CS140 HW #2

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January 21, 2013

Parallelization of Matrix-Vector Multiplication and the Power Method

This report describes the code and result of designing and implementing an algorithm for finding the highest eigenvalue of a matrix, called the Power Method. The algorithm is designed to run in parallel on N processors to enhance the performance. The Power Method can easily be described by the following Matlab code

Listing 1: Power Method algorithm implemented in Matlab (by John R. Gilbert)

Implementation in the C language

The code was implemented in C using the MPI library for parallelization. The design of the code was based on first partitioning the matrix operation between the N processors. First a matrix where generated in the function generatematrix(). This function generated $\frac{N}{nprocs}$ where nprocs is the number of processors. Further in the code each processors did operations on the same amount of rows. Further, following the algorithm in Listing 1, each processor generated a row column vector of dimension N with 1's in all the entries. Each processor executed the norm2() function on the vector. The parallelization used that helped the performance the most where implemented in the matrix-vector multiplication, in the function matVec(). Each processor performed a multiplication with each of the rows and the column vector, producing a column vector of dimension $\frac{N}{nprocs}$. The column vectors from all the processors where gathered in processor 0 using the MPI_gather library function to form the total matrix-vector product Ax. To make the total vector accessible to the other processors, MPI_Bcast where used. For more details the reader should look at the c-code implementations in functions.c.

Performance and timing

The c-code where tested on matrices of dimension N where N allways where the quotient $\frac{N}{nprocs}$ always was an integer. The algorithm proved successful and returned the same values as the matlab

nprocs	Execution Time (Seconds)
1	25.67
2	12.95
4	6.47
8	3.41
16	1.97

code, both using the matrix provided in the assignment text, and on an arbitrary matrix. For the timing of the code the dimension matrix dimension N=2400 where used, yielding 25.67 seconds of execution time running the code on one processor. The rest of the execution times can be found in Fig. 1 and Table 1.

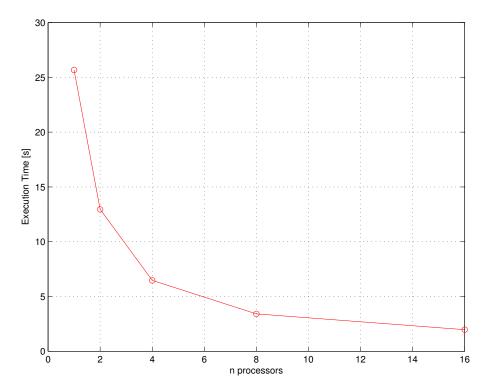


Figure 1: Plot of the execution times for the code running on 1 to 16 processors

As we can from Fig. 1 and Fig. 2 the parallelization of the code worked very well. On matrices with high dimensions the execution time where almost halved when the number of processors where doubled, for a small number of processors.

Tau Profiling Tool

The Tau Profiling tool where used to analyze the performance of the code both with a text based interface and with the graphical interface paraprof. The program was changed to do only 10 iterations of the main loop. At first the program ran with 4 processors, and than with 16 processors. The results of the generated text profile reports, pprof, are in the appendix. From the profile reports it shows that all the processors, except from node 0, have very similar characteristics. They all

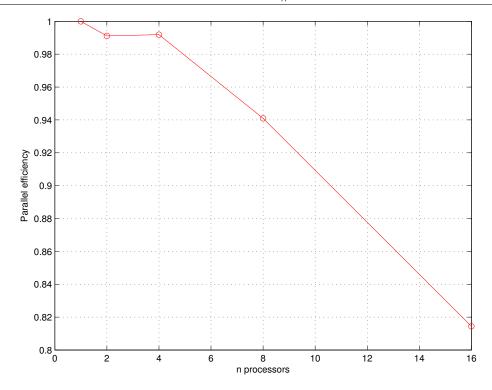


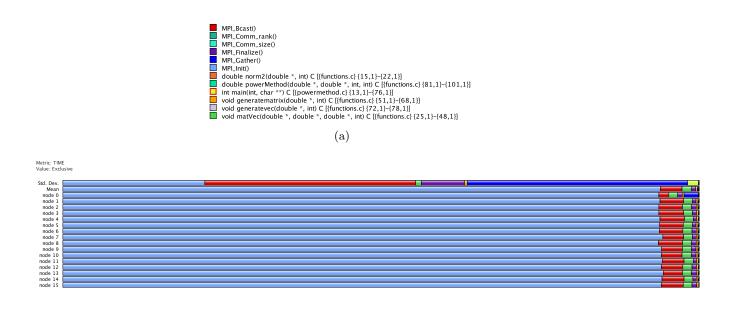
Figure 2: Plot of the parallel efficiency for the different numbers of processors

use most of their time on the initialisation, MPI_init . Beside this it is clear that the matVec() function, who is called in powerMethod(), uses a considerable amount of the execution time. Node 0 stands out from the other nodes with the amount of time used on the calls $MPI_Gather()$ and MPI_Bcast . Node 0, who has to gather data from all the other nodes, uses a lot of time on $MPI_Gather()$, while all the other nodes uses almost no time on this call. This effect is more reviling with many processors, and is probably one of the main causes why the parallel efficiency goes down with more processors. The call to MPI_Bcast has the opposite effect. Node 0, who is broadcasting data, uses less time on this call than all the other nodes, which are on the receiving side.

Conclusion

The results we got from this assignment was pretty much as expected, but we thought the parallel efficiency was surprisingly good. It was very satisfying seeing the difference between the execution time of the power method with 1 processor versus 16 processors. With many processors, the synchronisation with $MPI_Gather()$ and MPI_Bcast takes more time than the actual multiplication done in matVec(), and leads to less parallel efficiency. This is no surprise since moving data takes time.

From the figures in parafrof it was very quick and easy to get a first overview over the execution time for the different MPI functions. It was also easy to compare the running times between the different processors. From the text profile report, pprof, we got more detailed information.



(b)

Figure 3: The figure shows the execution time for the different MPI functions running on the different processors

Appendix

Pprof output for 4 processors

Reading Profile files in profile.*

NODE 0; CONTEXT 0; THREAD 0:

%Time	Exclusive msec	Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
100.0	2	1,115	1	7	1115667	int main(int, char **) C
92.1	1,027	1,027	1	0	1027312	MPI_Init()
6.4	0.249	71	1	23	71167	<pre>double powerMethod(double *, double *, int, int) C</pre>
6.4	68	70	10	40	7088	<pre>void matVec(double *, double *, int) C</pre>
1.1	12	12	1	2	12621	<pre>void generatematrix(double *, int) C</pre>
0.2	2	2	1	0	2505	MPI Finalize()
0.1	1	1	10	0	145	MPI_Gather()
0.1	0.61	0.61	10	0	61	MPI Bcast()
0.0	0.041	0.041	11	Θ	4	double norm2(double *, int) C
0.0	0.009	0.009	13	0	1	MPI Comm size()
0.0	0.004	0.004	13	Θ	0	MPI_Comm_rank()
0.0	0.004	0.004	1	Θ	4	void generatevec(double *, int) C
		3.004				·

USER EVENTS Profile :NODE 0, CONTEXT 0, THREAD 0

NumSamples MaxValue MinValue MeanValue Std. Dev. Event Name

10 2E+04 2E+04 2E+04 0 Message size for broadcast 10 5000 5000 0 Message size for gather

NODE 1; CONTEXT 0; THREAD 0:

%Time	Exclusive msec	Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
100.0 92.1 6.3	1 1,027 0.25	1,115 1,027 70	1 1 1	7 0 23	1027362	<pre>int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) C</pre>
6.3 1.2	68 13	70 13	10 1	40 2	7045 13063	<pre>void matVec(double *, double *, double *, int) C void generatematrix(double *, int) C</pre>
0.2 0.1	2 1	2 1	1 10	0	128	MPI_Finalize() MPI_Bcast()
0.0 0.0 0.0	0.408 0.036 0.008	0.408 0.036 0.008	10 11 13	0 0 0	3	<pre>MPI Gather() double norm2(double *, int) C MPI Comm size()</pre>
0.0	0.004	0.004	1 1 13	0 0	4	void generatevec(double *, int) C MPI_Comm_rank()

USER EVENTS Profile :NODE 1, CONTEXT 0, THREAD 0

NumSamples	MaxValue	MinValue	MeanValue	Std. Dev.	Event Name
10	2E+04	2E+04	2E+04		Message size for broadcast
0	0	0	0		Message size for gather

NODE 2; CONTEXT 0; THREAD 0:

%Time Exclusive Inclusive #Call #Subrs Inclusive Name

%Time	Exclusive msec	Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
100.0	1	1,115	1	 7	1115586	int main(int, char **) C
92.1	1.027	1.027	ī	Ó		MPI Init()
6.3	0.25	70	1	23	70504	<pre>double powerMethod(double *, double *, int, int) C</pre>
6.3	69	70	10	40	7022	<pre>void matVec(double *, double *, int) C</pre>
1.2	13	13	1	2	13232	<pre>void generatematrix(double *, int) C</pre>
0.2	2	2	1	Θ	2688	MPI_Finalize()
0.1	0.868	0.868	10	0	87	MPI_Bcast()
0.0	0.309	0.309	10	0	31	MPI_Gather()
0.0	0.037	0.037	11	0	3	double norm2(double *, int) C
0.0	0.007	0.007	13	Θ	1	MPI_Comm_size()
0.0	0.004	0.004	1	0	4	void generatevec(double *, int) C
0.0	0.001	0.001	13	Θ	0	MPI_Comm_rank()

USER EVENTS Profile :NODE 2, CONTEXT 0, THREAD 0

NumSamp							
	10 0	2E+0	4 2E+04 0 0	2E+04 0	0 0	Message siz	re for broadcast re for gather
NODE 3;	CONTE	XT 0;THR	EAD 0:				
%Time	Exc	lusive msec	Inclusive total msec	#Call	#Subrs	<pre>Inclusive usec/call</pre>	Name
100.0		1	1,115	1	7	1115479	<pre>int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C void generatematrix(double *, int) C MPI_Finalize() MPI_Gather() double norm2(double *, int) C MPI_Comm_size() void generatevec(double *, int) C MPI_Comm_rank()</pre>
92.I		1,027	1,027	1	23	7027340	MPI_INIT() double powerMethod(double * double * int int)
6.3		69	70	10	40	70319	void matVec(double * double * double * int) (
1.2		13	13	1	2	13481	void generatematrix(double *. int) C
0.2		2	2	1	0	2545	MPI Finalize()
0.1		0.648	0.648	10	0	65	MPI_Bcast()
0.0		0.337	0.337	10	0	34	<pre>MPI_Gather()</pre>
0.0		0.041	0.041	11	0	4	<pre>double norm2(double *, int) C</pre>
0.0		0.008	0.008	13	0	1	MPI_Comm_size()
0.0		0.005	0.005	1	0	5	void generatevec(double *, int) (
		0.003	0.003	15			MP1_COMM_rank()
USER EVE	ENTS	Profile	:NODE 3, CONT	EXT 0, THRE	AD 0		
NumSamp ¹	les	MaxValu	e MinValue	MeanValue	Std. Dev.	Event Name	
	10	25.0	4 2E±04	2E+04	A		for broadcast
FUNCTION	N SUM	MMARY (to	tal):				ze for broadcast ze for gather
FUNCTION	N SUM	MMARY (to	tal): Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
FUNCTION	N SUM	MMARY (to	tal): Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
FUNCTION	N SUM	MMARY (to	tal): Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
FUNCTION	N SUM	MMARY (to	tal): Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
FUNCTION	N SUM	MMARY (to	tal): Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
FUNCTION	N SUM	MMARY (to	tal): Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
FUNCTION	N SUM	MMARY (to	tal): Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
FUNCTION	N SUM	MMARY (to	tal): Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
FUNCTION	N SUM	MMARY (to	tal): Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
FUNCTION	N SUM	MMARY (to	tal): Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
FUNCTION	N SUM	MMARY (to	tal): Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
FUNCTION % %Time	N SUM	MMARY (to	tal): Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
FUNCTION	N SUM	MARY (to	tal):	#Call 4 4 40 4 40 40 40 40 40 40 52 4 52	#Subrs	Inclusive usec/call 1115556 1027342 70681 7039 13099 2518 85 63 4 1 4	<pre>Name int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C void generatematrix(double *, int) C MPI_Finalize() MPI_Bcast() MPI_Bcast() MPI_Gather() double norm2(double *, int) C MPI_Comm_size() void generatevec(double *, int) C MPI_Comm_rank()</pre>
FUNCTION	N SUM Exc	MARY (to slusive msec	tal):	#Call 4 4 4 4 4 40 40 44 52 4 52	#Subrs	Inclusive usec/call	<pre>int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C void generatematrix(double *, int) C MPI_Finalize() MPI_Bcast() MPI_Gather() double norm2(double *, int) C MPI_Comm_size() void generatevec(double *, int) C MPI_Comm_rank()</pre>
FUNCTION	N SUM Exc	MARY (to slusive msec	tal):	#Call 4 4 4 4 4 40 40 44 52 4 52	#Subrs	Inclusive usec/call 1115556 1027342 70681 7039 2518 85 63 4 1 4 0	Name int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C woid generatematrix(double *, int) C MPI_Finalize() MPI_Bcast() MPI_Gather() double norm2(double *, int) C MPI_Comm_size() void generatevec(double *, int) C MPI_Comm_rank()
FUNCTION	N SUM Exc	MARY (to	tal): Inclusive total msec 4,462 4,109 282 281 52 10 3 2 0.155 0.032 0.017 0.008 an): Inclusive total msec	#Call 4 4 40 4 40 44 52 4 52 #Call	#Subrs 288 0 92 160 8 0 0 0 #Subrs	Inclusive usec/call	<pre>Name int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C woid generatematrix(double *, int) C MPI_Finalize() MPI_Bcast() MPI_Bcast() double norm2(double *, int) C MPI_Comm_size() void generatevec(double *, int) C MPI_Comm_rank()</pre>
FUNCTION	N SUM Exc	MARY (to	tal): Inclusive total msec 4,462 4,109 282 281 52 10 3 2 0.155 0.032 0.017 0.008 an): Inclusive total msec	#Call 4 4 4 4 4 4 4 4 52 4 52 4 52	#Subrs 28 0 92 160 8 0 0 0 0 #Subrs	Inclusive usec/call	<pre>Name int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C woid generatematrix(double *, int) C MPI_Finalize() MPI_Gather() double norm2(double *, int) C MPI_Comm_size() void generatevec(double *, int) C MPI_Comm_rank() Name int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int)</pre>
FUNCTION	N SUM Exc	MARY (to	tal):	#Call 4 4 4 4 40 40 44 52 4 52 4 1 1 1 1 10	#Subrs 288 0 92 160 8 0 0 0 *Subrs	Inclusive usec/call 1115556 1027342 70681 7039 13099 2518 85 63 4 1 4 0 Inclusive usec/call 1115556 1027342 70681 7039	<pre>int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, int) C void generatematrix(double *, int) C MPI_Finalize() MPI_Bcast() MPI_Gather() double norm2(double *, int) C MPI_Comm_size() void generatevec(double *, int) C MPI_Comm_rank() Name int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int)</pre>
FUNCTION	N SUM Exc	MARY (to	tal):	#Call 4 4 4 40 4 40 44 52 4 52 4 52 1 1 1 1 10 1	#Subrs 28 0 92 160 8 0 0 0 0 #Subrs	Inclusive usec/call	<pre>Name int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C MPI_Finalize() MPI_Bcast() MPI_Bcast() double norm2(double *, int) C MPI_Comm_size() void generatevec(double *, int) C MPI_Comm_rank() Name int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C void generatematrix(double *, int) C</pre>
FUNCTION	N SUM Exc	MARY (to	tal): Inclusive total msec 4,462 4,109 282 281 52 10 3 2 0.155 0.032 0.017 0.008 an): Inclusive total msec 1,115 1,027 70 70 70 70 13 2	#Call 4 4 4 4 4 4 4 4 52 4 52 4 52 1 1 1 1 1 1 1 1 1 1	#Subrs 28 92 160 8 0 0 0 0 #Subrs 7 0 23 40 2 0	Inclusive usec/call	<pre>Name int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C woid generatematrix(double *, int) C MPI_Finalize() MPI_Bcast() MPI_Gather() double norm2(double *, int) C MPI_Comm_size() void generatevec(double *, int) C MPI_Comm_rank() Name int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C MPI_Finalize()</pre>
FUNCTION	N SUM Exc	MARY (to	tal):	#Call 4 4 4 4 4 4 4 4 52 4 52 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	#Subrs	Inclusive usec/call	Name int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C MPI_Finalize() MPI_Bcast() MPI_Gather() double norm2(double *, int) C MPI_Comm_size() void generatevec(double *, int) C MPI_Comm_rank()
FUNCTION	N SUM Exc	MARY (to	tal):	#Call 4 4 4 4 4 40 44 52 4 52 #Call 1 1 1 1 10 10 10	#Subrs	Inclusive usec/call	<pre>Name int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C void generatematrix(double *, int) C MPI_Finalize() MPI_Bcast() MPI_Gather() double norm2(double *, int) C MPI_Comm_size() void generatevec(double *, int) C MPI_Comm_rank() Name int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C MPI_Finalize() MPI_Bcast() MPI_Gather()</pre>
FUNCTION	N SUM Exc	MARY (to	tal):	#Call 4 4 4 4 40 40 44 52 4 52 1 1 1 1 1 1 10 1 10 10 11	#Subrs	Inclusive usec/call 1115556 1027342 70681 7039 13099 2518 85 63 4 1 4 0 Inclusive usec/call 1115556 1027342 70681 7039 13099 2518 85 63 4	<pre>int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C void generatematrix(double *, int) C MPI_Finalize() MPI_Bcast() MPI_Gather() double norm2(double *, int) C MPI_Comm_size() void generatevec(double *, int) C MPI_Comm_rank() Name Name Name Outpur (MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, int) C MPI_Finalize() MPI_Bcast() MPI_Bcast() MPI_Bcast() MPI_Bcast() MPI_Gather() double norm2(double *, int) C</pre>
FUNCTION	N SUM	MARY (to	tal):	#Call 4 4 4 4 4 40 44 52 4 52 #Call 1 1 1 1 10 10 10	#Subrs	Inclusive usec/call	<pre>Name int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C void generatematrix(double *, int) C MPI_Finalize() MPI_Bcast() MPI_Gather() double norm2(double *, int) C MPI_Comm_size() void generatevec(double *, int) C MPI_Comm_rank() Name int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C MPI_Finalize() MPI_Bcast() MPI_Gather()</pre>

Pprof output for 16 processors

Reading Profile files in profile.*

NODE 0; CONTEXT 0; THREAD 0:

%Time	Exclusive msec	Inclusive total msec	#Call	#Subrs	Inclusive I	Name
100.0	1	1,109	1	7	1109381	int main(int, char **) C
96.7	1,073	1,073	1	0	1073154 N	MPI_Init()
2.1	0.257	23	1	23	23181	$dou\overline{b}$ le powerMethod(double *, double *, int, int) C
2.1	17	22	10	40	2288 \	<pre>void matVec(double *, double *, int) C</pre>
0.7	8	8	1	0	8135 N	MPI_Finalize()
0.3	3	3	1	2	3441 \	void generatematrix(double *, int) C
0.2	2	2	10	Θ	261 M	MPI_Gather()
0.2	2	2	10	Θ	243 1	MPI_Bcast()
0.0	0.039	0.039	11	0	4 (double norm2(double *, int) C
0.0	0.012	0.012	1	0	12 \	void generatevec(double *, int) C
0.0	0.005	0.005	13	Θ	1 0	MPI_Comm_size()
0.0	0.003	0.003	13	Θ	1 0	MPI_Comm_rank()

USER EVENTS Profile :NODE 0, CONTEXT 0, THREAD 0

NumSamples MaxValue MinValue MeanValue Std. Dev. Event Name -----10 2E+04 2E+04 2E+04 0 Message size for broadcast 10 1248 1248 1248 0 Message size for gather

NODE 1; CONTEXT 0; THREAD 0:

%Time	Exclusive msec	Inclusive total msec	#Call	#Subrs	<pre>Inclusive usec/call</pre>	Name
100.0	1	1,104	1	7	1104604	int main(int, char **) C
97.1	1,072	1,072	1	Θ	1072019	MPI_Init()
2.1	0.256	23	1	23	23029	double powerMethod(double *, double *, int, int) C
2.1	17	22	10	40	2273	<pre>void matVec(double *, double *, int) C</pre>
0.5	5	5	10	Θ	514	MPI Bcast()
0.4	4	4	1	Θ	4548	MPI Finalize()
0.3	3	3	1	2	3424	void generatematrix(double *, int) C
0.0	0.161	0.161	10	Θ	16	MPI Gather()
0.0	0.039	0.039	11	Θ	4	double norm2(double *, int) C
0.0	0.015	0.015	1	Θ	15	<pre>void generatevec(double *, int) C</pre>
0.0	0.008	0.008	13	Θ	1	MPI Comm size()
0.0	0.003	0.003	13	Θ	0	MPI_Comm_rank()

USER EVENTS Profile :NODE 1, CONTEXT 0, THREAD 0

NumSamples	MaxValue	MinValue	MeanValue	Std. Dev.	Event Name
10	2E+04	2E+04	2E+04		Message size for broadcast
0	0	0	0		Message size for gather

NODE 2; CONTEXT 0; THREAD 0:

%Time	Exclusive msec	Inclusive total msec	#Call	#Subrs	<pre>Inclusive usec/call</pre>	Name
100.0	1	1,103	1	7		int main(int, char **) C
97.0	1,071	1,071	1	0	1071366	MPI Init()
2.1	0.257	23	1	23	23030	<pre>double powerMethod(double *, double *, int, int) C</pre>
2.1	17	22	10	40	2273	<pre>void matVec(double *, double *, int) C</pre>
0.5	5	5	10	Θ	511	MPI_Bcast()
0.4	4	4	1	0	4669	MPI Finalize()
0.3	3	3	1	2	3428	void generatematrix(double *, int) C
0.0	0.146	0.146	10	Θ	15	MPI_Gather()
0.0	0.04	0.04	11	Θ	4	double norm2(double *, int) C
0.0	0.016	0.016	1	Θ	16	<pre>void generatevec(double *, int) C</pre>
0.0	0.012	0.012	13	Θ	1	MPI_Comm_rank()
0.0	0.006	0.006	13	0	Θ	MPI_Comm_size()

USER EVENTS Profile :NODE 2, CONTEXT 0, THREAD 0

NumSamples MaxValue MinValue MeanValue Std. Dev. Event Name

```
NODE 3; CONTEXT 0; THREAD 0:
              Exclusive Inclusive #Call #Subrs Inclusive Name usec/call
 %Time
                                                                             usec/call
          1 1,103 1 7 1103833 int main(int, char **) C
1,071 1,071 1 0 1071370 MPI_Init()
0.259 23 1 23 23032 double powerMethod(double *, double 17 22 10 40 2273 void matVec(double *, double *, double 5 5 10 0 504 MPI_Bcast()
4 4 1 0 4730 MPI_Finalize()
3 3 1 2 3414 void generatematrix(double *, int)
0.118 0.118 10 0 12 MPI_Gather()
0.038 0.038 11 0 3 double norm2(double *, int) C
0.014 0.014 1 0 14 void generatevec(double *, int) C
0.006 0.006 13 0 0 MPI_Comm_size()
0.002 0.002 13 0 0 MPI_Comm_rank()
 -----
 100.0
                                                                                       10/13/0 MP1_Init()
23032 double powerMethod(double *, double *, int, int) C
2273 void matVec(double *, double *, double *, int) C
504 MPI_Bcast()
4730 MPI_Finalize()
3414 void generatematrix(double *, int) C
12 MPI_Gather()
  97.1
   2.1
    2.1
   0.5
   0.4
   0.3
   0.0
   0.0
   0.0
   0.0
    0.0
 USER EVENTS Profile :NODE 3, CONTEXT 0, THREAD 0
 NumSamples MaxValue MinValue MeanValue Std. Dev. Event Name
 ______
            NODE 4; CONTEXT 0; THREAD 0:
 %Time Exclusive Inclusive #Call #Subrs Inclusive Name
msec total msec usec/call
          1 1,103 1 7 1103954 int main(int, char **) C
1,071 1,071 1 0 1071374 MPI_Init()
0.247 23 1 23 23014 double powerMethod(double *, double *
17 22 10 40 2273 void matVec(double *, double *, double 5
5 5 10 0 516 MPI_Bcast()
4 4 1 0 4605 MPI_Finalize()
3 3 1 2 3467 void generatematrix(double *, int) C
0.11 0.11 10 0 11 MPI_Gather()
0.038 0.038 11 0 3 double norm2(double *, int) C
0.012 0.012 1 0 12 void generatevec(double *, int) C
0.006 0.006 13 0 0 MPI_Comm_size()
0.002 0.002 13 0 0 MPI_Comm_rank()
 100.0
  97.0
                                                                                          23014 dou\overline{b}le powerMethod(double *, double *, int, int) C
   2.1
                                                                                              2273 void matVec(double *, double *, double *, int) C
   2.1
   0.5
   0.4
   0.3
   0.0
    0.0
   0.0
   0.0
USER EVENTS Profile :NODE 4, CONTEXT 0, THREAD 0
 NumSamples MaxValue MinValue MeanValue Std. Dev. Event Name
            10 2E+04 2E+04 0 Message size for broadcast 0 0 0 0 Message size for gather
 NODE 5; CONTEXT 0; THREAD 0:
 %Time Exclusive Inclusive #Call #Subrs Inclusive Name
msec total msec usec/call
22907 dou\overline{b}le powerMethod(double *, double *, int, int) C
                                                                                       22907 double powerMethod(double *, double *, int, int)
2262 void matVec(double *, double *, double *, int) C
5036 MPI_Finalize()
492 MPI_Bcast()
3473 void generatematrix(double *, int) C
11 MPI_Gather()
3 double norm2(double *, int) C
14 void generatevec(double *, int) C
1 MPI_Comm_size()
0 MPI_Comm_rank()
 USER EVENTS Profile :NODE 5, CONTEXT 0, THREAD 0
```

2E+04 0 Message size for broadcast

0 Message size for gather

NumSamples MaxValue MinValue MeanValue Std. Dev. Event Name

0

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NODE 6; CONTEXT 0; THREAD 0:

%Time		Inclusive total msec	#Call	#Subrs	Inclusive Name usec/call
100.0	1	1 101			1101004

	IIISEC	totat msec			usec/catt
100.0	1	1,101	1	7	1101804 int main(int, char **) C
97.1	1,069	1,069	1	Θ	1069359 MPI Init()
2.1	0.247	22	1	23	22967 double powerMethod(double *, double *, int, int) C
2.1	17	22	10	40	2268 void matVec(double *, double *, double *, int) C
0.5	4	4	10	Θ	500 MPI Bcast()
0.4	4	4	1	Θ	4449 MPI Finalize()
0.3	3	3	1	2	3501 void generatematrix(double *, int) C
0.0	0.117	0.117	10	Θ	12 MPI Gather()
0.0	0.04	0.04	11	Θ	4 double norm2(double *, int) C
0.0	0.02	0.02	1	Θ	<pre>20 void generatevec(double *, int) C</pre>
0.0	0.006	0.006	13	Θ	0 MPI Comm size()
0.0	0.005	0.005	13	0	0 MPI_Comm_rank()

USER EVENTS Profile :NODE 6, CONTEXT 0, THREAD 0

NumSamples	MaxValue	MinValue	MeanValue	Std. Dev.	Event Name
10	2E+04	2E+04	2E+04		Message size for broadcast
0	0	0	0		Message size for gather

NODE 7; CONTEXT 0; THREAD 0:

%Time	Exclusive msec	Inclusive total msec	#Call	#Subrs	Inclusive usec/call	
100.0	1	1,108	1	7	1108454	int main(int, char **) C
96.5	1,069	1,069	1	0	1069599	MPI Init()
2.1	0.25	23	1	23	23130	<pre>double powerMethod(double *, double *, int, int)</pre>
2.1	17	22	10	40	2284	<pre>void matVec(double *, double *, double *, int) C</pre>
1.0	10	10	1	0	10871	MPI Finalize()
0.5	5	5	10	0	532	MPI Bcast()
0.3	3	3	1	2	3505	<pre>void generatematrix(double *, int) C</pre>
0.0	0.086	0.086	10	0	9	MPI Gather()
0.0	0.035	0.035	11	0	3	double norm2(double *, int) C
0.0	0.014	0.014	1	0	14	<pre>void generatevec(double *, int) C</pre>
0.0	0.005	0.005	13	0	0	MPI Comm size()
0.0	0.003	0.003	13	0	0	MPI_Comm_rank()

USER EVENTS Profile :NODE 7, CONTEXT 0, THREAD 0

NumSamples MaxValue MinValue MeanValue Std. Dev. Event Name

NODE 8; CONTEXT 0; THREAD 0:

%Time	Exclusive msec	Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
100.0	1	1,090	1	7	1090861	int main(int, char **) C
97.0	1,057	1,057	1	0	1057941	MPI Init()
2.1	0.267	22	1	23	22966	<pre>double powerMethod(double *, double *, int, int) C</pre>
2.1	17	22	10	40	2266	<pre>void matVec(double *, double *, int) C</pre>
0.5	4	4	1	0	4989	MPI_Finalize()
0.4	4	4	10	0	459	MPI_Bcast()
0.3	3	3	1	2	3524	void generatematrix(double *, int) C
0.0	0.206	0.206	10	0	21	MPI_Gather()
0.0	0.037	0.037	11	0	3	double norm2(double *, int) C
0.0	0.014	0.014	1	0	14	<pre>void generatevec(double *, int) C</pre>
0.0	0.005	0.005	13	0	Θ	MPI Comm size()
0.0	0.003	0.003	13	0	Θ	MPI_Comm_rank()

USER EVENTS Profile :NODE 8, CONTEXT 0, THREAD 0

NumSamples	MaxValue	MinValue	MeanValue	Std. Dev.	Event Name
10	2E+04	2E+04	2E+04		Message size for broadcast
0	0	0	0		Message size for gather

NODE 9; CONTEXT 0; THREAD 0:

%Time	Exclusive msec	Inclusive total msec	#Call	#Subrs	<pre>Inclusive usec/call</pre>	
100.0	1	1,090	1	7	1090874	int main(int, char **) C
97.0	1,057	1,057	1	0	1057936	MPI Init()
2.1	0.249	22	1	23	22947	<pre>double powerMethod(double *, double *, int, int)</pre>
2.1	17	22	10	40	2266	<pre>void matVec(double *, double *, int) C</pre>
0.5	4	4	1	Θ	4969	MPI Finalize()
0.5	4	4	10	0	491	MPI Bcast()
0.3	3	3	1	2	3513	<pre>void generatematrix(double *, int) C</pre>
0.0	0.322	0.322	10	0	32	MPI Gather()
0.0	0.037	0.037	11	0	3	double norm2(double *, int) C
0.0	0.013	0.013	1	0	13	<pre>void generatevec(double *, int) C</pre>
0.0	0.004	0.004	13	0	Θ	MPI Comm rank()
0.0	0.003	0.003	13	Θ	0	MPI Comm size()

USER EVENTS Profile :NODE 9, CONTEXT 0, THREAD 0

NumSamples	MaxValue	MinValue	MeanValue	Std. Dev.	Event Name
10	2E+04	2E+04	2E+04		Message size for broadcast
0	0	0	0		Message size for gather

NODE 10; CONTEXT 0; THREAD 0:

%Time	Exclusive msec	Inclusive total msec	#Call	#Subrs	Inclusive usec/call	Name
100.0	1	1,090	1	7	1090315	int main(int, char **) C
97.0	1,057	1,057	1	0	1057399	MPI Init()
2.1	0.247	22	1	23	22901	double powerMethod(double *, double *, int, int) C
2.1	17	22	10	40	2261	<pre>void matVec(double *, double *, int) C</pre>
0.5	5	5	1	0	5052	MPI_Finalize()
0.5	4	4	10	0	491	MPI Bcast()
0.3	3	3	1	2	3573	void generatematrix(double *, int) C
0.0	0.255	0.255	10	0	26	MPI_Gather()
0.0	0.039	0.039	11	0	4	double norm2(double *, int) C
0.0	0.009	0.009	1	0	9	<pre>void generatevec(double *, int) C</pre>
0.0	0.005	0.005	13	0	Θ	MPI Comm size()
0.0	0.004	0.004	13	Θ	Θ	MPI_Comm_rank()

USER EVENTS Profile :NODE 10, CONTEXT 0, THREAD 0

NumSamples	MaxValue	MinValue	MeanValue	Std. Dev.	Event Name
10	2E+04	2E+04	2E+04		Message size for broadcast
0	0	0	0		Message size for gather

NODE 11; CONTEXT 0; THREAD 0:

%Time	Exclusive msec	Inclusive total msec	#Call	#Subrs	Inclusive Name usec/call
100.0	1	1,096	1	7	1096643 int main(int, char **) C
96.4	1,057	1,057	1	0	1057706 MPI Init()
2.1	0.255	22	1	23	22931 double powerMethod(double *, double *, int, int) C
2.1	17	22	10	40	2264 void matVec(double *, double *, double *, int) C
1.0	11	11	1	Θ	11130 MPI_Finalize()
0.4	4	4	10	Θ	482 MPI Bcast()
0.3	3	3	1	2	3528 void generatematrix(double *, int) C
0.0	0.244	0.244	10	0	24 MPI Gather()
0.0	0.037	0.037	11	Θ	3 double norm2(double *, int) C
0.0	0.012	0.012	1	Θ	12 void generatevec(double *, int) C
0.0	0.004	0.004	13	Θ	0 MPI Comm size()
0.0	0.001	0.001	13	0	0 MPI_Comm_rank()

USER EVENTS Profile :NODE 11, CONTEXT 0, THREAD 0

NumSamples	MaxValue	MinValue	MeanValue	Std. Dev.	Event Name
10	2E+04	2E+04	2E+04		Message size for broadcast
0	0	0	0		Message size for gather

NODE 12; CONTEXT 0; THREAD 0:

......

	msec	Inclusive total msec			usec/call	
 100.0	1	1,090	1	7	1090713	int main(int, char **) C
97.0	1,057	1,057	1	0	1057745	MPI_Init()
2.1	0.251	22	1	23	22882	double powerMethod(double *, double *, int, int)
2.1 0.5	4	4	10	40 0	4909	MPT Finalize()
0.4	4	4	10	ő	481	MPI Bcast()
0.3	3	3	1	2	3567	void generatematrix(double *, int) C
0.0	0.236	0.236	10	0	24	MPI_Gather()
0.0	0.036	0.036	11	0	3	double norm2(double *, int) C
0.0	0.014	0.014	1 12	0	14	void generatevec(double *, int) C
0.0	0.000	0.000	13	9	9	MPT Comm rank()
						<pre>int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C MPI_Finalize() MPI_Bcast() void generatematrix(double *, int) C MPI_Gather() double norm2(double *, int) C void generatevec(double *, int) C MPI_Comm_size() MPI_Comm_rank()</pre>
		NODE 12, CON				
		MinValue		Std. Dev.		
10 0	2E+04 0	2E+04 0	2E+04 0	0 0	Message si	ze for broadcast ze for gather
10 0 IODE 13;CON 	2E+04 0 ITEXT 0;THR	2E+04 0 EAD 0: Inclusive	2E+04 0 	0 0 	Message si Message si Inclusive	ze for broadcast ze for gather Name
10 0 NODE 13;COM	2E+04 0 ITEXT 0;THR	2E+04 0 EAD 0: Inclusive total msec	2E+04 0 #Call	0 0 	Message si Message si Inclusive usec/call	ze for broadcast ze for gather Name
10 0 ODE 13;CON Time Ex	2E+04 0 ITEXT 0;THR	2E+04 0 EAD 0: Inclusive total msec	2E+04 0 #Call	0 0 	Message si Message si Inclusive usec/call	ze for broadcast ze for gather Name
10 0 ODE 13;CON Time Ex	2E+04 0 ITEXT 0;THR	2E+04 0 EAD 0: Inclusive total msec	2E+04 0 #Call	0 0 	Message si Message si Inclusive usec/call	ze for broadcast ze for gather Name
10 0 ODE 13;CON Time Ex	2E+04 0 ITEXT 0;THR	2E+04 0 EAD 0: Inclusive total msec	2E+04 0 #Call	0 0 	Message si Message si Inclusive usec/call	ze for broadcast ze for gather Name
10 0 ODE 13;CON Time Ex	2E+04 0 ITEXT 0;THR	2E+04 0 EAD 0: Inclusive total msec	2E+04 0 #Call	0 0 	Message si Message si Inclusive usec/call	ze for broadcast ze for gather Name
10 0 ODE 13;CON Time Ex	2E+04 0 ITEXT 0;THR	2E+04 0 EAD 0: Inclusive total msec	2E+04 0 #Call	0 0 	Message si Message si Inclusive usec/call	ze for broadcast ze for gather Name
10 0 ODE 13;CON Time Ex	2E+04 0 ITEXT 0;THR	2E+04 0 EAD 0: Inclusive total msec	2E+04 0 #Call	0 0 	Message si Message si Inclusive usec/call	ze for broadcast ze for gather Name
10 0 ODE 13;CON Time Ex	2E+04 0 ITEXT 0;THR	2E+04 0 EAD 0: Inclusive total msec	2E+04 0 #Call	0 0 	Message si Message si Inclusive usec/call	ze for broadcast ze for gather Name
10 0 ODE 13;CON Time Ex	2E+04 0 ITEXT 0;THR	2E+04 0 EAD 0: Inclusive total msec	2E+04 0 #Call	0 0 	Message si Message si Inclusive usec/call	ze for broadcast ze for gather Name
10 0 ODE 13;CON Time Ex	2E+04 0 ITEXT 0;THR	2E+04 0 EAD 0: Inclusive total msec	2E+04 0 #Call	0 0 	Message si Message si Inclusive usec/call	ze for broadcast ze for gather Name
10 0 ODE 13;CON Time Ex	2E+04 0 ITEXT 0;THR	2E+04 0 EAD 0: Inclusive total msec	2E+04 0 #Call	0 0 	Message si Message si Inclusive usec/call	ze for broadcast ze for gather Name
10 0 ODE 13;CON Time Ex	2E+04 0 ITEXT 0;THR	2E+04 0 EAD 0: Inclusive total msec	2E+04 0 #Call	0 0 	Message si Message si Inclusive usec/call	ze for broadcast ze for gather Name
10 0 0 0 0 0 13;CON 0 10 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	2E+04 0 	2E+04 0 	2E+04 0 #Call 1 1 10 1 10 11 13 13 13	#Subrs	Message si: Message si: Inclusive usec/call 1089178 1056270 22860 2257 5299 481 3613 18 4 12 1 0	ze for broadcast ze for gather
10 0 000 13;CON 000 0 0 97.0 2.1 2.1 0.5 0.4 0.3 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0	2E+04 0 0 ITEXT 0;THR cclusive msec 1 1,056 0.247 17 5 4 3 0.181 0.04 0.012 0.007 0.003	2E+04 0 	#Call #Call 1 1 1 10 1 10 11 13 13 13 ITEXT 0, THR	#Subrs	Message si: Message si: Inclusive usec/call 1089178 1056270 22860 2257 5299 481 3613 18 4 12 1 0	<pre>Name int main(int, char **) C MPI_Init() double powerMethod(double *, double *, int, int) void matVec(double *, double *, double *, int) C MPI_Finalize() MPI_Bcast() void generatematrix(double *, int) C MPI_Gather() double norm2(double *, int) C void generatevec(double *, int) C MPI_Comm_rank() MPI_Comm_size()</pre>

%Time	Exclusive msec	Inclusive total msec	#Call	#Subrs	Inclusive Name usec/call
100.0	1	1,089	1	7	/ 1089593 int main(int, char **) C
97.1	1,058	1,058	1	0) 1058327 MPI_Init()
1.9	0.253	21	1	23	<pre>21060 double powerMethod(double *, double *, int, int) C</pre>
1.9	17	20	10	40	2077 void matVec(double *, double *, double *, int) C
0.5	4	4	1	0	
0.3	3	3	1	2	? 3768 void generatematrix(double *, int) C
0.3	3	3	10	0	327 MPI_Bcast()
0.0	0.212	0.212	10	Θ) 21 MPI Gather()
0.0	0.036	0.036	11	Θ	3 double norm2(double *, int) C
0.0	0.017	0.017	1	0	17 void generatevec(double *, int) C
0.0	0.004	0.004	13	Θ	0 MPI Comm size()
0.0	0.003	0.003	13	Θ	0 MPI_Comm_rank()

```
USER EVENTS Profile :NODE 14, CONTEXT 0, THREAD 0
```

NumSamples	MaxValue	MinValue	MeanValue	Std. Dev.	Event Name
10	2E+04	2E+04	2E+04		Message size for broadcast
0	0	0	0		Message size for gather

NODE 15; CONTEXT 0; THREAD 0:

%Time Exclusive Inclusive #Call #Subrs Inclusive Name
msec total msec usec/call

100.0	1	1,097	1	7	1097394 int main(int, char **) C
96.4	1,057	1,057	1	Θ	1057727 MPI Init()
2.1	0.249	22	1	23	22822 double powerMethod(double *, double *, int, int) C
2.1	17	22	10	40	2253 void matVec(double *, double *, double *, int) C
1.1	11	11	1	Θ	11736 MPI Finalize()
0.4	4	4	10	0	493 MPI Bcast()
0.3	3	3	1	2	3662 void generatematrix(double *, int) C
0.0	0.181	0.181	10	0	18 MPI_Gather()
0.0	0.037	0.037	11	Θ	3 double norm2(double *, int) C
0.0	0.019	0.019	1	0	<pre>19 void generatevec(double *, int) C</pre>
0.0	0.006	0.006	13	0	0 MPI_Comm_rank()
0.0	0.005	0.005	13	0	0 MPI_Comm_size()

USER EVENTS Profile :NODE 15, CONTEXT 0, THREAD 0

NumSamples	MaxValue	MinValue	MeanValue	Std. Dev.	Event Name
10	2E+04	2E+04	2E+04	9	Message size for broadcast
0	0	0	0	9	Message size for gather

FUNCTION SUMMARY (total):

%Time	Exclusive msec	Inclusive total msec	#Call	#Subrs	Inclusive Name usec/call
100.0	22	17,574	16	112	1098413 int main(int, char **) C
96.9	17,029	17,029	16	Θ	1064342 MPI_Init()
2.1	4	365	16	368	22854 dou \overline{b} le powerMethod(double *, double *, int, int) C
2.1	280	360	160	640	2256 void matVec(double *, double *, double *, int) C
0.6	100	100	16	Θ	6256 MPI_Finalize()
0.4	75	75	160	Θ	470 MPI Bcast()
0.3	56	56	16	32	$3525 \text{ voi}\overline{d}$ generatematrix(double $*$, int) C
0.0	5	5	160	0	33 MPI_Gather()
0.0	0.606	0.606	176	0	3 double norm2(double *, int) C
0.0	0.227	0.227	16	0	<pre>14 void generatevec(double *, int) C</pre>
0.0	0.084	0.084	208	0	<pre>0 MPI_Comm_size()</pre>
0.0	0.066	0.066	208	0	<pre>0 MPI_Comm_rank()</pre>

FUNCTION SUMMARY (mean):

%Time	Exclusive msec	Inclusive total msec	#Call	#Subrs	Inclusive I	Name
100.0	1	1,098	1	7	1098413	int main(int, char **) C
96.9	1,064	1,064	1	0	1064342	MPI Init()
2.1	0.253	22	1	23	22854	double powerMethod(double *, double *, int, int) C
2.1	17	22	10	40	2256 \	<pre>void matVec(double *, double *, int) C</pre>
0.6	6	6	1	0	6256 I	MPI_Finalize()
0.4	4	4	10	0	470 1	MPI_Bcast()
0.3	3	3	1	2	3525 v	void generatematrix(double *, int) C
0.0	0.331	0.331	10	0	33 1	MPI_Gather()
0.0	0.0379	0.0379	11	Θ	3 (double norm2(double *, int) C
0.0	0.0142	0.0142	1	Θ	14 \	void generatevec(double *, int) C
0.0	0.00525	0.00525	13	Θ	1 0	MPI_Comm_size()
0.0	0.00413	0.00413	13	0	1 0	MPI Comm rank()