



# CS412 office hour

Apr 12, 2019

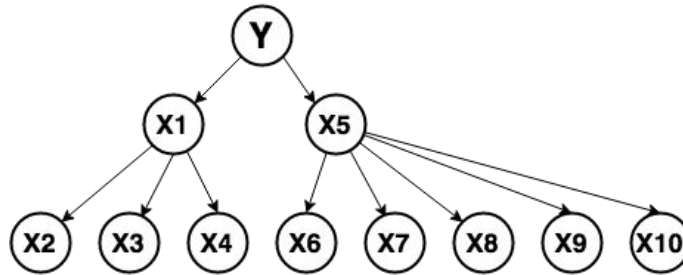


# Today's Office Hour

- Counting parameters
- QA

# #parameters in a Bayesian network

**Example:** Suppose our data has 3 different classes and 10 attributes, each with 2 possible values. How many parameters will our model have if we use a Bayesian network with three layers as pictured below?

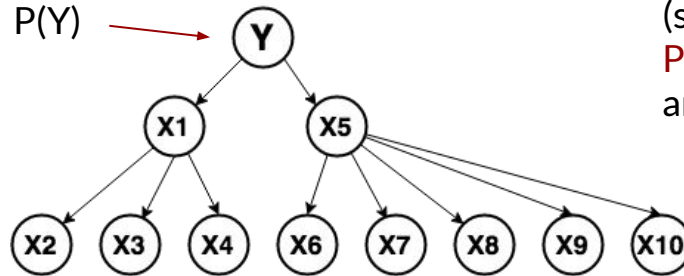


# #parameters in a Bayesian network

**Example:** Suppose our data has 3 different classes and 10 attributes, each with 2 possible values. How many parameters will our model have if we use a Bayesian network with three layers as pictured below?

Y=a1	Y=a2	Y=a3
p1	p2	p3

3 parameters



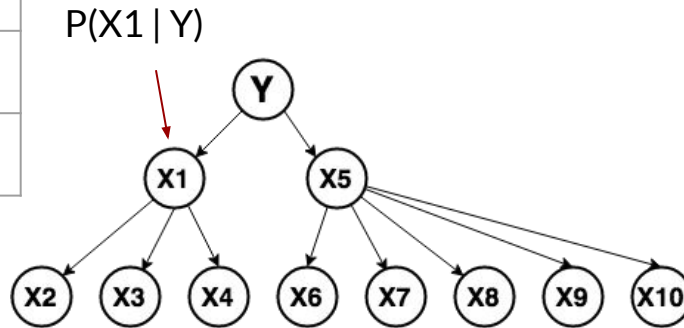
OR 2 free parameters  
(since the probabilities add up to 1)  
 $P(Y=a1)$ ,  $P(Y=a2)$   
and  $P(Y=a3)$  can be derived from them

# #parameters in a Bayesian network

**Example:** Suppose our data has 3 different classes and 10 attributes, each with 2 possible values. How many parameters will our model have if we use a Bayesian network with three layers as pictured below?

	Y=a1	Y=a2	Y=a3
X=b1			
X=b2			

6 parameters



OR 3 free parameters

$P(X1=b1 | Y=a1)$

$P(X1=b1 | Y=a2)$

$P(X1=b1 | Y=a3)$

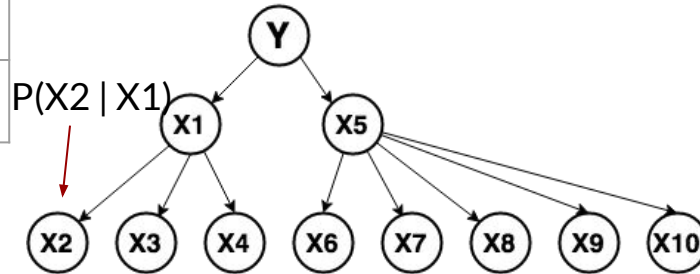
and  $P(X1=b2 | Y=a1)$ ,  $P(X1=b2 | Y=a2)$ ,  $P(X1=b3 | Y=a3)$  can be derived from them

# #parameters in a Bayesian network

**Example:** Suppose our data has 3 different classes and 10 attributes, each with 2 possible values. How many parameters will our model have if we use a Bayesian network with three layers as pictured below?

	X1=b1	X1=b2
X2=b1		
X2=b2		

4 parameters



OR 2 free parameters

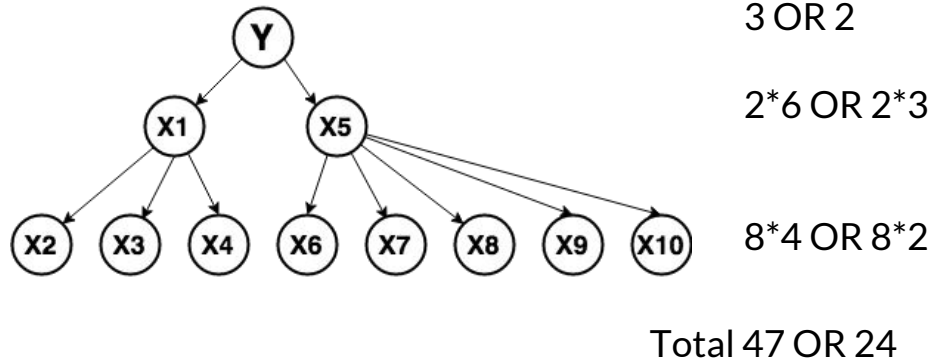
$P(X2=x1 | X1=x1)$

$P(X2=x1 | X1=x2)$

and  $P(X2=b2 | X1=b1)$ ,  $P(X2=b2 | X1=b2)$  can be derived from them

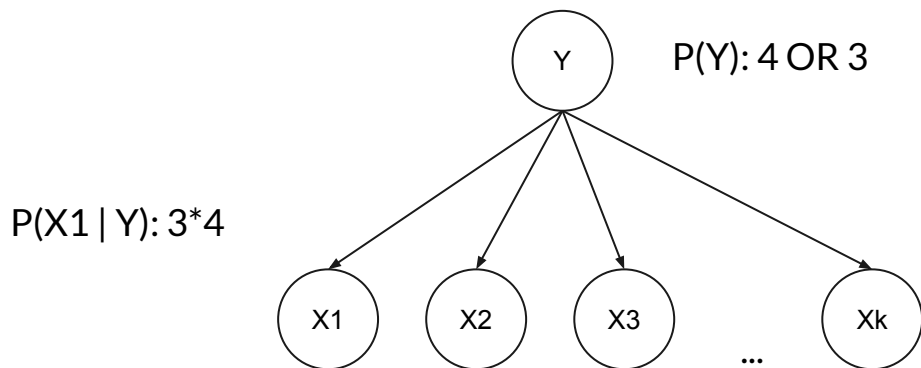
# #parameters in a Bayesian network

**Example:** Suppose our data has 3 different classes and 10 attributes, each with 2 possible values. How many parameters will our model have if we use a Bayesian network with three layers as pictured below?



# #parameters of naive Bayes

- A special case of Bayesian networks



Free:  $2 \times 4$

#classes (Y): 4  
#value\_for\_each\_dim: 3  
#feature\_dim: 10

Counting all:  $10 \times 3 \times 4 + 4 = 124$   
Counting free prams:  $10 \times 2 \times 4 + 3 = 83$