



The background features a collage of data visualization elements. At the top and bottom, there are network graphs with nodes and edges in shades of red, orange, and green. On the left side, there is a vertical strip showing a heatmap or a series of small plots with orange and red data points. The central text is overlaid on a white, angular geometric shape.

# **The *K-Medians* and *K-Modes* Clustering Methods**

# ***K-Medians: Handling Outliers by Computing Medians***

---

- ❑ Medians are less sensitive to outliers than means
  - ❑ Think of the median salary vs. mean salary of a large firm when adding a few top executives!
- ❑ **K-Medians**: Instead of taking the **mean** value of the object in a cluster as a reference point, **medians** are used ( $L_1$ -norm as the distance measure)
- ❑ The criterion function for the *K-Medians* algorithm: 
$$S = \sum_{k=1}^K \sum_{x_{ij} \in C_k} |x_{ij} - med_{kj}|$$
- ❑ The *K-Medians* clustering algorithm:
  - ❑ Select  $K$  points as the initial representative objects (i.e., as initial  $K$  medians)
  - ❑ **Repeat**
    - ❑ Assign every point to its nearest median
    - ❑ Re-compute the median using the median of each individual feature
  - ❑ **Until** convergence criterion is satisfied

# K-Modes: Clustering Categorical Data

---

- ❑ *K-Means* cannot handle non-numerical (categorical) data
  - ❑ Mapping categorical value to 1/0 cannot generate quality clusters for high-dimensional data
- ❑ ***K-Modes***: An extension to *K-Means* by replacing means of clusters with **modes**
- ❑ Dissimilarity measure between object  $X$  and the center of a cluster  $Z$ 
  - ❑  $\Phi(x_j, z_j) = 1 - n_j^r/n_l$  when  $x_j = z_j$  ; 1 when  $x_j \neq z_j$ 
    - ❑ where  $z_j$  is the categorical value of attribute  $j$  in  $Z_l$ ,  $n_l$  is the number of objects in cluster  $l$ , and  $n_j^r$  is the number of objects whose attribute value is  $r$
- ❑ This dissimilarity measure (distance function) is **frequency-based**
- ❑ Algorithm is still based on iterative *object cluster assignment* and *centroid update*
- ❑ A ***fuzzy K-Modes*** method is proposed to calculate a ***fuzzy cluster membership value*** for each object to each cluster
- ❑ A mixture of categorical and numerical data: Using a ***K-Prototype*** method