2_hat]

        z=[[Integer(y[i][j])+Integer(cs1_hat[i][j]) for j in_
 →range(len(cs1_hat[i]))] for i in range(len(cs1_hat))]
       r0 = [[low_bits(Integer(w[i][j]) - Integer(cs2_hat[i][j]), q, gamma_2)_u
 zz = [[mod_plus_minus(ze,q) for ze in zl] for zl in z]
        if max(map(max, zz)) >= gamma_1 - beta or max(map(max, r0)) >= gamma_2_
 ⊶- beta:
            z, h = None, None
        else:
            ct0_hat = [ntt_inverse(PolynomialRing(Zmod(q),__

    'x')(polynomial_mul(c_hat,t_hat,q)), q) for t_hat in t0_hat]

            h = [[make_hint((Integer(-1) *_
 →Integer(ct0_hat[x][y])),(Integer(w[x][y])-Integer(cs2_hat[x][y])+Integer(ct0_hat[x][y])),q,

→for y in range(len(w[x]))] for x in range(len(w))]
            ct0_pm = [[mod_plus_minus(y,q) for y in x] for x in ct0_hat]
            if max(map(max, ct0_pm)) >= gamma_2 or sum(map(sum, h)) > omega:
                z, h = None, None
       kappa += 1
    sigma = sig_encode(c_til, zz, h, l, gamma_1, omega, k)
    ctilt,zt,ht = sig_decode(sigma, gamma_1, Tq, l, k, omega)
   return sigma
def ML_DSA_Verify(pk, M, sigma, q, tau, gamma_1, gamma_2, omega, beta, Tq, k, u
 \hookrightarrow1, d):
   rho, t1 = pk_decode(pk, q, d, k)
   c_til, z, h = sig_decode(sigma, gamma_1, Tq, l, k, omega)
   ctil_, _ = c_til[:256], c_til[256:]
   if h is None:
       return False
   A_{hat} = expand_a(rho, q, k, 1)
```

```
tr = H1024(bytearray(pk))[:512]
  mu = H1024(bytearray(tr + M))[:512]
  c = sample_in_ball(ctil_, tau)
  ntt_z = [ntt(PolynomialRing(Zmod(q), 'x')(poly), q) for poly in z]
  A_NTT = matrix_mutl(A_hat, ntt_z, q)
  ntt_c = ntt(PolynomialRing(Zmod(q), 'x')(c), q)
  ntt_t1= [ntt(PolynomialRing(Zmod(q), 'x')([x*(2**d) for x in poly]), q) for_u
→poly in t1]
  t1_c = [polynomial_mul(ntt_t1[i], ntt_c, q) for i in range(len(t1))]
  fntt=[[(Integer(A_NTT[i][j])-Integer(t1_c[i][j])) % q for j in__
→range(len(A_NTT[i]))] for i in range(len(A_NTT))]
  waprox = [ntt_inverse(PolynomialRing(Zmod(q), 'x')(poly), q) for poly in_
  w_prime = [[use_hint(Integer(h[i][j]) % q,Integer(waprox[i][j]),q,gamma_2)__
→for j in range(len(waprox[i]))] for i in range(len(waprox))]
  c_til_ = H1024(bytearray(mu + w1_encode(w_prime, k, q, gamma_2)))[:(2*Tq)]
  zz = [[mod_plus_minus(ze,q) for ze in zl] for zl in z]
  return c_til==c_til_ and max(map(max, zz)) < gamma_1 - beta and_
⇒sum(map(sum, h)) <= omega
```

#### 1.1.2 Testes ao Dilithium

#### Função de teste

```
[]: def Dilitium_Test(version, message):
         q = 8380417
         d = 13
         tau=39
         1bd = 128
         gamma_1 = 2**17
         gamma_2 = (q - 1) // 88
         k = 4
         1 = 4
         n = 2
         beta = 78
         omega = 80
         if version == 65:
             tau=49
             1bd = 192
             gamma_1 = 2**19
             gamma_2 = (q - 1) // 32
             k = 6
             1 = 5
             n = 4
             beta = 196
             omega = 55
         elif version == 87:
```

```
tau=60
      1bd = 256
      gamma_1 = 2**19
      gamma_2 = (q - 1) // 32
      k = 8
      1 = 7
      n = 2
      beta = 120
      omega = 75
  time_start = time.time()
  pk, sk = ML_DSA_KeyGen(k, 1, q, d, n)
  time_kg = time.time() - time_start
  M_bytes = bytearray(message.encode())
  M_bits = bytes_to_bits(M_bytes)
  time_start = time.time()
  sign = ML_DSA_Sign(sk, M_bits, lbd, q, d, n, 1, k, tau, gamma_1, gamma_2,_u
→omega, beta)
  time_sign = time.time() - time_start
  time_start = time.time()
  is_valid = ML_DSA_Verify(pk, M_bits, sign, q, tau, gamma_1, gamma_2, omega, u
⇔beta, lbd, k, l, d)
  time_verify = time.time() - time_start
  return [time_kg, time_sign, time_verify, is_valid, pk, sk, sign]
```

#### Teste Manual Teste manual ao esquema de assinaturas Dilithium

```
[]: message = input("Enter the message: ")
    version = 1
    while version not in [44, 65, 87]:
        version = int(input("Enter the version 44/65/87: "))
    tkg,ts,tv,ver,pk,sk,sign=Dilitium_Test(version, message)

print("Key Generation Time: ", tkg)
    print("Signing Time: ", ts)
    print("Verification Time: ", tv)
    print("Public Key: ", bytes(pk))
    print("Public Key Size: ", len(pk))
    print("Secret Key: ", bytes(sk))
    print("Secret Key Size: ", len(sk))
    print("Signature: ", bytes(sign))
    print("Signature Size: ", len(sign))
    if ver:
```

```
print("Signature is valid.")
else:
   print("Signature is invalid.")
```

Key Generation Time: 0.6438472270965576

Signing Time: 1.5895066261291504 Verification Time: 1.1228954792022705

Public Key: b'\x18Y\x98\xc9\xceR\xeb\x97\xbd5\x96,9I\x89\x9cd\xf4\xd6\x1c5\xc7n \x05\xdc \xd4\x0bW[r\x14\xc1&!T\x87\x1f=:\xe1Vk\xb1\xca\xbfn4\\\xa2\xa2\x06\x16| \x07lt0\xd8\xd2\xa0!0\x8c\x82\x06\x01\x11\xf7\xa0:\xdaS\x15v[ \xb5\x92\xf5hK>\xf6,\x93\xe7\xc9UU\x84]\x9c3\xa48\x9d\x8bF\x88\xc4\xec\xdeK\xe22\x83WR\xbe&Q0o\xf1 t\xd3\xe7\xd1UM<\xfa\xc1\xa0M\x9e\xc2\x17F\xfew\x9bg\x9crpFZ\xc5\x167\xe3E\xa7\x 9e\xdb\x8b\xbb\*&\x11\xc3\xc2\x11\xbe%\xcbU\xf7\xddn\xf4\x7f\x12eB\xc0\x04,d\xbb\ xa2\xb0\x83N\xdaD\xdez\xf1\x9dM\xffJ\x113\xdb~y\x82\xddH\xf1(\xc1\x85\x95"\xa0z4 R\x0e\xef\x085\x03d8w\x96g\x11\x7f7\x9ap\xb8\xbb\xb0\x92\x1a\xd1\t\x8a3\xd4y\x10\x94\xdef\x9cy0PA/I\xe6\x13z\xe3\xfd\xbd\x8e&\x17\xee\n\x00\xca!\x08\xcc\xec\x8 fq\xbc\'\xdb>\*\x89\xf1\xbe\xa0\xfaH\x10\xa3yK\xce\xbe(\x8a\xc7\xe5\xf3\x03\x17& d7M\x19\xfc\xa0\x0e\xa9\x87j\xa3\xfdk\xc91<\xe4\xd4d\n\xe7\xeb^\xfe\x01\xa5\xc1\xd2\xeb\xaf\x13\x9a\x98\xe0\xdfA\x06\x97\xdcE\x1fi\xc1\x14\x920\xe0\x93\xf7\xed\x18[}\xa7\x88\x13\xc6\xcc\xe1-

 $LU0d\x04.\xf62\xed\x7fW\xb7\xcf\xab\x9b\xd4lGnh\xf5\x0f\xdf@c\xa0\x17\xd3\xe8\x$  $de\\xe4\\x10b\\x96\\x08\\xfc\\xb7\\xd3\\x11X\\x0c\\xe1L\\t\\r\\xe8mV\\xbe\\x1aP!\\xce\\xd7\\x01\\x$ a) $H\x88\xb4\xc9\xed\x98\x80\x18\x92Q\x9b\xcd\xce2\x961\xbd\xfc\xf8wh\x00\x15\x$  $9f.Q\xcf\xdap3\x91s\xfd\x96\xc9\xe8Le\x9a\x01\xbc\x1a\xae\x90\x9ey\xe02\x84Z1\xf$  $4\xfe\xf1\xce\x8b\x95^\xf1?\x11\xceCD\x9c{\xb0\x85S\xb2G3\x9bZ^\x0572\xa8\xf4\&5?}$  $B\x1c\x6\x96\x96\x41\x41\x8\x89\x4d\xdbc\x42\x87E\x1f\xe0t\xf1$  $\x16\x9cM@0\xa3\xe6\#=q\x99\x10\x81>\xc4\xd2^\xe4\xef:\x96\xce\xa5UT\xac\x9dx\xa$  $x90\xdeg\x180\x97\xfb\x87\x11m]\x19B@\x02f\x8d\xa58\xc1\xab5\rN7\xbb\x829\x$  $\label{lem:c1} $$c1^xa5\\x1c\\xde\\xe4\\xa2\\xcf\\xcc\\xdc\\x88F\\xa2\\x8f\\x0b\\xcd\\x94\\xa1\\xf1\\xc7\\x92D$  $\xb55\xee\x1a\xc4R\xb1Ib\xee\xf1C]:\xde\xbf\x13\xa5\xf3\xca\xe7e\x10Z\xa7\x8$  $xcfw\xfd^2\xa4\x94\xf5"\xbfN-$ 

 $\label{to:condition} $$ \x997\xbc<\x03\xeb\x05\xee\tc[M\x8f\xed)V2.\x07BTdj\xa8.\xe4\x96\x1f}\xd2k\xab\x98L\x8c\xf9*\x0c\xb9\x8c&\xb1\xbe\xc8\rt\xdeJ\xd1\xa5\xcf\xb9\x89\xab\'\xaa\x90 *\xfe\xd1\xc1\xee0\x1b\x7fZIn+\xd7\x9b\x13\{\xcb\xbc\xacc\x8b\x1c\x18\x9c\x96\xcd\x08i$*\x14[uu\x16\xf3n\xf0H\xe9\xab\xb4\xd3\xeeu\xb3s*t\x9f_g\x0c3e\xf6@H\x9e\xd1\x90y\xad\xe3QuH\r\xd6\x9s:\x90\xe1F\xd8\x85p\xdc\xe08\xd5\xbe\xba\xd6\xbb\xcd\xaj\x1a\xba\x11\x1c\xb1\xdc3|\xe8\x01\x0b\x1c?Le\xb1w*n\xd7V\x07<\x10\xc1\xb3\x1e\x1c\xf9\x10;\xfa\n\x93zT\xf8\x1c\x03^/\x9cq''\xf8|\x8f\xc6\x14f''\xbe\xbd\x00\x9d\xd3\xd3Dn\xc3\x84B\x9a\x85g\xa7C:p\xd6\xf5+,\xa5ZtGd\x8d:\xdb\xe2YP\xdb\xe2n\xc1\xb0E\xc3\x13\xe3x\xe59\x953\xd0i\x88\x85\xd2n\xae\xc4yD\xb3d\x87\xe9\xf9$ 

 $\x94\x1e(\xe8\x17\xd6D8z2HV\xd2\xb6\x0e\xdfy\x1e\xb7\x1fy\x8b\x93\xb7\x9c\x90@\x$  $9e\xd2\xd8U\xeb\xe2\xe5X] + B\xc9\xd6L\xf6u\xe9\xbdw\xbad\xed?\x92v\%\xb2\x1f\xca\xeq$ e7\xbcuk\xe2\xc5\x89\xa4\xbfR\x002\x7f\x17\xe2\x02\xf6\*\xbf\xd9\xd3\x95\x938\x9f  $\xa9hs\xa0e\xeT\x02\xdc\x16\xe4\xe4\xe4\xc3g\\xf2\x02\xa4p\xe7\xb7\x01\xe5\x81$  $m\x83a\xb1\xef\x86\xfe\xf1\x93\x8a\%*\xe6\xcc\x9c\xf9Lj^?|\xb0\xa3\t\&\xabHr\n\x12$  $x99\xc3\x88\x04\xa6+p!\xa0\x82\#\x06\x13\x0b7\xa1\xbb9\xe0\xc4^\xb4j\xee{F}\xed\x$  $e4C"\x06\x82T\x12^\xdf\x1f9\x92\x9a;\xa3G(\W\x0e\xf3\xf3\x99K\xbd\xdd"\xfc\x19\x0$  $3\xcby\xb7\xf9\x98ra\xb6\xe8)\&\x1b{\xa9\xd9\xe7\x045<\xca\xe9R\xb56\xaeK\x0cz\xb}$  $0\x04\xc7EM\xcb\xca\xf4\xb1\xdb\xa3,0\x895hI\xf4\xc3{\x02\x07z\xd2;\xb3\PT\xed}$  $xfe\\x96\\xc9\\xdf\\x11\\xb1;Q\\xef\\x92\\xb1%\\x9a\\xb8\\xd2\\xc3gk\\xe5z\\xc1\\x9d\\x1ah\\x10\\x$  $d9\x0b\x0f\xe2\x0f\xed\x0c\xa5\xbf\x0c^-\x0eM0\x8a\xd8\x90A\tW\xa8\xf63\xc7\xeq$  $19yzf\\xa1\\xf0G\\x18\\x8e\\xfd\\x89\\j\\x01\\xad\\xdb\\W\\xd1\\x1f\\xa0\\x12\\xaa\\xeaM\\x1c\\xf4f1\\$  $xf3G\xb6\xab\xb0\x1c\xcck\xb4\\xf3\xb4\x1c*\x84q\xb3\xb2\x0eE\xe6\xe9\xd7\xcc\x$  $caal\xb6I(\xa8\xfbL\xd1>k\xdfN{\xc9}\xd6M\x9b\xe7F\xdd(\y\xd5\x8d?,\x945\xb6\xc9Q)$  $x81M\xf0jP\xf6i\xbe9B\x98\x84\xf9$\xa3\xcc\x06\xf4\x11\xef\x8f\xde\xf2\x077i$  $(x9e\xc9\xd9\xea\xb2\x85J\xc4\x82v\xea\xbd\xa2,;~\x15\x17!\x9d\x034\xa7]\x1eR9\x1e$  $xaf\\x1f\\xa6\\x9f\\x87]\\1\\xe9\\xc8\\27\\xc7\\xc6\\xbe\\x0e\\x1f\\xd0Ta\\x8a!\\xec\\x87\\x11\\xe6$ be\xc9:\xa4\x85\xebDQ6\xd3\x18\x8a5\x97T:\x99\xd31\xb7\xacz\xf8\xfb\xe2K\xf0\$\x1  $xa6\x15\x9e5\xeb{x88\x0f\r\x95\x17\x12\x9dL\%xa0\x82\x8b\x0f\x82\xceI5\xa7\x82\x8b\x0f\x82\xe0f\x82\x$  $xc9\\xee\\x0f\\x14\\x83\\xe6\\xab\\x11\\xfa]K\\xa5\\xd0\\x1dtw\\xd3Dr\\xab\\xdf\\xa8\\xf8\\x9e\\x9$  $9N\xceK\xb8\x04p\xde^\x86:\xf1=\x95\x91\xdfK\xa9\x93\xec\x18\xd7\x1f\xe6\x19\xfb$  $3\K\xcb{x11Tf\xcaI\xeb \xd8\xe5\xcd\x08\'\xfe\xa1\xbe\xe0\xd0Yb7\xc3\x02\xa7\xe}$  $5\x83\xcf\xa6\xee\x03\xc4\x12\xa2![:"\xad\xaf\x83\xeb\x9c\x1d\xa7:\xe1X\xca\$   $xc0] V\times e2f\%xfe@\x1a\x1fI\x9a\xc1$\xe4B\xf3\xf7\xcc\xbb\xc9\xef\xae\x1e\xd2A\xe1 \x03\xf9\xbd\xb3\xb0w\xc2\xbfQ/}i\x12kh\x18\xc8\xa40\x9dW9w\xc6\xedw\n1\x07\%\xbd c`$1Ny\x10\xf4U\x01\xdf1`\xb80\x91u>\xc2+nf^p\x11\x8b\xfc\x98\x18\xee[\xea\x00\xd0\xbbv\x01\xb0^\x10\x9a\{\xeb\xff\xd1\xa5\xb8/0\xa6Y|V;,\x01\xfa\xbe\xaa\xa0\x9d\xf3\xc6\xd5\xadil"|\x8d\xd4\xc87\xbf2\xbb\xd1\x1e\xc9bJ\x0cJ\x1ba<\d67\xae\x00\xfbV\xe0\xcf\xeb\xd2Y:\xa2\xbf,\x85\xf8m\x1a]\xb7\xb3\xf7j-$ 

Public Key Size: 2592

 $9\x8bu\xeeS\x99)0L\xa6.i0\xfe\x17\x8c\xfd\x12'$ 

Secret Key: b'\x18Y\x98\xc9\xceR\xeb\x97\xbd5\x96,9I\x89\x9cd\xf4\xd6\x1c5\xc7n \x05\xdc \xd4\x0bW[r\x14\$S\xb7{E\xb8r\xd5\x86u\xfetf\xe5\x86U\xef]\x9d\xed\xf2\x 8eE\_U\xcf\x16\x03\x10\x9f\x969m\xf2\n\xb3+\xa5v@\xff4\x08d\xefi\xf0\xeb\xcb1\xbf\x18?\xf2\x90\xdd\xed\xb2C-

 $0\x91\x6\x92L\x8a\x12\x8c\x14e\x93\xc6PS\xa4\x88\xcaB(\x920\x84\x99\xa2\x05b\x$ a6a\x14\'2T\xb0\x8c\x147b\x11\xa6\x8cH\x96i\x01\xb4\x08\x0352\x80\xa6e\x90\x92\\ x19) i\xca\xb6PL8\x0ed\xc2m\x836Q\x14\x92\r\x03E\x00\x94\x80\x08\x011QH&\x80Z\xc4  $-\xc4\x98\%P\xc2a\x10\xc6i\x1c5\x02`FeH\x12\x85\x11\x93\x08\xd9\x84`\x8c\xb0M\x13$  $\xb2,\x00\xa4iR\x86\x0cS\xc8(\x9c\xc4M\x00\x17@\x1a\xc0\x89\x1c\x80,\xc4\x841\x8$  $0\x94,\xc9HIQ@b\x02\x16P\x8a\x16L\n\x12\x84\x8b@\x8aZ6\x08\xc2\&j\xc98\xc0\x062Z$ \xb2,!8!\xdc\x92m\x9a\x06\*\x19C\x80\x82D\x84\xc4\xc2a\x82\x84\x8c\x93\x08E\x0cE\  $x04\x92D\x8a\x189h\xa0\%\xd8H\x12EES0$\xc4\xa0$\x898\x00\x01\xa0\x00Q\xc2p\#\x02$  $\x06\x8c\x02\x12\x13\xb0\x800\xc8AA8\n\x00\x15d\x12\xb4L\xc20\x02R\xc8\x0c\x8a\x$ 06!I&\x11\x12\x03"D\x06BP\x98`\$@\*"\x11@\xdc\$\n\x18\x10\x8a\xe422\x98\xc8\x01\x00 @ \x13(\x11K\x82e\x18)\x12\x18\x08J\xda\x10a\x18\xa4\r\xa2\xb0\x0c\x82\x84\x08H2  $^{\circ}Bn\times3B\times0e\times11\times94q\times00\times06\times84\times1c\times14\times84R\times14r\times1a\times11\times04'J\ln\times08\times18$  $x8c\\x13\\x00\\x11\\xd9\\x98\\x90\\x84H\\n\\x98\\xb0m\\x19 $$x19\\x99\\x08C\\x82\\r\\x1a5\\x0e\\x8$  $2\xa6d\xc1\x04M\x98\x98\x90\x92\r\x0c0)\x03\xa01\x0c\x110K\xb6\x91\#\x801\x8b$  $x10\x0.x81"Q"\x0.x400*\x0.x81A\x0.x91\x16\x0.x4(\x1a4\x12.x10)$  $\d^0\d^0\x16Q\xda2\taDb\x90\xc8h\x99\xc8\x05\x84\xa8\%PD,\x0b\xc7\x04\x80\x96m\xa1$  $Fq \ x81 \ x99 \ x10 \ x90 \ x12 \ x139 \ x44 \ x14 \ x4a \ x1aI \ x84 \ x0c \ x16F \ xc9 \ x$  $06B\x0c0 \x84\x84E\x8a&J\xa4\x14\x8c\xa0p\xc4(ICB\rS\xa6\r\x03\xc4hK\xc41 \xa0M$  $A\x19\x19\x8aPB\x06L\xb6\%\x98''x89\x83\x00i\x88\xa0$\xdcD\t\xe4\xb6!\x14\xc3\t\x$  $83\x96m\x0c\x82AX\x12R\xc10\%b\x8c\x01\xa7LH2R\x80\x16,\x10\x10"\xdb\xb8%d\x12\x$  $80CF\x81\x1c\xb1D\xc8\xc4\%\x83\x88D\xa21\x83\xa0mCDn\xc2\xa2h\x14\xb3A\x83\x18\$  $nA\&\x8cS\x18d\\\x02-\x10\xc91\xc2\xa6e\x1b\x98-$ 

 $\label{thm:convected} $$ \x8a\x00\x01\x1a\x00q\x1b9,\x81\xc0e\xd220\x142p\x81\xc6a\xc94\x91\x89\x00\x0c\x19\x17P\xc0\xa2\x80"\x14I\x08\xb6\x91\xa4\x06\x11\x89\xc0D\xa28\&[\x06\x01\x94\&\x89\x00GM\x894N\x90\&\x8d\xc1\x08\x02\x00F\x10\xa2&\x06\x98\x04.\x1c\x08F\x14C \x1cEH\x81\x18F\x18\xb3\t\xd8\x14N\xe4\x06\x05A\x18\x11\x0b\x84\x8c\x90\x08n\x94\xa8\x90\xd98\x8d\n\xc6!\xa1@\x0cS\xb2\x80S\xc2P\xa1 0e\x89\xb01\x99\x08q!\xb11\x14\xc51\xd92\x08YBa\x01!.\x1a7-$ 

 $\label{thm:c1m} $$ \xc1m\timesdb&E\times0b\timesb0!\timese42\timest\times11\timesb4qX\timesb^*\times87\times84L\times10.\x8b ^A\times94E\times1aA!\times89\times94\times8c\timesc\times16\r\timesd9\times10\times88\times18e\times94\times44\times88\times03HR\#\times86\times00\times1c\%\times08\times04\times87\times11\times1110R"Qa0\times02\times19\times830\timesd4BlS\times02*\#\timesc7I\times08\times140\times8b\times80hI(.L@p"IR\times11\times06\times0e\timesd8\times92\times04\times120j\times01\times91,\timesa3\times08\times91\times11'\times8c^\times82\times\alpha'\times8d!\times23)C\times00N\times93\timesa4hQ\timesa80\timesd4\timesc8M@\times04m\times0b\times88q\times9a\times04F\times08(\times81\times12\times8d\times120)X89L\times02\times81\times19F^*\timescc\times10-\x12\times11"\t"\times8c\timesc8\timesb2\times03\times1n\times034\times8dT\&\%\times81\timesc0\times89\times122-$ 

 $\xc0\x80,\x82B\x11\x92\x12\x85\xcc\x04!\x03\xc2\x85\xc82\x8a\xda\xc6\x89\x08\x19\x19\x02p\x12E\&\xd9\x10\x12\x11\xa4^$\xa7 K\x841\x90$ 

 $\label{thm:column} $$ \x81\x12\x6\x01\x80\x82d@\x12N\x01H \x84\x92\x84"3\x0c\t\xa1(\x1cDL"I-\x01\x19-T\x82\x8d\x8cH*\xc8\x16A\xe4\xa4AR\x90\x88\x12\xa5hD0\x80\xcc\x98Q \x12\x11\x94D . \x8b\xc4D\xd32,\x8c\x80\x91\x83\xa8\x10\x12E\&\xd9\x10\x12}Z0\xbc\xbfHu$y\xdc0\xc4\x18K\xf8\xe8\x8af\xcf\xb8|\xd4\xce.\xba\xf5\xb1\xad\x11\x90\x90\&R\x92\xf5Nn\xd43\x1dV\x8ay\x17\x0b\xceN0\xc7\x07[\xab\xeb]-$ 

 $\label{thm:condition} $$\xd5p8\times(x17)\times x194\times(x12)\times x12)\times x10\times(x11)\times x110\times(x11)\times x194\times(x12)\times x194\times(x12$ 

 $\xcb\x03\xf0\xd8\x97\x93\xf4L\x95\x05n:L280\xa5\xb5\xb2\xacj3\xc1P/(*N\xfb\x9d\x$  $80\x9d\xb01\xb6\xa93kP\xeb\xbae\xdcb\xb2\x96\to\xe0K[\t\xf1\xc1\xgd\xf8\xa0\x97\xe0\xe0]$  $x9d\x6\x85\xbe\xced\xd3.\x0c\x8d\x0ff$G\x07\x94\xac\x01\xf0\x0c\xaeW\xe90\xe0=g$  $\x0c\xfe0\x87\x19\xfa\n\x91\xec\xfa0Y\xee\xf3\xc8i\xb2h\xd4\x94y\x95\x9a)\xe6\xe$  $6{x18}xe4\x0f]\x15U\xd8\xb9\xf2\xac\xc6\xb9 L,\xaf\xf9\xa2\x89eF\xf5\x95\x04\xc$  $7\xc6\xcdJy=5r\x13\x0c\x863d\x18\x147\x94\x1d\xb9\xc8\x1f\xe2\x03X\xaf\x01Z\xab$  $F\xbd\xecb\x8ft\x80\xc2\xe4\xe1\xec*\x193I\x08\xa3\xa2\xa6\xd5\xc4\x08\x8b\x13\x$  $02}\x38$Z\x14\x97X\xd9+?V\xd3\xd8\xf6\xc5\xe9\x83\x14GM\x8cQ\x91o"\x1d\x9d\xe8~7$  $\xd9\xb7Z \xf0]\x06\xc5\nM\xacIp\xf9\xe3\x7f]\x98Ea\xaa\xa3\xf2\x19\xbd_\xf1Z\x1$  $4\xd7\xe8\x1e"\x93\xab\xee]\xec\x8e\xd4\x8a\xd6nI!\xoc\xe1\xc4_\xfe\xcb\x84\xfe\$  $xbe0b\x94+\r\x86\x91h\p\x12^N\xd2\xc1\x06\xaf\x86\xe7w\x8f\xc8\x18>\xa63\x80\x1f$  $\x30\x830\x006\x94\xfc\x18\n\x17\xdc\xa9\xfd\x1c\xc6\xef6\xba3"\xc7\x12\xae$  $b\xec*\x11\xd5mD\xb3v\x95\#!\xbc\xfbN\xf1|\xd7\xd9\xee]\x03w3v)\x95M}G*\xbf\xe62\xb$  $xf4\x07\xa4\x11\xb8\xc4V\cCff\xf8\x00\xd2\&\xafLL \xe1\xcd1\xbb\x95\x11\xffaWC\x$  $a0x\\x1eb\\x80\\xcc\\x8e\\xdd\\x9de\\x172\\x8a.\\x8d\\x11\\xcdg\\xe1\\xb0\\r\\x92\\x8c\\xa7p\\xd0{\{$  $| \%3[\xc7\x82\x06\'\x1f\x92\xd9\xf2{o\xc7Gj\x028\xc0\xa1\x07}] \times 03\xb7\xd3\x0bA\xb} | \xb7\xd3\x0bA\xb$  $e^4\xa2\x1b\xe8\xac1\xc8\x0c\xaa}e^3aA^1\x03\xd9,\xf2\'\xbe\x06,\xb9\xa9)+\xbe^2\x$  $e9^x91\x01\x01\x01\x05\x02\x1e\x09\xbe\x01\x03!\x012\x1b1\x06\x05z\x00\xbe\x08e\$ 

 $\label{thm:linear} $$1\sqrt{5}\x06\xef+!\x17r+\x7f\xa6\xa0\xd2\xab\xa8"\xde\xb6{}=n\xcc\xdd^\x96 $$1''\xdc\xff\W\xb7x\xb7\x91\x98Z\xf1Ma\x81\x94\x1ab\xe2\xa76m>r\xf7\x93\x8aY<\x89 \xd5\x82\x03\xbd\x8c\xa42;5\xc1x\xc8!k\xd1=\xfeC\xe5gM\xfc\x80{\xfd\x92yVfA\x08\xe2)A\xf5''\x9d\x15\x02\xbd\x829\xa4\xf8\x8dx\x07\x7f5z\x91\xf6\x87\xc9i\x07X\x0c \x8d\xda\xe2\xd7p\x8b\xfb\xe08De''\x95\x91\x04? b\x18MG%\xe4+\xe6o\xe8\xb9\xea\xb9$ 

 $\x9e&a\\xe3v\\x1e\\x1d\\xf2\\xc5\\x83\\xea!W\\x8dSB\\x85\\xb5A\\xcc\\x9903\\xfd(\\x9c$\\xea\\xb9\\xbe\\xe9J\\xc99\\x9a!\\xb6\\xf3&s_y=P\\x10\\xe9\\x16\\xaa\\x87\\x1e\\x14\\x0b&x9a\\xd4e\\xe8\\xe8\\x4e8\\x4e8\\x52\\x4e6\\xd2\\x86\\xd2,\\xa6c+\\r\\x1d\\x02\\xac\\t\\xd0^\\x12\\x9f\\xadP\\xcd\\xf4;G0\\x86\\x93z\\xa0\\xe1\\xbc\\xddTB\\xfc\\x0e\\x90V\\xdbd\\xeb\\xad\\x04J\\r\\xfdk2\\xe5\\xc0\\x15:Z\\xb5\\xc4\\x1e^\\xc1\\xf8\\xa8\\x92\\x19x\\xb1c\\x0e\\xbfsa\\x05!Y\\xbasK\\x8b\\x01\\x8d\\xf1\\x01i\\xab9\\xab\\xfdrS\\x15\\x94\\x86\\xde\\x00^a\\xb0\\xd2\\xe05\\xa2>g\\xc2\\xefquSQQ'ML$\\xc6z\\xa9kSA\\xb2f9\\x1e\\xe2\\xd1W?t\\xbb\\x08\\xcb\\xb9+\\xb8V\\xcf\\xb9\\xca\\xa4\\xb2(^-$ 

 $\x9e\xbe5\xof\xear\x8fW\x10\xfd\x0b\x13\xe6\xcc\x19\xe0:\xa3\x06\xb6?\x1a\x9a\xbc\xf3\xe1\x84\x05\xdf/M\xfd\x11\x03o\x1e\xfc\x0c\xad\x15\r\xe4\xb0\x96J\xbd\xb2\x12\xd5\xa1\x15\x94\tep\x97\xc5,\xc3\x85\x10\x06\xc9\x13b\xec\xe2\xe3\x86\xf5F\xee\xdb\xf0!\xcb\x9f\x1b\x8e\x16\x86V=\xdc\xaf\x9f\x06q\xa9\xfb\xcd5"\x84EA\xd9\xd2\xe9\x8c\xb3'\x1b\x8e\x16\x86V=\xdc\xaf\x9f\x06q\xa9\xfb\xcd5"\x84EA\xd9\xc3\xf8RZ\x9b\xc3\x11!*#\xe4d\xf/\xec\x870\xb3\xe5e\x07\xa4H\xd4i\xe4V@\x93\xb2\x80\x07(\x06\xee\xc5\xee\x997\xf0m?C\xb5\x05\xbd\n\x82\xca\xf6\x85\x80A\xb3:?:1\xd9\xcf\xffj\x18:\xee\x13\xe8\x995\x1f\xe0\x1b\{Sa\xe6e\x0b\x0b\xcd\x80\xc1\xc4v\x10\xb3\x10\x9830y\xb7\x99\x90\x1f\x8e\x13\{,j\xbeY\x94\xeb\%\xf6\xb3,\x87\x99\xa5\xa9\xb0\x99\xbb\xb4\xfbs\x03\xfc10\xe0T\xb8\xbd\x0e\x0e$ 

 $\x89\xc4\xa6iA\xd3\xa2\xcc5\xc9\xab\xc7\x15\xe6\x10\x84\xa3\x05.=\x8f\xb1. \xa5\xc8\x948\xdb\x88b\x99\xfav\xa6\x84\xf3]\xde\x19\xa9\xa9\xbe\xd6\xcePP\'B\xa1\x98$ 

 $\xf1+\xc4\xc3\x000\xd0\x9a\x92\xca\x1a\xa5\x88\xc4\xd7\xcd&d\xee\xcb\x12@8\x004\xf0n\xb0\xa9>\xfa\x01^\xcez5=R\x99\x84\xa4-$ 

 $F\xa8\r, v\x05\xces/xdd3\xed\xc5\xb22\xf4/\x9aEe\xd3\x07ah\xsbd\x9aBB9\xa7\xc0$  $\xef(\xf6\x1bSj\xb5\xdc\xdb\xffL(\x98\xdd\x99\eq\xd9\x1b\xb9\x8d\xe5\x19B\x1d\x1$  $2\x14Y\x86\xb0h\xd6hg\x91\x1e\xea\x80d\xd4\xc1\x0b\xe4\x8er\xfc>\&\xa6\xd9\xd$  $6^xf0)\times8aT\timesb9\\xof\timesc3\\xd2D\timesc3\\xb04w%x88\\x12+xc9o\\x85\{\\xc6\\xb7\\xe2\\xc9\}$  $xac\t\xc8a\xb0\xc7t\'\x18\x12\xadK\x0fd\x1d\xe9\xa5\xbd\x82\x16\xf8\x85\xee.=!$$  $x7f\x8c\x84\xfa\#,\xf1\x08\&L''"c\x9d\xa9\x0b\x80\x91\xdfc\xa1\x8f\x06\x0e\x04$  $\xfbK\x19\xbfN\xb3>\xf7\xba0a\x92.R\xc4\xca\xf5\x82\x10\xc4\x0e\xa3(\xd4\x7fm1!a)$ \x07\x14\xf7\xb9\xefn6R\_\x92\x10\xaf")<#\xb5s\x18e\\x97Y<\x1f\xac!(;\xd36M H\xda \x84S\x1aJ\x83\x18L\'\xd1{\xd2\x96Y\xbaNn\xd7b\x9d\xa2\x9a\xd3\x8a\x06`]\xc4  $\xd4\x67\x8c\xbd\xfe}\xdd\x82*\x15u\xa5\r\x1e\x96WA\xaf\x11s\x16\x14\xcfU\x$  $1a1\xfe\x98\x1a\xc8\x81\xe0\xdd\xc5\xce\#\xc2\xce\xdaC\x81\xb8\x14\xb0\xcf0\W\xbd\$ x08yxa4xc9x89mhxd1xfcx06xe1xdexf7?3x17xd8xddpxc4xf3Yxa9x08T<0- $\xa5\xb7\xf7\x94\x01\xf9\xce\xe3\xf0\xda\x$  $01\x91Q\xd1|\xe4\x1f9\x9f^6\xd3N\x8dw\xfa\xcb\xd2P\xe5\xcb\xbd\x9a\x14WH\xa8\xec$  $\x04\x19Ww\xbf\x8c\xdfe\xb3\xdc\x00F\x95\xb0\xcb\xc6\xb2^-L2\x0f\xbe\x99;\xf9?w\$  $xa7v\times x96\times d4L\xb0\xae\xa8V\x98\times e0\xbfJ\x0f\xff\xd5\xca\xb7\xb0\xce")\x99\xeq$  $b2\x0b\xebB0\x0bK\xb40\xd8\xbf-$ 

 $\xce\xf7\x8c\xd7\xdc\x91\xfb\xdbh\x9e0\xc6\\xd2\xb2\x90 \xc9\xae\x93\xd1\xc8\xc5p\x0b\xb8\x9e"4-$ 

 $\label{thm:condition} $$ \frac{x_14b}x_84\cdot x_02\cdot x_01\cdot x_01\times x_00\times x_01\times x$ 

 $\label{thm:converse} $$ \x07\x01{\x9a\x189o\x99\x1f\xf4\x01;\x16\x17\xd6}\xf7\xed\r;\x9a\x8e\xfe\xed\x86\xed\x10\x14\x98\x828Cu\x1b\xe5>\xf7\xb3F\xc8\x1d6H\x12\xbf\xf3\xc8@:\xe6\xb9\x1f\xd8\r#N\xe3\\xe6\xe6\xfbJ\x7f>8 f\x93\xfe\x05\xa7\r\xf6q\xbd\xd7\xb7!\xe2\x04\xf8\x04L\x1fX\xa3}\xb0\x9a\xfcI\x89\xcf\xe7\x11\xed\xab\xa1\xee\xfd\x91\x1f\x06\xbf\x00\xc1\xf8\xbaB\xffwo\xc0\xa7\xfe\xc7@+~\x01w\xdd\xae2g\xcfE\x87\x87\x9a3\xf4b\xcf\xa20+\x08\xfd$$ 

r xaa x07 xad x16 xcb xe2 x03 xee xadi xaa x94 x86

Secret Key Size: 4896

 $\label{thm:b'\xc5}\xd7\x12Ec\x1aWz\x8c0::J\n\xc2\xbd\xb0\x87.\xf8\xc4Q$\x9e0u+B \xe7\x04\xd0\xe7\xed\xb3\t!E\x8f\x18\x13\xce\xe5\xc0\xc8\\xfa\xef\(\x98\}\#\xf0V\xb8\xb6\xe9C\n''\x90gS\xd9\xd9\xc0gB\x0eU\x980`_k"\x81\xf1\xbf\xa4\xcbX\x16\xaa2\x93B\xde\xb1\x88\x1f\xd3\x19\x17\x03\x02\xc8\x1c\x07Jz\'\xf4\xecY''\x13\xbeg\xf9\xbe\x13\xef\xb6v\xe1\xea\xb2k\x14-$ 

 $\label{thm:cond} $$ \x93\x8c\x99+\x92\x12\x01\xee\xf9\xa2\xff\xf2\xb8\x91\xf2!\x1f!\x1c<\xcb\xdc R\xdb\x05\x83u0\x0f\xc0\x08o\xd8\xc7g\xff}\x95\xee\xb2\xed\x01\xd2\x0e\xc8Z(\x9e\x8e\xd7\x80\x12\xcb\x0c\xb9b)\x80\x03\xc8\x7f\xa6\tfD\xd6^\xa4\x16\x04\xea\xc0AB\x9eL\x98\x04^\xefs''\xd0\xf1\xef\xb6\xcb\xda\x15**\x93\x1b\xe0Av\x1f0\x19\xf7\x04\x02\x0b\x1cGGzV\xf5lN"C\xbd\x97\xf0\xbe\xc4\xee\xc6\x84\xe1\x89\xb3[\x10-$ 

 $\xc3\x8c\t$\x92\x83\x01\xfe\x08\xa31\xf2H\x94\xf2A\x1fA(<\x06\xcb\xfc^\xdb5\x83e):\x0f\xda\x07?\xd3\xc7\xc6\xfd-$ 

 $"S\xcag\x10\xbf\xb3\xf7\xb6\xa3\xe1\x9a\xb3k\xa0-$ 

\xc3\x91\x99\x95\x92r\x01\xee8\xa3o\xf9\xb8\xb4\xf2Q\r!\x18<\x0c\xdc\xa0\xdb  $5\x0ui\x10\xf0\noR\xc7\xc7\xc4\x01Y\x88J(\x91\x90w\x8d\x12\x9e\x0)$  $b\xc9h)\xd4\x038x\xa6\$f\xe4\xd8^\x89\x16d\x83 \xf4CA\xdf^h\xae\x85\x9c\xcc\xf0\&V$  $31\xd5\x0c \x86E)y\xde\xa5p\xbfi\xa0\x7fT\xe1q\xd9\x13\xec\x97\x8c"\xf7\xa4\x98$  $x1c\\\x85\\\x92\\\xce\\\x86\\\x94\\\xbe{xc6}\x94\\\xbe{xc6}\x94\\\xbe{xc6}\xe94\\\xbe{xc6}\xe94\\\xbe{xc6}\xe94\\\xbe{xc6}\xe94\\\xbe{xce}\xe94\\\xbe{xc$  $\x07D\x11\xe2^m\xae\x95\x99\xcc\xbd\&\xb6\xe4L\xe7\xd4\x81X\x9e\x83\xe0\xc1hr\x9e\xe3$  $\x0\x1b\xeef\x1f\xc1\xab\xaci6\xb8\x98\x83\xfb)\x84\xdc\xd4\x0c\n\x87E\x13y.\xab\xaci6\x12y.\xab\xaci6\x12y.\xab\xaci6\x12y.\xab\xaci6\x$  $60c\xbf\x0b\xa1\x0fQ\xe1g\xd9\xf3\xf3\x97I\#w\x96\x98\xfc:1\xf8\x1cai\xa0\xfad\xd$  $d \times 3 \times f^4 \times f^3 \times d^1 \times f^1 \times h^3 \times d^1 \times f^3 \times d^1 \times h^3 \times d^$  $e\x8a\x99\x1c\xb1\&V\xe4,\xde\xd4\x89W\xbe\x83\xe0\x0ejB\x9a\xa0\xa1\xee6)\xc1\x9$  $f\\xac\\x99A\\xb8k\\x82\\xcb\\x84\\x80\\xd5,\\x10\\x87K\\x14\\xf9\\x1d\\xa6xc\\xcf\\t\\xa1\\x8cQ\\$  $xc1p\xd9\x16\xf8\x87;\#\x02\x97\xe8\xfb:}\xf8\x1cai/\xfa\xf4\xeb\xa34\x7f\xa4\xe9$  $\xdc\x98\xd3\xf1\xf8\xbaw\x03\xda\xac\xd2\xde\x19\xac\xa4\xa96\xd2\xf6\x86\#?\xcf$  $F\x18\x1cvM1\x8bWQ\'\xdf\xe8\x8d5\xf3\x040{>$4A\xe1^h\xae\x85\x99\xcc\xb0\xc6U\x}$  $e4K\xdd4\x81W\x99\x830\x12j\x81\x9a0\xab\xeeg)\xf1\x8a\xacoAxi\x82\x07?4k\xd5\x1$  $6\x10\xf7D\x14\x86\x1e\x86pc\xc5\t\xa1\x7fQ\xe2qY\x13\xf8\x9e\s\xf6\x96\x8e\xfb\$ \xa5\xd91\xd2\xa3\x86\xa3M\xcf\xc4\x18\xec|M\x87\x8b7N\'e\xe8\xfd5\xf3)N[ \$>A\x0

 $1_h\xa4\x85\xa9\xcb\xb0&V\x04M\xdd\xd5\x81\x97\x9f\x83\xec\x11\xbar\x9a\xaf\xab\$  $xaee) \times x0x8b \times x0x8b \times x941 \times 95 \times x10 = x10 = x10 \times x10 \times x10 = x10 \times x10$  $x11\xe1q\xed\x13\x08\x99<9\xf7\x16\x99\xfb6\x81\x08\x1ebW0\xaad\xeb\x9a/?4\xeb\x$  $\label{label} $$ da\x84\x83\xa2\xf7\xa9vCz\xac\xda\xe4\xb9\\xa5\xa22b\xa6\x86/M\xff\xc6\x18"} $$M\x$  $92\x8b[M\xd7^\xe8\x936\x134NK\xf1\xb4\xc^\xe6\x81\x1au\xfa;\x95\xd4\x06\xa21\xe$  $e\xb4\xfala\xb51\xd2q\x00\xc7T\xb7\xf0\xce\xe8\xc2\xec:\xf9\xb9"Lu\xfb\xc03$  $\x05\x05\x07\x01\xfbp\xd8\x8cV \x00\xa6(s)\x93\xc76R\x11F\x19f\x90\x95\x1$  $e\x0e\xc5\xefR\xda\xb7\xa1\x8f7F1\x05\x95F^{k}\xdav\x1f\x8a\xfb+\xe1\xb9\x1d\xd1$ `\x1e[\xa9\xe2\x8eV\xc9\xf3E\x15\xfdR\xd0\xdd\x00\xec\'\x9a\x9e\xfb\x88F+\x1e\x9  $x99\xb7\x00\xd1\xe8Z\xec\xfa\xe0\xb9kK\xe5\xf7\r(\x03\xaf\xdb9\x93Z\x08\xff\xd0L$  $r\xd8\x98V\x13\x00\xd6\x19sp\x94wCR EY\\x90\xe1\x1e\xce\xbd\xefU\xdbG\x88\x8f\x$  $18F \times d1 \times 0f \times 95 \times 4^x \times 0f \times 7f \times 3xfbs \times 29 \times 18 \times d1 \times f1 \times 1d; \times 2x \times 06W9$  $\xdfE\x8e\xfd''\xca\xdd\xfd\xeaG\x96\x9e\xc2\x88\xa6/\x1e\x92YA5\xcdb\xda\x01:t\x$  $f9>\x85D\x06\x92G^\times\xd5\xfabee\xe2\xd1\\\xfe\x86\x94\xb7\xee\xd1XS\xec=\xe1\xf9QK$  $z \times f7 \times d+x03 \times d2 \times dy \times 8Z \times 8Z \times ff \times a0Kr \times e^x99 \times c6 \times 0f \times 00 \times 9f \times 19Cm \times 94 \times c2$  $Cr"E\x1d\\x10\xd6\x1e\x03\xbe\xefS\xdb\xa8\x89\xef\x06F,\x10\xd5\xb6\xeq1\xcd\xe9$  $v\x1f\x84\xdb1\xe2\xb5\x18\x91\x01\x1eU\xac\xc2\xfeV\xc5\xdf\xe5\x84\xfdE\xcb\x88$  $d\x01\xeb\x95n\xcd\x886/\xde\x99Y\xfd4\x9da\xda~:\x84\xfa>\xa5D\x16\xa3G\xe8\xd$ 4\x8ame\xc0\xe1Aq\xfe\xb3\x94\xd7\xf0\xd1\xd6RL;\xe1\xcbR{u\xf7\xfe\*\xb3\xbf\xdb  $\x0e\xbe\xd1Rk\xb8\x89\x86\x07F1\x10\x98\xb6\c^21X\xeaF\x1f\x84\xf2k\xb2\xb9\x18\x$  $b7\\x00\\xe2\\xed\\xfe\\xe6\\xc8\\xdf1\\x85\\xddP\\xcb\\xe0\\x00\\x1b(\\x95\\x98\\xcb8F/\\x1$  $2\x9\xc9\xf14\xe7\x8a\x81:j\xfa^\x95D\x08\xa2\x17\xee\xd4\xfalE\xb4\xe1\xd5qn\xd5q$  $xc7\\x94\\xf0\\x91\\xe8R\\xf8:\\xf1\\xb8RYu\\xb7\\r+\\xfb\\xbe\\xeb8\\x89\\x88\\xaf\\xd1K\\x$  $82\x08yW\x0f\x05\xa6)sm\xa2\xc7\x93Q!d\x19\xfc\x8f\xd5\x1e\x0e^\xf0R\xd9\xb7y\x8$  $f\x07V1\x96\xb6\x7f\{\x1c]\xear\x1f\xf4\xfbk\xd9\xb9\xe8\xd0\x00\x1e[\x8c\xe3\xf$  $eN\xc9\xafD\x85\x02S\xeb\xdc\x00\xdf\'\x95\x9e\xcb\x98F\xaf\x1d\x89\xff\xd8\xfc$  $\x9d,\x07\xc9\xa4\xf4G\x13\x96\x98\xb9\x89\x1fu\xccY\xa5R\xa9\xa3\xd6\n''\x95|]$  $x9dv\times 30x1d\times 96R<\\xed\times 4x1a\times 84\\xbe\times 2x14\times 6x1xf2\times f8\\xb3/x8eW\times c6s1\\x$  $8b1\x7f\xef\xb2\xeb\x82\x83T\x11v\x17\xf3^\xc7\xc9\xa8\x9a\xa3{:.xc3\x82\xb1\x80}$  $b\x1e\x1b\xc3\x03\{\xbfy\xcd\xc1\x93\xdc\xb3\x07\xca18\xfc\x81?\x8a\xf5\xd8\xfc}$  $961a\x9d\xf7\x9f-$ 

 $\xd4\x19\x8b\xce\x88\x14\xdf\x83r\xe9\xb2u\x98Whrf\xf9\xef\xb9\xf2\xa2\#T\x0ez\xb73\xc0\xc2X{\xa3t4\xe3!\xb2\x89\xf6N\xe6CT\x18\x02R\xa60\xdc\xf6N\x9e\xc7z\x82\x9c\xf3\xce\xbb\xa3\xfeA7\xbf{\xae\x1b\xb9\xf6Z\y\xc4\xcd\xa3\x0c\xb4\x02\xd1,}$ 

 $:T+\x00\#\x08\x7f(6LU;\xebcxx\xf0M\xd8\x89\xc1b\xa1Y\x1a\xec3!ir\x95e\xfe\xa2\x90$  $R\x14\x04\xb9\xa3\xe0\xabLo]\xfc\xf2\x8c\x81\x0c\x974\x01~\x94\xcdu\x07\xd3+\x83$  $\x82a\xc9v\xa3\xf5^{\xb1\x2f\xb6\xe9\x19\xcb=yg\x83\xb5f\x8e\xec\xa3\x0b\xab$ \x12Y0\xf3\x1f\xa8\xd4tF\x96U\x8c\x82\xefvL\x94 bH6>\xf2\xd5\x96\x8d\xcc\x86\x9a  $\xc7y\xbd: \xf6\x15QY\x879\xf40\xd0\xea\x07\xef16\xa3U\x8b\xf2c\{w\x10E\xd8\xf2c\}$  $xbc\xc1b\x93Y\x03\xed\xf3\x12i\x97\x95\xb5\x06\xa3\xe4R\x84\x0c\xb9\x9a\xe0KMo\x$  $01\xfd\xc2\x82\x811\x97t\xfd}''\xce\xd5\xfe\xd21\x82\xf2f\xc9\xe5\xa3\xd5V{Y} \xb$  $f\xc2\xe9\xa9\xca=yg\x93\xb5\xc6\x97\xec\xb9\n[\x1eYh\xf3?\xa8\xd4\xe7F\x86L\x8c$ \xdb\xef\xe6T\x94\x08bx8>\xfe\xd5\x96\x8e\xcc{\x99\x97\x7f\xbd\xe7!\*[\xf6\xf80\x  $c9\x60\x00\x61\xf6\xcU9\xf2\xf3\x88w\xd8C\x88\xba\xc1m\x92\xc9\n\xe$ d"x12yx93x95ax06xb3xf0Rx01rtx93xe0xa6L?x0fxfdxe2x83x81<x97?xf $d\xfd\#\xceo\x00C\|\x82\{e\x99\xd6\xa3\xf6V\xbba\x87\xc2\x19\xaa\xcaCyw\xa3\xb5k\x$  $98\x8c\xc3\n\xaf\x1d\xf9\xf3\x15\xa8T\xf4F\x90M\x9c\xd1\xefiV$\x1fbQ8\xbe\x02\x$  $d6\x87\x8e\xdc\x86\x99\xc4\x7f}\xd9!\xc0Z\xa6\xf500\x8diT0\xce\xe3\xc7^1/\xac\xa$ 5; xf2gx88gxf1Cxcbxb9adx92`nxad4x12dx92x05ex06x9fxf0Bx13rxb3x93 $xa0^{xc2}xf5xa9x1a=yx81xa3x85fx98xdfxc3jxaax1d^3$ 

 $\x04\x16\x97\x90\xd2\xafvV\x84 \x82H8<\x96\x96\x96\x41\x86\xa9\xc7\$  $x7f\x0\x01\x02\xf8\xf5\xcfX\x8d:T\x90\xd0\xe3\t\x7fq7\xacK;\x82c\x88^\xf0\xd3$  $\xd8\xb9\xaeb\xc2Z\n\xf2h\x92\x93eF\xa3\xf0X\x14\xbd\xb9\x93\xd4\xab\x0co\r$  $xe9\xa9\xa5u\x93\xb4\x84\\x92\xf2[\x84\x99\x00\xc1\xba\xed5\xf0nt\x17\xdfs~\%x1$  $29\xd7\xc07\x06\xfQ\x9c+\xb6\x82\x93\x87H\\xd2BZ\xfe\x84\xaf@a0Fm\xaa\xc9\&\x88$ >I\xd4 \xc8\x8c\x15\xc8K\xbd\x00\xaf\xd2\xcf\x14i\xc0?\xecKS\xfb\x11\xd4Z\xedy#\  $xdd\\xa6\\xef\\xce\\xef\\xd0\\x10\\xd5\\xf6\\x8a\\xa2\\x$  $f7\x98?\x9\x9e\x09\x06r)\xffG)\xf27\x08\xe15H5\xaeu\x94\x94f\x92\xc1[\xd4\x9e\x9]$  $x93\x00\xc8\xba\xad\x1f\xf0\x12u\x17\xe3s\xc1\$R\&\xd7\xf57\x06\xe9Q\xd0+\xf6t\x93$  $\xc9H<\xc8B\x05\xfe\xa4\xac0\xb90\xa6k\xaa\xea\&\xf8EI\xde!\xe8\x87\x15\xb0K\r\xf$  $6\xe^{xd0\xb4g\xc0Z\xeckL\xfb\x15\xd4\xba\xf4y\xb7\xdd\x06\xfb\xce\xf6\xfem\xf3}$ %IH\xde\xdbfB}\xe2B\xd0F\xd5g\xfe\x8a\xd9\xf7hF\xa9\xbf\xc96e)\xba\xffG,\xf2.\x0  $8QGHn \times f \times 83 \times 4^{2} \times 80 \times 0 \times 10^{1} \times 10^$  $x16&\xe7\xf17\xfb\xe7\xe1\xcc+\xbdu\xb3\xc6H\xc9\xe2\t\xfe^\xad\xe0\xc0Q1\xe$  $a\x09\&\x90E\xa9\xd4!\xc7\x88\x95\xa7K\xbc\xf4\xfeB\xd0\x0ciPp\xecNL\x8b\x11\xd4T$  $\xf4)\xb3\xdd\xa7\xfa\xfe\xfe\xf352H\xcf\xdb6?}\xe0A0A\xd5x\xfe\xda\xe1\$  $xf7\xcFY\xce\xc9\x0e\x99\xae\xffK,\xa27\x08\xf4GxT\xaf\x8e\x83\x04\x84f\x87\xc$  $2k\x83\x92\x0e\xc1*\xed\x1f\xf2\x1e5\x16\xe3u\xbe\xf4\x11\&\xce\xf0\x87\x06\xe8M$  $xcc[\xb6u\xa8\xc7\xd8\)\xc9@\n\x8e\x84\xad;\xc1oGl\xa7\xd9\&\x87EG\xd4\xb1\xc9\x8$  $8\x19\xa8k\xbd\xf4\xa3B@\x14i\xc0oLLL\xf5\x11\xd4Y\xf4y\xb3\xdd\xa7\xfa\xc7\xfa>$  $\x1d\xf3\x1e3\xd8\xce\xdbd?-$ 

 $\xe3A\xc9@\xd5g\xfe\x90\xe27\x9aF\xb3\xce\x99\x05e\&\xaf\x0fH,\xfd7X\xe0GSU\xdft\xe0GSU\xe0GSU\xdft\xe0GSU\xe$ 

 $x83 \times x6 \times x92 \times c2 [ x84 \times x02 \times x00 \times c1 \times x9f \times x9f \times x10 \times x12 \times x10 \times x12 \times x10 \times x10 \times x12 \times x10 \times$ 

 $f\x84\x07\x81\x10X\x84\x1b\x92u\xcb\xbf\x0e\x13\x94\xaa\x7f\xdb\%xf1\x87\xdbv A\n\x0cP\xd9\xad\x1eT!\xbbSn\%P?\t\x8c2\xbf\xcdr\x9a6v\xe5)\x0e\xf4=T5F\xc2P\xbcm$  $M\x9b\xb8C\x1a\xea\xbb\x87y\x05yc\x0f\x02\xc20\xf0\xe1\xdc:\x9a\x13vAa\xbd\x11\x$  $adu \times 16^z \times 481 \times 10^x \times 10$  $f\x6^T\x86^T\x10\x12\xcc19H\x1ef''\x85\x87s\x10\x80\x83\xab\x9aua\xb$  $e\x1e\x12\x94\xda\x7fK\x1c\xf1\x96\xdbv*A\xeb\x0cp\xdb\xad\xeaS\xf1\xb5S\xa9\%\xc$  $0=\tx822\xaf\xc8r\xbc5\xb6\xec)\x1f\xf4\xedb5\xbd\xc2\xc0\xb0m\xb1\x9bhP\x1a\x8$  $4\x05\x05\x10co\xfd\xc1\xd9\xf0q\xe2:\x8d\x13\x96\x1da\xe7\x12m}\x16\#y:\x94$  $\x87\x9d\xfc\x88\x0c\xd8\'\x9f\x9a\rhN\x94\x91m\xaa\xc4\xefx\xfc\x86\xd2J\xe9\x1$  $8\xe7\x08\x13\xec69\x06\x1ef\x1d\x85\x02tPi\x83\&\x9b5k\xbe\x10\x11\x94\xda\x7f\x$  $e1\\x1c\\xe1\\x97\\xdbo*a\\xea\\x0cZ\\xdb\\x9d\\xefS\\x0e\\xb5S\\x9e%P>\\x99\\2\\xad\\xc7\\xf2\\xd$  $a5c\xecY\x0f\xf4>d\x05\xb6\xc2a\xb0\xad\x9d\x9b\xb7P\xbaz\xbd\x87g5\xf8b\x1e\xfd$  $!\x60\x60\x61\x07\x90\x12\x13q\x1e\x12\x0c\x11\x0c\x$  $0c8\x19\x9f\xeb\x0e\xe8H\x94\x01n\xea\xbc\xef\xd0\xfcF\xd0\JY\x19g\x0f\x13\xc96\x$  $b9\x08\x1e]\x1d5\x07t\x16hs\x1c\x9b^kn\x0e\x11\x95\xda\x8f\xdb\x1c\xdb\x97[w*7\x]$  $ea\\xc0\\xdb\\xee\\xa3!\\xb5D\\x9e\\x05P>\\xff{2\\xbe}xc7}\\xda\\x95v\\xec\\x13\\x0e\\xe4=$  $d:\xb6\xb2P\xb0s\x9d\xcb\xb8P!z\x1d\x88g\xfb\xf8\x12\x10\xfd\xc5\xdf\xe1\xe1=zc$  $v\x1en\x0d\x02\xad^> \t\xaa\x94\x8b\x9a\x0c\x89\x0c\xe0\x18\xaf\xe9\x0eaJ4\x01n\$  $xa0\xf(xc8\xfc\x95\xd0\xcaY\x19\xf3\x10C\xcc64\x08\xbef\x1d\x8a\x07d\x11h\x$  $84\x1b\xebtk\xcd\x93\xda\xdb\xbc\xf0\x97\xd5v\xea@\xea\nP{\xeeY!ET\x9e}$ "P~\x08|?1\x91\xf9\$\'i}\xc9\xdeEW1\x8c\x9f\xa0\xad\xb3\xbe\x15\x1c"%4;Ro\x81\xac  $\x13\x1f&+2<'$ 

Signature Size: 4627 Signature is valid.

**Testes Automáticos** Testes automáticos aos diferentes niveis de segurança do Dilitium. Nestes são testados os tempos de geração de chaves, assinatura e verificação da assinatura, bem como os tamanhos da chave pública, privada e assinatura e se o algoritmo funciona corretamente.

```
[]: times = {"44": [], "65": [], "87": []}

for i in range(10):
    message = "".join([chr(randint(65, 90)) for _ in range(randint(100,10000))])
    print(message)
    for version in [44, 65, 87]:
        tkg,ts,tv,ver,pk,sk,sign=Dilitium_Test(version, message)
        print(version,tkg,ts,tv,ver,len(sk),len(pk),len(sign))
```

```
if not(ver):
            print("Invalid Signature")
        times[str(version)].append([tkg, ts, tv, len(pk), len(sk), len(sign),
 →len(message)])
# Times and lens from Dilitium 44 Tests
dil_dsa44_kg_times = [x[0] for x in times["44"]]
dil_dsa44_sign_times = [x[1] for x in times["44"]]
dil_dsa44_verify_times = [x[2] for x in times["44"]]
dil_dsa44_pk_len = times["44"][0][3]
dil_dsa44_sk_len = times["44"][0][4]
dil_dsa44_sign_len = times["44"][0][5]
dil_dsa44_message_lens = [x[6] for x in times["44"]]
# Times and lens from Dilitium 65 Tests
dil_dsa65_kg_times = [x[0] for x in times["65"]]
dil dsa65 sign times = [x[1] \text{ for } x \text{ in times}["65"]]
dil_dsa65_verify_times = [x[2] for x in times["65"]]
dil dsa65 pk len = times["65"][0][3]
dil dsa65 sk len = times["65"][0][4]
dil_dsa65_sign_len = times["65"][0][5]
dil_dsa65_message_lens = [x[6] for x in times["65"]]
# Times and lens from Dilitium 87 Tests
dil_dsa87_kg_times = [x[0] for x in times["87"]]
dil_dsa87_sign_times = [x[1] for x in times["87"]]
dil_dsa87_verify_times = [x[2] for x in times["87"]]
dil_dsa87_pk_len = times["87"][0][3]
dil_dsa87_sk_len = times["87"][0][4]
dil dsa87 sign len = times["87"][0][5]
dil_dsa87_message_lens = [x[6] for x in times["87"]]
```

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44 0.2915046215057373 0.8287069797515869 0.5780596733093262 True 2560 1312 2420 65 0.4006361961364746 1.0208897590637207 0.6984672546386719 True 4032 1952 3309 87 0.616485595703125 1.4487121105194092 0.9335939884185791 True 4896 2592 4627 EPANRKGKSOPMMRBYHAUTZXVPGUPLRCRAIUILLIEKDVBSRRKEISJXZIXNVAFZOZDQDTTQQPNZIKXTMJVS YOXIQIQTNRVPBMPZAVLBYQITCFNGCWNSSBRNAZFSGAYCDNEJCKYDCXPHAXPSOBZGWSXABGMUAUGTSNBX HBCDKVOKAIAZNHWNDZSOHKOREKZTAOODPQXSBUCWPNTVHRVTNLUPYDTEYZDQCAZJQVTATOPBXOHXBNNI EXVGUMJSAQGMZGFZPPCEQERMLQZUVGJBMTUOBWLOKPLJSYTNHPPJMKKISBRPZGVTEOZVZYEPATDOJBQH GVATCEENMMTZLSMIONMDPPNPMVRRJZXXYLJHHPUTSZRHIDRZSALPFGRPLCRGRLGKUPCSRAHFRKUGPZWS GFEIENFWYIEJOYMOBAZAVDPGYIKHPPPIOAZKQZAHTRKETDHBQQMAMIHIRVSZILMQKDSCQIWSAUKBAWSI

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GAZNDYJTNFJAJJFYGADVLIBWKRVRWFKFNXCUTJHPMJEPJLUMBSQLILVAIIWVBEAQNPNMLHISWTHJBUPF VILMFPXMUMOLLGMBAAMFJSVMGTLRBILBLOGFQWIOBSSQZMNRUVAXLDYPGXSYCYSUNKKIZPTCFEPGOEMB IYGRZBVTGAKNGEOBTKGFWFHUQEUURIAFGKAHXMXYDKYIKKLQOZDGTWCTZOPFFGVECFQIRNMFSJVHCISU NFCEIKXBFLUNSTGYBULHUDDVVNGLSSPZWBHJXURAYCADMWAYSGKGRPROZSXYCLSKVZNBPSGFVCNTWYHQ CKUKUKQRLQVWULPTLPFDKBSZEGWQQGFDRAYFWSNSRPHIXVCJHVNIMHUDNAHMIZFRUWJXIRCBXMKICGRO  $\tt XTVJQHCTYXGEDGMIWTWGHBEJOMYCZVTAYMNULVJVCOCRHRWWWNQBMUBWJRVEETHISENYVRDHCEJVHPWD$ WQYKKXYRQITRKKZSUSZQJWATDHWARFVYLKJMLQBLSWSSBUOXBINTULDLKMNIEXKRDGECKVMUTGLIDFDS RCEIJOXLNHLCFVCPTRFHVYQWZNSYFCFNBQOVGTFWTTVDGEXBSZGBEHREOUKOSASJODBHLHOIDNGMWBTW PPJUKWWESHBFQQBLKFDAPAUDEZTXSSCCVJJJSCFJPOHUAIFRVSGWTROIGBKJOQLVYGIQFJHFKVCVLKRN VOHNVELOQRCJJTOUBUBNQKVWDUVGDIJQLAKIDUKVVZZVVJLRAJVPFZYUUWUCBIBFOBTZHAJNIUZBGLMT TDXBEZWFUEFJKSUIDXIERCTCLDKWXZROTKFGDYWTPVCCPNRRROLRLXHOSDDWUQIGIPELGVDXUUVCDIUL LSGFZORNRRWYMBRUEDDFYSAVQPENFDBWXCRKTHRBQNWIPZTPFWEQPXRTVWDOBLMHAIEIPQSVRLUVTEHA XSPLPXYKAFVUDBCGNGXCRKMDRZCNHGLERLKZECWXESJCCOPTCSMFTYTOQEHITGHIRPEVLSCLXXTRODAY TUIFJJWLRQKREOJETTARCOXJEDZUXVMQJXBXLSOYKAEIMLPZATLZVHFNLSKEEIBVZMCRFYRWFIISKCHY SRVGWAJMPSLHPWSVRXDTQLIHTVLGQZVWVOIXCYIDENLVVNUZHXNFRWJXMNCXULZGWFMBAMVNVRPGYTLL HIUPOSBZGSMSWFXLOLFWFQMINEYAIZPUQVYTHGFJKFZRPSLZBLPLDJAKAORVBRZDVGEDZELKIDAZEOLK NODKZWIYEQGMPKNYXTXGHBMGBRXBYQUHRENYDMNKFOFTZMLPZTGNDZFBVZXGOUIILJWQZZOFFZDWUOWZ TPAZACQTUNSEEMUJZJFAOGZKKLUAEYQFNIHMGUVQTEBZFVHXCNTOLBWXDTWZXOXHHLBQAGNZJTJZTFCZ BQGLNVZLOJNHBUMSIQZIFTUMAKPWPCXPNNZZLGZUTECBTSTEFTQOPLMMUUGXWNDWBUJYBJKYEZUUOEBH ZQNAQDIWERJORANLOLSCURZAECYYZXPRQDCZRPROXHNMKCPSSHCVKMTJSEUQHSKSWCOIBMIRDRSCYJEW RIHTRGPXLEIMBXURESFVAAEHVTNYRBCIWRFVWUKWEYJZSXXMEDPFCIKMSOYLXKPQPBAZKAMKULURVFLY EGMPYJVDFPTLMYUVDOSYCMQVVYCHMKMGGLFWZKUFKOHHVRPSJMIBRVZMULDVEVSAZNGRVUIUCHBZYVMS AICMAFEGUGWSLDJHOWYWWZPXCTQDKBKIDOJWKKSPBZNNRKDJNISOGGRHCGEDEZDMQQZWWNUFRAPMZHQC CVUFSIXQBVQEPPVABORIORLMYAJWOUKBDNLTVDBLGFZRIRUUMCVBSGZSWUTXUGUYQANQFHXYEVIBYIRQ CJJWVZCDRSRXMZEMHFIVGKRRHCUORWEFPCOAYSLEFBPDEEJPTIIJXNJKWVWHCIIDKDUAZWEMOGBBQWAK SDLYJBHBHDVKDDCXDTBJOCIUVEVDNJDDWIKTHQMYQGTHKBZWJIOBCWVDQHKXBOVUMZNPGMXSZZBZAVBM KQYNDJJANVYKVCJBAHERMWNJDXYXWPWXJCPPSUGUVJTYUNIMTXLINKLNJJZDXFPTLWSHJCZEJXDOKFPN CYSOAZKRXAKRFDZNRRSDBHJIIZDFRZCITUHRNTITDTGNQTVJDOGXEFLYQGZSVJEILQVEHPKUIRRLSQVW UVYRBBSJCAFZFMMQITZTLTIAKQBASRNCZTKWDCSTFUUOKWVHPPXUQWRGZQBWLVOAKPLOZGCIUCAHUKKG TOQLGMWVZUDJXRMRIMRZWLNNMLLKFZMANBKBCJHNTHJOANCROIRJYJDHMPXZXENYPAMKHQEKIIGYJUBG TOIQNLFUQKCBGECCGOWHTZIUGTCVGBECGJBAKKBDDHRSNTVDVUVJJYBGWNBMDTCGOSCGEIJNUATDFWUI XRFBUWQHYENILXOYETOYEDMYPNDSHFSHSYYVJSYTTADYJYDWZXVEDWRVPMOEBGCWAPMDIMNBICZRCWJU RRUDHVYYCWZHYMROOGFURICLXWHRLMCUQJDYCKRXYHRXSQOKEBPUXOZJIPGHODUQUOMDDPAHARFYAGZX TPVCIIALSTTOFSSMWYHMOBROGJPAQCJFFMWPYJQYQ

44 0.2540774345397949 1.2427127361297607 0.5044355392456055 True 2560 1312 2420 65 0.4168095588684082 1.0502116680145264 0.800607442855835 True 4032 1952 3309 87 0.6289963722229004 2.205531120300293 0.9468729496002197 True 4896 2592 4627 EOJTNAOVRQVWKXZBEVMLEYVMHMMTXSKDGSAJVUWHMFMPBPTBTKTMAAOGXHNSPAYMMQTJCLVPOHFNAQLH BCPMJRVEMRLIJXQVGYXAWVCYDVABQRJVMMJVVHXJKTFWACVTLIAKBZXEIDVVYLPPKYFIOHFEKFYOEZGO WNKXWCCZZFCVTWDAEPWQOETXXKKKKLMDZNOQNCSKPUIMNJOZTEOTEQQWTVLKBNQGWNRSIORLEYTTNFGA UFTTLHGGLIJUILPUNTDWVGKLJPTEEHVUTENNYYDKTRMGPLQVBLJQROJIBXWDQIAXFZXMGKGLADZXZSFI RPZMRSRQCHSICPCTPUUYQGEEXTVKJPBNBNSHVBUKOFIASEIBSMPOCKUNERGERHTOCBTPQTJVTGAVBEKK LYDSCQFZCSQDFWSXJHWSHGSYNQMTRUIHBOQFKVNEILYBZYKZNRVIVBPXOGDSSCNMYWTRNVMPEZWTDBXU QIYAIDTPJPEHKEWZVDFUPBYZKKFQBPPXHIIOEMTUDIXARBCFAAIEDBDBUHJPUYDZMBNYYGTKYXLUJHSA VSNQBYVHPQJQFNWWNJKWKWUCUVTKQNEVAXDCAJFCSRIICGVHMOWRSHUVWHVHJLZJOJIAUXJIZVCUFVGS YXAXIOUWIXRCPPJNYZXYVEFGWUZRGTGVCYPOEEVXAMSEVQJIKJYWUJJHEKLPJISPMEXOULFICTDYHJLS MZVLGPIIQNVNDLIWSYZKJQUBUQVEUMDBGDKSJTZDBBNXSMVNECYBMGGUFOIJCAAIVSPNUMCWCOUFYRVV FCOMKNRBUJTVGJZEFLXWHFQNIJTOCEAUYXSUOTMVHIRJSCYEJHMOFNGGKGXYQHRIHFLJBRLOJNKBKUXO QIOPYCMXPKBKBLULXXROWFRQVOFHKDYIVOHGHBWKVUEOEEFRXGGVBBQLDPSYVYEOOFJQGNKBZLEXQYGL GZBYGAQNOPHEMCKGOEWTJVQUMADQFQXOZPMDDUNAMAFJACCVYEBRCRLFIUGYIKUVKFFMLNAOINIYUAMW NIYCKYDNIKVAWCAJCTSRUCASHDABFYWNLQNKLEZPOBNXCHPXENUUDDBNFAMFMBDPWNCOVZZLJGYMKXJW XZHTTBCYUHXWRXPHMTYVPKNTIKPMJJTMDCTLRUSVNVFIFHXKSTPDQFWTSFHIBTSIPPYCAVVUNJ

44 0.27495336532592773 1.1669583320617676 0.528548002243042 True 2560 1312 2420 65 0.4261138439178467 1.0554020404815674 0.6892261505126953 True 4032 1952 3309 87 0.5976171493530273 3.8513965606689453 0.9567966461181641 True 4896 2592 4627 JEWRMDYEDTJAUDLSUBMVYWGEFSHDAWANXQJDYGQBCSNEFOMRAKJPLJBEJSLTYHULIDUWUXFTECAUUCTA JDMRRGBHEAYATGMUOWDXTAQUZMJIXUDOZKIBCJMUFLAFOGLQQDYVVLYMILPJSCDESHNFEFBDUJLYUVML GWPCFOTTUDPNQBNFAYRMANQVHECEULFJFFKLOUSBSXQJAAJFURDYREJFCYCDGVDAGMWSYFNAOOZSZEDR AWFMEHAKRDQRGZLJESUMRSOVSRDKHGEVFIQNABPKPTBTHTQSKMDQVOXJOLAZPNJXKYOTAZOQSENJYLNP INIFAOGRNCQCRQRGVBBNMRYOXYVELHJGWDXTKYRKPSPCLLVLUBEEYMETVLXYNSSCCUDVLDTGKBHFYAYK FVGRGELQEFDZFDLOVMMXGESBUQAEADFGVPEDLVCMOTDLRSFYRXODPIVHNJQSIZQMWGXNUXKZTTKFDXEC CWPNNUEMGTROTHKMKZVGTNBEHVYWGZNNPZSTHYCBEDIQQEKYMOEUONIPUDRSAKZITRPLMYZKGIIOYNOF EYIMPGVJQIJJUCBLYSIFEWOTSHNVWWLGSSCHHRVHINMCKVHOYUJOUGTTHRSXXJFFKQAGQEEVDDMGMKPC FKGQRSXVSCHDCINIOFNPJAORINNEWEWYINOVGDPXPIBFAJPJUUEBJYAHEBWLJHCPBTVGENBRZSFIJNYC ZAIYBEXKUMTYNBHDWWNRZBZDNAWCCAQXRUDNVDTPNKHUJKCJUCETJNHSLZJXPHWFWASMDLKVVHDVMHDS RMNDBBUPNUMZOHDWCTRPYNAWQHOTOCFDBABXKHRYOMZBKQPYVXZELKDAGNZTUUJNWEQTPPWQGROMYROF OJJFEIEMJLRDIKEZEEAMKQWJCTRGHMFMUYXJBXBLEBROGGXMCDKYHXIWEVMQUWGCNDSTMIYXKXFUEPFH TJYSPRMXGCYROJUPPMOPGTZXVAWQIXIVRNXKNLVUJIUZISPMQGQVMQHJXWZUGYEATBJVITIWBNJYNVRO CGELCWWVLOIPFCWEOOKBZRPPAAQMSYZMWIIILGHPGEYZITEKKGFIRCPRQXVXILOOXSDRVZQXNAUIIFVB YDGFHWBHXEYREDAPBOZYBQNNHQEUMQDYIWEFVUJLATMWMGCRERWMHCTMEHRCCWHLDNHMQJQIMLARCUZH RLQPAIZLAEEOFBUODUJEDXYTRJKQHJEAHQBCJIRBUPKDZKMARMQCFQDJNESDKZXHYGHYDGIUHSHNBWSR XBJVJKQRMKBBBDNFTDACIBEDESDBKRQDDWWODAINKXJBQFKBSQDQYEVVMOLWUCGOSLGVZZTZVXXTISRC

AWMRUVACRNRAKGSLPCQPNLFNMDDRRGQXBQTEELTHENQCMVSBMBQWEHKBGQGSESFLWHESDDBMWQWEXLJC ZSEEWVMIKXAHEWVKAWQELLDLJGDHKUNBIXFQMFQQZNDGIYJRVDZVRMUBVAQJRUUIKLMIWWLPCQWJLLHW TSXDVAWPERQECMHNSBBCQSLWUWYOQZNAPNQHHSRUKNXLVDYQDBHEEMDNMLETBISRYFXTYJYGIFLKOJRE RXKDZQXDMAZCNETNGURIFXBLRNHWTLDEITDNLBFUCZUQDOFRXFYHTXUUPESZLMKOIZDSIZMAXGSWYACX DILNLIGZJKJSPITLMHDLGUZXNYWFOEREWGVHLZXBXOIEDHMMLTXKVQVLMDEBNFLWDYVORBAOWPQZKKWJ ISNKJNAPOESRXVUKPAXPUMLDZWHABJLNXVADOJKVVMGADEIXZLHWPHJGPNUNPKKOKEPFCEVFEQCPVIYW YBEHRENNXNZJWJGKEKENDHYEUIWAFNMNSNPRZZMQWJJNDCSMNGWPTYJRMYXGEQUDGLWVAXRWNTPFNMBB SFFQIKNGUAMFHGUHMUOBZQRCFKFZXMOZDDQIDKBNKWDQWCLUURIVQBFNAJSHTMRMEYKUXXRPXPSQYEDY VIIAXHHSOZLVRSOPTWUGBINRWKOREFYNRDMZKZNKJOCAALOPVQCWYYYHWBYVUOPOBWXHOYJFFTPPSGQA TVTNZPSAJPGASARTCVPXOFBMXWQJVXPAQSWBFSAWNSILLLLIVNAWPJJUDHZPTRMTCYITAXLFKUBACXNA KKQDIEUROYMGUFSPGYCAGXPQELDREAXQIQSYAQZEGZGDQCAYMBSHLGNUDXCDAABJURZNTJICFNAITSIC QLLBWUBDTFYODZJTBZGAUWSAARCVTZYBFXGPXXWYKHXKMVHQUIAOTHNFEMHFVSVCVXKERNHZEPKKPVWC MGZJFFSCKUNRJRUDNTCRMVMQQKHSRVYOEIQWCNCTNDAJJZMNBQLCZAVGHPHEMRRDSKZLJYBBZRDBRJVD QDEKHADDANIARBPXDACKXFLIVSDYDIPMPALWCLURWKXRKFZMVVAVFGNOEGYGXCCQZCKUWGDDQTAXSGLW NIVYIYWEVMHQKVUIMVQUBVFSYNDFNLYNLEQDIHTHVFMMUIXOADAYZNEWSVWVSAIHABQQCXKEMGXCRM 44 0.24931979179382324 1.6546177864074707 0.4809255599975586 True 2560 1312 2420 65 0.4059009552001953 2.165740489959717 0.6893339157104492 True 4032 1952 3309 87 0.6015064716339111 2.2950634956359863 0.9502155780792236 True 4896 2592 4627 YLPJPSUUYVTRGBZVZXPKZWWIVEDUGRCQVXDROORUFMVDLGNOLLTZQIUOSNWRLWTYORHIEHSGLNIAPWBB HLXQXDSCQJKXGIRJKYZXDRWAXCYOTLXYQNWRTJUDOEXSVHYCSZFRZNPPHCGUIWMLHYZJGGBAREUHSBJB NPYHSUXZWGAPBNJUIQHRCSXEQJPPKEUIEQOPSFLUOBKYVWHGYVTUBSKHZOZRFCXVKCVTMZTIOAFOKUOL LMPKDMKHVIJMQQPBOBBNYUBUGOSKPLHWEKMAJKRXHRLEDXUSRPYMTLTEIBNWWGVENOSXKIQUIRLSCRYU SOTVYZUUHLXLILWUNHZWMQEWAKIPBVDCMKPNMUWKKRUWGWANHXIXCDVBFDGPYTHTVHHMWVVAZYRTZLMH IMJBKIREAGETSTLWSMRDNYFDZYLKBTTGOOZXIULWURKOMBXEYKUTPTYCQQBPPGQIRRRIMZSXSUFHWWSL EQJOQKCKOLAXYFCXYCAQVVIICSTDJTUXIPLYSETKQCRRVMVWUKWBFIHFIUBYZEMZLKKSDSGQDTACWJJD MXOPIFDQIIJZNUJELMRDHBUJZIPWYKLLSDFAIBPRHONHKTFQYNZZVTIMFHSADREZLWRWIDUZAANJOELU TZFBBUJZRZVSOSJTOIPPJPCRGSEHVUZLYSBDLRPWWLEZWSYPALQRUOMQYZBNNQBCEVQHDWQSEAIYDIPA HQSCHMGFAZRIIMLAJYTDTIBSBKMVTOTTPWYNINJCVWFTPPRPYCWKSVJUOHLXHTFUPQHUXGLCZTGXTMNK TFGMIJFGUTJMLEHRHVQJMMGYWDNKHTYMYOCQVBUISHFXKMJGTVBVNSLARRHWXPBBQFAYYFPHYHQLPEWJ FAWNZJJFIYTDIKUYKSAMELZVRHDRGXAEHSRKCJCSKYSSPBNMXABRWEZDURPVAKDZEVQRCYFFHDLSVKLT CJNGFGXZTPUNHJSWAFYUPKQPUYWXNQFNZCAJIZDWEJBNYGAAKBBXVFWXTOFCCHDTVFZKLIFFPMZFTXXS DCETNUJXQSZMNGBCBTQUAFGZYWCKJFNCHMQWKGLUIOXMBJEEAXJUMLXJXNNZANCXZBXEXQADQRNLIEMM GFMKGRAANXUMATLHZMUPMMYQKZYUGGPBQWAIGWURCZIXBHKFRRHNTACNHRSASCSADMSUKKTCCNYQNWJL UHYUVZITJZWKVNKDVPGEJVYZGBXCKDYCMFALVMMOAWCURIXSQTLEYKUKEPGGNVNLRQDKQMFTULUKGJQM TQOZUVBLHBPFTMZXDSPPNPLHSXGMMZFYMOISWBKPGGJFLAKNGMOFIBUEGTJTIVVNRZDLHVGJKBXCHJXB OBHPHSPHPLKZITNTRPJRSQAGUVVZUHPAFLDUXNJAUCGTZWTKZLSIAHQTAKTWQNLWPZSHKARNWAUNYSTB BYWOCFJVEYUZRRKBWRRCJPTKITKVLBEJNNZQNHKNEVONMCVWUYKHLAGGMYHOZBKPAVAPCZPDHRTUEEGR PVMQKUBDXETDOZEANUJUTGOCHSKDQMXNAJZYTERXUFEOIECLAGRGNMQBAOCXXHNXAACDFHSPILPJYHEZ ATFBKXKUAMCFJHOKJZXKOMKEDJPKVVFZEXYEZTELSCUGRKSBYVWVAJYSXKSXJIHQNCYSXQTXDNVOKJDT PNVGURIJCKOISMKBQPTCCHQVPUFUMRURWTIVJRAYGAELGDCJVIBPJSFFSZABRAQGBJRAJZXCTHMKIMXX AUHWVVYYKIFMKEKBAEMRFQPYROGYWYORVSZSEWCWBUMQQIXSGVZJQIJYTNNVWHJVFIUAVUNPDCLWCWPD LKHCBYBDLQNLSJCWTLPHGLADTJQHAYNRMGWXMKKNBASIIBVQJAJPVMHWURLKAHJKVPCUTCIHIZZNOPID RABPTOFRDHCHZBQNWQIGFTDNVDNWAJNXPPCGUGOGMILFEHCRYTWHQYHZYIYYAFNHMSXIWMYNGRJZHDYI ABCLWAZPJPWWXJAMGLQRKIHNUHQWWNMZZCEZCGDNDAZLSJDLJWQAXYNGWIMDUECIHPMFKMZPDDZDLNLS XJBIRINKPKPSAQVSJAGDUOXJEFJZQMLGURKHWFQWEFQAAQLJCIRJRCHVJZUNSHPBPQBCUUTNTOZEKWDF KCEQGHXEWNUCUFGEWMNYLADZYASXWTSDJZSDBLAYIGDLNGHARGWPABUTQNBOUJYPYDYCZOBHYUNCEDGL AGIKEEVRBUHMJFAXDPXKYGGLTPFUAOYELKMMCTNBPOEBGOVKDXBRJWLDOJHYZLHRXKBBEEQFZGIPJK 44 0.25923871994018555 0.7205150127410889 0.5112712383270264 True 2560 1312 2420 65 0.4136624336242676 1.600691318511963 0.674079418182373 True 4032 1952 3309 87 0.5887405872344971 2.9642181396484375 0.9496622085571289 True 4896 2592 4627 BXVJNWPJWUXRMCJGSFUULEIODCTBKUPDTAWFPHIPGPCTTGLCSULEXOZMXRWEEBPCYMWDCFSKPXOZEICH QVDLGYCLBEUYRVPQQQGSIREVFPVFSRLXZLRFBRNZUTMYKVYWTEUTIRKVGXSOIJAZMAXDTUXADYRXNVVE RXOPYGFWITFXWSDAUMZIOBTWIVTAWWYKFMWYQEODOWNWAUVBAVEVQJVQJRQXZQSOKJWFCOHGYGASNSYJ GPACLLSVMKAXTRLEYCUXTVXOGCKVJWBQEKODVWSHZFIDJCYGVCJJAZEMJUVRQYCTVRTSVUZRLIUHYCSX ZNTRZKRBUMHJXXZZAYDBHVKAVDBKYSJWAMHGBQDYVGQSYGSFEZKUSBSYFKABFVRZHJOHSVFQPUIDOJXN LIFXYIIEMJXLEQWBEZJXBNGYQVZLXHXMNIYKMZTFDDFKJOSIIMBLXPUBVHHFHKUGGQOPVEOPUUDGBAXK YPROWUESMGCRXSKHPSXVDWGGSYAFENROCTIIERKUIGQDLQXYLHYONHEMKUCTHPSNELEAZAEWVNOBNVJT XVLJNECJUGCFJFZANAKNWJLZCDOYBCPUWORVKUBOXJRIYTZHVGPSTGKDDGURHBADOYCTOYXGTTKEROKG URGUMWQBJTXWAOZCZUEAMPYDCODRNOKIXZDVRYIJSLYLTNZCVABTURCQHALULSHCHLPBAYMHSIIYGZNR DGDHLXTTYXEFLNZHISMAFXSHIIXYYRWBFJWCCMUVCGVSHJQVHIGUJILYGREPYDPYQJQUJARFCBTWTUSC EPMXCXTGDCTRHEEIVODOQDCPNEIFLYQWRTPJZYKXDJFRTRETATBWHEQRCRCNLIWYRDTAPBBILFRGHMPQ IXGXAGJJRKGKCGTJMCCJSUQVTRHRLEDOOZOZFUTILCDCTRHZANVMXWZMHXTIMFGBCHRTFMERUVPJRAAO SCQTXZWUDZNJJXREAKRQUUHDQVMBKKWHXFFVKPRFXPVQGCUYGKJKNTRHDKDANETSEZWPBTEUDMIOZFII WVIAEZRRFRQCHXAVMSERERHDKIXNQKUYGRVXNBXGJZQHDRBMQLAYUHNFSKLOZQZJUFLQMETUDJLTQXTD SMQYWBVNBQVZXGMSXKYDHHNURQDLEFONICVQSNRVRZZARCZHEPQDRTYHZBRFEVQRLAHYXGNEJUOCEHQT KFQVSHFZTSUEUZUKVKKOUUOYOZCNEFFUJFCZQPQKIYTIWAORVPMKHAYKOVLXJBFZQIWQOACHXQVAYJXR VTOQRAWCDCYLVCTCSZBNVBFSAZKXVZYUVJXZYHLIEFIMRWZCNEPAVWRZOMACUKKDIRGVCBVMXEPTMKEI MLCOOYVNDLZLYDCGIPWVSLRQSPFWAVZQFNMGFZEDKCBVYFLOPLQJSLSZBOMZEFWNQOOQGMREGBXOANYL YWWPPWSEXBCNYPFKKYQWCYHMBIMMWOMLHFDTBTXTEQYAZIMZZICKJZTACOSCWGIGFDHLFFRQCFWGTRUV LLQKDVDVZXABEVRBFTKMGABIIXJDFEDQREMVVHSYOCFTYBVMPXXOWJVDJVKRVSJQOAZQETEWLNSHWJZD JFEIRNTCKLPMBTWHPSVXRCHJAKRBCWWOAKWUHPKJVRHCYMWYZKQIQUSXDMGFNKJYERLIHLCRRSZEHCSH ZNTPKTGCDEMXJPANUWAGUFSTTOVEXIISJOAHTSKUNNKNFEXCUAVYXXNQAXBLKYPNZYLQOMCMLEAWIWFY NUOUTUQXXRDSNRYXHSDZDDXACOJNJXNZPMTVXOEUCARWNXFQZZHFIOVUKBZHBAIWDQWVRUINQWGBVAKD YGAVWLQWRXIAGNWPMRQADMYORUNUHQIHZQMQFQYDQNBVTAQYHENLVLNTOJPTURMMZGHPDPIZBKRCNSNV OLMHTSOIGXYKWWVBGGJPURYBUDFVCABUOWXAREXFVBOOJNGFAVUSWJXZSMRIDHVPGKNILCARBCQNGUHG RAGTYQYJVSNDKRVHYWTJVLODQPIYGLGUFSVHWLEVZMEOUBGPMTIHENCHADRCMFPNBJSEIDLTEJZCEAAJ PMEKOORSFXERBMLGDZAPECJNWVNJKFNIARLEHUQQDGZOUVVTHUZVSATWOMVRFKFWRDVWBPFYEMNPUHFP WBNHMTUBAIVFUXGQWWEDZJNRDYWFMLVFXNEODTSFSZVEQDXZISEUOEGLRSMDPFJLIOCWEQXAXNFXLFQQ BEFEZCRSEOPJNSKPDUWBMXGYBCIIIVVHUPEMVLXAUJZDINPGDOSUFTVGSFMAFTDPPQSJEJCQKPYXBNYW SUSESSOTDJHWISOTNDLJIMXWFPZUXUUZZEDGLWURWJFCIFPDUZUZRWZUPZEZUYFBMZBBTNQNMZWQKZIU LHXFHSCDYWCVITTTSKYQWZQDQPENECEXUTIYNOIKTTZJGXZUDISOJHBEBAEFLFQJAKIJEYWVUBNLBPEW CCEXCZIKKTSZJLNNXUNWXGNCMYKOGMDBIJKXCDOJAWMJOSZTYIQYEVSFWORATVTWGSAZESFPBWVECXBS ZYOJMBPTUOGERLUVWGOBWYKOXOVQJXCZNDPVMUYWQKOVLXLUZUOQZNVQBVQMMFYOXHFTWQDYCDAJZLLH TISAOEQVVBQEXASEFSTHKWTBUUALEFLMVOBJVSASMKHUXOZYYCEWFGCKSDAKFPBXREIVZYAQADQNXZVS BKUYJJTHFVIDXFGYHOXRVRUQRNJTSUCNVSBGDURLCZJCTJMOEVYXISKWJELACXUXIUUOFFYWFTGUQUHO OPTKMKABPQTQVMIKZVMRETPFMVMBFJNXTWKPMVKVSYVIXZBHTGGBTLPFRFUACQUIVLZMXCMYGDPXVAEM UONYLNLXCULGGUVUOIJNAGWEHLRKRDMHFADZBBTLYLJSPLAJWBGSFRCCWMBMJBIKEIPWFVJNBGGAZLHG EQEJWZONQBXUJQELCRIXMXDLXCPTDOKYFXGGVSIHQEETFSTLPWAYDIEBWWBREBOZBJCKALFUDXZVZJEY NJCWVMUZYAIVDKAZUFEHIMMRDEDMITHEZVDLCXDVQPTBWXDAZNYBVEJKMRPDAETONMADDUVKLERDVZHB YHGVNDOVWHYZXWQOQDKEFCCGWCEWBEDBYDIYLXVLDDWHLWRVTBLXHOODHRISEBGNDPPCSJKHDQRZXZZT MSUSVKRVXLPAVZJFEUMJKTWHSQUMLCIYAJYTTIXECLVREYUVGHQGCTOVRQBPRFCEUDSPTMVADVGROHPI JJLBJJQXFGYAXPIOURBMPMDIIWOGVANZRVAKOZBDOLLKHQLAKQMGCFUHAZLKNYIYDQDPUHSDSTSJXJDG NWCIKAQXEYJGXCZVYIPDMUYWVUXJPXDAIZGEPDBHXKLUBWZWFJMKJALNNSDPLKTUQBWRMFJHOUZGBVEB CNKAOCPNQRNYGZIYGOFFYVTWLHQLRMTMVYINGRNFPENIKNVBORMAZEVZVCIJFBHAZCFEVPGYAYRJZIZI NKHJBSJZYXQAVNVZLUZEJOWZNCDHMZIPWSRCPXCBKMTVBOSTOKURRCPZPEGDMBKKNCEJUEOCTWZKUVML RATQWATKLJLVGVZKACXEYNKBIBJTIMCIGIHLVBJBZWNHJJ010WPCKYXKWPPFFFRLFKUCRJNAUEONOBPR  ${\tt BVGKLCQJTRWOCDXYJMMLVUORNSENMDSRFLRAJKOZVARFEZXBHFXKFIDCNVZPMGNZMFAXEPYROBTSQLSH}$ LKMUXOHZDRPZILKMYKJHTKRYBWXCJZYFCBQSBSIEMVDEUCGKSFJMBXRVSHIMEFKWEVGYUOLTXUFQOLNK VXLKCNIJEZNPXDZXMHFBSZIIQCYQDHYEWRUSYRPVINEESDRUGBLBQATSLLALULAMKXOFPFURHFZTDAUR JDAKYCXUIIJFGDRSCMWLEQEKYNDRPVSKKTKMMLMQMXDLTWWWRZJRANFZCAYPWFFAGDLVHHWUYKHKIBZG RMGANJCNHIFMEBOZPHUZHEEGRNKNHPGREZFZHAVYMMUOWXQATHQHEDYDZZZZREZEEYXFLQQBSBGITRGY FXKLYMINQIZILKRYNASCSWQXKZUYMLULWZWAHGWYBEAHNFNYVDKNWQMAKKPXPMZWQZLCRIENNYRBUBMG MMISSEXPYASWNVQWGHKWWKJIHNPYYFWHCDDGJEXUIAHLWTLYNLOGFPVUWPGWPZYFRTLSARXWDMHEETGL NMJKMVPUZLJKVHRUIKJQGFHJFBIQUOGNWPLOXYAUFDURJGJSYONYSRLZFZMKVMJQDWZSKFYUSGZSZNII XHHZLCBIEODQGONNNUGSCBAQXXARFIELMJHDXJZYGJXWKKVEERCSFOIXFJJAUCXWUEBFGTEPEKAXQQSG TNFLFOSLRULLUAFVWXEAONRSMCWKAYNJRKGWSRTAVYEEBHYKZLWHEXNLQQYBUNYWEVNJDLQVUELNJHSA FPQSGXMFEPKHTVDQIWFDQMKIJHHYOEZIWXXPDUHGCSGSWLTMYQLNJUQKTYTWYHDXCWAGIABDYBRPMYBK NZXKWNVRVGILWYDEUQSEHNXBODEWZYTYWDIZJWQEULLPICEUYGCNNVVFLWQVBUFFGIZKJGJUMREDRJWS DJXLQXLNCWNQBRBJQWLUXUZYLJKBNCLCFLKRGCPRVXBSCIIVNZIDZPSSAPHYCYNBXCZEEJAASABMOINP ESVTEVHTTEKJOMZSVELTOXTNEKPFQZJNZCMDDMKRTYCSXUECZJIUVPLOMMASLIDNAZRBCZDSCWHVBNDF IPCOVRSGOFJXXXPCHJOKJVGFWVHTWOUMKRHZLMXTCLGJJYQFKXTRCPJIRWOLQJBFFRAYYZGXKBNFVZBI YELWIXQVTTKJBCWPMCBSTNQRFDGAJBDVDTWOLDTZUHASFGWMFLRFWKDIHTANYWWXKJQPJGENITTQWSIL YYBPSLOHTVBLFWTXDTVYJUHUTERXYGHWDPJQBPTFUMMMQUZQWFUEOPWWFCSNUDXDBLXXYOXCNDPTYJQX GSSSMPTZOEBDARBEOJTVSMZHWYLQWRWKABSXTWIETHXQGQVNJCAVWUFYMDCCYNZZOWTCFCBWAXNGPNFC AZQIHXBCVVVMJQBCGCVZQMMQRFHQZPOYLJYOWPWBYDPKUJOXPIULSVCJXMRKXHMMWKLJNQZNSPDMQJBD MYKBUQJJTDFSLJBREBYHCEQYIKPUUTFCBTBGVZCLYIAGMWONPFXTWWQQMEZCALYPFJAKIWUEBFMNISCX AKDYIPRMXRUPFTFFDDJBLHOACYNJNQMMXCMXQHCSGTWSOAFCAKOQMBJEPLWSEIMMSDIXWYLPXDQHAKHS ZPQNQXWXSLEBHLGUPALPODJSXYDIWTFMBTBCWSXEEZWRXQFPJJIPVKFPQQJXWRSXVNPIOPLSZWFDNJJJ HKJFEAPDOVVRILPZVHMUFDNSOVUQRSGHCOZPBHJMRRNMGOIPUVPQMRKCMZCLIVNEFOLPKSNFYNWZFOPI BHYHWBANKQEAZOFLBOAFKSYHOBNWTLKJOFHKJYCFTDFGYYFOCKPAVNDNKNLVEGTMNWHTMRJJIZOMADIN SLJUGKDLWBOOEASAAUGVKGPCZLADVTGDJNSZQZIVNMICGVAKXFFCSBKDVPONBZRXBLSZRNXSQPEOTABZ VRHZZYVZBMPMGVUNORILXEBNIDUTSWFWVEFMIZKUKHUPAYLULAVZUXLLBTHSXWKDLKPHOSKXYCZCAHXN YQCQMRNKOKWUDIRFGLEEGOJTPBQAMKXWNWSJFQZHALYIEFONOGCETSYBPOBNDDAEWYWEZSPVMCCAXUMA KKPFETYLOZUYELNNFXCGTGQQHQKLTNAJJKTIMIXARMHDNHASDUNYVOLVHRWYDPZASKREXYWTZVDYXZUC VBUZYONGCMSHMPIDCHIGXYABQGZHFUXHKNEQCMKUUXGHZDOYRZZHUVPJTNKOFOPLBXZMQBWVRVLJDDVB PJFRNFMAJTMFQSUTIHSFZFNZYXRFKBOPXXWWBKOFYHZQCUABAXUXRYWNGZVCTYXKARIEXYESMVSDLWDU GEWMMFNASPHGQAAVGHWQSMZQYBHGPRSSAOXIIGNOUGHJLLTWKTAZOKZTWGVBDQVGTDCFFYRMRLUDGRPT SXOTPIAZWABYAGXVNYCMTGVYPWLGAHVGOGJIVMNZZCAKOSPNIVPANQEQWRSDISWQMQNEVACIETROUMKL IIFPMFUZFCYCHMEUUEPLYCVGDWHEXLGRSMDUIECDMKPJJMIZVUIAWJBERAHDFDAAJKNZKFRYTQKLZWIZ XLLMOHEGBGHWXMXHRQDYDUBIZJDEQPDJBFXXKPVXDQLBJAIJECYYTZJXBHQMHGHTCSRMVORBOBZGLVDI AVVKEEJBHKTWLGHVPOQKCUWXAIMLSDVTALXTKFZSKRQNBAPHOHPXWUGVBXBDBGFKPPCGYPPYQLLUPBWN VBYZYXIFMRRNYCZTGGFKTTZRNSQOWXPMQQPRMEGXLTTUKPIZWUDYTTKWMVGRLEXXNKRZNEGOFBRIHBOJ 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UJDRFYIDRMFGEGLHZPKQRKAUONCPENPPGLFXHUFCEVTFQSFZBLNYUZTOZDGUPDFDXEQXHBHEJJPYGOAX RNLRRZWKLQFHYHPSNZXNCWKHSYHIHEUKYYCNRXJQOSOHIJWYNNSXTDGAHJIXFSVKFWVNLMPHSRNFMFRA DVGYLRXDYGHVIDVTFMXXHUKJBLHVOZGWUYCCTIGQTGZXVGBNIFBEUAAGPJGZMWNYGXRTQWQCPWIPTLWI ULAEZSHMWMVWDOVNOPQKFLXIJVHQAUSNCGVRIPPPTAIDVDWQAAGLECBSUQNZWCYHVIWNJGJBPEVFIINT EMYYBWWUDYLIHKGFKMDELEBAHNVDDCFOKJOPFGLWAOYEZXKGFNEKEUOQEGEEPYZUJRSOCHEEOALRCFMC AFJHRZEIUXKHMXNBKBYBPVBUOYMKZPZMYKAHOGCJIJDONHYBMFBCKBCRGTNPOIMYRUXDAQNJHQDMWZVE MJECSMDJGRLNUNYSEHYNUHTVHLKLBCQDGTBXGHSZAOJTEXCPCPKRKCTZMTFUWGQDOPPWBLLXOLKBMTWG KKBNSZHEHCDYQZXLNFNHXJOSZQWLCTKIOEESBLADLVEPXDBXBLCPEAQXLKOMXEVARUXLXLTAFBHHKXPI NVQBLYDMQJCULVXLNTQVGGTRLCDPTARGOVVGOCZSAYWDIGOROQRNHOJNTOODDUDNSICWNEKXGATGTZCM DONQFYYPMKCXBALEKBVHNNIZSXIASMQIMFSNGBYPUCHXOLOOCERVTHNFRPOXFJIBOEEWBLBFEEPTVULO HTCODTWOFGFZVIRQETBORHRDKTCVOJNZDQEVZLDRFQFLZPUTJBWEGAGPCUKYJHZNJCJSMEAFZYUOUIXL DBLWOIRQNMAGPSUGUFNJYZKMDXCVQFXCIIJKOCIQDAGMUQIUIQNGUBTXCCHTVFWPQNEQDHYEYTKTHQDM FKDEZRCMLLJZTQCRDPANTKWTFAINRHCZQBDUGTJPJJCKECODBGXDHQZVUFNABEKSXWFTVDILCTDJWKWI FZMLORAULMAOUACUOECMWPYZHJKNAWDQDQFBMFBXLKTYRBZJPATXNGUNCAHYCACNSDKPRJONAMSNOKXO REDNBQZQRSBRUDCGAQELIMSRFWLGNYXOFSPVYLKEIMZSMUAHHPKLKJXGIIVRZWKJPRJNUHWRDNUMIWVO IAHFGNBYJWSXXVLZZAHPEILZVQCNWPOTUWQSTOIXNAGAQGYGLKTTHNWMKPXBTMLUJQOECTZTYCACCNKN BIGPLXMNKJVDGGFAWCHHRUNBUMQZKEVFTZRDTWGPKHCITVYFNOFAAOVGXEEWAZLWFPSRCJNNWPWEYNSD CNYACBWFQXPNZFRDADBFKQXPPBCKZCIMTWMUMQKYBDWOTSEYMCIMYOTSOSCHOPNTORNESKGHANQKUTDH GSEOMSJICKTNUDLOLRJRCCFUTDLMOEEHNGAHMGIHBHGREFLVXRTDAOPFJNAIGEPTTHDOZZTJUOVAWGNE KTEUORQHERZXOWXPEKLGNWTRVQHBXDORSTWIVAAGTBQIICTZHPAQGJUICNVKGQFPEMBLAGUDSGQVPUMT XHPIQFNHXQD0IEGSIXYSVWAENFCSLFPTNUWVBRBMLBTTFLGTGBGMJTGWSBFDWFQEJJTYVEI0ISDNWELC JVTEWZUHRLRJFAMGADALKVSPNMPGQFQDPORTVASXUDWPVCUSKLPHDTEIBQFYVPPFTZYSVXXPJJRVHAMV SHFQLZKYTPOITARUVSBGFPYGABGSGDUNSEZQMDLXOYDDOIRVHIPWSPWCBKVAWUDPCUXRRITZFQXVJCNZ QOUFLUYNMBREEJHFMQMQEVTPJKFGFKMJGLSEFQRHZNQLVCSTJIVVPKRCAJJLUZUFPXGBILUDVMQLRHFC RTKEBHXKTGRUXYCZYIQJRXYTVJXYIGCYTWSCUGJYEQJVDZCZOZDPEPHVBGKMYGRXQMVDNCEWMWCMKXWR FMSEVBJYWHZPOHJRDQSLTOEEYDMQZSOZHJNDMUFICDARQADXPQAGJJYHAHGIZAXKIDBDULIKPOBHQUKG JYQHNXRUKTIFHXYXDHVNSKNQASLGLKYPUZVREXNQMYEDEZHCWKQWTVJQDJYAWPFTVZJCVAWBQXAJVTUC DEEQPYAWVMCSZUHPEENDWKKIOGTQWIRMVVUEWVFMJSZYCDTHONODHQPQNQJORGTGUTQJAZUFLLYIVVVB KNRBBESGKKSGYKUDGUEAMFWZDOSODYNGWYEVAEINPSIMXRGAVJDAJOUDJIHUPJSKERRQNZBFZWKZKGHY AXOGGRPQGEAVHYIZTVHABPXSMBAJPRMCBWHYATZOFCWMGNNGKICGABIEMEFFFJPRWHDHDOTNDKHFEQNY FAXZZSHGIZQWHQTCRBIEMIMBCMOWRYRJEXUCKMWLYOKPCRXXALZCBUPOWBKCFCZLMMPTQHYJAESVPDNB BTQAPWHPXKEMVRRIOICPOUSOBGLKVRFAVJHCFXBKZCHAVLXLZUWTXJVQSRJOURCYGFWKXENASCTKEJIN OHUSWWPGGUOAKDZQOOEFPJFAGCDMGWIDMQERYJXPOMEDUHFNLGSXJZDQGXIFGCBZDTCCLIJFVBYMNHYT CIAPKUSGSATKYAZPYFIDVXCJDBYCWJQNVMRKAAKPYBPVCQBMDEUWABOTVCCUJJMPWQYLXPMAGIXXJUXH RAHZWFDRWQHKPIINLOXGODOEQGAHWJTWORHYKRAGULUVVXLURVPZFBEHORQVJXBBNBWDFKCTIDHRMZVY SFKUCYHMPKZAUPURUEEMUZHYXKXMTFARLC

44 0.24645256996154785 0.72286057472229 0.4840826988220215 True 2560 1312 2420 65 0.40004944801330566 1.5957915782928467 0.6678259372711182 True 4032 1952 3309 87 0.5849287509918213 2.1938328742980957 1.0342812538146973 True 4896 2592 4627 ZZXSAIXKZACBNYNBUNRIJEDBWBPVLDVLNDCEHHHBBUEIXKXFRLWKCUJFTGXHTJWCOQRFRACWYWLEWDU AGYLLLJLFIUAOTCEZUMEJVDOAYAAMQZJJOXVTNBOTUVUCXSTWFYMIJHGOLXFLSSVZBSFBELPFURYXOJZ DGHBXNMQYBHAAKDZNOHPBOFRZVENDHTRABLWFNCQBAMRGVHFXMZYAGHDMEMCYZMHQGDLUVQKVXRXQSXQ PGDYPEIYJZWLLQFGGCHKYPJBDYZDABPSDMQGGLDHUUDBCOIFREEBJKJIYQTYJOWXDUZSEQLJTWIOPWAX AFREEXHAYJUMWSYARRDYBUWRPDQIEJZHEMJYEJHAIVTDOOSDWZPNJQXFTPTMDOXMGKXBGKENYDABECZR LNETFJCAOTHXDNJDAFBFKZKFAWQCJPZZIUHEYYJEYFBLXIWPMQGGUWDZONIULHBLIWIXCJKVBCWOXEGB UZJWPYAQXJLIJRLYPFZJZGXXYZKTXRRKHYOOAGACGJECSYWMFAVLALOQVKJYAEPZDPKVYIGOKVWYAIGX GYHJOJFYLLZSMCPGCQJWBEVFXNFQQWFXHMNOGIUFCPAITAWYYNWKMBUBYTLWWDZWGQYDBBKIOBZPEMUN HUUKTUOEAILEDDURJNRVTUOMYMFZTBXABEQVPWXADAVRDQJCJOKVOUHQSXAHLHTDYEFOAAMBUFMODAYT

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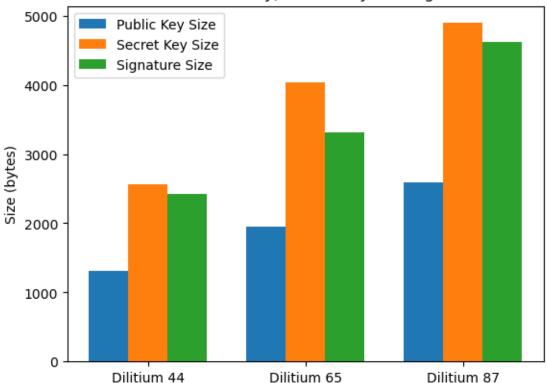
65 0.4000530242919922 1.0009934902191162 0.7651100158691406 True 4032 1952 3309 87 0.5886468887329102 2.2697908878326416 0.944166898727417 True 4896 2592 4627 PDSCGAKDLCQYZNLHBCDNXHLNCYLVCUJRFRYBOUBZBIPJDQIRKNPRVFZGVXXCXTZGXPSROQCWASARXZYL IVFLEBABZXHPUXEPMCBKRQEEYBRCAMDFUGSPCBHGGQJBCCDQVRVGUKXHXRGOVJBXLJHVUBWABNQCHBYV ZHBNNOMZAUILZJCZWNTTBDSOUSMBCXATPYIGTROSUUCCRMFTBLLNIBOTSFGZWWZVKBAQTGCPIEXNJHIZ MXKUZTBTNZPPWLLRPCIEPTHXCJVUQGNSIHFZBEWCTRQVWBBYNJFBAVXRKQGIIOIXQTHBPGQOCEANNOEQ ROKKXVNDBBSIAKDPMIYACXMVYGWPPNKULWLSYXCRSZUASLTCJIMBZVDNNBSRAYKEATFGHQWXWFNSGGXL LPZJQVKHPJDPSIZETPXTPLQZJCAFINJAYWBFEZHMSBQBHSFZZMKTLQFJBCYBJVISNVLKPOZURQFZQHHW LSSMBSNOCGOYJHOWPAWFGUDYGCCMUSTHTHNVBYZLZXHTLHGDWMBMYEPHXQXVMCURCTGCQFMTYSEVAYOD PISAZZEIJQEFDGUNFURLQXUDVNPGBNDLSQTTVUPEORKMVZPBYJSPQOLBYEVBFYAJSVAZZWBXZUSWGBEV EFVAZFROBYCXUQXNYGKXVOAIMRATMXSHCWJDJFBMNBEYLBFEQHPKFOFVCGLMVIODZTIJCDPQAXBBPRJV IQHRRWTLNCCTVSASRRUNUQLAEXKJOEJDZEYWSDRCQYFZCSMYKMFJFSZQNCNRWMGPTLDLOEXFSSWOCFVZ SMWLAUZLMDSAYTXCDLIUBSNFBLYSUZVRNPLUZEKRQFTHJFXUDDJASJXLFRWGVEQLBCFLIVFPFQBADQJE XLOAEOONLMDSGYVUJWIQCKSEYQXQRKWGHVSSJMJXOAJKHXCOCDOVWBXTQAOBRVOKVPAWGFEODGHQIZPX QIONVWNLWXKTJVIDPZYEDZQXFXRPXBIJFUKSOSCYJVDQSKZWEQDBKQRBCYGFUKHATMQVEDSCCNXUKOMN SLUDTBJMNWMBGTGAJDLPHLHRPAFJYPPPBLSWKXBLJVJEHKWPZQGRQAUVBIJTUPORQIQWCHPOEUASOUBW KQGQJBTGKGWXCVODDDAUJCAVNPTVQKXDJIJJANSESSDXRBXIALWLOIRSAWNFOUEPPBIDYKOVXCBQTAFW MSCRWJWCPWVQQCTHBAKVILXLLQZSAWTREXIQHRBGWUMJPAHZWQKKZXNUCREDMSEZZDCTGGLWVKYVQSNK VREVTBDKTIQTFZXHKNGIKWFBPDDBVWGFPTHKSAZIWDOBQITADNJCFSREOBLVHLSXHDIHSDNWGBWYBVEB SLJZLVWGEGXAZYOJPXKNXCLSCUORFBXIAJJQQKNKOVBFLJKTMXHBEELHGVTMKSIKMOUTRWOQVNTTRQGO SHSNVHAHNWOWVYQWMUUSJXLYUEKDOCQJCPKMPOJOYSMFJVOYBLSXLHJQNVDVMNGGJQZQWVYQFGYQIHFW ZIDAGHGVCIAADNXHUVUDDUFDSSLJXQRMXVJWWDTPPAWASKPBXDMPMFZMLPZCHUOKWTQDNBFIIFPPOMAP ROWXNZTLKSMFOLMHOQDOTDPVAPZCQNXXTSQZJPHDNRUWRZHQNQDUQNTQTNDLJCHRQKXHLQUZUCLTEYSH JSRYUOJEFHIUERCQLAMSOYIKAWLHXOTOYCSHTJUQJEXWASPLPYWZCEOLJZDGEJLFBPPGHEYLAQCAXEPK YFWYYVIORRHJKHIHFASOMINEGFGKVWCGKYCEWBADHCPKAUQENRVUBEUUFLFXZUYOYEXSTABSAXGVYHBD QJNKMRLFTATCIVKTXORGLPHVILYKGDKIZGRLNEVTDGESGFKGDMSQHOCLAJMZONFVQPEKVCFAUUELBVSO YISQKXKNMORNBZMOMBWKRKGMEGWEITGPHMIEECQFXVQYZIOGZYISAPAIQNLXBDVIAEUGSVILAWIZUSEO IQQAJPLZMDPJFWKCGKIZLXTVDZLOCNXAGUDPWIHGAGTTIZOPXEEFUPRQFCPQNECNNTYSWYBBHREQSCVQ SOIPFGOWKPVYAJOXDJLTPFXJWGWSHTPAVMDACITGIMQYTFBYTHKHZYXHVDHWPEGZYBPPFJGNBLYQUNUB VGZGQNRXPBLRDHPLWKMXSLCHSNZRWDSZKFUNTGDHBNRDCNZDMGUEPTFWVSWZOBJLWWATJBFRVOHDCEZI SFSJRFABSJNYVQSUJMHPHWFLDKTUFFTCLFYYVEBOYVRMSCMCNOQRKASPQVWGMAXAYWTBSZXQWDHDTHOB XFRXTOEJBBDSJSXAMMNKULXMXWMDRGVRTFRJORAERKZROPYIMETTGGBIBLZYCXUZOWLKNLRDVCHVJOJD FIOEPWYGKIYNKDUEQWXLJONCYFYKAJZCOTLXPFYKQKSQJYEMGHUIYUWBVXCJKHNZJBHCEDZNCCPDKZLA HOHRXLWEDFGUVZKEDVUGDVPUDPQJBXHSZUFJSHAZZJCEHQSKKXPVGMNHXOTWQEMLYNSUXXPDRLTNWIQM ADWUPGNJYUJODMCHRSZLZGXCECCGWJDESGBYAICAXOXPUBQQULXZJOHVSWTACYJMRZQJUFWEMDDDQRYN DTOLUUAJPRQPLNAROXPKDWYYMSNSMMNERQDODORDBYBKCLBYZGYWJKHEUZLNFDBBPZPFQTOQRASULFKY BSQEQHESUYVLAYIOTLTOJFKNAEBXQJTZOJDONTMFMIXZJSNKWWXIZTIIMZABWSVZHGOWTQMDVCFJGVPJ QSMLTAWMRNQGDKRFHVOHWHXVTXMXHASNGTCJKGBIGZQIJXCIVEKZCTESYDLQVYDPRTKXRFPRVSJGUNHG WWLEAIUXFVWYHZMKUXVTRFCUUZABLDBTLVMMQHKCLVJSYOTCDYRIVJUSWINJUFSLRYDSYYCCPAPZBZBH XBVQREINKFAAGLENGAMIRMOGZWUDAYZBQDDYTFPUDUBQZNANZBGQRTLNKGHGOPHBKCNSZFNLUPMHMRUQ MPUBMQVJYEVJYVMRBHENXVATEICZMOCXMQZIPDYPNTGCKWNTSREELBGVYDYAMCAGCCFJDKZYEHDUTDLJ FMXYAFXNQIJXTOERNTOVZWXQMKOMQNWSJPYIRBJVYPHIRTMZMZYSQAVVBPNPCSTOCUCGNXEFZBEOKHRX UGOGKGYAJXBANJOVNJTOAAAGFFHSRMMERATSQBKMIBQFXYCLDBYDQOIKAACIXNUIBVOJYTTQSXTWYTTD YPWDWSRQDDITOCFONJXVDQKFGNHTIKJADLWMZHYGVHBDASHXWXNVFOMJDJDQXKOOYLXWVAJWLPLZGRMF QMXGCMHSNXTKZDISRBRZRJCGZQPSRENQFFGKODPKCVHCYCEVCNHUVGVGIEYCFNNOQAZOLUONTDQKJHIY RBBAPGKKADUDKNGKJIIIEOELZXZVDWPXHSTJLMOAZZSCFSLXRYCFUJOOJMGDXOZGXZAQZSIEFUBIEZWX MZULRHTKMEXEVWEXLCRZFOKABMKBBYULSYOLDMRQRZXQZPASQIZJEEZFNBLQGKREABPXJRKQHALXKHPY VEJTQYBGCILXOORRBUMOTOHZLDDOZTYAIICVBXJSRAJZEHBHTWKTWNFUWWSQUHZDFYICMBVRYUZNXEAY COOTFCFKMYKEGSYDXYEFZUKKQGZWJTQRMQWPUGRGFGMEMIRYMBGSVZRTEGKNSHBIUCJFICKPPGMMLACT BDCYAHFCEFSAULZSCMIZLNWXFBGOXQBXHOUTCFWRUOAANWBGRLAHENBFMHZRILDFELMMONBMZUYMQOIB QKTMCKHWGDHQCJKGTOJFFYFXLPCLBEBQBWEIDWGGRZSAIMIEFGCFCQRKXQDUKUNTXIKCFRSCBBWCDCTZ  $\tt CRWUAAPYUKXBMOCVCQJTGIPQXBPWAYZCFQNTTVDELAHHNEPRTUBFSSIDVWBZRDDHFJTMLPPEZYMFDYYT$ RUGXEAYORGPSNOIJRKNQWMSNBOXKMGKSZYDERFWWJYBMTZLIOQDCNEMLLKWIWVHONRMWUGTPANXAMLCN ZYNVJXHOYNRTQTPPEUQSTUJIARQUPPZUVYKUDEJTFPMZUHEMNXTZLARFQKYLBBGGRLGGBEDALQJHPQBT XIXJWAIEPVTZIKICAWHDNRJPOWFYDQDPIXABYIALTKFWCSSAWIRIBSNPJWMCAVBMWERIBDDLNYTMJJBD XNDEIVFZKQJBYFNXCXZIOEXQJNNFGNAOWGOMPUBASLTYBRZUEBMDOIEIEKWTBJECKRZCFQBUIEMJZYDZ YNBOWPCQHGMQLSWOKJTOCSEMRQKSYLTPMNUQBSAQPAQTMNXAFJRKWNDAOOXVSSKGIFXSHGPUXRVTHELU UGGJLDIPTZXXKSWFMOMEGEERBQMKGECFHSTSTOAWCRABJJMXPEYDWPNZREHFDFXEAHYQQESNBNNMLVLB QCMTBUDSYAUKULMVIQHCGBATHJWGDEUZDCXKVLUIRBOYDAXCHXCWQZNWNELCBAMQDXJJEEBYKEAZBYRY PRNGDFDHEEDCXIBMSVDQMJWSWHMMHMLXZGRTGYXCUSCISSILREBGJVVBDYIOLPEGJKNTPUFQPSDUKNFU JUEXYABUFRDCXBRCOGVZTHFSQQEXYNLUNRMUUIQKWDWNQUCVGVQPPTFFBVKDCBANBNAYTHEWQAFBYCHX MCGNLHSVMTMSSKJKPAPWSRLKFLPHPOESFQXTSUIBOBESMRWQBJMGXJMLAKHNNYCVCKQAZZRUWSDFMRCH NIOERRHCKJRIHREZWQATZFTDXNAAKCZKPABSMQFAZFLLMRLSYXUQHXWXRRDQHWYBBXVRSEGTFJITTQOA VCLCFUPBVLVJMWKPIMAOBCTGYZAUPWHBGHCTHFHNNTAQXDJPEJPMUFDIVFRADJQROZZCDDGAZNWJMRVY YDNTHTVHUSBHPQFOUDNSJWPIHBVQDLFPNCMZDABQJNHTZTMWPRNBAPJUVDUEGLOQWRBEENNIYDDETSTW ZGJYREVTYYHQLZGZMFHVTWLLNDATDKLTKTIKSHGWPAMOWHGUJBPSLOUPACSVAJNFUWFMWHJPNFSEPDYF PAAEMUSJIOJHXGQOLGMYRRAHKOIGYWLLQZPNDSOSBWPXMOTHSJSFHBZRPJOURCIPVEEGBOVUYKRGCUWZ VZZTPXZSQYUOFAZRWFCFJKPENNHABRBPKHHZCQTYWIACPWOOJOZMJZFTBOMOMEJYDLPETLUAYSUJONHE FYEZANMQLOEIKMYCCNHSGLXKWHGWKZFENQRYNLOEOJBIAGTVCYDVHOWKTKWAPRRVIKJFIFTEMFGXNAJQ XQPBLCSHPQFFRKLJGGTDAUNAZYVOUGNZOBGBSZMEMSGRXZBEHZJDJDMWYPQDRKQMUBLMLQLQYWQNJTPC NHWYSDSXPKGUXJHTHRHXFYYOHCYLPNMUOXGRUERBDTGVDBIJGQUZDRGPLGPJKCCKKEYRDQEAGDNJROXG WTZAHJKEYUGMMIUKFTDJGADXLGHFMQPBLSMSEXJTPEOSNKWLCKAEILTLYFHGQFOLHTSIDFFSPRNQIECU HQUKMHFXYGXNFSONYEDJJCAMFZEYTBAMEHSURFETXXJCFVKVAIRGAOOHMDTYOVHXOASUZHRRNSIUHXOJ HDYEITHBZFRIWAGHLMGTJQLNZKSUHXXDNMTWHHWBZWVRPSQGMEIMYTURQWEVTDIZWJTHLKGGDSEVEWXQ CLZJGGDMIIGBZBRJVXQYQDCCOPJFLDQVNGCAZVWNMLLXNIFWCVJIVGJULNKMEGWVIHBEYEBEONJZJCEV HFLCHYROFWSPPKJFPNNOXNRRZUGEGGYXAMVRLWMOLUHYRFVMHAJJUYGTODFBSJYUNXRVYPLMXQCDZAZT IGZGZRMGKZUSULGUKOWMWFPZZGJTGAKGIXKVJPPUDNNFYHGXQRUJFBRCLYUZBNTBIRCYLGVFIWDGBMBG GFFVMBFOHEEHVYGZWDLLGNCFSLZURCIYWXJNZIISSYTBRSKBWBWJJHQDIXHFLNPOGDNLGBOFFAMGWPHA QGMXGSFUECQXPDPQBYCWLNDSCDWFNGRFLXUQHTFUXAGJHSNCVVRMLZJTJHIORMTBQVISLJWWLKSTESYE XLMXWGEPXTVILGMYNVKZBMRVOPGPONXQOLUPYMVIRKFZGQHTQPVWWZODNUETVFGBJIFJEQMHBIGAGUFB LPAPMLJBCASTDGFQHSOYYXABPVPZIHDPGGEDSHKEHGZCLTTLIDRRXAFOQHIZCKYAADFNRVHLOYHSPAUU GJMVVCYMJSXCUJQZZXXKEIAGJHNKSXUJCELLPDNBLKSLHPMQVZITDLOKQFCWJVXOCGKQPHXSCTLXOQXM EONFGOJVNNOXFMHMJUKBHTARWJEVJIJWCHQXQSNPXTHBODPLJPBIEVRMQCPSODOHFQLCVFAPEKKNZFJW ZVAUZGAVKVOSYYSXEQHISVGJHKXPMOAWTFIZWICAGEZCTEROYPFGCJWOCHTNCIHIWKOTDJGKAMRY1OFQ PZWPPNUKNSGBMWVPWPFENMHPOFNILAYFOIMOCZHOEIGUJZFMWUUFYZNBBFDTATRDRJKXMITRSAZKAILJ JQPOYVHYEEHFFHFIUVBPRJYFXREPMULSGEPMSJEEMRZCFVJHF0F0HB0BGZEKPQDI0VXNSFMTSQRZGZWJ CKRTRHYWHAOKJJTNVTNZFIAOOZOZCITFDBLVCBKLDDKSFMJJOSWTOREJXQEYDHLPDLPGZZXPAKZNKWNO UYNFCDJSGACAKAVBYAVODUFUJCGVTQQYLRGUSKATEOMQWOQJGJLTNWPDSRYTQGHVAKSOMEBYMHGLSFSK VRYIZWIHTGCGUQYEPXVBTIHOWNTGDEUMCRJNHYFDTYQZFRJZVDJESYCJNFZGXOZQNTABITKLKOYYOANR TJOFZEWZGRGPSXFQZQRBYUCAYEDHTCIKRLNKBVLZWYGPZYBJMHMXFJHIBJYOZFIAPINTPGHSPHQNWBOG OQSLJJIDCTUFTNKEAWHGBFVYSYJDOMLZSPOLBABCQFVMZAYRJLEKGHTRNZPKJFHZQVTEXRNNAUEFAPAY MXOCZDAGMMAFAWNVIVNSOKGIJAVHHHDFAOILUPEUONXUEMSEUCYGNVYVWMNKQCCRSJIVOJWBDGUOEGVA RWSIEJWXLDTNQKRHZHYLMSIOFQGQOGTPRZLTXUDWPGGNQMYQJTENOAQLCRTXSTQMVCPRBSCPQZGWBADW ZOYYOGXFZWAGWJOPEOEZTRQISSQSOJRNBWCLAIBTWMXVMLTMYOHQOOHEFBUANTEWGWFPCQNELZHFQMOM NAQMGZYCIIMMERTLOJFXEFUVHEWSEVGUQQJOOHJDWMWEQOSDNXQBHOZNSNBHVJJDMMEDARWCSPDOPYXF LGTMYGGKZXZMJYZRGWLLDNJRLTYXYJYCTGKNUVBTIOUKUXDSTCDCZYZSQSXATIFBXPHEXKRRBQFCEZKO AKVBRSUAMDJGNJCJXJLRAYKJSMHKBRCUQMNHTQRTTGPUVWVKEJJEEGPHWLZNMKPDSPLRCSKJKSGEBIPA XQYLTUYXEPATLOZYACWWCJAKFUMHVLIZVZUMRUPZHNILNROMEOERVRZHJSBKSBVSJEAXZUOUBSWRDBIJ YVYVTLSQYEGHCPWPHXSMRBEPDHHOOFCLLXBPQCTOZFCDWEETQMBNJUYWSPURRTQKJJNLFNXZENFHIYCL CGGPFJADJBAGZEKPXLJAPGYNWLHXNXIQXIFFHDGWBEZPZGHJYWZPUXWTRHLTIBKWIGGLFRRMHYPLWCKJ CKWEIXNXLQHFZQWQTRLTPTRNJDHLXIUXMLMCXEDWNBEDVYBZHCULJQBCYSRLHUQPZIDIKKOAPHWPVHRY QKTNLMGRKCZUXNCQIIODSXVIYKNIBKEJCTCYIZBVANTMATFGIKALRVTZSDQQZMYOBBSTQDABJLARWHWZ BLPRCCWEWDEHIEPTGHXKOGHRZWBXCOLTCPQHYWJARQQBYYEJDCAXGAWPTTFTVSFHZIVKUZMYPJZERWOV LTAVWFDEUUIXSCLFDIFPJLVTMPLUBTGFQZGKUJYZBFPFLPIBXNYLYWTBBZGAPEQZMOYVYVDRTACRBHEH DNOSPKDUTTHIXCUIWNZCDLQGMARTEPVXDTRXFHAJCPHMOIPXQMXXGMZGRBYFXAUSIOKTLPIYIKNQQFNJ PGTYWSYSNXMLUAIPIHONUWMHGLBDTWPKJJXADWFNTWEFUORMILEKFWRZMTPLKGFGQFEHKRQOULZJULNX OVQFMQWZWEFPBACAEWZQXDKWZUMFPLYJRFHAXTLVJNMBABCJVGXUNYSMVAZYAPRAQBOPZYKAOVUGBVES RFIYWGAJAYGYKNYPBIXFLWUNEWNFEIEOCBWFNUDMLQIVBOBUBZHBOHZQJOEZCNGBJJQXAZSMMCLXRPLK EFRLQFXZSCMTJYHZNKABRSBDIETYXNHZKAGMULMTIFBWIYKHBDUQVLIPITEEXCGRMIAEAJUUCTZAAEEK FMMINCQFRCISPFQFTENLKWQWGKHGCRZYVFEUHEISMHPZYZDIKIEEJMQRIOSWQJGRPVFPAAEKYEUOLZKJ UMFZMSYJFHWCRFZFKTRFJMQPXTJYMJAJLBSIZCYAZFQWXSSUFVOMDRLRDPHWLTUFENPJWZWIHPXDVZNU OKWDANGDPGKZPYCZPCLSIAMQAVDEXTPXAYQCKUOOGCUPKDZAGFKJODDGPRZTYBASXRDDALPFHNGDQESA QSZJCWBPIRVRADHKBYVKSFTMWNWQKAWQZLJXXJSLSZSPJDTRZQFWDPCEINRFMBOXYTUEZFBMUQTYAUZF WWJCBSLRAWFDPRKHZHNYGFASSYEZJDQENDICYRTRXAIEQWPKLVJYCUVZUTYIRTLIJLODWENPJPJWNIQD VRALCTQJNUUIENSAIBFOKCIPNTVVPOGXTTHYOWNACDFULXDWOAMMOPJWMYSLJRHRXEYHMVXHZUEUBQSN UJYCPNBMOQAARNBSGFODYCOLLTBEQHBCJDQYSQISNWEXFGVDWBSGNDZBAEF0FHVPWYTCSECCEKBNUSMK XOBBMYVXRZSJAXBODBUCWDLQYFGRFDTMVHYKMHYPQOVCRCFDRWQPVGXDSRGUPESVYBADVFHKFCAKDQPY NMKSMQOBHYJZXQGGZBOAXOZVLEOQCKIHCQXUSVKYPSIOIZWYDFKRKWZCBCARBXPSAFZREGSFUVFQOJOT LYAWWNUUSHGRLXRDHWHVBORAHCPYNBTOVVNQZBOOKXJDCDXJCEZGYMDNGJBQOTTLQRGLPBXILXMSZBAN TYZBRTVCNDBIRVFFSVSEWYSOXSQNVBYMTNUQCQYKJYRADBZZAPTJCARYWTEFSBSDXFKFBWVTWOSMAGJZ KLROWAKFACSZBZAEMWAFFNXCFOZEEXSSUALPZDIIUTLDEXKDEYCFDLZVORGEPSCORSXTDIDAMSZMKWIF RFFCFXAFFPQYHORIBBJCNZVYVWAGZITIBUZMOUDVIYKJWFFDCDQZENZYSSPTOGGSJNSZESFOENCLORPI VFYCHYUYABAGISDLZHKUABEZJKKCECFRQKDMEUPSZXIMMLPYRLWNADXEPLQDSXYDOIZGAKDNUTZKIPDK RGXGKAQOJLUFVNAAOFZISHLNMVLRDMCTUHJWWKLDIBWVTFZNJUAUBGCVYDKAKNGLFSIAVLRAIZBMUNLJ MPAXSJCPRNLEDEDKRZBPOWJQMLRCILWEUQGJWVESLZPJMYLFUDYPHLXCDAHJTGEQXVGDRWYXCQEMFBXI CZQKGSJUDHWYAWLRBNALYPHXVDKAMFCUQWDIEMONBIZYKYNYIXZVNRERRYZGKASAIXILPWVMYITRZQ 44 0.26203465461730957 1.186126470565796 0.49564266204833984 True 2560 1312 2420 65 0.41565752029418945 2.7970757484436035 0.6748759746551514 True 4032 1952 3309 87 0.5848491191864014 3.0973775386810303 0.9338617324829102 True 4896 2592 4627

#### Análise aos resultados

#### Tamanhos da chave Pública, Privada e Assinatura

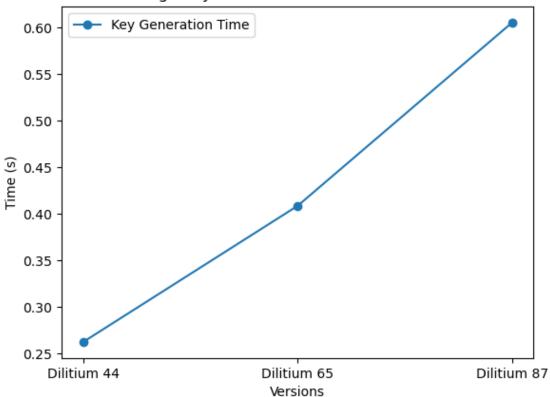
```
[]: labels = ['Dilitium 44', 'Dilitium 65', 'Dilitium 87']
     pk_lens = [dil_dsa44_pk_len, dil_dsa65_pk_len, dil_dsa87_pk_len]
     sk_lens = [dil_dsa44 sk_len, dil_dsa65_sk_len, dil_dsa87_sk_len]
     sign_lens = [dil_dsa44_sign_len, dil_dsa65_sign_len, dil_dsa87_sign_len]
     x = np.arange(len(labels))
     width = 0.25
     fig, ax = plt.subplots()
     rects1 = ax.bar(x - width, pk_lens, width, label='Public Key Size')
     rects2 = ax.bar(x, sk_lens, width, label='Secret Key Size')
     rects3 = ax.bar(x + width, sign_lens, width, label='Signature Size')
     ax.set ylabel('Size (bytes)')
     ax.set_title('Sizes of Public Key, Secret Key and Signature')
     ax.set_xticks(x)
     ax.set_xticklabels(labels)
     ax.legend()
     plt.show()
```





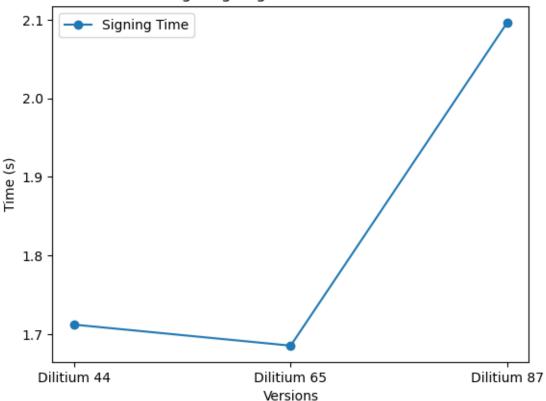
## Tempo médio de geração de chaves

# Average Key Generation Time for Each Version



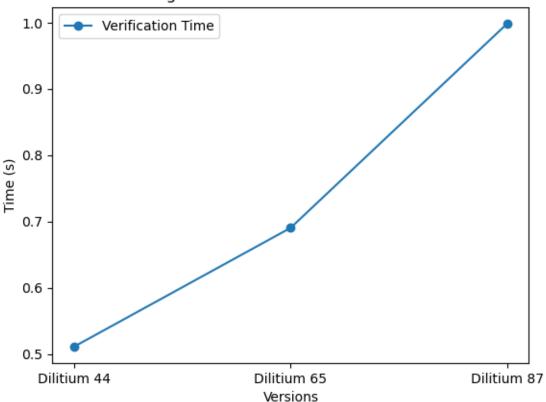
## Tempo médio de assinatura de mensagens





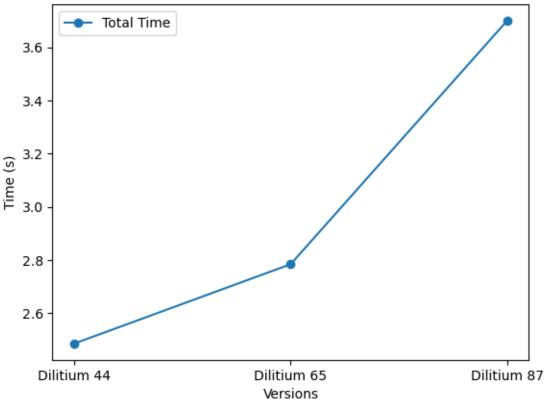
## Tempo médio de verificação de assinaturas

## Average Verification Time for Each Version



#### Tempo médio total

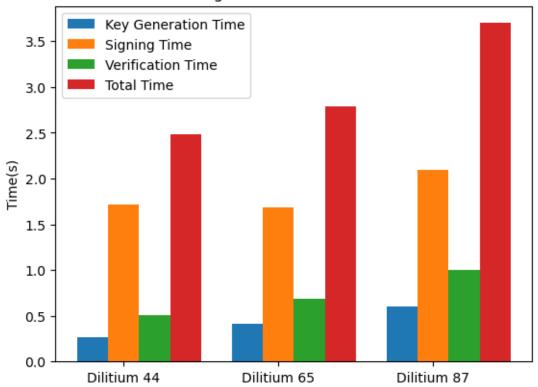
# Average Total Time for Each Version



## Comparação dos tempos médios das várias componentes

```
total_times = [sum(dil_dsa44_kg_times)/len(dil_dsa44_kg_times) +__
 ⇒sum(dil_dsa44_sign_times)/len(dil_dsa44_sign_times) +
 ⇒sum(dil_dsa44_verify_times)/len(dil_dsa44_verify_times),
 sum(dil_dsa65_kg_times)/len(dil_dsa65_kg_times) + sum(dil_dsa65_sign_times)/
 -len(dil_dsa65_sign_times) + sum(dil_dsa65_verify_times)/
 ⇔len(dil_dsa65_verify_times), sum(dil_dsa87_kg_times)/len(dil_dsa87_kg_times)⊔
 sum(dil_dsa87_verify_times)/len(dil_dsa87_verify_times)]
x = np.arange(len(labels))
width = 0.2
fig, ax = plt.subplots()
rects1 = ax.bar(x - width, kg_times, width, label='Key Generation Time')
rects2 = ax.bar(x, sign_times, width, label='Signing Time')
rects3 = ax.bar(x + width, verify_times, width, label='Verification Time')
rects4 = ax.bar(x + 2*width, total_times, width, label='Total Time')
ax.set_ylabel('Time(s)')
ax.set_title('Average Times for Each Version')
ax.set xticks(x)
ax.set_xticklabels(labels)
ax.legend()
plt.show()
```

## Average Times for Each Version



#### 1.1.3 Tabela de Resultados

```
'Average Verification Time': [sum(dil_dsa44_verify_times)/
 →len(dil_dsa44_verify_times), sum(dil_dsa65_verify_times)/
 →len(dil_dsa65_verify_times), sum(dil_dsa87_verify_times)/
 →len(dil_dsa87_verify_times)],
        'Average Total Time': [sum(dil_dsa44_kg_times)/len(dil_dsa44_kg_times)_
 →+ sum(dil dsa44 sign times)/len(dil dsa44 sign times) +
 ⇒sum(dil dsa44 verify times)/len(dil dsa44 verify times),
 sum(dil_dsa65_kg_times)/len(dil_dsa65_kg_times) + sum(dil_dsa65_sign_times)/
 →len(dil_dsa65_sign_times) + sum(dil_dsa65_verify_times)/
 elen(dil_dsa65_verify_times), sum(dil_dsa87_kg_times)/len(dil_dsa87_kg_times)_

sum(dil_dsa87_verify_times)/len(dil_dsa87_verify_times)]}

# dont use pandas
def format_cell(content):
   return f"{content:<30}"
# Print the header with separators
header = (
   format_cell("Version") + "|" +
   format_cell("Public Key Size") + "|" +
   format_cell("Secret Key Size") + "|" +
   format_cell("Signature Size") + "|" +
   format_cell("Average Key Generation Time") + "|" +
   format_cell("Average Signing Time") + "|" +
   format_cell("Average Verification Time") + "|" +
   format cell("Average Total Time")
print(header)
print("-" * len(header))
# Print the data rows with separators
for i in range(3):
   row = (
       format_cell(data['Version'][i]) + "|" +
       format_cell(data['Public Key Size'][i]) + "|" +
       format_cell(data['Secret Key Size'][i]) + "|" +
       format_cell(data['Signature Size'][i]) + "|" +
       format_cell(data['Average Key Generation Time'][i]) + "|" +
       format_cell(data['Average Signing Time'][i]) + "|" +
       format_cell(data['Average Verification Time'][i]) + "|" +
       format_cell(data['Average Total Time'][i])
   print(row)
```

Version |Signature Size 

Time   Avera	age Verification Time	Average Total Time
Dilitium 44	1312	12560
2420	0.262730201	1
1.7121216985914443	0.511027230	1567925
2.4858791298336453		
Dilitium 65	1952	4032
3309	[0.408703386]	78359985
11.6854148209095001	0.690295547	246933   2.784413754940033
Dilitium 87	2592	4896
4627	0.605251278	1960624
2.0962279524121965	0.998417036	8739537
3.6998962674822122		