

Gegebene Werte:

$$A_{0-1} := 1$$

$$A_{0-2} := 1$$

$$a_D := 1 \text{ dB}$$

$$a_s := 40 \text{ dB}$$

$$f_{pb} := 10000$$

$$n := 4$$

$$R := 10000$$

$$C := 1 \cdot 10^{-9}$$

Berechnung Polfrequenzen, Nullfrequenzen und Polgüte:

$$\varepsilon := \frac{1}{\sqrt{10^{0.1 \cdot a_s} - 1}} = 0.0100005 \quad \dots \text{Welligkeit im Sperrbereich}$$

$$s_P(k) := \frac{1}{-\sin\left(\frac{1+2 \cdot k}{2 \cdot n} \cdot \pi\right) \cdot \sinh\left(\frac{1}{n} \cdot \operatorname{asinh}\left(\frac{1}{\varepsilon}\right)\right) + 1i \cdot \cos\left(\frac{1+2 \cdot k}{2 \cdot n} \cdot \pi\right) \cdot \cosh\left(\frac{1}{n} \cdot \operatorname{asinh}\left(\frac{1}{\varepsilon}\right)\right)}$$

$$s_Z(k) := \frac{1i}{\cos\left(\frac{1+2 \cdot k}{2 \cdot n} \cdot \pi\right)} \quad \dots \text{Nullfrequenzen}$$

$$Q_P(k) := \frac{-|s_P(k)|}{2 \cdot \operatorname{Re}(s_P(k))} \quad \dots \text{Polgüten}$$

$$s_P(0) = -0.171 - 0.476i$$

$$s_P(1) = -0.505 - 0.241i$$

$$s_P(2) = -0.505 + 0.241i$$

$$s_P(3) = -0.171 + 0.476i$$

$$s_Z(0) = 1.082i$$

$$s_Z(1) = 2.613i$$

$$s_Z(2) = -2.613i$$

$$s_Z(3) = -1.082i$$

$$Q_P(0) = 1.478$$

$$Q_P(1) = 0.554$$

$$Q_P(2) = 0.554$$

$$Q_P(3) = 1.478$$

$$\Omega_{P1} := |s_P(0)| = 0.506$$

$$\Omega_{P2} := |s_P(1)| = 0.559$$

$$\Omega_{Z1} := |s_Z(0)| = 1.082$$

$$\Omega_{Z2} := |s_Z(1)| = 2.613$$

$$Q_{P1} := Q_P(0) = 1.478$$

$$Q_{P2} := Q_P(1) = 0.554$$

Wählbare Werte zuordnen:

$$C_{5_1} := C = 1 \cdot 10^{-9}$$

$$C_{5_2} := C = 1 \cdot 10^{-9}$$

$$R_{B_1} := R = 1 \cdot 10^4$$

$$R_{B_2} := R = 1 \cdot 10^4$$

$$k := \cosh \left(\frac{\operatorname{acosh} \left(\frac{\sqrt{\frac{10^{-0.1 \cdot a_D}}{1 - 10^{-0.1 \cdot a_D}}}}{\varepsilon} \right)}{n} \right) = 2.339$$

Entnormierte Pol-/ Nullstellenkreisfrequenzen bestimmen:

$$\omega_{P1} := 2 \cdot \pi \cdot f_{pb} \cdot \Omega_{P1} \cdot k = 74339.6$$

$$\omega_{P2} := 2 \cdot \pi \cdot f_{pb} \cdot \Omega_{P2} \cdot k = 82144.333$$

$$\omega_{Z1} := 2 \cdot \pi \cdot f_{pb} \cdot \Omega_{Z1} \cdot k = 159041.723$$

$$\omega_{Z2} := 2 \cdot \pi \cdot f_{pb} \cdot \Omega_{Z2} \cdot k = 383960.684$$

C_1 berechnen:

$$C_{1_1min} := \frac{C_{5_1} \cdot A_{0_1}^2 \cdot (Q_{P1}^2 \cdot (\omega_{Z1}^2 - \omega_{P1}^2) + \omega_{P1}^2)^2}{\omega_{Z1}^4 \cdot Q_{P1}^2 \cdot (A_{0_1} - 1) + \omega_{Z1}^2 \cdot \omega_{P1}^2 \cdot Q_{P1}^2 \cdot A_{0_1} \cdot (A_{0_1} - 1) + \omega_{P1}^2 \cdot A_{0_1} \cdot (\omega_{Z1}^2 - A_{0_1} \cdot \omega_{P1}^2)} = 2.172 \cdot 10^{-8}$$

$$C_{1_2min} := \frac{C_{5_2} \cdot A_{0_2}^2 \cdot (Q_{P2}^2 \cdot (\omega_{Z2}^2 - \omega_{P2}^2) + \omega_{P2}^2)^2}{\omega_{Z2}^4 \cdot Q_{P2}^2 \cdot (A_{0_2} - 1) + \omega_{Z2}^2 \cdot \omega_{P2}^2 \cdot Q_{P2}^2 \cdot A_{0_2} \cdot (A_{0_2} - 1) + \omega_{P2}^2 \cdot A_{0_2} \cdot (\omega_{Z2}^2 - A_{0_2} \cdot \omega_{P2}^2)} = 2.626 \cdot 10^{-9}$$

$$C_{1_1} := 22 \cdot 10^{-9}$$

$$C_{1_2} := 2.7 \cdot 10^{-9}$$

R_A berechnen:

$$R_{A_1} := \frac{R_{B_1} \cdot (\omega_{Z1}^2 - A_{0_1} \cdot \omega_{P1}^2)}{\omega_{P1}^2 \cdot A_{0_1}} = 35770.083$$

$$R_{A_1} := 36 \cdot 10^3$$

$$R_{A_2} := \frac{R_{B_2} \cdot (\omega_{Z2}^2 - A_{0_1} \cdot \omega_{P2}^2)}{\omega_{P2}^2 \cdot A_{0_1}} = 208483.325$$

$$R_{A_2} := 200 \cdot 10^3$$

R_3 berechnen:

$$R_{3_1} := \frac{C_{1_1} \cdot \omega_{Z1}^2 - \sqrt{C_{1_1}^2 \cdot \omega_{Z1}^4 - 4 \cdot C_{1_1} \cdot C_{5_1} \cdot A_{0_1}^2 \cdot \omega_{P1}^2 \cdot (\omega_{P1}^2 + Q_{P1}^2 \cdot \omega_{Z1}^2)}}{2 \cdot C_{1_1} \cdot C_{5_1} \cdot A_{0_1} \cdot Q_{P1} \cdot \omega_{P1}^3} = 1019.002$$

$$R_{3_2} := \frac{C_{1_2} \cdot \omega_{Z2}^2 - \sqrt{C_{1_2}^2 \cdot \omega_{Z2}^4 - 4 \cdot C_{1_2} \cdot C_{5_2} \cdot A_{0_2}^2 \cdot \omega_{P2}^2 \cdot (\omega_{P2}^2 + Q_{P2}^2 \cdot \omega_{Z2}^2)}}{2 \cdot C_{1_2} \cdot C_{5_2} \cdot A_{0_2} \cdot Q_{P2} \cdot \omega_{P2}^3} = 2887.827$$

$$R_{3_1} = 1 \cdot 10^3$$

$$R_{3_2} = 2.7 \cdot 10^3$$

 R_4 berechnen:

$$R_{4_1} := \frac{1}{C_{1_1} \cdot C_{5_1} \cdot R_{3_1} \cdot \omega_{P1}^2} = 8071.64$$

$$R_{4_1} := 8.2 \cdot 10^3$$

$$R_{4_2} := \frac{1}{C_{1_2} \cdot C_{5_2} \cdot R_{3_2} \cdot \omega_{P2}^2} = 19006.84$$

$$R_{4_2} := 18 \cdot 10^3$$

 R_2 berechnen:

$$R_{2_1} := \frac{-Q_{P1} \cdot R_{3_1}}{Q_{P1} + R_{3_1}^2 \cdot C_{1_1} \cdot C_{5_1} \cdot Q_{P1} \cdot \omega_{P1}^2 - R_{3_1} \cdot C_{1_1} \cdot \omega_{P1}} = 749432.005$$

$$R_{2_2} := \frac{-Q_{P2} \cdot R_{3_2}}{Q_{P2} + R_{3_2}^2 \cdot C_{1_2} \cdot C_{5_2} \cdot Q_{P2} \cdot \omega_{P2}^2 - R_{3_2} \cdot C_{1_2} \cdot \omega_{P2}} = 698494.457$$

$$R_{2_1} := 750 \cdot 10^3$$

$$R_{2_2} := 680 \cdot 10^3$$

 R_6 berechnen:

$$R_{6_1} := \frac{R_{B_1} \cdot Q_{P1}}{C_{5_1} \cdot \omega_{P1} \cdot (R_{3_1} \cdot R_{A_1} \cdot C_{1_1} \cdot Q_{P1} \cdot \omega_{P1} - R_{B_1})} = 2527.122$$

$$R_{6_2} := \frac{R_{B_2} \cdot Q_{P2}}{C_{5_2} \cdot \omega_{P2} \cdot (R_{3_2} \cdot R_{A_2} \cdot C_{1_2} \cdot Q_{P2} \cdot \omega_{P2} - R_{B_2})} = 1106.214$$

$$R_{6_1} := 2588 \cdot 10^3$$

$$R_{6_2} := 1 \cdot 10^3$$