

Homework 10

Tanja Kaiser

Exercise 2. Find the decimal expansion of the binary number $(111\dots 111)$ (with n 1's).

max we can share with n in base b .

$$\Rightarrow 2^n - 1 \quad (\text{e.g. } 10^2 - 1 = 99)$$

$$(b^k - 1)$$

Exercise 9. How many distinct five-card poker hands contain:

1. *One pair* (poker hand containing two cards of the same kind and three cards of three other kinds).
2. *Two pairs* (poker hand containing two cards of the same kind, two cards of another kind and one card of a third kind).
3. *Three of a kind* (poker hand containing three cards of the same kind and two cards of two other kinds).

$$\textcircled{1} \quad \binom{13}{1} \cdot \binom{4}{2} \cdot \binom{12}{3} \cdot \binom{4}{1}^3$$

$$\textcircled{2} \quad \binom{13}{2} \cdot \binom{4}{2}^2 \cdot \binom{11}{1} \cdot \binom{4}{1}$$

$$\textcircled{3} \quad \binom{13}{1} \cdot \binom{4}{3} \cdot \binom{12}{2} \cdot \binom{4}{1}^2$$