

Question 1

It depends on the existing parity bits

d_{\min}' could be 3

$$n=4$$
$$k=1$$

0

0

x_1

0

x_1

0

$x_1 \oplus x_2$

0

0

0

1

1

1

0

0

1

1

$$d_{\min} = 3$$

$$\Rightarrow d_{\min} = 5$$

$$G = (u_1 \ u_2 \ u_3) \begin{pmatrix} I & 0 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \\ \vdots & \vdots & \vdots \end{pmatrix}$$

Supposons que la distance minimale est 3.

Ce nouveau code, pour les codes à une distance 3, va ajouter 2 de distance
 $\rightarrow 5$ ou

20
02
00

10
01
00

Q2

$$\left(\begin{array}{ccc|c} 1 & 0 & 0 & \\ 0 & 1 & 0 & \\ 0 & 0 & 1 & \\ \hline 1 & 0 & 0 & p \\ 0 & 1 & 0 & \\ 0 & 0 & 1 & \end{array} \right)$$

$$\left(\begin{array}{cccccc} 1 & \cancel{1} & \cancel{1} & 0 & 1 & 0 \\ 0 & \cancel{1} & \cancel{1} & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & \cancel{1} & \cancel{1} & \cancel{1} & 0 & 1 \end{array} \right)$$

$$\rightarrow \left(\begin{array}{cccccc} 1 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{array} \right)$$

Q3

lexer code

- sum $\in E$
- 0 $\in E$ ✓

1 3 1

Q5 bijechivé alre C₁ et code Fp

3^3

2^3

$$(1 \ 1 \ 1 \ 1) \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix}$$

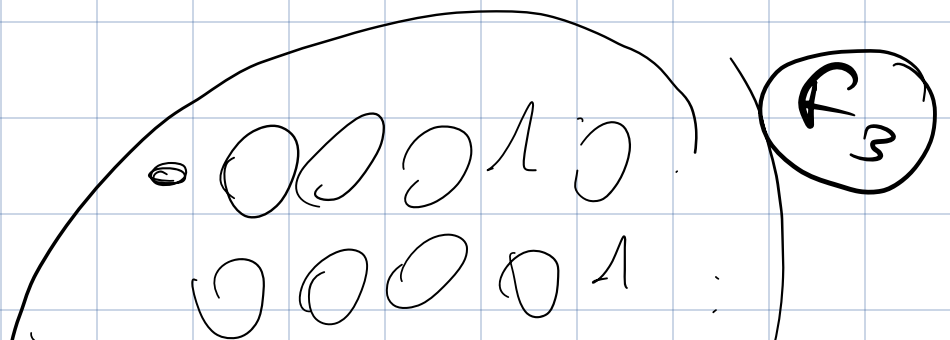
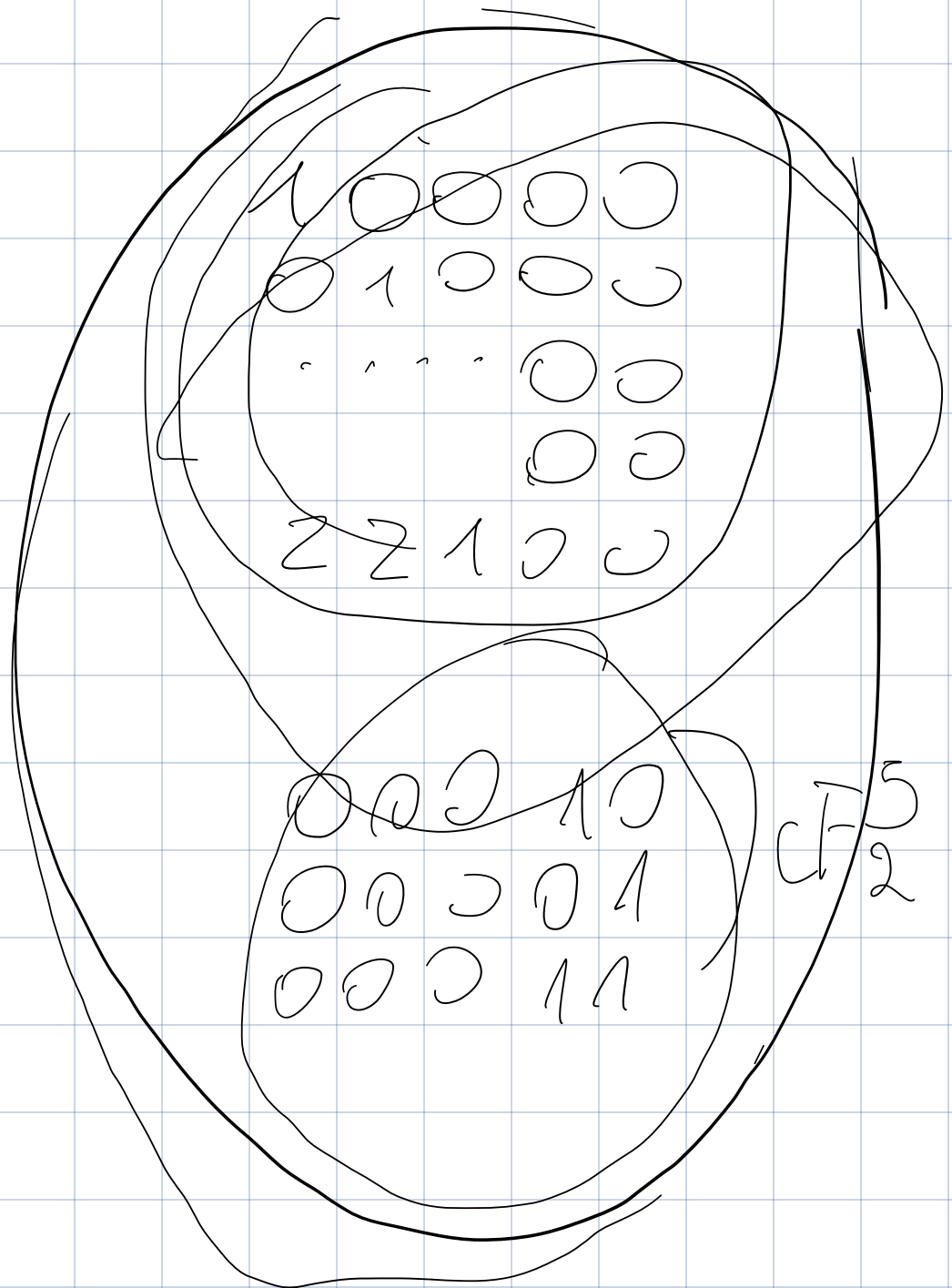
$$= \begin{pmatrix} 1 \end{pmatrix}$$

$$d_{\min} = 4$$

$$\begin{array}{cccc} 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \end{array}$$

Q9 \rightarrow 9 de dimensões?

22101



$\begin{matrix} 0 & 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{matrix}$

$C_1 \subset F_3$

$m=5 \quad k=2$

$\begin{matrix} 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 \end{matrix}$

$\begin{matrix} 2 & 0 & 0 & 2 & 2 \\ 1 & 0 & 0 & 1 & 1 \\ 2 & 1 & 0 & 1 & 0 \\ 1 & 2 & 0 & 2 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 2 & 1 \\ 0 & 2 & 0 & 1 & 2 \\ 1 & 1 & 0 & 0 & 2 \\ 2 & 2 & 0 & 0 & 1 \end{matrix}$