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$$a) \vec{\tau}_A = \vec{AP} \wedge \vec{P}$$

$$= (r \cos \alpha \hat{e}_x + r \sin \alpha \hat{e}_y) \wedge F \hat{e}_y$$
$$= r \cos \alpha \cdot F \hat{e}_z$$

$$\frac{d\vec{L}_A}{dt} = \vec{\tau}_A$$

$$\vec{L}_A = \vec{r} \wedge m\vec{v}$$

$$\vec{L}_A = I \cdot \vec{\omega}$$

Si $\alpha \in \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$, $\frac{d\vec{L}_A}{dt}$ est positif selon \hat{e}_z ,
donc $\vec{\omega}$ est selon \hat{e}_z
donc la rotation est antihoraire

Si $\alpha \in \left[\frac{\pi}{2}, \frac{3\pi}{2} \right]$, $\frac{d\vec{L}_A}{dt}$ est négatif selon \hat{e}_z , donc $\vec{\omega}$ est selon $-\hat{e}_z$ donc la rotation est horaire.

⑥ L'accélération angulaire est proportionnelle au moment de force.

$$\dot{\vec{L}}_A = \vec{M}_A$$

$$\vec{L} = I \vec{\omega}$$

$$\frac{d\vec{L}}{dt} = I \cdot \dot{\alpha}$$

$$\vec{M} = I \cdot \dot{\alpha}$$

$$= r \cos \alpha \cdot F \hat{e}_z$$

F fixé $\Rightarrow \cos \alpha$ max quand $\alpha = 0$ ou $\alpha = \pi$.

③

$$\lambda = \frac{\pi}{2} \quad \omega \quad \lambda = -\frac{\pi}{2}$$

$$e_p \wedge e_\phi = e_z$$

$$\vec{\Pi}_0(m_1 \vec{g}) = \vec{OA} \wedge m_1 \vec{g}$$

$$\vec{H}_0(m_2 \vec{g}) = \vec{OB} \cap m_2 \vec{g}$$

$$= OB \cdot m_2 g \cdot \sin \phi \cdot \hat{e}_3$$

$$\vec{M}_0(\vec{T}_1) = \vec{OA} \wedge \vec{T} = 0$$

$$\vec{M}_0(\vec{T}_2) = \vec{OB} \wedge \vec{T} = 0$$

$$\vec{L}_0 = \vec{L}_{0,m_1} + \vec{L}_{0,m_2}$$

$$= \vec{OA} \wedge m_1 \vec{v}_1 + \vec{OB} \wedge m_2 \vec{v}_2$$

$$= d_1 m_1 \dot{\phi} d_1 \hat{e}_z + d_2 m_2 d_2 \dot{\phi} \hat{e}_z$$

$$= (d_1^2 m_1 + d_2^2 m_2) \dot{\phi} \hat{e}_z$$

$$\frac{d\vec{L}_0}{dt} = \vec{M}_0$$

$$= (d_1^2 m_1 + d_2^2 m_2) \dot{\phi} \hat{e}_z$$

$$(d_1^2 m_1 + d_2^2 m_2) \ddot{\phi} =$$

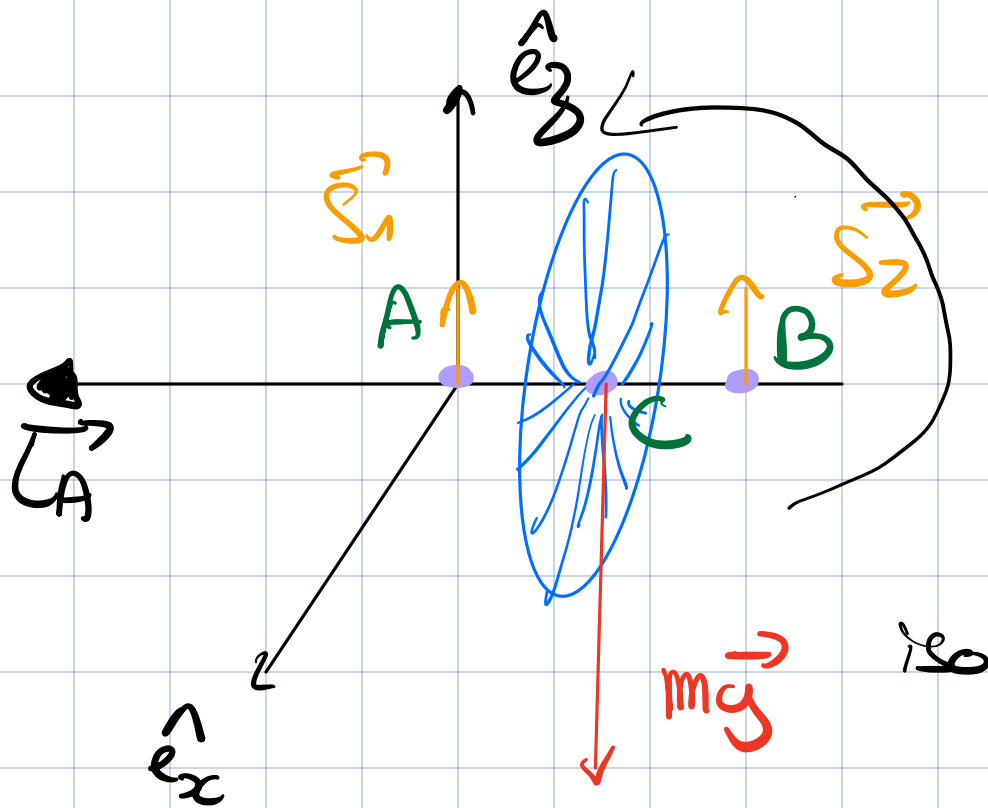
$$- d_1 \cdot m_1 g \cdot \sin \phi - d_2 m_2 g \sin \phi$$

$$\Leftrightarrow (d_1^2 m_1 + d_2^2 m_2) \ddot{\phi}$$

$$= - (d_1 \cdot m_1 + d_2 m_2) g \sin \phi$$

$$\Leftrightarrow \ddot{\phi} + \underbrace{\frac{(d_1^2 m_1 + d_2^2 m_2)}{(d_1 m_1 + d_2 m_2)}}_{\omega_0^2} g \sin \phi = 0$$

③



$$\frac{d\vec{L}_A}{dt} = \vec{M}_A$$

$$\vec{M}_A(\vec{S}_1) = \vec{AA} \wedge \vec{S}_1 = \vec{0}$$

$$\vec{M}_A(m\vec{g}) = \vec{AC} \wedge m\vec{g} = -AC \cdot mg \cdot \hat{e}_x$$

$$\vec{M}_A(\vec{S}_2) = \vec{AB} \wedge \vec{S}_2 = AB \cdot N \cdot \hat{e}_x$$

$$(AB \cdot N - AC \cdot mg) \cdot \hat{e}_x = 0$$

$$\frac{d\vec{L}_A}{dt} = -AC \cdot mg \cdot \hat{e}_x$$

elle va tourner autour de l'origine