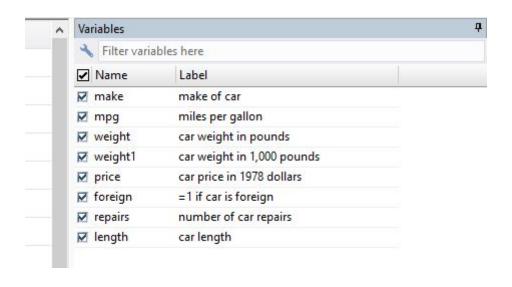
Simple linear regression

We will use a car data set and our dependent variable is mpg (miles per gallon) vs our independent variable car weight.





Description of our response variable and predictor variable but lets first create our global variables

```
global ylist mpg
global xlist weightl
```

. describe \$y	list \$xli:	st		
variable name	storage type	display format	value label	variable label
mpg weight1	byte float	%8.0g %9.0g		miles per gallon car weight in 1,000 pounds

Data Summary

				st \$x11st	summarize \$ylis
Max	Min	Std. Dev.	Mean	Obs	Variable
35	14	4.757504	20.92308	26	mpg
4.33	2.02	.6950794	3.099231	26	weight1

. sum	nmarize \$ylist,	detail						
	miles per gallon							
	Percentiles	Smallest						
1%	14	14						
5%	14	14						
L0%	15	15	Obs	26				
25%	17	16	Sum of Wgt.	26				
) 응	21		Mean	20.92308				
		Largest	Std. Dev.	4.757504				
5%	23	25						
90%	26	26	Variance	22.63385				
15%	29	29	Skewness	.8806144				
98	35	35	Kurtosis	4.243808				

Question

Can the weight of a car statistically significantly predict a car's miles per gallon?

Hypothesis

H0: Car weight can not statistically significantly predict a car's miles per gallon Ha: Car weight can statistically significantly predict a car's miles per gallon

The level of significance

alpha = 0.05

ASSUMPTIONS

Determine if data meets requirements to perform a linear regression.

1.0000

1.0000

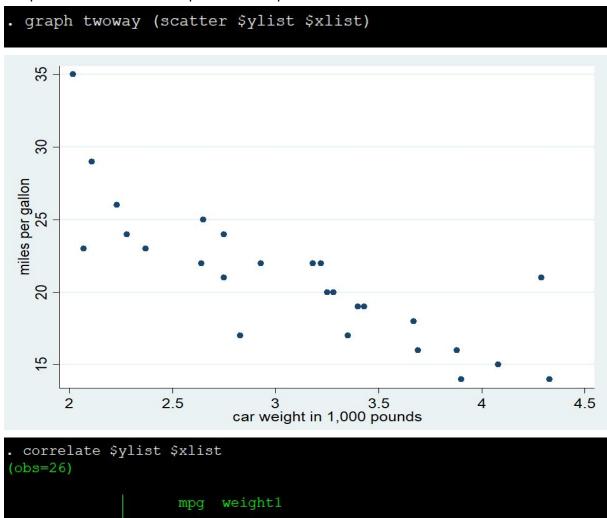
-0.8082

mpg

weightl

Assumption #1: Your response variable should be measured on a continuous scale. **Assumption #2**: Your independent variable should be measured at the continuous or categorical level.

Assumption #3: There needs to be a linear relationship between the dependent and independent variables. Let's plot a scatter plot and check



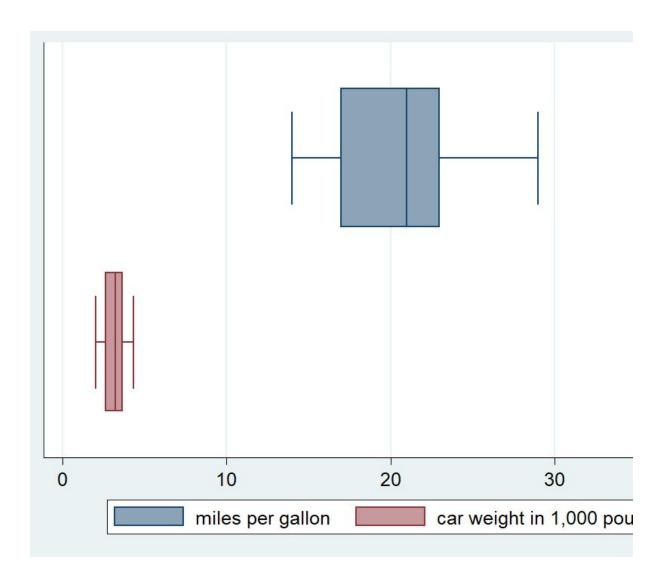
As seen above the two variables appear to be linearly related

Assumption #4: You should have independence of observations. which you can easily check using the **Durbin-Watson statistic**, which is a simple test to run using Stata.

```
. dwstat

Durbin-Watson d-statistic( 2, 26) = 1.991873
```

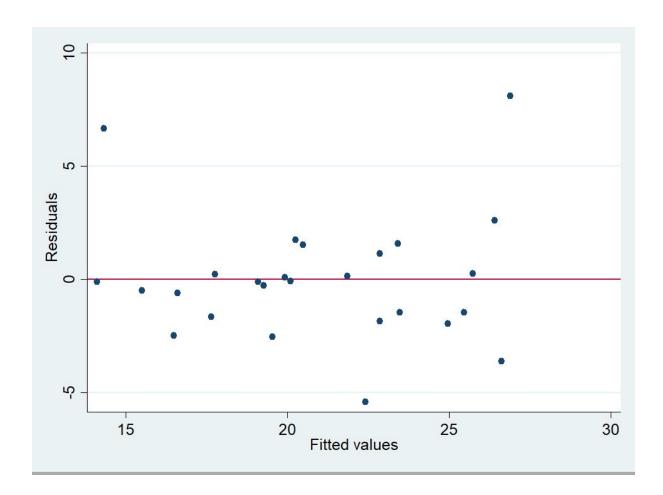
Assumption #5: There should be no significant outliers. We use box plot



Assumption #6: Your data needs to show homoscedasticity, which is where the variances along the line of best fit remain similar as you move along the line.

One of the major assumptions given for type ordinary least squares regression is the homogeneity in the case of variance of the residuals. In the case of a well-fitted model, if you plot residual values versus fitted values, you should not see any particular pattern. Now, what if the variance given by the residuals is not a constant? In this case, the **residual variance** is called **heteroscedastic**. The most commonly used way to detect heteroscedasticity is by plotting residuals versus predicted values. We should not have any side narrower than the other.

. rvfplot, yline(0)



We can also use non-graphical commands as shown below. The first test on heteroscedasticity given by imtest is the White's test and the second one given by hettest is the Breusch-pagan test.

Both test the null hypothesis that the variance of the residuals are homogenous.

estat imtest Cameron & Trivedi's decomposition of IM-test Source chi2 6.39 2 0.0410 Heteroskedasticity 0.1090 Skewness 2.57 Kurtosis 0.0667 3.36 Total 12.32 4 0.0151 estat hettest Breusch-Pagan / Cook-Weisberg test for heteroskedasticity Ho: Constant variance Variables: fitted values of mpg 1.48 0.2239

Assumption #7: Finally, you need to check that the residuals (errors) of the regression line are approximately normally distributed.

First we run the regression as shown below

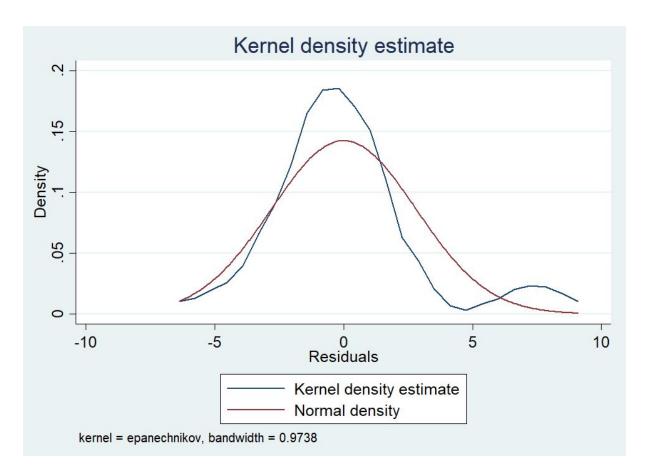
Source	SS	df	MS	Numb	er of obs		26
				- F(1,	24)		45.19
Model	369.567767	1	369.56776	7 Prob	> F		0.0000
Residual	196.278387	24	8.1782661	1 R-sq	uared		0.6531
				— Adj	R-squared	=	0.6387
Total	565.846154	25	22.633846	2 Root	MSE		2.8598
mpg	Coef.	Std. Err.	t	P> t	[95% C	onf.	Interval]
weight1	-5.531496	.8228604	-6.72	0.000	-7.2297	97	-3.833196
cons	38.06646	2.611177	14.58	0.000	32.677	26	43.45566

We the use the predict command to generate residuals

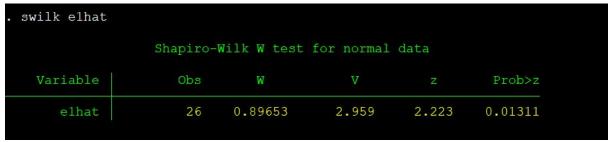
. predict elhat, resid

We finally use kdensity command to plot a kernel density plot with a normal option requesting that a normal density be overlaid on the plot.

```
. kdensity elhat, normal
(n() set to 26)
```



We can also use Shapiro-Wilk W test for normal data as shown below. The p value is based on the assumption that the distribution is normal.



As seen above this assumption fails as the test is significant.

Simple linear interpretation

Source	SS	df	MS	Numb	er of obs		26
				- F(1,	24)		45.19
Model	369.567767	1	369.56776	7 Prob	> F		0.0000
Residual	196.278387	24	8.1782661	1 R-sq	uared		0.6531
				— Adj	R-squared		0.6387
Total	565.846154	25	22.633846	2 Root	MSE		2.8598
mpg	Coef.	Std. Err.	t	P> t	[95% Con	f.	Interval]
weight1	-5.531496	.8228604	-6.72	0.000	-7.229797		-3.833196
cons	38.06646	2.611177	14.58	0.000	32.67726		43.45566

A linear regression established that weight of a car could statistically significantly predict mpg (miles covered by the car per gallon), F(1, 24) = 45.19, p < .05 and the weight of a car accounted for 65.3% of the explained variability in miles covered by the car per gallon. The regression equation was: predicted miles covered by the car per gallon = $38.066 - 5.531 \, x$ (weight of the car).

Plotting a regression line

