

Exercise 1

$$\textcircled{1} \sum \vec{F}_{ext} = -m\vec{g}$$

$$\textcircled{2} \sum \vec{F}_{ext} = m\vec{a}$$

- référentiel inertiel
- repère $(O, \vec{e}_x, \vec{e}_y)$

$$\Leftrightarrow m\vec{a} = -m\vec{g}$$

$$\Leftrightarrow \vec{a} = -\vec{g}$$

$$\vec{a} = \frac{d\vec{v}}{dt} \quad \text{On primitive}$$

$$\vec{v} \begin{cases} v_y(t) = -gt + v_{0y} \\ v_x(t) = v_{0x} \end{cases}$$

$$\vec{v} = \frac{d\vec{OM}}{dt}$$

$$\vec{OM} \begin{cases} y(t) = -\frac{1}{2}gt^2 + h \\ x(t) = v_0 t + x_0 \end{cases}$$

$$y_0 = h$$

$$\textcircled{3} \quad -\frac{1}{2}gt^2 + h = 0$$

$$\Leftrightarrow t^2\left(-\frac{1}{2}g\right) + h = 0$$

$$\Leftrightarrow t^2\left(-\frac{1}{2}g\right) = -h$$

$$\Leftrightarrow t = \sqrt{\frac{h}{\frac{1}{2}g}} = \sqrt{\frac{2h}{g}}$$

$$x\left(\sqrt{\frac{2h}{g}}\right) = v_0 \sqrt{\frac{2h}{g}}$$

$$d = v_0 \sqrt{\frac{2h}{g}}$$

$$\Leftrightarrow v_0 = \frac{d}{\sqrt{\frac{2h}{g}}}$$

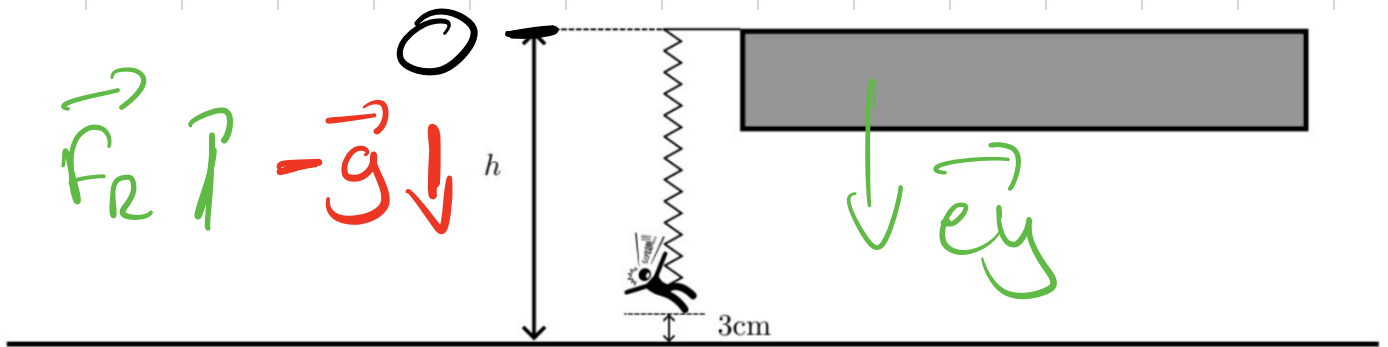
$$\frac{h}{\frac{1}{2}g}$$

$$h \times \left(\frac{2}{1}\right) \times \left(\frac{1}{g}\right)$$

Exercise 2

(p1)

①



$$\textcircled{2} \quad \sum \vec{F}_{\text{ext}} = m \vec{a}$$

$$\vec{F}_R = -k (D_y - l_0) \vec{e}_y$$

$$\vec{P} = m \vec{g}$$

$$\Leftrightarrow m \vec{g} - k y(H) \vec{e}_y = m \vec{a}$$

$$\Leftrightarrow g - \frac{k}{m} y \vec{e}_y = \vec{a}$$

On primitive :

$$\vec{a} = \frac{d\vec{v}}{dt}$$

$$\vec{v}_y = \vec{g}t - \frac{k}{m} t \Delta y \vec{e}_y$$

$$\vec{y} = \frac{1}{2} \vec{g} t^2 - \frac{1}{2} \frac{k}{m} t^2 \Delta y \vec{e}_y$$

$$v_y = t \left(g - \frac{k}{m} \Delta y \right)$$

$$0 = t \left(g - \frac{k}{m} \Delta y \right)$$

Soil $E=0$ Soil

$$g - \frac{k}{m} \Delta y = 0$$

$$\Rightarrow g = \frac{k}{m} \Delta l$$

$$\Rightarrow k = \frac{g}{\Delta l} \times m$$

$$\sum \vec{F}_{\text{ext}} = m \vec{a}$$

$$\Rightarrow \ddot{y}m = gm - ky$$

$$E) \ddot{y} = -\frac{k}{m}y + g$$

$$= -\frac{k}{m}y + g$$

$$\omega = \sqrt{\frac{k}{m}} \quad b = g$$

$$\ddot{y} = -\omega^2 y + b$$

$$= -\omega^2 \left(y - \frac{b}{\omega^2} \right)$$

$$u = y - \frac{b}{\omega^2}$$

$$\ddot{u} = -\omega^2 u$$

$$u(t) = C \cos(\omega t + \varphi_0)$$

$$\dot{u}(t) = -C\omega \sin(\omega t + \varphi_0)$$

$$\ddot{u}(t) = -C\omega^2 \cos(\omega t + \varphi_0)$$

$$\dot{y}(0) = 0 \quad \dot{y}(0) = 0$$

$$y(0) = 0$$

$$y = u + \frac{b}{\omega^2}$$

$$= C \cos(\omega t + \varphi_0) + \frac{b}{\omega^2}$$

$$y(0) = C \cos(\varphi_0) + \frac{b}{\omega^2}$$

$$-C \cos(\varphi_0) = \frac{b}{\omega^2}$$

$$\dot{y}(t) = -C\omega \sin(\omega t + \varphi_0)$$

$$C\omega \sin(\varphi_0) = 0$$

$$\sin(\varphi_0) = 0$$

$$\Rightarrow \varphi_0 = 0$$

$$-C = \frac{b}{\omega^2}$$

$$\Rightarrow C = \frac{-b}{\omega^2}$$

$$\begin{aligned} \textcircled{2} \quad y &= \frac{-b}{\omega^2} \cos(\omega t) + \frac{b}{\omega^2} \\ &= \frac{-b}{\omega^2} (\cos(\omega t) - 1) \end{aligned}$$

$$= g \times \frac{m}{k} \left(-\cos\left(\sqrt{\frac{k}{m}}\right) + 1 \right)$$

$$2g \times \frac{m}{k} = y_{\max}$$

$$2g \frac{m}{k} = h - \Delta s$$

$$\Leftrightarrow \frac{k}{2gm} = \frac{1}{h - \Delta s}$$

$$\Leftrightarrow k = \frac{2gm}{h - \Delta s}$$