

Student: Simon Kong

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Algorithm Steps

Main

```
step 0: inFile ← open the input file
        RFprettyPrintFile , labelFile, propertyFile ← open from args[]
        numRows, numCols, minVal, maxVal ← read from inFile
        dynamically allocate zeroFramedAry.
        newLabel ← 0
step 1: zero2D (zeroFramedAry)
step 2: loadImage (inFile, zeroFramedAry)
step 3: Connectness ← ask user from console
step 4: if connectness == 4
        connect4Pass1 (...)
        imgReformat (zeroFramedAry, RFprettyPrintFile)
        printEQAry (newLabel, RFprettyPrintFile)

        // print the EQAry up to newLabel with proper caption
        Connect4Pass2 (...)
        imgReformat (zeroFramedAry, RFprettyPrintFile)
        printEQAry (newLabel, RFprettyPrintFile)
        // print the EQAry up to newLabel with proper caption

step 5: if connectness == 8
        connect8Pass1 (...)
        imgReformat (zeroFramedAry, RFprettyPrintFile)
        printEQAry (newLabel, RFprettyPrintFile)
        // print the EQAry up to newLabel with proper caption
        Connect8Pass2 (...)
        imgReformat (zeroFramedAry, RFprettyPrintFile)
        printEQAry (newLabel, RFprettyPrintFile)
        // print the EQAry up to newLabel with proper caption
step 6: trueNumCC ← manageEQAry (EQAry, newLabel)
        printEQAry (newLabel, RFprettyPrintFile)
        // print the EQAry up to newLabel with proper caption
step 7: connectPass3 (...)
step 8: imgReformat (zeroFramedAry, RFprettyPrintFile)
step 9: printEQAry (newLabel, RFprettyPrintFile)
        // print the EQAry up to newLabel with proper caption
step 10: output numRows, numCols, newMin, newMax to labelFile
step 11: printImg (labelFile) // Output the result of pass3 inside of zeroFramedAry
step 12: printCCproperty (propertyFile) // print cc properties to propertyFile
step 13: drawBoxes(zeroFramedAry, CCproperty)
step 14: imgReformat (zeroFramedAry, RFprettyPrintFile)
step 15: print trueNumCC to RFprettyPrintFile with proper caption
step 16: close all files
```

Source Code

Main Class

```
package Project_5;

import java.io.BufferedReader;

public class Main {
    public static void main(String[] args) throws IOException {
        if(args.length != 4) {
            System.out.println("Invalid number of arguments.");
            System.exit(0);
        }
        //Initialize variables
        String inputFile = args[ 0 ];
        String prettyPrintFile = args[ 1 ];
        String labelFile = args[ 2 ];
        String propertyFile = args[ 3 ];

        //Initialize readers
        FileReader inputReader = null ;
        BufferedReader buffInReader = null ;
        Scanner input = null ;
        Scanner userInput = null;

        //Initialize writers
        FileWriter outputWriter1 = null ;
        BufferedWriter output1 = null ;

        FileWriter outputWriter2 = null ;
        BufferedWriter output2 = null ;

        FileWriter outputWriter3 = null ;
        BufferedWriter output3 = null ;

        try{
            // Open input
            inputReader = new FileReader( inputFile ) ;
            buffInReader = new BufferedReader( inputReader ) ;
            input = new Scanner( buffInReader ) ;

            userInput = new Scanner(System.in);

            outputWriter1 = new FileWriter(prettyPrintFile);
            output1 = new BufferedWriter(outputWriter1);
```

```
outputWriter2 = new FileWriter(labelFile);
output2 = new BufferedWriter(outputWriter2);

outputWriter3 = new FileWriter(propertyFile);
output3 = new BufferedWriter(outputWriter3);

// initialize variables
int numRows = 0 ;
int numCols = 0 ;
int minVal = 0 ;
int maxVal = 0 ;

if( input.hasNextInt() ) numRows = input.nextInt() ;
if( input.hasNextInt() ) numCols = input.nextInt() ;
if( input.hasNextInt() ) minVal = input.nextInt() ;
if( input.hasNextInt() ) maxVal = input.nextInt() ;

CCLabel ccObj = new CCLabel( numRows, numCols, minVal, maxVal ) ;

ccObj.loadImage(ccObj.zeroFramedAry, input);
output1.write("Original Image: \n");
ccObj.imageReformat(ccObj.zeroFramedAry, output1);

// user input
int connectness = 0;
boolean flag = true;
while( flag ) {
    try {
        System.out.println("Please enter 4 or 8 for connectness:");
        String val = userInput.next();
        connectness = Integer.parseInt(val);
    } catch (Exception e) {
        System.out.println("Invalid input. Try again.");
    } finally {
        if (connectness == 4 || connectness == 8) flag = false;
    }
}
userInput.close();
```

```

if( connectness == 4 ) {
    ccObj.connect4Pass1();
    output1.write("Zero Framed Array after pass 1 with padding (4 connectness): \n");
    ccObj.imageReformat( ccObj.zeroFramedAry, output1);
    output1.write("Equivalence Table after pass 1 (4 connectness): \n");
    ccObj.printEQAry(ccObj.newLabel, output1);
    output1.write("Zero Framed Array after pass 2 with padding (4 connectness): \n");
    ccObj.connect4Pass2();
    ccObj.imageReformat( ccObj.zeroFramedAry, output1);
    output1.write("Equivalence Table after pass 2 (4 connectness): \n");
    ccObj.printEQAry(ccObj.newLabel, output1);
}

else if( connectness == 8 ) {
    ccObj.connect8Pass1();
    output1.write("Zero Framed Array after pass 1 with padding (8 connectness): \n");
    ccObj.imageReformat( ccObj.zeroFramedAry, output1);
    output1.write("Equivalence Table after pass 1 (8 connectness): \n");
    ccObj.printEQAry(ccObj.newLabel, output1);
    output1.write("Zero Framed Array after pass 2 with padding (8 connectness): \n");
    ccObj.connect8Pass2();
    ccObj.imageReformat( ccObj.zeroFramedAry, output1);
    output1.write("Equivalence Table after pass 2 (8 connectness): \n");
    ccObj.printEQAry(ccObj.newLabel, output1);
}

int trueNumCC = ccObj.manageEqAry();
output1.write("Equivalence Table after Management: \n");
ccObj.printEQAry(ccObj.newLabel, output1);
ccObj.connectPass3(trueNumCC);
output1.write("Zero Framed Array after pass 3: \n");
ccObj.imageReformat( ccObj.zeroFramedAry, output1);
output1.write("Equivalence Table after pass 3: \n");
ccObj.printEQAry(ccObj.newLabel, output1);
ccObj.printImg(ccObj.zeroFramedAry, output2);
ccObj.printCCproperty(ccObj.propertyFiles, output3);
ccObj.drawBoxes(ccObj.zeroFramedAry, ccObj.propertyFiles);
output1.write("Zero Framed Array after Drawing Boxes: \n");
ccObj.imageReformat( ccObj.zeroFramedAry, output1);

finally {
    if( input != null ) input.close() ;
    if( output1 != null ) output1.close();
    if( output2 != null ) output2.close();
    if( output3 != null ) output3.close();
}

```

CCLabel Class

Constructor

```

public class CCLabel {
    public int numRows, numCols, minVal, maxVal, newMin, newMax, newLabel, trueNumCC;
    public int[][] zeroFramedAry;
    public int[] nonZeroNeighborAry, eqAry;
    public Property[] propertyFiles;

    public CCLabel(int rows, int cols, int min, int max){
        this.numRows = rows;
        this.numCols = cols;
        this.minVal = min;
        this.maxVal = max;
        this.newMin = 99999;
        this.newMax = 0;
        this.newLabel = 0;
        this.nonZeroNeighborAry = new int[5];

        int eqSize = (this.numRows * this.numCols)/4;
        this.eqAry = new int[ eqSize ];
        for(int i = 0; i < eqSize; i++) {
            eqAry[i] = i;
        }

        this.zeroFramedAry = new int[this.numRows + 2][this.numCols + 2];
        zero2D(this.numRows + 2, this.numCols + 2, this.zeroFramedAry);
    }
}

```

Zero2D, minus1D, loadImage

```

public void zero2D(int r, int c, int[][]ary) {
    for(int i = 0; i < r; i++) {
        for(int j = 0; j < c; j++) {
            ary[i][j] = 0;
        }
    }
}

public void minus1D(int size, int[] ary) {
    for(int i = 0; i < size; i++) {
        ary[i] = -1;
    }
}

public void loadImage(int[][] ary, Scanner input) {
    for(int i = 1; i < this.numRows + 1; ++i) {
        for(int j = 1; j < this.numCols + 1; ++j) {
            if( input.hasNextInt() )
                ary[i][j] = input.nextInt();
        }
    }
}

```

Connect4pass1

```

public void connect4Pass1() {
    for(int i = 1; i < this.numRows + 1; i++) {
        for(int j = 1; j < this.numCols + 1; j++) {
            if( this.zeroFramedAry[i][j] > 0 ) {
                int a = this.zeroFramedAry[i-1][j];
                int b = this.zeroFramedAry[i][j-1];
                // Case 1:
                if( a == 0 && b == 0 ) {
                    this.newLabel++;
                    this.zeroFramedAry[i][j] = this.newLabel;
                }
                // Case 2:
                else if( a != 0 && b != 0 ) {
                    int min = Math.min(a, b);
                    int max = Math.max(a, b);
                    this.zeroFramedAry[i][j] = min;
                    this.eqAry[ max ] = min;
                }
                // Case 3:
                else if( a != 0 || b != 0 ) {
                    if( a == 0 ) this.zeroFramedAry[i][j] = b;
                    else this.zeroFramedAry[i][j] = a;
                }
            }
        }
    }
}

```

Connect4Pass2

```

public void connect4Pass2() {
    for(int i = this.numRows + 1; i > 0; i--) {
        for(int j = this.numCols + 1; j > 0; j--) {

            int p = this.zeroFramedAry[i][j];
            if(p > 0) {
                int c = this.zeroFramedAry[i][j+1];
                int d = this.zeroFramedAry[i+1][j];

                case 1:
                if( c == 0 && d == 0);
                case 2:
                else if( c == d && d == p);
                case 3:
                else if(((p != c && p != d) ||
                    (c != d && c != p) ||
                    (d != p && d != c)) &&
                    (c != 0 && d != 0)) {
                    int min = Math.min(Math.min(c, d), p);
                    if( p > min) {
                        this.eqAry[p] = min;
                        this.zeroFramedAry[i][j] = min;
                    }
                }
                step 3
            else {
                this.zeroFramedAry[i][j] = this.eqAry[p];
            }
        }
    }
}

```

Connect8Pass1

```

public void connect8Pass1() {
    for(int i = 1; i < this.numRows + 1; i++) {
        for(int j = 1; j < this.numCols + 1; j++) {
            if( this.zeroFramedAry[i][j] > 0 ) {

                int a = this.zeroFramedAry[i-1][j-1];
                int b = this.zeroFramedAry[i-1][j];
                int c = this.zeroFramedAry[i-1][j+1];
                int d = this.zeroFramedAry[i][j-1];

                Case 1:
                if( a == b && b == c && c == d && d == 0 ) {
                    this.newLabel++;
                    this.zeroFramedAry[i][j] = this.newLabel;
                }

                else if( a != 0 || b != 0 || c != 0 || d != 0 ) {

                    int[] arr = {a,b,c,d};
                    HashSet<Integer> labels = new HashSet<Integer>();

                    for(int k = 0; k < 4; k++)
                        labels.add(arr[k]);

                    ignore zeroes
                    labels.remove(0);
                    if(labels.size() == 1) {
                        case 2:
                        for(int n : labels)
                            this.zeroFramedAry[i][j] = n;
                    }else {
                        case 3:
                        int min = 999999;
                        int max = 0;
                        for(int n : labels) {
                            if(n < min) min = n;
                            if(n > max) max = n;
                        }
                        this.zeroFramedAry[i][j] = min;
                        this.eqAry[ max ] = min;
                    }
                }
            }
        }
    }
}

```

Connect8Pass2

```

public void connect8Pass2() {
    for(int i = this.numRows + 1; i > 0; i--) {
        for(int j = this.numCols + 1; j > 0; j--) {
            int p = this.zeroFramedAry[i][j];
            if(p > 0) {
                int e = this.zeroFramedAry[i][j+1];
                int f = this.zeroFramedAry[i+1][j-1];
                int g = this.zeroFramedAry[i+1][j];
                int h = this.zeroFramedAry[i+1][j+1];

                case 1:
                if( e == f && f == g && g == h && h == 0);
                case 2:
                else if( e != 0 || f != 0 || g != 0 || h != 0 ) {
                    int[] arr = {e,f,g,h};
                    HashSet<Integer> labels = new HashSet<Integer>();
                    for(int k = 0; k < 4; k++)
                        labels.add(arr[k]);
                    ignore zeroes
                    labels.remove(0);

                    case 2 bypassed with > 1
                    if(labels.size() > 1) {
                        case 3:
                        int min = 999999;
                        int max = 0;
                        for(int n : labels) {
                            if(n < min) min = n;
                            if(n > max) max = n;
                        }
                        this.zeroFramedAry[i][j] = min;
                        this.eqAry[ max ] = min;
                    }
                }
            }
            else {
                this.zeroFramedAry[i][j] = this.eqAry[p];
            }
        }
    }
}

```


connectPass3

```

public void connectPass3(int numCC) {

    this.propertyFiles = new Property[numCC + 1];
    for(int i = 0; i <= numCC; i++) {
        propertyFiles[i] = new Property();
    }

    for(int i = 1; i < this.numRows + 2; i++) {
        for(int j = 1; j < this.numCols + 2; j++) {
            int p = this.zeroFramedAry[i][j];
            if( p > 0) {
                this.zeroFramedAry[i][j] = this.eqAry[p];
                p = this.zeroFramedAry[i][j];
                if (p < this.newMin) this.newMin = p;
                if (p > this.newMax) this.newMax = p;
                propertyFiles[p].setLabel(p);
                propertyFiles[p].incPixels();

                if(propertyFiles[p].minR > i) propertyFiles[p].setMinR(i);
                if(propertyFiles[p].minC > j) propertyFiles[p].setMinC(j);
                if(propertyFiles[p].maxR < i) propertyFiles[p].setMaxR(i);
                if(propertyFiles[p].maxC < j) propertyFiles[p].setMaxC(j);
            }
        }
    }
}

```

manageEqAry

```

public int manageEqAry() {
    int readLabel = 0;
    int index = 1;

    while( index <= this.newLabel) {
        if( index != this.eqAry[index] ) this.eqAry[index] = this.eqAry[ this.eqAry[index] ];

        else {
            readLabel++;
            this.eqAry[index] = readLabel;
        }
        index++;
    }
    this.trueNumCC = readLabel;
    return this.trueNumCC;
}

```

PrintEQAry, printImg, printCCproperty

```

public void printEQAry(int label, BufferedWriter output) throws IOException {
    for(int i = 0; i < label; i++) {
        output.write(i + " ");
        output.write(this.eqAry[i] + "\n");
    }
    output.write("\n\n");
}

public void printImg(int[][] ary, BufferedWriter output) throws IOException{
    output.write( this.numRows + " ");
    output.write( this.numCols + " ");
    output.write( this.minVal + " ");
    output.write( this.trueNumCC + "\n" );

    for(int i = 1; i < this.numRows + 1; ++i) {
        for(int j = 1; j < this.numCols + 1; ++j) {
            int numDigits = getNumDigits(this.newLabel);
            int modSize = (int) Math.pow(10, numDigits);
            if( (ary[i][j] != 0) && (modSize % ary[i][j] < modSize) ) {
                int modDigits = getNumDigits(modSize);
                numDigits = getNumDigits(ary[i][j]);
                for(int k = 0; k < modDigits - numDigits; k++) {
                    output.write(" ");
                }
            }else if( ary[i][j] == 0) {
                int modDigits = getNumDigits(modSize);
                for(int k = 0; k < modDigits - 1; k++) {
                    output.write(" ");
                }
            }
            output.write( ary[i][j] + " ");
        }
        output.write("\n");
    }
}

public void printCCproperty(Property[] propertyFile, BufferedWriter output) throws IOException {
    output.write( this.numRows + " ");
    output.write( this.numCols + " ");
    output.write( this.newMin + " ");
    output.write( this.newMax + "\n" );
    output.write( this.trueNumCC + "\n" );

    for(int i = 1; i <= this.trueNumCC; i++) {
        Property cc = propertyFile[i];
        output.write(cc.label + "\n");
        output.write(cc.numPixels + "\n");
        output.write(cc.minR + " " + cc.minC + "\n");
        output.write(cc.maxR + " " + cc.maxC + "\n");
    }
}

```

imageReformat

```

public void imageReformat(int[][] ary, BufferedWriter output) throws IOException {
    for(int i = 1; i < this.numRows + 1; ++i) {
        for(int j = 1; j < this.numCols + 1; ++j) {
            int numDigits = getNumDigits(this.newLabel);
            int modSize = (int) Math.pow(10, numDigits);
            if( (ary[i][j] != 0) && (modSize % ary[i][j] < modSize) ) {
                int modDigits = getNumDigits(modSize);
                numDigits = getNumDigits(ary[i][j]);
                for(int k = 0; k < modDigits - numDigits; k++) {
                    output.write(" ");
                }
            }
            if( ary[i][j] == 0 ) {
                int modDigits = getNumDigits(modSize);
                for(int k = 0; k < modDigits - 1; k++) {
                    output.write(" ");
                }
            }
            output.write(". ");
        }
        output.write("\n");
    }
}

```

drawBoxes

```

public void drawBoxes(int[][] ary, Property[] propertyFile) {

    for(int i = 1; i <= this.trueNumCC; i++) {
        Property cc = propertyFile[i];
        int minRow = cc.minR;
        int minCol = cc.minC;
        int maxRow = cc.maxR;
        int maxCol = cc.maxC;
        int label = cc.label;

        left to right on top and bottom
        while(minCol <= maxCol) {
            ary[minRow][minCol] = label;
            ary[maxRow][minCol] = label;
            minCol++;
        }

        minCol = cc.minC;
        top to bottom on left and right
        while(minRow <= maxRow) {
            ary[minRow][minCol] = label;
            ary[minRow][maxCol] = label;
            minRow++;
        }
    }
}

```

Property Class

```
package Project_5;

public class Property {
    public int label, numPixels, minR, minC, maxR, maxC;

    public Property() {
        this.label = 0;
        this.numPixels = 0;
        this.minR = 99999;
        this.minC = 99999;
        this.maxR = 0;
        this.maxC = 0;
    }

    public void setLabel(int val) {
        this.label = val;
    }

    public void incPixels() {
        this.numPixels++;
    }

    public void setMinR(int val) {
        this.minR = val;
    }

    public void setMinC(int val) {
        this.minC = val;
    }

    public void setMaxC(int val) {
        this.maxC = val;
    }

    public void setMaxR(int val) {
        this.maxR = val;
    }
}
```


Equivalence Table after pass 1 (4 connectness):

| | |
|----|----|
| 0 | 0 |
| 1 | 1 |
| 2 | 2 |
| 3 | 3 |
| 4 | 3 |
| 5 | 5 |
| 6 | 5 |
| 7 | 7 |
| 8 | 5 |
| 9 | 9 |
| 10 | 10 |
| 11 | 1 |
| 12 | 12 |
| 13 | 13 |
| 14 | 14 |
| 15 | 13 |
| 16 | 16 |
| 17 | 13 |
| 18 | 18 |
| 19 | 19 |
| 20 | 17 |
| 21 | 21 |
| 22 | 22 |
| 23 | 23 |
| 24 | 24 |
| 25 | 23 |
| 26 | 25 |
| 27 | 27 |
| 28 | 22 |
| 29 | 29 |
| 30 | 30 |
| 31 | 31 |
| 32 | 31 |
| 33 | 24 |
| 34 | 24 |
| 35 | 35 |
| 36 | 36 |

Zero Framed Array after pass 2 with padding (4 connectness):

[illegible]

Equivalence Table after pass 2 (4 connectness):

| | |
|----|----|
| 0 | 0 |
| 1 | 1 |
| 2 | 2 |
| 3 | 3 |
| 4 | 3 |
| 5 | 4 |
| 6 | 5 |
| 7 | 7 |
| 8 | 3 |
| 9 | 9 |
| 10 | 10 |
| 11 | 1 |
| 12 | 12 |
| 13 | 13 |
| 14 | 14 |
| 15 | 13 |
| 16 | 16 |
| 17 | 13 |
| 18 | 18 |
| 19 | 19 |
| 20 | 13 |
| 21 | 21 |
| 22 | 22 |
| 23 | 23 |
| 24 | 24 |
| 25 | 23 |
| 26 | 25 |
| 27 | 27 |
| 28 | 22 |
| 29 | 29 |
| 30 | 30 |
| 31 | 31 |
| 32 | 31 |
| 33 | 24 |
| 34 | 24 |
| 35 | 35 |
| 36 | 36 |

Equivalence Table after Management:

| | |
|----|----|
| 0 | 0 |
| 1 | 1 |
| 2 | 2 |
| 3 | 3 |
| 4 | 3 |
| 5 | 3 |
| 6 | 3 |
| 7 | 4 |
| 8 | 3 |
| 9 | 5 |
| 10 | 6 |
| 11 | 1 |
| 12 | 7 |
| 13 | 8 |
| 14 | 9 |
| 15 | 8 |
| 16 | 10 |
| 17 | 8 |
| 18 | 11 |
| 19 | 12 |
| 20 | 8 |
| 21 | 13 |
| 22 | 14 |
| 23 | 15 |
| 24 | 16 |
| 25 | 15 |
| 26 | 15 |
| 27 | 17 |
| 28 | 14 |
| 29 | 18 |
| 30 | 19 |
| 31 | 20 |
| 32 | 20 |
| 33 | 16 |
| 34 | 16 |
| 35 | 21 |
| 36 | 22 |

[illegible]

Equivalence Table after pass 3:

| | |
|----|----|
| 0 | 0 |
| 1 | 1 |
| 2 | 2 |
| 3 | 3 |
| 4 | 3 |
| 5 | 3 |
| 6 | 3 |
| 7 | 4 |
| 8 | 3 |
| 9 | 5 |
| 10 | 6 |
| 11 | 1 |
| 12 | 7 |
| 13 | 8 |
| 14 | 9 |
| 15 | 8 |
| 16 | 10 |
| 17 | 8 |
| 18 | 11 |
| 19 | 12 |
| 20 | 8 |
| 21 | 13 |
| 22 | 14 |
| 23 | 15 |
| 24 | 16 |
| 25 | 15 |
| 26 | 15 |
| 27 | 17 |
| 28 | 14 |
| 29 | 18 |
| 30 | 19 |
| 31 | 20 |
| 32 | 20 |
| 33 | 16 |
| 34 | 16 |
| 35 | 21 |
| 36 | 22 |

Zero Framed Array after Drawing Boxes:

[illegible]

Data 2 4 connectness: labelFile

[illegible]

Data 2 4 connectness: propertyFile

| | | |
|------------|-------|-------|
| | 11 | |
| | 4 | |
| 30 35 1 23 | 16 32 | |
| 23 | 17 33 | |
| 1 | 12 | |
| 44 | 1 | |
| 2 6 | 17 8 | |
| 13 15 | 17 8 | |
| 2 | 13 | |
| 4 | 1 | |
| 2 31 | 18 7 | |
| 4 32 | 18 7 | |
| 3 | 14 | |
| 37 | 31 | |
| 3 23 | 19 4 | |
| 11 31 | 30 8 | |
| 4 | 15 | |
| 1 | 8 | |
| 8 6 | 19 8 | |
| 8 6 | 23 11 | |
| 5 | 16 | |
| 1 | 33 | |
| 9 7 | 19 28 | |
| 9 7 | 30 33 | |
| 6 | 17 | |
| 1 | 1 | |
| 10 8 | 21 13 | |
| 10 8 | 21 13 | |
| 7 | 18 | |
| 1 | 3 | |
| 14 11 | 22 14 | |
| 14 11 | 24 14 | |
| 8 | 19 | |
| 73 | 5 | |
| 14 17 | 25 15 | |
| 29 25 | 29 15 | |
| 9 | 20 | 22 |
| 1 | 9 | 1 |
| 15 10 | 26 9 | 30 16 |
| 15 10 | 30 11 | 30 16 |
| 10 | 21 | 23 |
| 1 | 1 | 1 |
| 16 9 | 30 14 | 30 25 |
| 16 9 | 30 14 | 30 25 |

Equivalence Table after pass 2 (8 connectness):

| | |
|----|----|
| 0 | 0 |
| 1 | 1 |
| 2 | 2 |
| 3 | 2 |
| 4 | 1 |
| 5 | 5 |
| 6 | 6 |
| 7 | 1 |
| 8 | 1 |
| 9 | 9 |
| 10 | 10 |
| 11 | 11 |

Equivalence Table after Management:

| | |
|----|---|
| 0 | 0 |
| 1 | 1 |
| 2 | 2 |
| 3 | 2 |
| 4 | 1 |
| 5 | 3 |
| 6 | 4 |
| 7 | 1 |
| 8 | 1 |
| 9 | 5 |
| 10 | 6 |
| 11 | 7 |

Zero Framed after pass 3

Zero Framed Array after pass 3:

[illegible]

Equivalence Table after pass 3:

| | |
|----|---|
| 0 | 0 |
| 1 | 1 |
| 2 | 2 |
| 3 | 2 |
| 4 | 1 |
| 5 | 3 |
| 6 | 4 |
| 7 | 1 |
| 8 | 1 |
| 9 | 5 |
| 10 | 6 |
| 11 | 7 |

Zero Framed Array after Drawing Boxes:

[illegible]

Data 2 8 connectness: labelFile

[illegible]

Data 2 8 connectness: propertyFile

```
30 35 1 7
7
1
91
2 4
30 15
2
41
2 23
11 32
3
74
14 17
30 25
4
4
16 32
17 33
5
33
19 28
30 33
6
11
21 13
30 16
7
9
26 9
30 11
```

Data 3 4 connectness: prettyPrintFile

Original Image:

[illegible]

Zero Framed Array after pass 1

Zero Framed Array after pass 1 with padding (4 connectness):

[illegible]

Equivalence Table after pass 1

| | | | |
|----|----|-----|-----|
| 0 | 0 | | |
| 1 | 1 | | |
| 2 | 2 | | |
| 3 | 3 | | |
| 4 | 4 | 50 | 50 |
| 5 | 1 | 51 | 47 |
| 6 | 2 | 52 | 52 |
| 7 | 5 | 53 | 50 |
| 8 | 5 | 54 | 54 |
| 9 | 9 | 55 | 50 |
| 10 | 4 | 56 | 56 |
| 11 | 11 | 57 | 57 |
| 12 | 12 | 58 | 58 |
| 13 | 13 | 59 | 59 |
| 14 | 14 | 60 | 60 |
| 15 | 15 | 61 | 61 |
| 16 | 16 | 62 | 62 |
| 17 | 17 | 63 | 63 |
| 18 | 10 | 64 | 64 |
| 19 | 19 | 65 | 65 |
| 20 | 14 | 66 | 66 |
| 21 | 16 | 67 | 67 |
| 22 | 14 | 68 | 65 |
| 23 | 16 | 69 | 69 |
| 24 | 24 | 70 | 70 |
| 25 | 16 | 71 | 71 |
| 26 | 5 | 72 | 72 |
| 27 | 27 | 73 | 73 |
| 28 | 28 | 74 | 74 |
| 29 | 29 | 75 | 75 |
| 30 | 30 | 76 | 76 |
| 31 | 31 | 77 | 77 |
| 32 | 32 | 78 | 63 |
| 33 | 33 | 79 | 79 |
| 34 | 30 | 80 | 80 |
| 35 | 35 | 81 | 81 |
| 36 | 32 | 82 | 75 |
| 37 | 37 | 83 | 83 |
| 38 | 33 | 84 | 76 |
| 39 | 39 | 85 | 85 |
| 40 | 39 | 86 | 63 |
| 41 | 16 | 87 | 87 |
| 42 | 31 | 88 | 88 |
| 43 | 43 | 89 | 84 |
| 44 | 44 | 90 | 76 |
| 45 | 45 | 91 | 91 |
| 46 | 46 | 92 | 92 |
| 47 | 44 | 93 | 89 |
| 48 | 48 | 94 | 86 |
| 49 | 49 | 95 | 79 |
| | | 96 | 96 |
| | | 97 | 97 |
| | | 98 | 94 |
| | | 99 | 63 |
| | | 100 | 95 |
| | | 101 | 101 |
| | | 102 | 100 |
| | | 103 | 103 |

Zero Framed Array after pass 2

Zero Framed Array after pass 2 with padding (4 connectness):

```
. . . . . 1 . . . . . 2 . . . . 3 . . . . . 4 .
. 1 . . . . 1 . . . . . 2 . . . . 3 3 . . . . . 4 .
5 1 1 . . 1 1 1 . . . . . 2 2 . . . . 3 3 . 9 9 9 9 . . . 4 4 .
. . 1 1 1 1 1 1 1 . . . . . 11 . . . . 12 . . . 9 13 . . 4 4 .
. . 1 1 1 1 1 . 1 1 . . . . . 14 14 14 14 . . 15 . . . 16 . 17 . 10 10 . .
. 19 . 1 1 . 1 1 1 1 . . . . . 14 14 14 14 14 . . 15 . . . 16 . 16 . 18 . .
. . 1 1 1 1 1 1 1 . . . . . 14 14 14 14 14 14 . 15 . . . 16 . 16 16 16 . .
. 24 . . 1 1 1 1 1 . . . . . 14 . 14 14 14 14 14 . . . 16 16 16 16 16 16 . .
. . 1 . . 1 1 1 . . . . . 14 14 14 14 14 14 . 27 . . . 16 16 16 16 16 16 . .
. . 1 1 1 1 1 . 28 28 . . . . . 29 . 14 14 . 14 14 . 30 . 27 27 . . 16 16 . 16 16 16 16 . .
. . . 1 1 1 1 1 . 28 . 31 . . . 32 . 33 . 14 14 14 . 30 30 . 27 . . 16 16 16 . 16 16 16 16 .
. . 35 . 26 . 1 . . . 31 31 . 32 32 . 33 . 14 . 37 . 30 . . . . 16 16 16 16 16 16 .
. . . . . . . 31 31 . . . . . 39 . 39 . . . . . 16 16 16 . 16 16 16 . .
. . . . . . . 31 31 . . . . . 39 39 39 . . 43 . . . . 44 44 44 . 41 . . . . .
. . . . . . . 45 . . . . 46 . . . . . . . . 44 44 44 . . . . . 48 48 .
. . . . . 49 . . . . . 50 50 50 . . . . . 44 44 44 . 44 44 44 . . . . . 48 48 .
. . . . . 52 . . . . . 50 50 50 50 . . . . . 44 44 44 44 44 44 44 . . . . .
. . . . . 54 . . . . . 50 50 50 50 50 . . . . . 47 44 44 44 44 44 . . . . .
. . . . . 56 . . 57 . . . 50 50 50 50 . . . . . 58 . . 44 44 . 44 44 . . . . .
59 59 59 . . 60 . 61 61 . 50 50 50 50 50 50 . . . . . 62 . . 44 44 44 . 63 63 63 63 . . 64 64 .
. . 59 . 65 . . 61 . . 50 50 50 50 50 . . 66 . . . . . 67 . . 44 . . 63 . 63 63 . . 64 64 64
. . . 65 65 . . 69 . 70 . 50 50 50 . . 66 66 . . . . 71 . 72 . . 63 . 63 63 . . .
. 73 . . 65 65 . . . 74 . . . . 75 . . . . 76 . . 72 . . 77 77 . 63 . 63 63 . 63 . .
. . . . 79 . 80 . 81 . . . 75 75 . 83 . 76 76 76 . 76 . 85 . . 63 63 63 63 . .
. 87 . 88 88 . 79 79 . . . . 82 . . . 76 76 . 76 76 . 76 . 91 . 63 63 63 . .
. 87 87 . . 79 . . . . . 92 . . 76 76 76 76 76 76 76 76 . . 63 63 63 63 . .
. . 87 87 . 79 79 79 96 . . . . 97 . 76 76 76 76 76 76 76 . . 63 63 63 63 . 63 .
. . . 79 79 79 79 . . . . . 101 . . 89 76 76 . 76 76 76 . . 63 63 63 63 63 63 63 .
. . 100 100 95 79 79 79 79 79 . . . . . 101 . 103 . 84 76 76 76 76 . . . 94 94 . 63 63 63 63 . 104
```

Equivalence table after pass 2

| | | | |
|----|----|-----|-----|
| | | 50 | 50 |
| | | 51 | 44 |
| 0 | 0 | 52 | 52 |
| 1 | 1 | 53 | 50 |
| 2 | 2 | 54 | 54 |
| 3 | 3 | 55 | 50 |
| 4 | 4 | 56 | 56 |
| 5 | 1 | 57 | 57 |
| 6 | 2 | 58 | 58 |
| 7 | 5 | 59 | 59 |
| 8 | 1 | 60 | 60 |
| 9 | 9 | 61 | 61 |
| 10 | 4 | 62 | 62 |
| 11 | 11 | 63 | 63 |
| 12 | 12 | 64 | 64 |
| 13 | 13 | 65 | 65 |
| 14 | 14 | 66 | 66 |
| 15 | 15 | 67 | 67 |
| 16 | 16 | 68 | 65 |
| 17 | 17 | 69 | 69 |
| 18 | 10 | 70 | 70 |
| 19 | 19 | 71 | 71 |
| 20 | 14 | 72 | 72 |
| 21 | 16 | 73 | 73 |
| 22 | 14 | 74 | 74 |
| 23 | 16 | 75 | 75 |
| 24 | 24 | 76 | 76 |
| 25 | 16 | 77 | 77 |
| 26 | 1 | 78 | 63 |
| 27 | 27 | 79 | 79 |
| 28 | 28 | 80 | 80 |
| 29 | 29 | 81 | 81 |
| 30 | 30 | 82 | 75 |
| 31 | 31 | 83 | 83 |
| 32 | 32 | 84 | 76 |
| 33 | 33 | 85 | 85 |
| 34 | 30 | 86 | 63 |
| 35 | 35 | 87 | 87 |
| 36 | 32 | 88 | 88 |
| 37 | 37 | 89 | 76 |
| 38 | 33 | 90 | 76 |
| 39 | 39 | 91 | 91 |
| 40 | 39 | 92 | 92 |
| 41 | 16 | 93 | 76 |
| 42 | 31 | 94 | 63 |
| 43 | 43 | 95 | 79 |
| 44 | 44 | 96 | 96 |
| 45 | 45 | 97 | 97 |
| 46 | 46 | 98 | 63 |
| 47 | 44 | 99 | 63 |
| 48 | 48 | 100 | 79 |
| 49 | 49 | 101 | 101 |
| | | 102 | 100 |
| | | 103 | 103 |

Equivalence Table after management

| | | | |
|----|----|-----|----|
| 0 | 0 | | |
| 1 | 1 | 51 | 26 |
| 2 | 2 | 52 | 32 |
| 3 | 3 | 53 | 31 |
| 4 | 4 | 54 | 33 |
| 5 | 1 | 55 | 31 |
| 6 | 2 | 56 | 34 |
| 7 | 1 | 57 | 35 |
| 8 | 1 | 58 | 36 |
| 9 | 5 | 59 | 37 |
| 10 | 4 | 60 | 38 |
| 11 | 6 | 61 | 39 |
| 12 | 7 | 62 | 40 |
| 13 | 8 | 63 | 41 |
| 14 | 9 | 64 | 42 |
| 15 | 10 | 65 | 43 |
| 16 | 11 | 66 | 44 |
| 17 | 12 | 67 | 45 |
| 18 | 4 | 68 | 43 |
| 19 | 13 | 69 | 46 |
| 20 | 9 | 70 | 47 |
| 21 | 11 | 71 | 48 |
| 22 | 9 | 72 | 49 |
| 23 | 11 | 73 | 50 |
| 24 | 14 | 74 | 51 |
| 25 | 11 | 75 | 52 |
| 26 | 1 | 76 | 53 |
| 27 | 15 | 77 | 54 |
| 28 | 16 | 78 | 41 |
| 29 | 17 | 79 | 55 |
| 30 | 18 | 80 | 56 |
| 31 | 19 | 81 | 57 |
| 32 | 20 | 82 | 52 |
| 33 | 21 | 83 | 58 |
| 34 | 18 | 84 | 53 |
| 35 | 22 | 85 | 59 |
| 36 | 20 | 86 | 41 |
| 37 | 23 | 87 | 60 |
| 38 | 21 | 88 | 61 |
| 39 | 24 | 89 | 53 |
| 40 | 24 | 90 | 53 |
| 41 | 11 | 91 | 62 |
| 42 | 19 | 92 | 63 |
| 43 | 25 | 93 | 53 |
| 44 | 26 | 94 | 41 |
| 45 | 27 | 95 | 55 |
| 46 | 28 | 96 | 64 |
| 47 | 26 | 97 | 65 |
| 48 | 29 | 98 | 41 |
| 49 | 30 | 99 | 41 |
| 50 | 31 | 100 | 55 |
| | | 101 | 66 |
| | | 102 | 55 |
| | | 103 | 67 |
| | | 101 | 66 |

Zero Framed Array after pass 3

Zero Framed Array after pass 3:

```

. . . . . 1 . . . . . 2 . . . . 3 . . . . . 4 .
. 1 . . . . 1 . . . . . 2 . . . . 3 3 . . . .
1 1 1 . . 1 1 1 . . . . 2 2 . . . 3 3 . 5 5 .
. . 1 1 1 1 1 1 1 . . . . 6 . . . 7 . . . 5 5 .
. . 1 1 1 1 . 1 1 1 . . . . 9 9 9 . . . 10 . . 11 . 12 . 8 . 4 4 .
. 13 . 1 1 . 1 1 1 1 . . . . 9 9 9 9 9 . . 10 . . 11 . 11 . 11 . 4 .
. . 1 1 1 1 1 1 1 . . . . 9 9 9 9 9 9 . 10 . . 11 . 11 11 11 .
. 14 . . 1 1 1 1 1 . . . . 9 . 9 9 9 . 9 9 9 . 15 . . 11 11 11 11 11 11 .
. . 1 . . 1 1 1 . . . . 9 9 9 9 9 9 . 15 . . . . 11 11 11 11 11 11 .
. . 1 1 1 1 1 . 16 16 . . . . 17 . 9 9 . 9 9 . 18 18 . 15 15 . . 11 11 . 11 11 11 11 .
. . . 1 1 1 1 . 16 . 19 . . . 20 20 . 21 . 9 9 9 . 18 18 . 15 . . . 11 11 . 11 11 11 11 .
. . 22 . 1 . 1 . . . 19 19 . 20 20 . 21 . 9 . 23 . 18 . . . . 11 11 11 11 11 11 .
. . . . . . . . 19 . 20 . 21 21 . 24 . 24 . 25 . . . 11 11 . 11 11 11 .
. . . . . . . . 19 19 . . . . . . . 24 24 24 . . 25 . . . 11 . . . .
. . . . . . . . 27 . . . . 28 . . . . . . . 26 26 26 26 . . . . 29 29 .
. . . . . . . . . . 31 31 31 . . . . . . . 26 26 26 . 26 26 26 . . . . 29 29 .
. . . . . . . . . . 31 31 31 31 31 . . . . . . . 26 26 26 26 26 26 . . . .
. . . . . 33 . . . . 31 31 31 31 31 31 . . . . . . . 26 26 26 26 26 26 . . . .
. . . . 34 . . . . 31 . 31 31 31 . 31 . . . . . . . 26 26 . 26 26 . . . .
37 37 37 . . 38 . 39 39 . 31 31 31 31 31 31 31 . . . . . 36 . . 26 26 26 . 41 41 41 41 . 42 42
. . 37 . 43 . . 39 . . 31 31 31 31 31 . . . . . . . 44 . . 45 . 26 . . 41 . 41 41 . 42 42
. . . 43 43 . . 46 . 47 . . 31 31 31 . . . . 44 44 . . 48 . 49 . . 41 . 41 41 .
. 50 . . 43 43 . . . . 51 . . . . 52 . . . . 53 . . 49 . . 54 54 . 41 . 41 . 41 .
. . . . . 55 . 56 . . 57 . . . . 52 52 . 58 . 53 53 53 . . 59 . . . 41 41 41 41 .
. 60 . 61 61 . 55 55 . . . . 52 . . . 53 53 . 53 53 . 53 . . . 41 41 41 41 .
. 60 60 . . 55 . . . . . 53 53 53 53 53 53 53 53 . . . 41 41 41 41 41 .
. . 60 60 . 55 55 55 . 64 . . . . . 65 . 53 53 53 53 53 53 53 . . . 41 41 41 41 41
. . . 55 55 55 55 . . . . . 66 . . 53 53 53 . 53 53 53 . . . 41 41 41 41 41
. . 55 55 55 55 55 55 55 . . . . . 66 . 67 . 53 53 53 53 53 . . . 41 41 . 41 41 41

```

Equivalence Table after pass 3

| | | | | |
|----|----|----|----|--------|
| | | 48 | 29 | |
| | | 49 | 30 | |
| | | 50 | 31 | |
| 0 | 0 | 51 | 26 | |
| 1 | 1 | 52 | 32 | |
| 2 | 2 | 53 | 31 | |
| 3 | 3 | 54 | 33 | |
| 4 | 4 | 55 | 31 | |
| 5 | 1 | 56 | 34 | |
| 6 | 2 | 57 | 35 | |
| 7 | 1 | 58 | 36 | |
| 8 | 1 | 59 | 37 | |
| 9 | 5 | 60 | 38 | |
| 10 | 4 | 61 | 39 | |
| 11 | 6 | 62 | 40 | |
| 12 | 7 | 63 | 41 | |
| 13 | 8 | 64 | 42 | |
| 14 | 9 | 65 | 43 | |
| 15 | 10 | 66 | 44 | |
| 16 | 11 | 67 | 45 | |
| 17 | 12 | 68 | 43 | |
| 18 | 4 | 69 | 46 | |
| 19 | 13 | 70 | 47 | |
| 20 | 9 | 71 | 48 | |
| 21 | 11 | 72 | 49 | |
| 22 | 9 | 73 | 50 | |
| 23 | 11 | 74 | 51 | |
| 24 | 14 | 75 | 52 | |
| 25 | 11 | 76 | 53 | |
| 26 | 1 | 77 | 54 | |
| 27 | 15 | 78 | 41 | |
| 28 | 16 | 79 | 55 | |
| 29 | 17 | 80 | 56 | |
| 30 | 18 | 81 | 57 | |
| 31 | 19 | 82 | 52 | |
| 32 | 20 | 83 | 58 | |
| 33 | 21 | 84 | 53 | |
| 34 | 18 | 85 | 59 | |
| 35 | 22 | 86 | 41 | |
| 36 | 20 | 87 | 60 | |
| 37 | 23 | 88 | 61 | |
| 38 | 21 | 89 | 53 | |
| 39 | 24 | 90 | 53 | |
| 40 | 24 | 91 | 62 | |
| 41 | 11 | 92 | 63 | |
| 42 | 19 | 93 | 53 | 99 41 |
| 43 | 25 | 94 | 41 | 100 55 |
| 44 | 26 | 95 | 55 | 101 66 |
| 45 | 27 | 96 | 64 | 102 55 |
| 46 | 28 | 97 | 65 | 103 67 |
| 47 | 26 | 98 | 41 | |

Zero Framed Array with boxes drawn

Zero Framed Array after Drawing Boxes:

[illegible]

Data 3 4 connectness: labelFile

30 40 0 68

[illegible]

Data 3 4 connectness: propertyFile

| | | | | | |
|------------|-------|-------|-------|-------|-------|
| | 13 | | 37 | | |
| | 1 | | 4 | | |
| 30 40 1 68 | 6 2 | 25 | 21 1 | 49 | |
| 68 | 6 2 | 1 | 22 3 | 2 | |
| 1 | 14 | 14 24 | 38 | 23 26 | |
| 55 | 1 | 14 24 | 1 | 24 26 | |
| 1 1 | 8 2 | 26 | 21 6 | 50 | |
| 12 10 | 8 2 | 37 | 21 6 | 1 | |
| 2 | 15 | 15 25 | 39 | 24 2 | |
| 4 | 4 | 22 32 | 3 | 24 2 | |
| 1 23 | 9 26 | 27 | 21 8 | 51 | |
| 3 24 | 11 27 | 1 | 22 9 | 1 | |
| 3 | 16 | 16 8 | 40 | 24 11 | |
| 5 | 3 | 16 8 | 1 | 24 11 | |
| 1 28 | 10 9 | 28 | 21 24 | 52 | 61 |
| 3 29 | 11 10 | 1 | 21 24 | 4 | 2 |
| 4 | 17 | 16 12 | 41 | 24 17 | |
| 9 | 1 | 16 12 | 46 | 26 18 | 26 4 |
| 1 37 | 10 16 | 29 | 53 | | 26 5 |
| 6 39 | 10 16 | 4 | 21 31 | 36 | 62 |
| 5 | 18 | 16 38 | 30 39 | 24 19 | 1 |
| 5 | 4 | 17 39 | 42 | 30 27 | 26 32 |
| 3 31 | 10 23 | 30 | 5 | 54 | 26 32 |
| 4 34 | 12 24 | 1 | 21 38 | 2 | 63 |
| 6 | 19 | 17 7 | 22 40 | 24 29 | 1 |
| 1 | 7 | 31 | 43 | 24 30 | 27 16 |
| 4 25 | 11 10 | 35 | 5 | 55 | 27 16 |
| 4 25 | 15 12 | 17 11 | 22 4 | 20 | 64 |
| 7 | 20 | 23 17 | 24 6 | 25 3 | 1 |
| 1 | 4 | 32 | 44 | 30 10 | 28 10 |
| 4 30 | 11 14 | 1 | 3 | 56 | 28 10 |
| 4 30 | 13 15 | 18 6 | 22 19 | 1 | 65 |
| 8 | 21 | 18 6 | 23 20 | 25 9 | 1 |
| 1 | 4 | 33 | 45 | 25 9 | 28 18 |
| 4 35 | 11 16 | 1 | 1 | 57 | 28 18 |
| 4 35 | 13 17 | 19 5 | 22 25 | 1 | 66 |
| 9 | 22 | 19 5 | 22 25 | 25 12 | 2 |
| 37 | 1 | 34 | 46 | 58 | 29 17 |
| 5 17 | 12 3 | 1 | 1 | 1 | 30 17 |
| 12 25 | 12 3 | 20 4 | 23 8 | 25 20 | 67 |
| 10 | 23 | 20 4 | 23 8 | 25 20 | 1 |
| 3 | 1 | 35 | 47 | 59 | 30 19 |
| 5 26 | 12 22 | 1 | 1 | 1 | 30 19 |
| 7 26 | 12 22 | 20 7 | 23 10 | 25 28 | 68 |
| 11 | 24 | 20 7 | 23 10 | 25 28 | 1 |
| 47 | 5 | 36 | 48 | 60 | 30 40 |
| 5 30 | 13 19 | 1 | 1 | 5 | 30 40 |
| 14 39 | 14 21 | 20 23 | 23 24 | 26 2 | 28 4 |
| 12 | | 20 23 | 23 24 | 28 4 | |
| 1 | | | | | |
| 5 34 | | | | | |
| 5 34 | | | | | |

Data 3 8 connectness: prettyPrintFile

Original Image:

[illegible]

Zero Framed Array after pass 1

Zero Framed Array after pass 1 with padding (8 connectness):

[illegible]

Equivalence Table after pass 1 (8 connectness):

| | |
|----|----|
| 0 | 0 |
| 1 | 1 |
| 2 | 2 |
| 3 | 3 |
| 4 | 4 |
| 5 | 1 |
| 6 | 4 |
| 7 | 2 |
| 8 | 8 |
| 9 | 1 |
| 10 | 4 |
| 11 | 11 |
| 12 | 12 |
| 13 | 13 |
| 14 | 14 |
| 15 | 13 |
| 16 | 16 |
| 17 | 13 |
| 18 | 18 |
| 19 | 19 |
| 20 | 20 |
| 21 | 16 |
| 22 | 12 |
| 23 | 13 |
| 24 | 16 |
| 25 | 13 |
| 26 | 25 |
| 27 | 16 |
| 28 | 13 |

Zero framed after drawing boxes

Zero Framed Array after Drawing Boxes:

[illegible]

Data 3 8 connectness: labelFile

30 40 0 13

[illegible]

Data 3 8 connectness: propertyFile

```
30 40 1 13
13
1
103
1 1
23 17
2
68
1 14
14 27
3
7
1 28
4 31
4
62
1 30
14 39
5
1
6 2
6 2
6
1
14 24
14 24
7
85
15 25
30 40
8
52
16 1
30 12
9
4
16 38
17 39
10
50
20 17
30 30
11
5
21 38
22 40
12
8
22 16
27 20
13
1
24 2
24 2
```